

# Laboratory #3: System Identification of the dc-to-dc Buck converter

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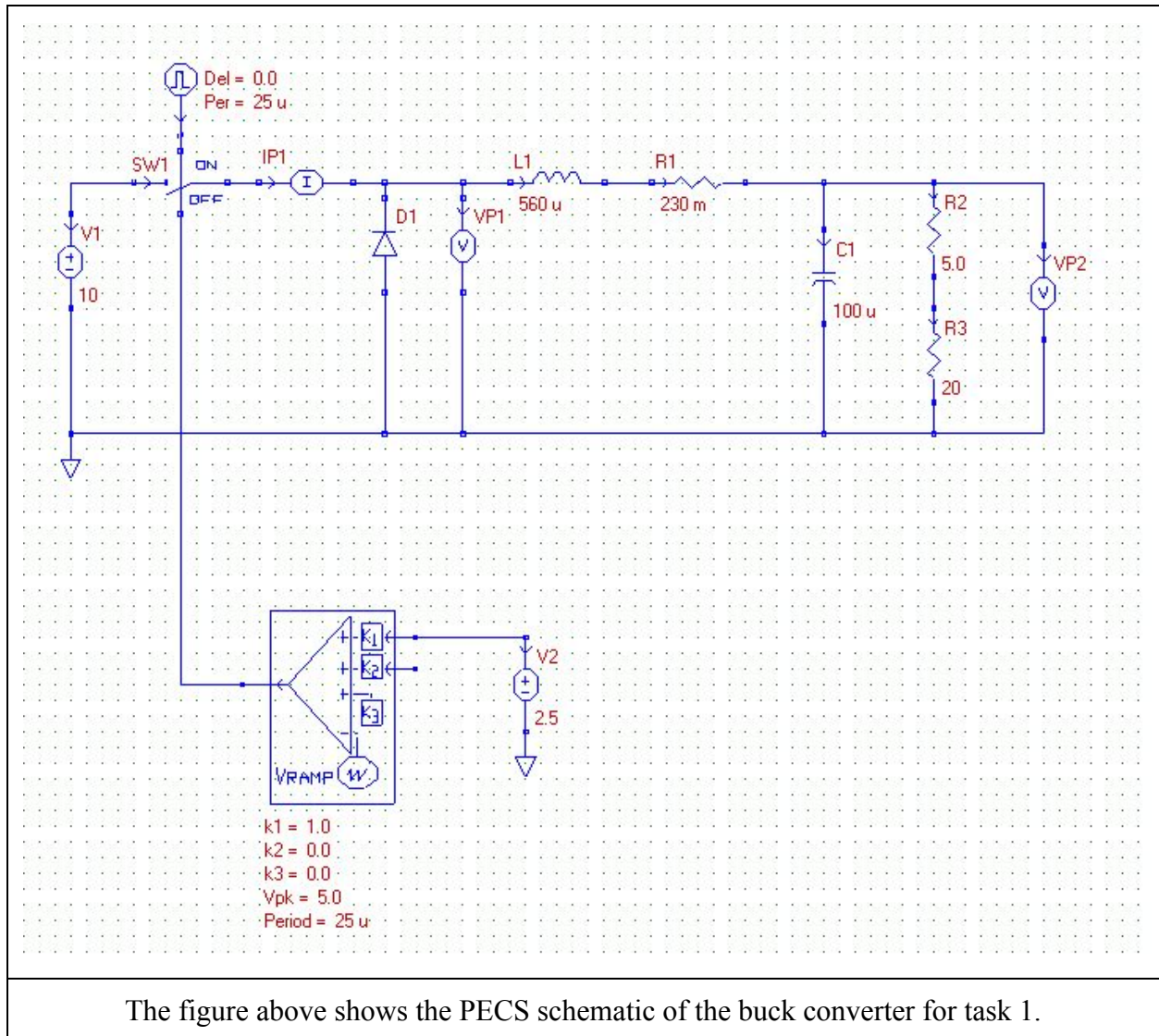
ECE 317 - Signals and Systems III

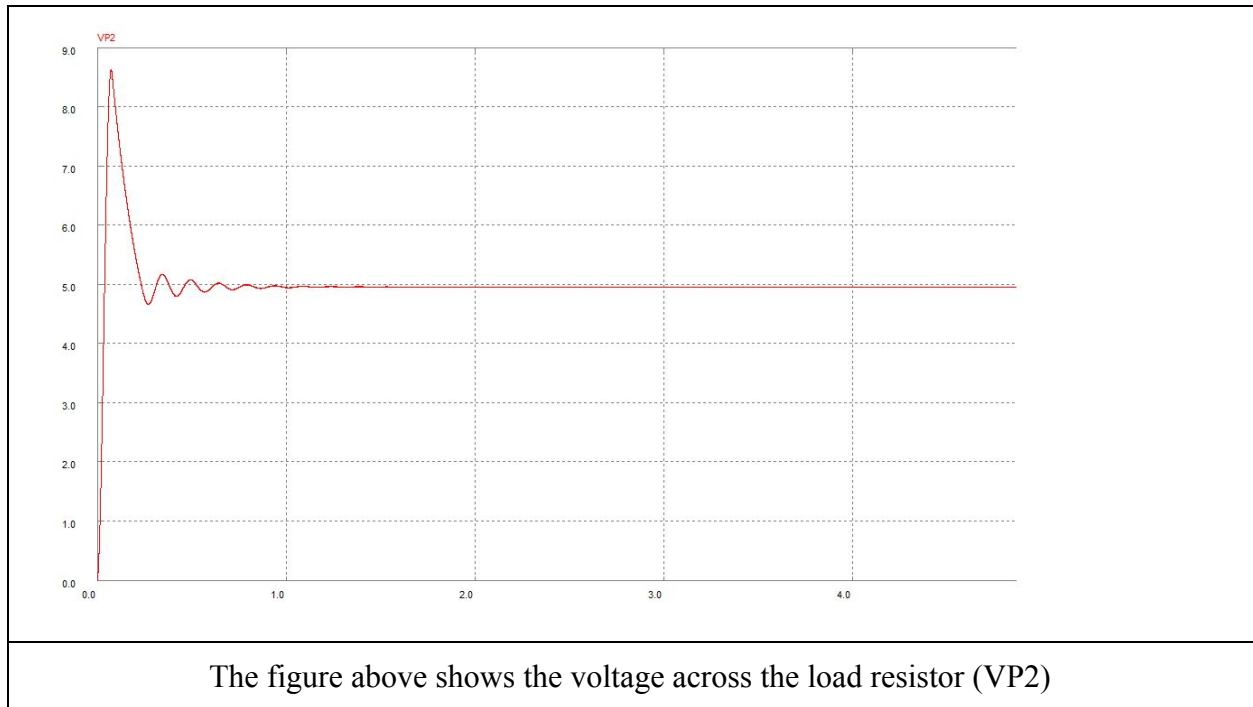
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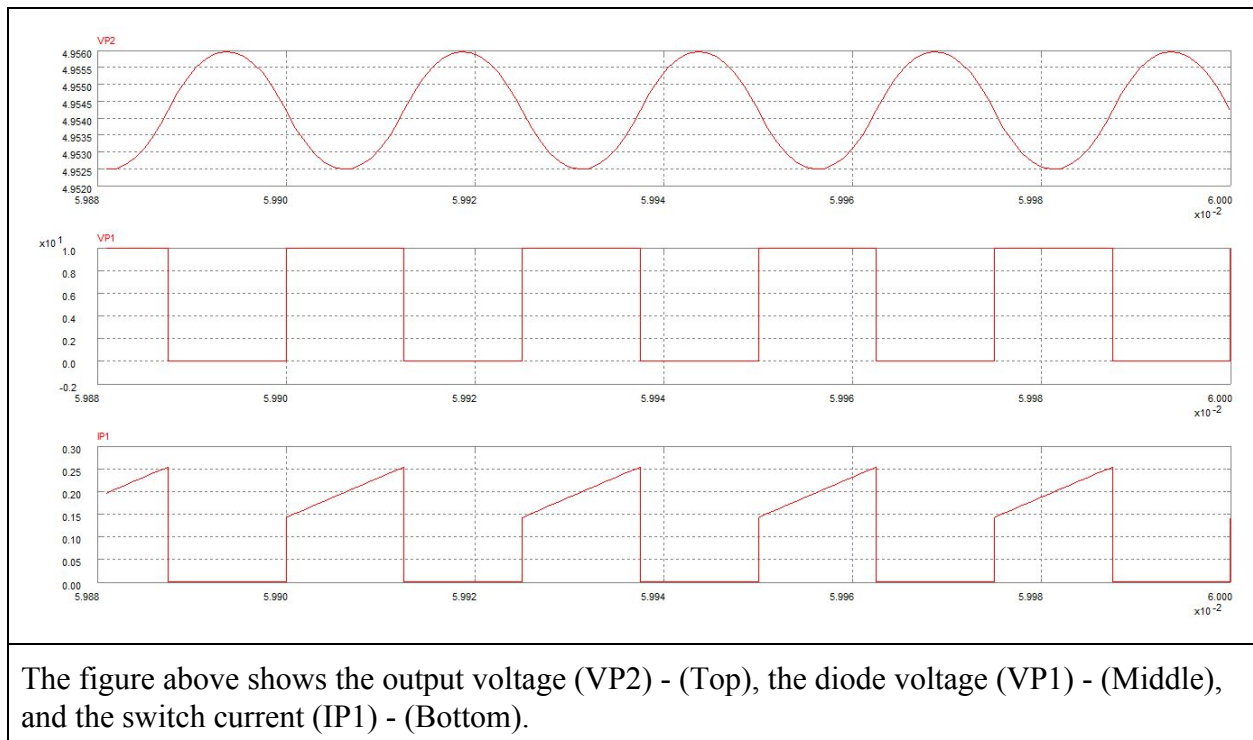
## Task 1:





As the figure above shows, there is a large start-up transient before the steady state voltage is established. This steady state voltage is 4.95 V.

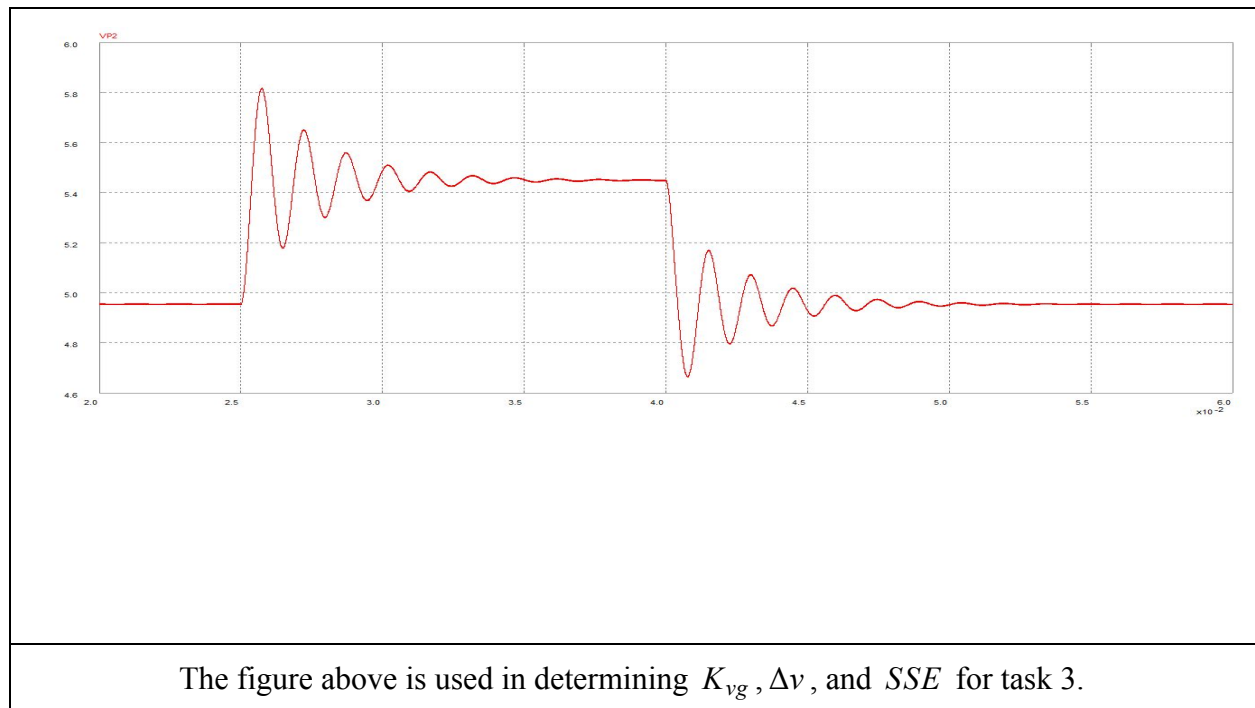
## Task 2:



Average output voltage	4.954 V
Peak-to-peak output voltage (ripple)	3.44 mV
Peak-to-peak diode voltage	10 V
Peak inductor current	254 mA
Frequency of waveforms (all same freq)	40 kHz
Duty ratio	50 %

The duty ratio is set by the modulator in the circuit. The modulator has a sawtooth generator that is set by the Vpk and the Period. The sawtooth generator peak voltage of 5 V is compared to the voltage from the V2 supply of 2.5 V. The modulator output starts by being off while the voltage from the sawtooth generator ramps up. As the voltage from the sawtooth generator crosses 2.5 V, the output of the modulator turns on until the voltage from the sawtooth generator drops back down to 0 V.

### Task 3:



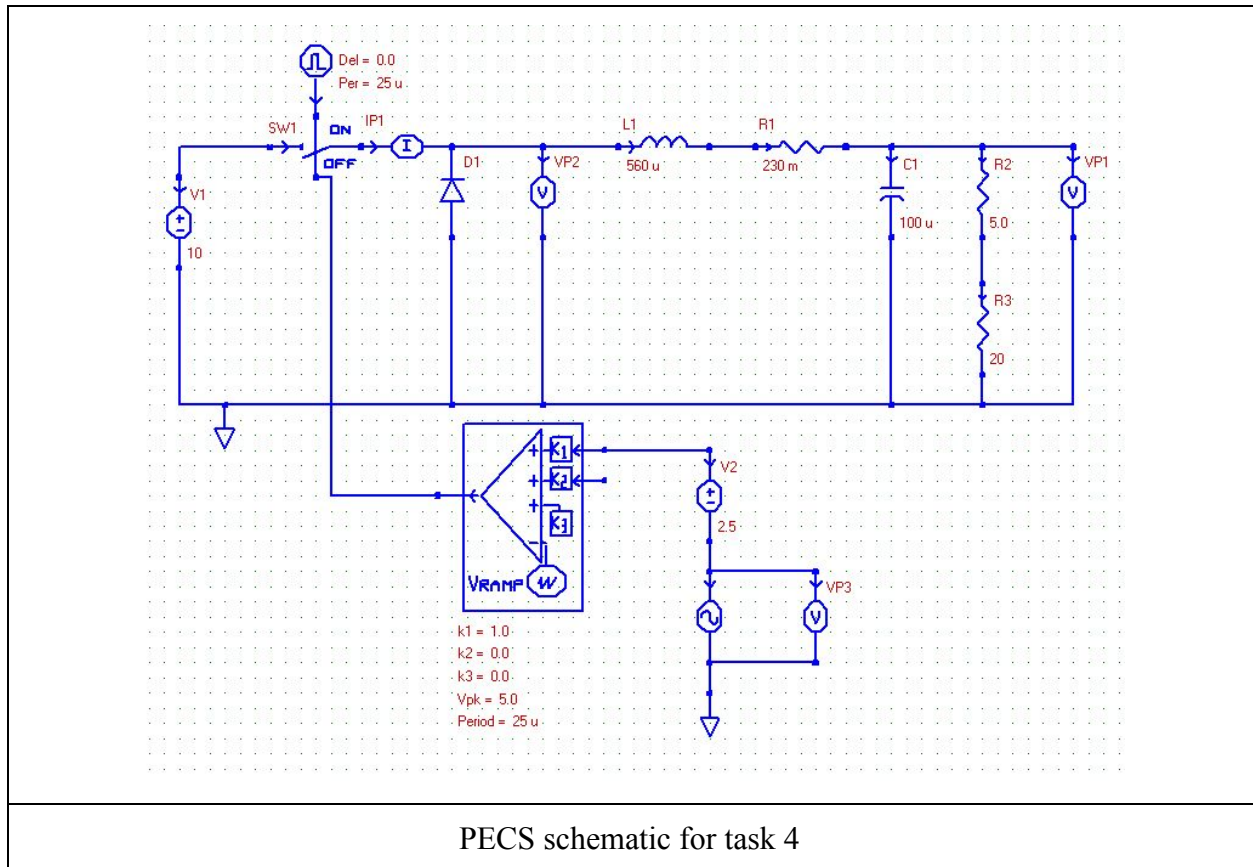
$$K_{vg} = \frac{\Delta c}{\Delta v} = \frac{c_{final} - c_0}{v_{final} - v_0}$$

$$K_{vg} = \frac{5.45 V - 4.95 V}{1 V} = 0.5$$

show formula for SSE

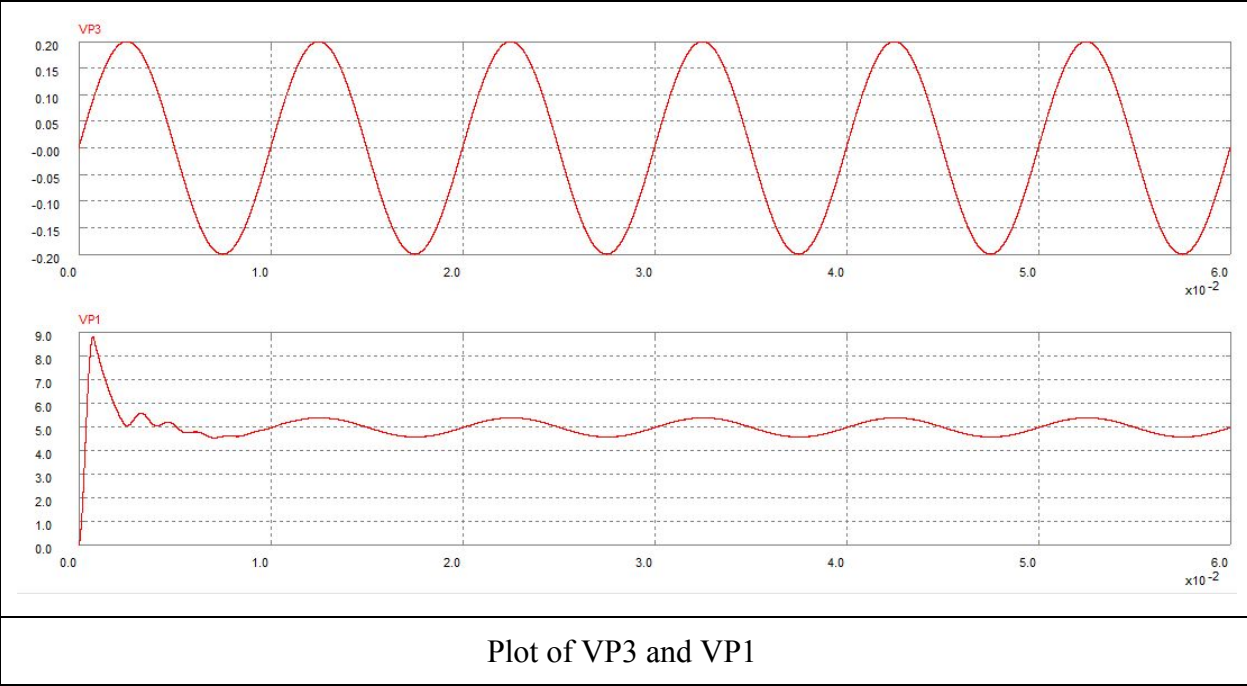
The maximum peak-to-peak output voltage deviation is 1.15 V and the steady state error is 0.5 V

#### Task 4:



Solving for filter corner frequency:

$$F_c = \frac{1}{2\pi\sqrt{LC}} \Rightarrow \frac{1}{2\pi\sqrt{(560 \times 10^{-6})(100 \times 10^{-6})}} = 673 \text{ Hz}$$



Peak-to-peak voltage	
VP3	0.4V
VP1	<del>0.8V</del> 0.81V

- VP3 and VP1 are in-phase.

Solving for  $K_{vd}$  :

$$G_{PWM} = \frac{1}{V_m}$$

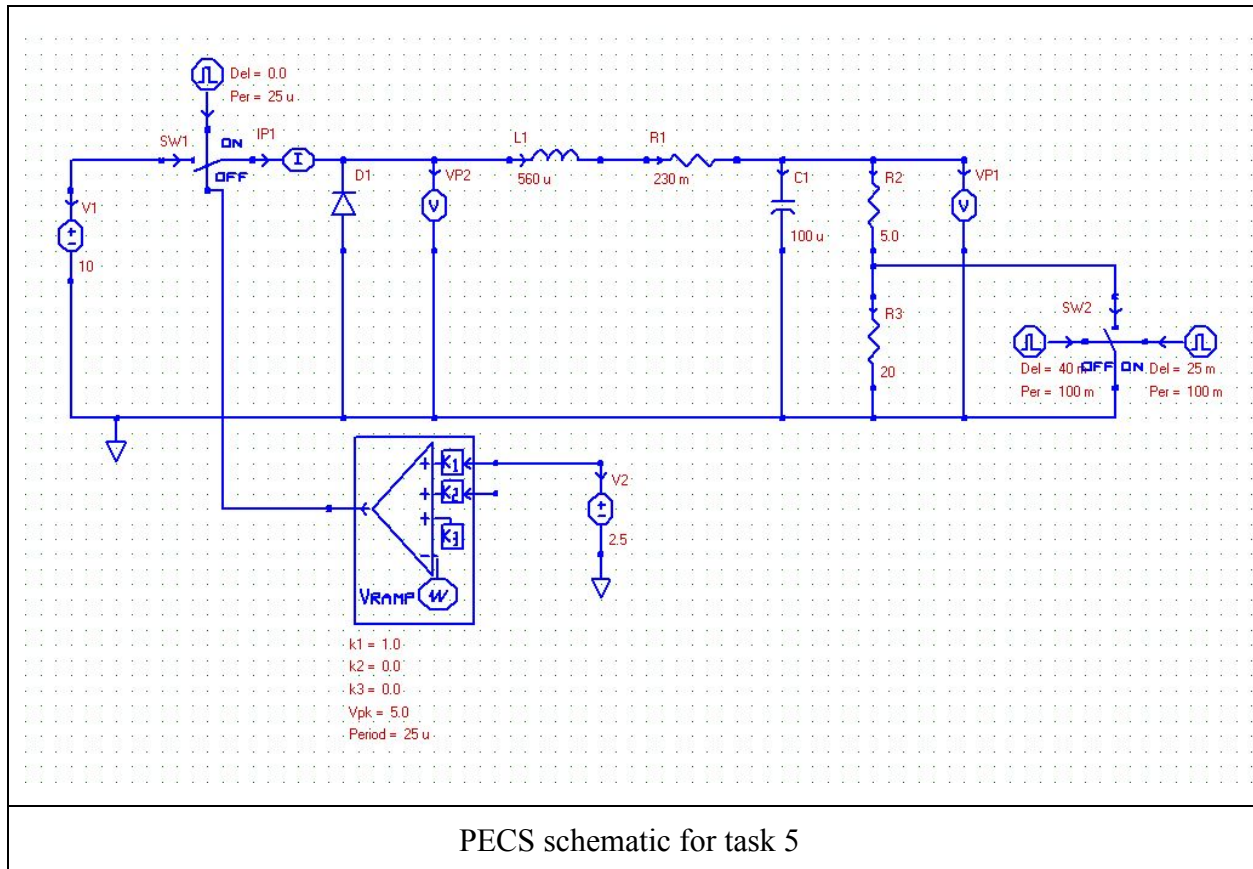
$$\widehat{V_c} = V_m$$

$$G_{LPF} \approx 1$$

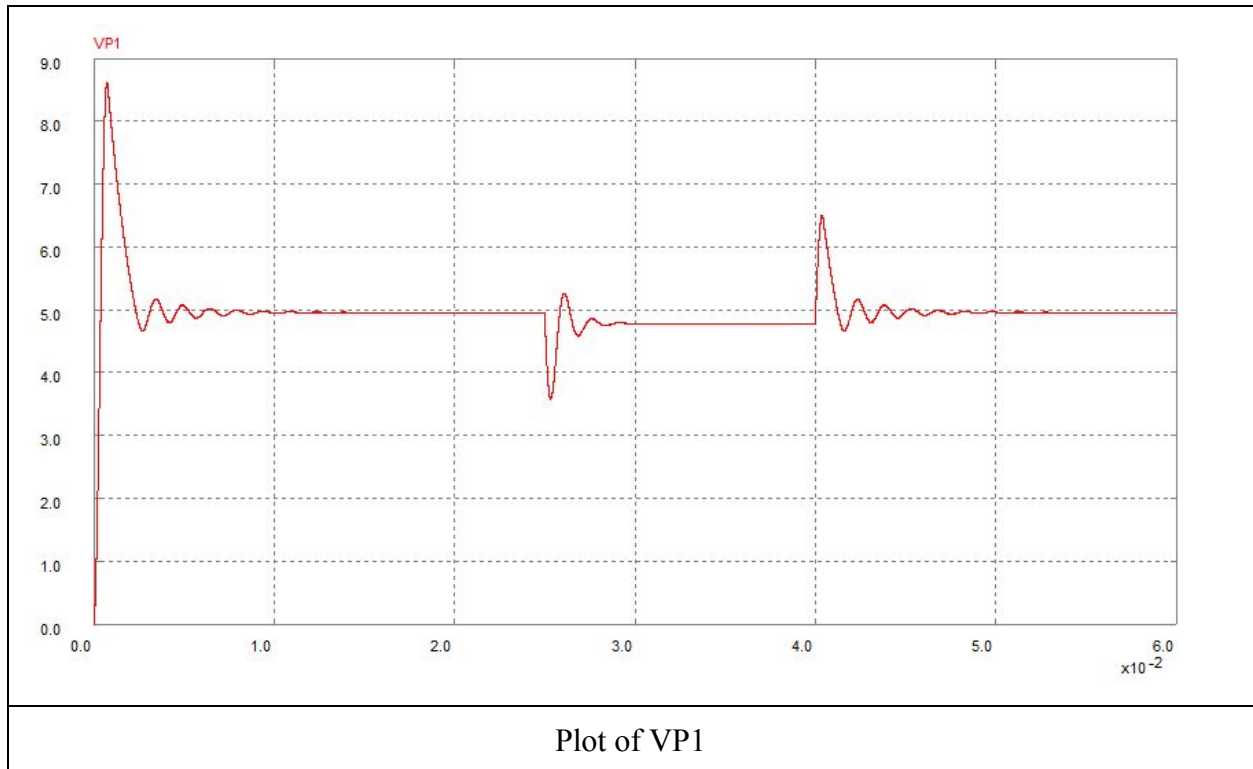
$$\frac{\widehat{v}}{\widehat{v_c}} = \frac{1}{V_m} \cdot K_{vd} G_{LPF} \Rightarrow \frac{0.8}{0.4} = \frac{1}{5} \cdot K_{vd}(1)$$

$$K_{vd} = \cancel{10} \quad 10.125$$

### Task 5:







Maximum peak-to-peak output voltage and steady state error:

$$\Delta V = 6.5 - 3.6 = 2.9V$$

$$SSE = 4.956 - 4.779 = 0.177V$$

**Task 6a:**

$$T(s) = -G_c(s)H(s)G_{vd}(s)G_{PWM}(s)$$

Using the previously found value  $K_{vd}$  and  $G_{vd}(s) = K_{vd}G_{LPF}(s)$ . We get the following:

$$T(s) = \frac{-1}{CLs^2 + (Cr_L + \frac{L}{R})s + 1}$$



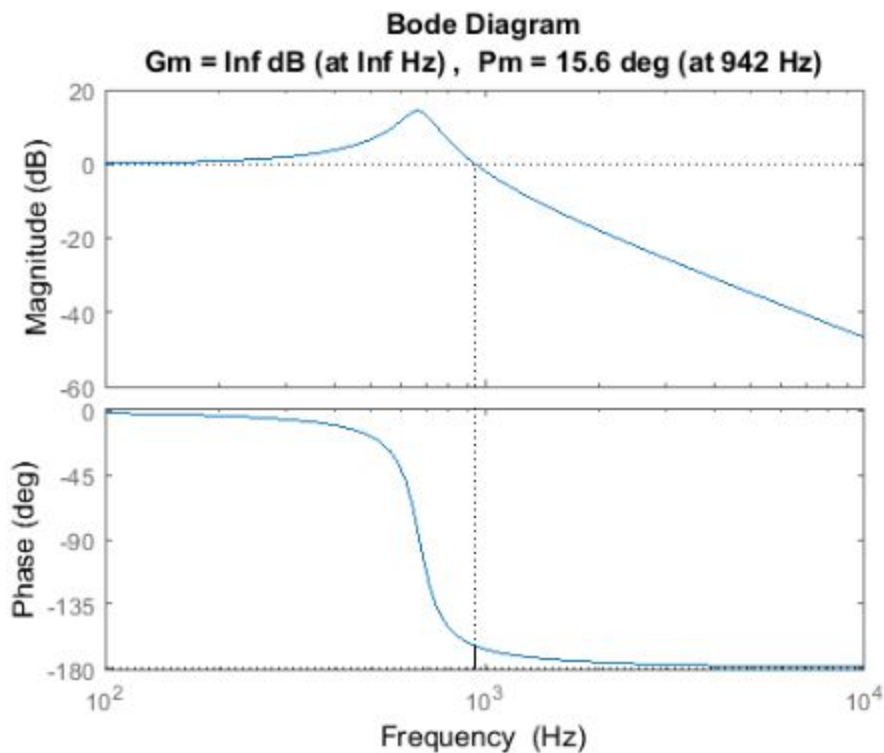
```

s = tf('s');
% LCR Low Pass Filter Component Values
C = 100e-06;
R = 25;
r = 230e-03;
L = 560e-06;
% Gain Loop Function
G_loop = 1/(C*L*s^2+(C*r+(L/R))*s+1);

figure(1)
margin(G_loop)
h = gcr;
h.AxesGrid.Xunits = 'Hz'; % display the frequency in Hz
h.AxesGrid.TitleStyle.FontSize=12; % increase font size
h.AxesGrid.XLabelStyle.FontSize=12; % for readability
h.AxesGrid.YLabelStyle.FontSize=12;

```

Loop Gain Bode Diagram Code



The above shows an infinite gain margin, a phase margin of 15.6 degrees, unity gain frequency at 942 Hz, and the phase never crosses -180 degrees, establishing a stable system.

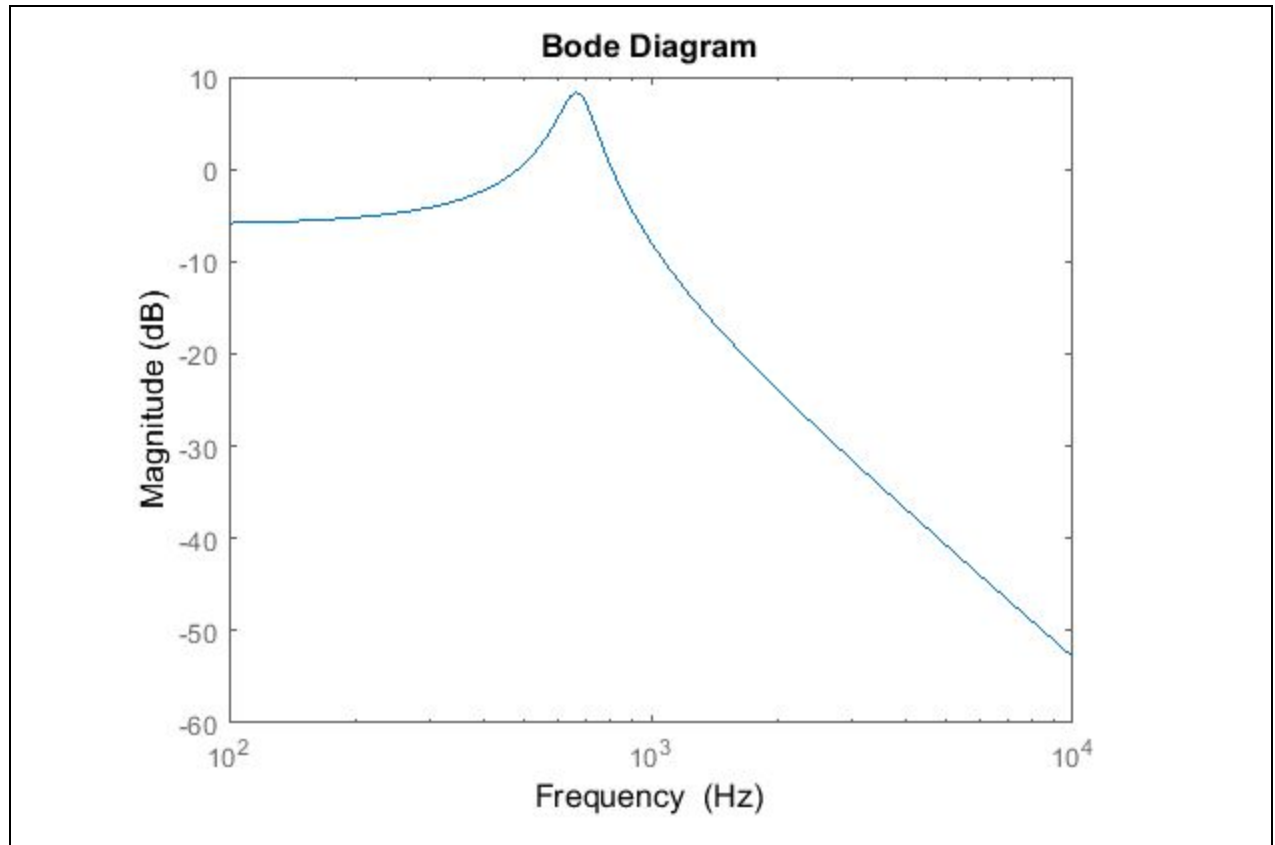
### Task 6b:

Using the previously found  $K_{vg}$ .

$$G_{vg}(s) = K_{vg}G_{LPF}(s) = \frac{.5}{CLs^2+(Cr_L+\frac{L}{R})s+1}$$

```
s = tf('s');  
% LCR Low Pass Filter Component Values  
C = 100e-06;  
R = 25;  
r = 230e-03;  
L = 560e-06;  
% Gain Transfer Function  
G_vg = .5/(C*L*s^2+(C*r+(L/R))*s+1);  
  
% Bode Magnitude Function  
bodemag(G_vg);  
  
% Convert frequency to Hz  
h = gcr;  
h.AxesGrid.Xunits = 'Hz'; % display the frequency in Hz  
h.AxesGrid.TitleStyle.FontSize=12; % increase font size  
h.AxesGrid.XLabelStyle.FontSize=12; % for readability  
h.AxesGrid.YLabelStyle.FontSize=12;
```

Bode Magnitude Diagram Code



**Task 6c:**

$$-Z_{out} = (R + r_L) \parallel R \parallel \frac{1}{sC} = \frac{-r_L(1 + \frac{sL}{r_L})}{CLs^2 + (Cr_L + \frac{L}{R})s + \frac{(r_L + R)}{R}}$$

Where  $(r_L + R) \approx R$  when  $r_L \ll R$ , so that

$$-Z_{out} = \frac{-r_L(1 + \frac{sL}{r_L})}{CLs^2 + (Cr_L + \frac{L}{R})s + 1}$$

```

s = tf('s');
% LCR Low Pass Filter Component Values
C = 100e-06;
R = 25;
r = 230e-03;
L = 560e-06;

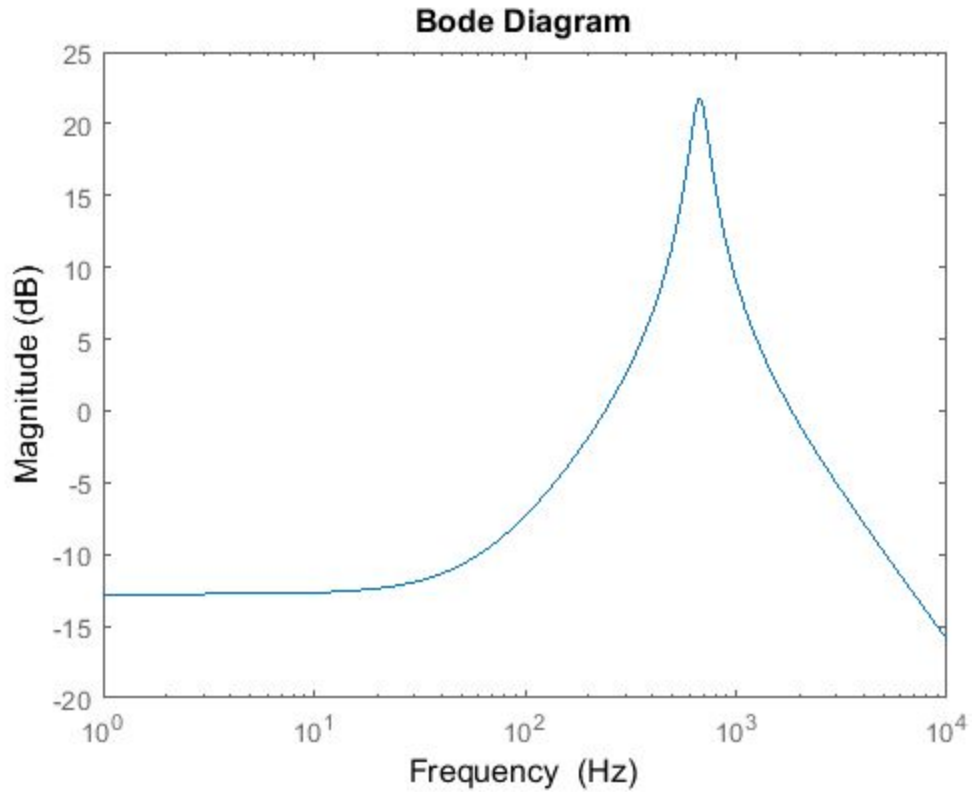
% Impedance Out Transfer Function
Z_out = -(r+s*L)/(C*L*s^2+(C*r+(L/R))*s+1);

% Bode Magnitude Function
bodemag(Z_out);

% Convert frequency to Hz
h = gcr;
h.AxesGrid.Xunits = 'Hz'; % display the frequency in Hz
h.AxesGrid.TitleStyle.FontSize=12; % increase font size
h.AxesGrid.XLabelStyle.FontSize=12; % for readability
h.AxesGrid.YLabelStyle.FontSize=12;

```

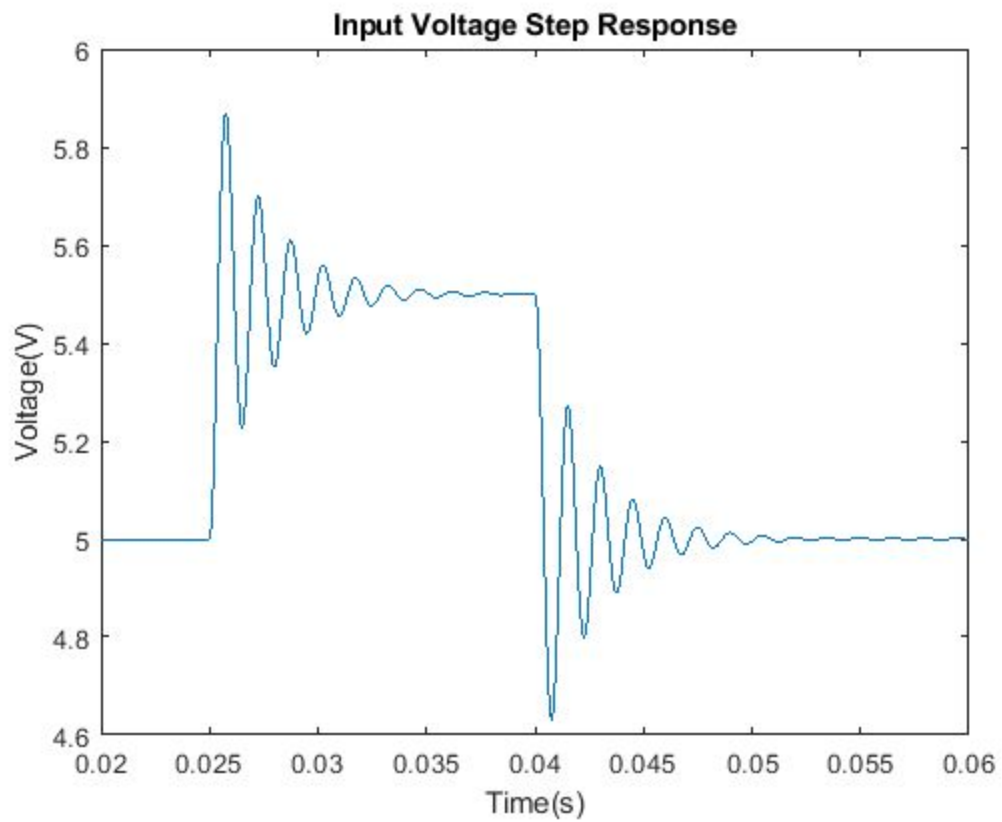
Impedance Bode Diagram Code



### Task 6d:

```
s = tf('s');  
% LCR Low Pass Filter Component Values  
C = 100e-06;  
R = 25;  
r = 230e-03;  
L = 560e-06;  
  
Vg = 10; % Input voltage  
D = 0.5; % K_vg  
V = D*Vg; % Steady state voltage  
  
% Gain Transfer Function  
G_vg = .5/(C*L*s^2+(C*r+(L/R))*s+1);  
  
t = linspace(0.02, 0.06, 1000);  
u = zeros(size(t));  
ind = find(t>=0.025 & t<=0.04); % Step is between 0.025<t<0.04  
Vg_diff = 1;  
u(ind) = u(ind) + Vg_diff; % Form input vector containing the step  
figure(2)  
y = lsim(G_vg, u, t); % Simulate the step response  
plot(t,y+V) % Add steady state voltage to the output and plot it  
title('Input Voltage Step Response');  
xlabel('Time(s)');  
ylabel('Voltage(V)');  
del_v = max(y) - min(y) % Peak-to-peak vo  
SSE = y(ind(end)) % Steady state error
```

Input Voltage Step Response Code



```
del_v =  
1.2367  
  
SSE =  
0.4988
```

Deviation Voltage and Steady State Error

**Task 6e:**

$$-Z_{out} = \frac{-r_L(1+\frac{sL}{r_L})}{CLs^2+(Cr_L+\frac{L}{R})s+1}$$

```

s = tf('s');
% LCR Low Pass Filter Component Values
C = 100e-06;
R = 25;
r = 230e-03;
L = 560e-06;

Vg = 10; % Input voltage
D = 0.5; % K_vg
V = D*Vg; % Steady state voltage

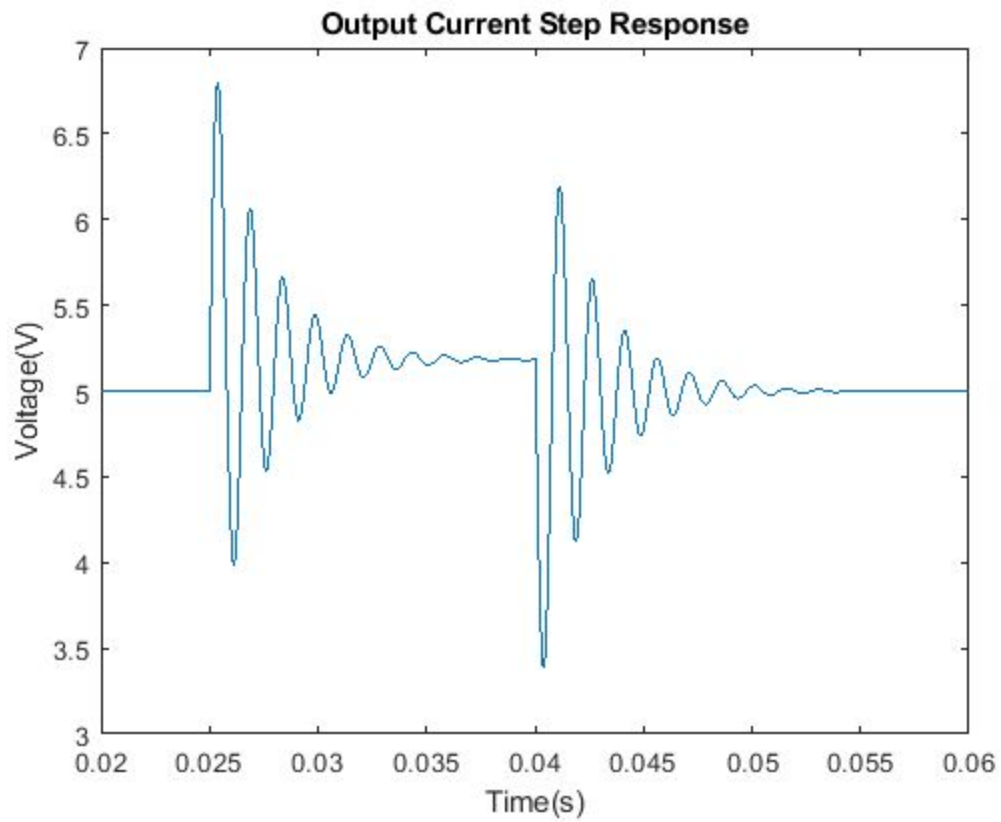
% Impedance Out Transfer Function
Z_out = -(r+s*L)/(C*L*s^2+(C*r+(L/R))*s+1);

Io_1 = V/25; % load current before step. (25 ohm load)
Io_2 = V/5; % load current after step. (5 ohm load)
Io_diff = Io_2 - Io_1; % current step
t = linspace(0.02, 0.06, 1000);
u = zeros(size(t));
ind = find(t>=0.025 & t<=0.04); % step is between 0.025<t<0.04
u(ind) = u(ind) + Io_diff;
figure(1)
y = lsim(-Z_out, u, t);
plot(t,y+V)
title('Output Current Step Response');
xlabel('Time(s)');
ylabel('Voltage(V)');
del_v = max(y) - min(y)
SSE = y(ind(end))

```

Output Current Step Response Code





```
del_v =  
3.4141  
  
SSE =  
0.1843
```

Deviation Voltage and Steady State Error

## Results:

Transfer function DC gains:

	From PECS	From model: Symbolic	From model: Symbolic Evaluated
$K_{VG}$	0.5	D	0.5
$K_{VD}$	<del>10</del> 10.125	$V_G$	10

Margins and associated frequencies:

Gain Margin	Phase Crossover Frequency	Phase Margin	Gain Crossover Frequency
Infinite	<del>Never</del> infinite	15.6	942

Step response characteristics table:

	PECS	Matlab	
Vg step:	0.5	<del>0.5</del>	1.15 and 1.24
Vg step SSE:	498mV	498mV	
$i_{out}$ :	1946mV	<del>176mV</del>	2.92V and 3.41V
$i_{Out}$ : SSE	174mV	184mV	

Comparison of results for V and Iout changes:

It may be due to the fact that the model we use in Matlab takes the assumption that  $r_L + R = R$  where in the PECS simulation it includes  $r_L$  in all of the calculations. Some additional artifacts may arise in the fact we are adding a large signal step after simulation to the output of matlab. **Matlab simplification of switching**

Simple symbolic expression for SSE for a step in v:

$$\text{Error} = R(s) - C(s)$$

$$C(s)=R(s)T(s)$$

$$T(s) = \frac{D}{1+(\frac{s}{\omega_0 Q})+(\frac{s}{\omega_0})^2}$$

$$R(s)=\frac{1}{s}$$

$$\text{Error} = R(s)(1 - T(s))$$

$$= \frac{Qs^2 + \omega_0 s - (D-1)Q\omega_0^2}{Qs^2 + \omega_0 s + Q\omega_0^2}$$

When ~~s~~→0

SSE = 1-D

## Lab 3 Grading Sheet

### 1. Task 1:

- (i) Your PECS schematic\_\_\_\_\_ /1
- (ii) Start-up transient plot \_\_\_\_\_ /1
- (iii) Steady state output voltage value\_\_\_\_\_ /1

### 2. Task 2:

- (i) Plot of output voltage, diode voltage and switch current in proper format  
/3
- (ii) Average output voltage value\_\_\_\_\_ /1
- (iii) Peak-to-peak output voltage ripple value\_\_\_\_\_ /1
- (iv) Peak-to-peak diode voltage value\_\_\_\_\_ /1
- (v) Peak inductor current\_\_\_\_\_ /1
- (vi) Switching frequency\_\_\_\_\_ /1
- (vii) Duty ratio\_\_\_\_\_ /1
- (viii) Explanation of how duty ratio is set \_\_\_\_\_ /2

### 3. Task 3:

- (i) Simulation plot\_\_\_\_\_ /1
- (ii)  $K_{vg}$ \_\_\_\_\_ /2
- (iii)  $\Delta v$ \_\_\_\_\_ /1
- (iv) SSE\_\_\_\_\_ /1

### 4. Task 4:

- (i) Your PECS schematic\_\_\_\_\_ /1
- (ii) Filter corner frequency in  $Hz$ .\_\_\_\_\_ /1
- (iii) Plot of VP3 and VP1 in proper format\_\_\_\_\_ /1
- (iv) Peak-to-peak of VP3 and of VP1\_\_\_\_\_ /2
- (v) In-phase or out of phase?\_\_\_\_\_ /1
- (vi)  $K_{vd}$ \_\_\_\_\_ **1**\_\_\_\_\_ /2

### 5. Task 5

- (i) Your PECS schematic\_\_\_\_\_ /1
- (ii) Simulation plot of VP1\_\_\_\_\_ /1
- (iii)  $\Delta v$ \_\_\_\_\_ /1
- (iv) SSE\_\_\_\_\_ /1

### 6. Task 6a:

- (i) Loop gain transfer function\_\_\_\_\_ /2
- (ii) Your complete MATLAB code\_\_\_\_\_ /1
- (iii) Matlab plot\_\_\_\_\_ /1

(iv) Unity gain and phase crossover frequencies, phase and gain margins values  
/2

7. Task 6b:

(i)  $G_{vd}$  transfer function \_\_\_\_\_/2

(ii) Your Matlab code \_\_\_\_\_/1

(iii) Your Matlab plot \_\_\_\_\_/1

8. Task 6c:

(i)  $-Z_{out}$  transfer function \_\_\_\_\_/2

(ii) Your Matlab code \_\_\_\_\_/1

(iii) Your Matlab plot \_\_\_\_\_/1

9. Task 6d:

(i) Your complete Matlab code \_\_\_\_\_/1

(ii) Matlab plot \_\_\_\_\_/1

(iii)  $\Delta v$  \_\_\_\_\_/1

(iv) SSE \_\_\_\_\_/1

10. Task 6e:

(i)  $Z_{out}$  transfer function \_\_\_\_\_/1

(ii) Your Matlab code \_\_\_\_\_/1

(iii) Your Matlab plot \_\_\_\_\_/1

(iv)  $\Delta v$  \_\_\_\_\_/1

(v) SSE \_\_\_\_\_/1

11. Results (summary):

(i) Transfer function DC gains' table \_\_\_\_\_ **2.5** \_\_\_\_\_/3

(ii) Margins and associated frequencies table \_\_\_\_\_ **1.5** \_\_\_\_\_/2

(iii) Step response characteristics table \_\_\_\_\_ **1** \_\_\_\_\_/2

(iv) Comparison of results for  $\Delta v$  and  $i_{out}$  changes \_\_\_\_\_ **1** \_\_\_\_\_/2

(v) Simple symbolic expression for SSE for a step in  $\Delta v$  \_\_\_\_\_ **1** \_\_\_\_\_/2

Report: \_\_\_\_\_/5

**Total:** \_\_\_\_\_ **65** \_\_\_\_\_/70