

2.1

a)

$$M = 1$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(2/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 4.199} \leq 0.05$$

$$(1/2N) \times 4.199 \leq 0.0025$$

$$(4.199/0.005) < N$$

$$840 \leq N$$

b)

$$M = 100$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(200/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 8.8} \leq 0.05$$

$$(1/2N) \times 8.8 \leq 0.0025$$

$$(8.8/0.005) < N$$

$$1760 \leq N$$

c)

$$M = 10,000$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(20,000/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 13.41} \leq 0.05$$

$$(1/2N) \times 13.41 \leq 0.0025$$

$$(13.41/0.005) \leq N$$

$$2682 \leq N$$

2.11 (a)  $N = 100$

$$E_{out}(g) \leq \sqrt{E_{in}(g)(8/N)\ln((4m_h(2N)/\delta))}$$

$$E_{out}(g) \leq \sqrt{E_{in}(g)(8/100)\ln((404(200)/.1))}$$

$$E_{out}(g) \leq E_{in}(g) + 1.043$$

(b)  $N = 1000$

$$E_{out}(g) \leq \sqrt{E_{in}(g)(8/N)\ln((4m_h(2N)/\delta))}$$

$$E_{out}(g) \leq \sqrt{E_{in}(g)(8/1000)\ln((4004(2000)/.1))}$$

$$E_{out}(g) \leq E_{in}(g) + 0.356605$$

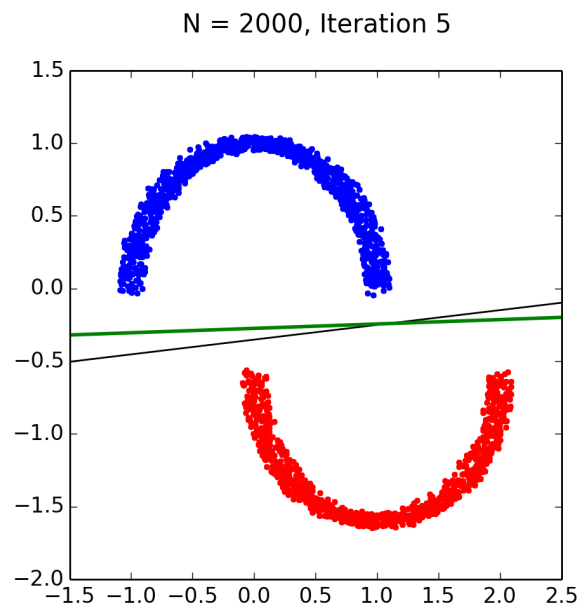
2.12

You would need a sample size of approximately 420,000.

(Updated version on Github)

Problem 3.1

(a) The final hypothesis is  $[-1, 0.1103083, -3.64935025]$



(b)  $[-0.32275335, 0.09317685, -0.91814928]$

Using the perceptron, it is taking a risk that the hypothesis may not be as accurate. However, using the linear regression, you are getting a more static result.