

2.1

a)

$$M = 1$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(2/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 4.199} \leq 0.05$$

$$(1/2N) \times 4.199 \leq 0.0025$$

$$(4.199/0.005) < N$$

$$840 \leq N$$

b)

$$M = 100$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(200/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 8.8} \leq 0.05$$

$$(1/2N) \times 8.8 \leq 0.0025$$

$$(8.8/0.005) < N$$

$$1760 \leq N$$

c)

$$M = 10,000$$

$$E_{out}(g) \leq E_{in}(g) + \sqrt{(1/2N)\ln(2M/\delta)}$$

$$(M, N, \delta) = \sqrt{(1/2N)\ln(2M/\delta)} \leq 0.05$$

$$\sqrt{(1/2N)\ln(20,000/0.03)} \leq 0.05$$

$$\sqrt{(1/2N) \times 13.41} \leq 0.05$$

$$(1/2N) \times 13.41 \leq 0.0025$$

$$(13.41/0.005) < N$$

$$2682 \leq N$$