Student: Date:	Instructor: Richeng Piao Course: ECON 2560 - Applied Econometrics	Assignment: Practice Problem Set 2
provided to me are intended solely for personal question set available to any third parties with	cribute the practice question set. I understand a late and reference. I will not share, copy, reprout explicit authorization from the rightful owner associated with the practice question set and with	roduce, distribute, or make the practice r or the authorized distributor. I respect the
Signature		Date
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Signature		Date
Determine whether the following variables a	are random or not:	
1. The gender of the next person you will recommendate the number of days in a week. (2)	om (3) Random (4) Random	dom (5) ORandom random Not random
ID: Review Concept 2.1		
·	✓ are independent and you know their distribution	one
• •	g the value of $X$ tells you nothing about the value	
<ul> <li>A. The variance of X might be different</li> <li>B. X and Y might be independent.</li> <li>C. The mean of X might be different from D. All of the above.</li> </ul>	from the variance of Y.	
Answer: B. X and Y might be independent		
ID: Review Concept 2.2		

3.		tX denotes the amount of raing the same month.	nfall in your home	etown during a g	given month and \	Y denotes the nur	mber of children	ı born in Los
	Which of the	following statements best ex	plains why $oldsymbol{\mathit{X}}$ and	Y are not indep	endent?			
	OA. The a	amount of rainfall may tell you	ı something abou	it the season an	d, since births are	e seasonal, it may	y also tell you so	omething abou
	OB. The v	variance for the amount of rai	nfall in inches is	equal to the vari	ance of the numb	er of children bor	'n.	
	O. The r	atio of the amount of rainfall	in inches to the n	umber of childre	n born is usually	one.		
	O D. The e	expected value of rainfall in in	ches is equal to	the expected nu	mber of children b	oorn.		
		e amount of rainfall may tell yout the number of children bo	-	out the season	and, since births a	are seasonal, it m	nay also tell you	. something
	ID: Review	Concept 2.3						
4.	the random v	number of applicants who apparaishe $X$ is given in the follower table by calculating the cum	wing table. The o	utcomes (numbe	er of applicants) a			stribution of
				Outcom	e (Number of ap	plicants)		7
			0	1	2	3	4	
		Probability distribution	0.35	0.30	0.12	0.15	0.08	
		Cumulative probability distribution						]
		ity that there will be at least to	L	,	and the probabili	ty that there will b	oe at most three	applicants is
	Answers 0.3	35						
	0.6	65						
	0.7	77						
	0.0	92						
	1.0	00						
	0.3	35						
	0.0	92						
	0.2	23						
	ID: Concep	t Exercise 2.1.1						

5.	An econometrics class has 80 students, and the mean student weight is 145 lb. A random sample of four students is selected from the class, and their average weight is calculated. Will the average weight of the students in the sample equal 145lb?
	O A. Yes.
	○ B. No.
	Using this example, which of the following best explains the sample average $\overline{Y}$ ?
	$\bigcirc$ <b>A.</b> The value of $\overline{Y}$ is not random, but it differs from one sample to the next.
	$\bigcirc$ <b>B.</b> Although each observation $Y_i$ is random, the value of their average, $\overline{Y}$ , is not random. $\overline{Y}$ is equal to the population mean.
	$\bigcirc$ <b>C.</b> Because each observation $Y_i$ is drawn at random, the value of their average, $\overline{Y}$ , is also random. The value of $\overline{Y}$ differs from one same
	$\bigcirc$ <b>D.</b> The value of $\overline{Y}$ is random. However, it is the same for all samples.
	Answers B. No.
	C.
	Because each observation $Y_i$ is drawn at random, the value of their average, $\overline{Y}$ , is also random. The value of $\overline{Y}$ differs from one sample to the next.
	one sumple to the next.
	ID: Review Concept 2.4

6.	Observe that for a random variable	Y that takes on values	0 and 1, the expe	cted value of Yi	s defined as follows

$$E(Y) = 0 \times Pr(Y=0) + 1 \times Pr(Y=1)$$

Now, suppose that X is a Bernoulli random variable with success probability Pr(X = 1) = p. Use the information above to answer the following questions.

Show that  $E(x^8) = p$ .

$$E(x^8) = ( \times ) + ( \times p) =$$

(Use the tool palette on the right to insert superscripts. Enter you answer in the same format as above.)

Suppose that p = 0.16.

Compute the mean of X.

(Round your response to two decimal places)

Compute the variance of X.

(Round your response to three decimal places)

Compute the skewness of X using the following formula:

$$\frac{E(X-E(X))^3}{\sigma^3} = \frac{E\left(X^3\right) - 3\left[E\left(X^2\right)\right]\left[E(X)\right] + 2\left[E(X)\right]^3}{\sigma^3}$$

(Round your response to three decimal places)

Compute the kurtosis of *X* using the following formula:

$$\frac{E(X-E(X))^4}{\sigma^4} = \frac{E\left(X^4\right) - 4[E(X)]\left[E\left(X^3\right)\right] + 6[E(X)]^2 \left[E\left(X^2\right)\right] - 3[E(X)]^4}{\sigma^4}$$

(Round your response to three decimal places)

Answers 0

$$1 - p$$

1

р

0.16

0.134

1.864

4.470

7.	In May, Seattle's daily high temperature has a mean of 65°F and a standard deviation of 7°F.
	The formula to convert degrees Fahrenheit °F to degrees Celsius °C is:
	$^{\circ}$ C = $\frac{5}{9}$ ( $^{\circ}$ F - 32)
	Use this information to answer the following questions.
	Compute the mean of Seattle's daily high temperature in degrees Celsius °C.
	The mean of the daily high temperature in degrees Celcius = C
	(Round your response to three decimal place.)
	Compute the standard deviation of Seattle's daily high temperature in degrees Celsius °C.
	The standard deviation of the daily high temperature in degrees Celisius = C
	(Round your response to three decimal places)
	Compute the variance of Seattle's daily high temperature in degrees Celsius °C.
	The variance of the daily high temperature in degrees Celsius = C
	(Round your response to three decimal places)
	Answers 18.333
	3.889
	15.124
	ID: Exercise 2.5

8.	Suppose the random variable Y has a mean of 36 and a variance of 25. Let $Z = \frac{1}{\sqrt{25}}(Y - 36)$ .
	Show that $\mu_Z = 0$ .
	$\mu_{Z} = E \begin{bmatrix} & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & \\ & & \\ & & \\ & & \\ & & \\ & \\ & & \\ & \\ & & \\ & \\ & \\ & & \\ & \\ & \\ & \\ & \\ & $
	(Round your responses to two decimal places)
	Show that $\sigma_Z^2 = 1$ .
	$\sigma_Z^2 = var \left[                                   $
	(Round your responses to two decimal places)
	Answers 0.20
	36
	0.20
	36
	0.20
	36
	0.04
	ID: Exercise 2.8
9.	The expected value of a discrete random variable:
	○ A. is the outcome that is most likely to occur.
	O B. is computed as a weighted average of the possible outcome of that random variable, where the weights are the probabilities of that
	○ C. equals the population median.
	O. can be found by determining the 50% value in the c.d.f.
	Answer: B.  is computed as a weighted average of the possible outcome of that random variable, where the weights are the probabilities of that outcome.
	ID: Test A Ex 2.2.1

10. The variance of $\overline{Y}$ , $\sigma_{\overline{Y}}^2$ is given by the following formu	10.	following formula
--	-----	-------------------

- $\bigcirc$  A.  $\sigma_{Y}^{2}$ .
- $\bigcirc$  B.  $\frac{\sigma_Y^2}{n}$
- $\bigcirc$  C.  $\sigma_{Y}$   $\frac{\sigma_{Y}}{\sqrt{n}}$
- $\bigcirc \ \mathbf{D}. \quad \frac{\sigma_Y^2}{\sqrt{n}}.$

Answer:  $\sigma_{Y}^{2}$ .

ID: Test A Ex 2.2.2

11. 
$$\sum_{i=1}^{n} \left(ax_i + b\right) =$$

- $\bigcirc$  **A.**  $n \times a \times \overline{x} + n \times b$ .
- $\bigcirc$  **B.** n(a+b).
- $\bigcirc$  C.  $n \times a + \overline{x}$ .
- $\bigcirc$  D.  $\bar{x} + n \times b$ .

Answer: A.  $n \times a \times x + n \times b$ .

ID: Test A Ex 2.2.3

## 12. The mean and variance of a Bernoulli random variable are given as:

- A. cannot be calculated.
- $\bigcirc$  **B.** *p* and *p*(1 *p*).
- $\bigcirc$  **C.** np and np(1-p).
- O. p and  $\sqrt{p(1-p)}$ .

Answer: B. p and p(1-p).

ID: Test A Ex 2.2.4

13. For a normal distribution, the <i>skewness</i> and <i>kurtosis</i> measures are as for
--

- O A. 1 and 2.
- OB. 1.96 and 4.
- Oc. 0 and 3.
- O and 0.

Answer: C. 0 and 3.

ID: Test B Ex 2.2.1

14. 
$$\sum_{i=1}^{n} \left( ax_i + by_i + c \right) =$$

- **A.**  $a \sum_{i=1}^{n} x_i + b \sum_{i=1}^{n} y_i + c$ .
- **B.**  $a \sum_{i=1}^{n} x_i + b \sum_{i=1}^{n} y_i + n \times c.$
- $\bigcirc$  C.  $a\bar{x} + b\bar{y} + n \times c$ .
- O.  $a \sum_{i=1}^{n} x_i + b \sum_{i=1}^{n} y_i$ .

Answer:  
B. 
$$a \sum_{i=1}^{n} x_i + b \sum_{i=1}^{n} y_i + n \times c$$
.

ID: Test B Ex 2.2.2

## 15. Assume that you assign the following subjective probabilities for your final grade in your econometrics course (the standard GPA scale of 4 = A to 0 = F applies):

Grade	Probability
Α	0.20
В	0.50
С	0.20
D	80.0
F	0.02

The expected value is:

- O A. 3.5.
- **B.** 3.0.
- Oc. 3.25.
- O D. 2.78.

Answer: D. 2.78.

ID: Test B Ex 2.2.3

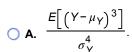
	$y = \frac{x - \mu_X}{}$					
	$\sigma_{\chi}$					
	where $\mu_{x}$ is the mean of x and $\sigma_{x}$ is the standard deviation. Then the expected value and the standard deviation of Y are given as:					
	O A. 0 and 1.					
	Cannot be computed because Y is not a linear function of X.					
	O. 1 and 1.					
	Answer: A. 0 and 1.					
	ID: Test B Ex 2.2.4					
17.	In a basketball match, a shooting guard can either throw the ball in the basket and score points for his team or miss it and not score. Each successful basket is worth one point.					
	The shooting guard's ball throw is an example of a (1) random variable, because the outcomes are (2)					
	Suppose the shooting guard successfully throws the ball in the basket 4 out of 10 times. Complete the probability distribution of the shooting guard's ball throws (X).					
	X Successful throw Unsuccessful throw					
	P(X)					
	The expected value of the shooting guard's throw is, and its variance is					
	Now assume that each successful basket is worth two points.					
	The expected value of the shooting guard's throw is and its variance is .					
	and to talking it is a short of grant of the first of the far and					
	(1) O Bernoulli (2) O binary O continuous O a continuum of possible values					
	Answers (1) Bernoulli					
	(2) binary					
	0.4					
	0.6					
	0.4					
	0.24					
	0.8					
	0.96					
	ID: Concept Exercise 2.2.1					

16. Consider the following linear transformation of a random variable

18.	Suppose Walmart introduces an offer of a flat 35% discount on the entire bill for the purchase of any electronic item. It also offers an additional \$75 discount on the entire bill for the purchase of any kitchenware item, conditional on the purchase of an electronic item. Let <i>X</i> denote the before-discount expenditure of a shopper who purchases both an electronics item and a kitchenware item, and let <i>Y</i> denote this shopper's after-discount expenditure.
	If $\sigma_X$ denotes the standard deviation of this shopper's before-discount expenditure, the standard deviation of the after-discount
	expenditure of this shopper is
	(Carefully enter your response as an algebraic expression, using the proper notation in the proper format.)
	The value of variance is
	○ A. always non-negative.
	O B. always positive.
	O. always negative.
	On none of the above.
	Answers $0.65\sigma_{\chi}$
	A. always non-negative.
	ID: Concept Exercise 2.2.2

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19. Which of the following expressions is used to calculate the skewness of a distribution?



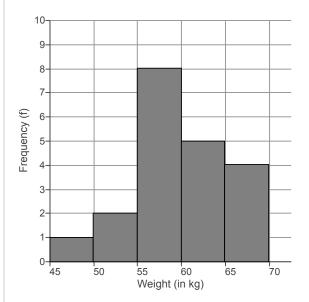
- $\bigcirc \ \mathbf{B.} \ \frac{ \textit{E} \Big[ \big( \mathbf{Y}^{-} \mu_{\mathbf{Y}} \big)^{3} \Big] }{ \sigma_{\mathbf{Y}}^{3} }.$
- $\bigcirc \mathbf{c.} \ \frac{E\left[\left(Y^{-}\mu_{Y}\right)^{4}\right]}{\sigma_{Y}^{4}}.$
- $\bigcirc \ \mathbf{D.} \ \frac{ \textit{E} \left[ \left( \mathbf{Y}^{-} \boldsymbol{\mu}_{\mathbf{Y}} \right)^{2} \right] }{ \sigma_{\mathbf{Y}}^{2} }.$

The given figure shows a histogram. The histogram suggests that the distribution is (1) \_\_\_\_\_.

The kurtosis of this distribution is (2) \_\_\_\_\_.

- (1) O symmetrical
- (2) onegative
- negatively skewed
- o positive
- positively skewed

- Answers B.  $\frac{\textit{E}\!\left[\left(\mathbf{Y}^{-}\boldsymbol{\mu}_{\mathbf{Y}}\right)^{3}\right]}{\sigma_{\mathbf{Y}}^{3}}.$ 
  - (1) negatively skewed
  - (2) positive
- ID: Concept Exercise 2.2.3



Joint Distribution of Weather Conditions and Commuting Times

	Rain (X = 0)	No Rain ( <i>X</i> = 1)	Total
Long commute (Y = 0)	0.17	0.10	0.27
Short commute (Y = 1)	0.18	0.55	0.73
Total	0.35	0.65	1.00

Compute the mean of	FΥ

(Round your response to two decimal places)

Compute the mean of X.

(Round your response to two decimal places)

Compute the variance of X.

$$\sigma_X^2 =$$

(Round your response to four decimal places)

Compute the variance of Y.

$$\sigma_Y^2 =$$

(Round your response to four decimal places)

Compute the covariance of X and Y.

(Round your response to four decimal places)

Compute the correlation of X and Y.

(Round your response to four decimal places)

Answers 0.73

0.65

0.2275

0.1971

0.0755

0.3565

21. Use the probability distribution given in the table below and consider two new random variables, W = 9 + 3X and V = 1 + 2Y, to answer the following questions

Joint Distribution of Weather Conditions and Commuting Times

	Rain (X = 0)	No Rain (X = 1)	Total
Long commute (Y = 0)	0.19	0.10	0.29
Short commute (Y = 1)	0.68	0.03	0.71
Total	0.87	0.13	1.00

Compute the mean of M	/.
-----------------------	----

<b>-</b> /14A			
=(MA)	- 1		
$\square$	_		

(Round your response to two decimal places)

Compute the mean of V.

(Round your response to two decimal places)

Compute the variance of W.

$$\sigma_W^2 =$$

(Round your response to four decimal places)

Compute the variance of V.

$$\sigma_V^2 =$$

(Round your response to four decimal places)

Compute the covariance between  $\it W$  and  $\it V$ .

(Round your response to four decimal places)

Compute the correlation between W and V.

(Round your response to four decimal places)

Answers 9.39

2.42

1.0179

0.8236

-0.3738

-0.4083

22. The following table gives the joint probability distribution between employment status and college graduation among those either employed or looking for work (unemployed) in the working age U.S. population.

	Unemployed (Y=0)	Employed (Y=1)	Total
Non-college grads (X = 0)	0.0616	0.6263	0.6879
College grads (X = 1)	0.0150	0.2971	0.3121
Total	0.0766	0.923	0.9996

The expected value of $Y$ , denoted $E(Y)$ , is	. (Round your response to three decimal places.

y 1 - E(Y).

The unemployment rate is the fraction of the labor force that is unemployed. Show that the unemployment rate is given by $1 - E(Y)$
Unemployment rate = $1 - E(Y) = 1 - 0.923 = 0.0766$ .
$E(Y \mid X=1)$ is . (Round your response to three decimal places.)
$E(Y \mid X = 0)$ is . (Round your response to three decimal places.)
The unemployment rate for college graduates is, and the unemployment rate for non-college graduates is (Round your responses to three decimal places.)
A randomly selected member of this population reports being unemployed. The probability that this worker is a college graduate is , and the probability that this worker is a non-college graduate is . (Round your responses to three

Are educational achievement and employment status independent?

- $\bigcirc$  **A.** Since Pr (X = 0 | Y = 1) = Pr (X = 0), educational achievement and employment status are independent.
- $\bigcirc$  **B.** Since Pr (X = 0, Y = 1) = Pr (X = 0), educational achievement and employment status are independent.
- $\bigcirc$  C. Since Pr (X = 0, Y = 1)  $\neq$  Pr (X = 0), educational achievement and employment status are not independent.
- $\bigcirc$  **D.** Since Pr  $(X=0 \mid Y=1) \neq$  Pr (X=0), educational achievement and employment status are not independent.

Answers 0.923

decimal places.)

Pr(Y = 1)

0.952

0.910

0.048

0.09

0.196

0.804

D. Since  $Pr(X=0 \mid Y=1) \neq Pr(X=0)$ , educational achievement and employment status are not independent.

Suppose that w = 0.46. Compute the mean and standard deviation of R.  The mean is	23. Suppose you have some money to invest—for simplicity, \$1—and you are planning to put a fraction $w$ into a stock market may and the rest, $1-w$ , into a bond mutual fund. Suppose that \$1 invested in a stock fund yields $R_s$ after 1 year and that \$1 invested fund yields $R_b$ , suppose that $R_s$ is random with mean 0.07 (7%) and standard deviation 0.06, and suppose that $R_b$ is random with mean 0.05 (5%) and standard deviation 0.04. The correlation between $R_s$ and $R_b$ is 0.23. If you place a fraction $w$ of your most stock fund and the rest, $1-w$ , in the bond fund, then the return on your investment is $R = wR_s + (1-w)R_b$ .							
The standard deviation is		Suppose that $w = 0.46$ . Compute the mean and standard deviation of $R$ .						
Suppose that w = 0.69. Compute the mean and standard deviation of R.  The mean is		The mean is . (Round your response to three decimal places.)						
The mean is		The standard deviation is . (Round your response to three decimal places.)						
The standard deviation is		Suppose that $w = 0.69$ . Compute the mean and standard deviation of $R$ .						
What value of w makes the mean of R as large as possible?  w = maximizes \(  \) (Round your response to two decimal places.)  What is the standard deviation of R for this value of w?  \( \sigma = \) for this value of w. (Round your response to two decimal places.)  What is the value of w that minimizes the standard deviation of R?  \( \text{w} = \) minimizes the standard deviation of R. (Round your response to two decimal places.)  Answers 0.059  0.039  0.064  0.045  1  0.06  0.26  ID: Exercise 2.22  24. The correlation between X and Y:  A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr (X, Y) = \( \frac{\cov (X, Y)}{\vert \cov (X, Y)} \).  Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.		The mean is . (Round your response to three decimal places.)						
w = maximizes $\mu$ . (Round your response to two decimal places.)  What is the standard deviation of $R$ for this value of $w$ ? $\sigma$ = for this value of $w$ . (Round your response to two decimal places.)  What is the value of $w$ that minimizes the standard deviation of $R$ ? $w$ = minimizes the standard deviation of $R$ . (Round your response to two decimal places.)  Answers 0.059  0.039  0.045  1  0.06  0.26  ID: Exercise 2.22  24. The correlation between $X$ and $Y$ :  A. can be calculated by dividing the covariance between $X$ and $Y$ by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr $(X,Y)$ = $\frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between $X$ and $Y$ by the product of the two standard deviations.		The standard deviation is . (Round your response to three decimal places.)						
What is the standard deviation of <i>R</i> for this value of <i>w</i> ?  \[ \sigma = \qquad \text{for this value of } \sigma. \text{(Round your response to two decimal places.)} \]  What is the value of w that minimizes the standard deviation of <i>R</i> ?  \[ w = \qquad \text{minimizes the standard deviation of } \text{ <i>R. (Round your response to two decimal places.)} \]  Answers 0.059  0.039  0.064  0.045  1  0.06  0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i>:  \[ \text{A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  \[ \text{B. is the covariance squared.} \]  \[ \text{C. cannot be negative since variances are always positive.} \]  \[ \text{D. }  \text{is given by corr } (X,Y) = \frac{\cov (X,Y)}{\var (X)\var(Y)}. \]  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.</i>		What value of w makes the mean of R as large as possible?						
<ul> <li>σ = for this value of w. (Round your response to two decimal places.)</li> <li>What is the value of w that minimizes the standard deviation of R?</li> <li>w = minimizes the standard deviation of R. (Round your response to two decimal places.)</li> <li>Answers 0.059 <ul> <li>0.039</li> <li>0.064</li> <li>0.045</li> <li>1</li> <li>0.06</li> <li>0.26</li> </ul> </li> <li>ID: Exercise 2.22</li> </ul> <li>24. The correlation between X and Y:  <ul> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y)/var (X)var(Y).</li> </ul> </li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li>		$w = $ maximizes $\mu$ . (Round your response to two decimal places.)						
What is the value of w that minimizes the standard deviation of R?  w =		What is the standard deviation of <i>R</i> for this value of <i>w</i> ?						
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Answers 0.059 0.039 0.064 0.045 1 0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = $\frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.		What is the value of w that minimizes the standard deviation of R?						
0.039 0.064 0.045 1 0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = $\frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.		w =  minimizes the standard deviation of $R$ . (Round your response to two decimal places.)						
0.045 1 0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = $\frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.		Answers 0.059						
0.045 1 0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = $\frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.								
1 0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = \frac{\cov ( <i>X</i> , <i>Y</i> )}{\var( <i>X</i> )\var( <i>Y</i> )}.  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.		0.064						
0.06 0.26  ID: Exercise 2.22  24. The correlation between <i>X</i> and <i>Y</i> :  A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.  B. is the covariance squared.  C. cannot be negative since variances are always positive.  D. is given by corr ( <i>X</i> , <i>Y</i> ) = $\frac{\text{cov}(X,Y)}{\text{var}(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.		0.045						
<ul> <li>D: Exercise 2.22</li> <li>The correlation between X and Y: <ul> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> </ul> </li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>		1						
<ul> <li>ID: Exercise 2.22</li> <li>24. The correlation between X and Y:</li> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>		0.06						
<ul> <li>24. The correlation between X and Y:</li> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>		0.26						
<ul> <li>24. The correlation between X and Y:</li> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>		ID: Exercise 2 22						
<ul> <li>A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>								
<ul> <li>B. is the covariance squared.</li> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>	24.	The correlation between <i>X</i> and <i>Y</i> :						
<ul> <li>C. cannot be negative since variances are always positive.</li> <li>D. is given by corr (X,Y) = cov (X,Y) / var (X)var(Y).</li> <li>Answer: A. can be calculated by dividing the covariance between X and Y by the product of the two standard deviations.</li> </ul>	○ B. is the covariance squared.							
is given by corr $(X,Y) = \frac{\text{cov }(X,Y)}{\text{var }(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between $X$ and $Y$ by the product of the two standard deviations.								
is given by corr $(X,Y) = \frac{(X,Y)}{\text{var}(X)\text{var}(Y)}$ .  Answer: A. can be calculated by dividing the covariance between $X$ and $Y$ by the product of the two standard deviations.								
		is given by corr $(X,Y) = \frac{\cot(X,Y)}{\cot(X)\cot(Y)}$ .						
ID: Test A Ex 2.3.5		Answer: A. can be calculated by dividing the covariance between <i>X</i> and <i>Y</i> by the product of the two standard deviations.						
		ID: Test A Ex 2.3.5						

25. The following table gives the joint probability distribution of the speed of a car (*C*) and the incidence of an accident (*A*), where *A* = 0 when no accidents have occured and *A* = 1 when an accident has occured:

	<b>C</b> = 25 kmph	C = 45 kmph	<b>C</b> = 95 kmph
A = 0	0.02	0.05	0.15
A = 1	0.08	0.25	0.45

Complete the following table with the marginal distributions of the speed of a car (C) and the incidence of an accident (A).

	<b>C</b> = 25 kmph	<b>C</b> = 45 kmph	<b>C</b> = 95 kmph	Marginal probability (A)
A = 0	0.02	0.05	0.15	
A = 1	0.08	0.25	0.45	
Marginal probability (C)				

Complete the following table with the conditional distribution of the speed of a car given the incidence of an accident, i.e., C given A.

	<b>C</b> = 25 kmph	<b>C</b> = 45 kmph	<b>C</b> = 95 kmph	Total
Pr(C A=0)				
Pr(C A = 1)				

(Round your answers to two decimal places.)

The conditional expectation of the speed of the car, given no accidents take place, $E(C A=0)$ , is kmph.	
And, the conditional expectation of the speed of the car, given an accident takes place, $E(C A=1)$ , is kmph.	
(Round your answers to two decimal places.)	
The probability $Pr(C = 95 A = 1) = $ and the probability $Pr(C = 95) = $ .	
The probability of having an accident (A) and the speed of a car (C) are (1) events because (2)	

- (1) O dependent
- (2)  $\bigcirc Pr(C = 95|A = 1) = Pr(C = 95)$
- independent
- $\bigcirc$  Pr(C = 95|A = 1)  $\neq$  Pr(C = 95)

Answers 0.22

0.78

0.10

0.30

0.60

1.00

0.09

0.23

0.68

1.00

0.10

0.32

0.58

1.00

77.20

(1) dependent

72.00 0.58 0.60

(2)  $Pr(C = 95|A = 1) \neq Pr(C = 95)$ 

ID: Concept Exercise 2.3.1

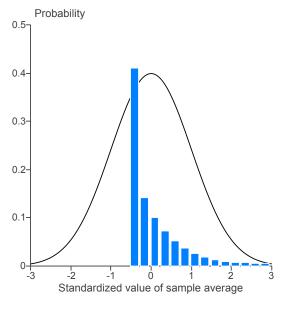
26.	Let there be two players in a game, Player 1 and Player 2. Consider a jar containing 5 snakes. 3 of the snakes in the jar are venomous, while the remaining 2 are non-venomous. In the game, both the players have to put their hand in the jar one after the other and pick a snake out. Each snake, if picked out of the jar, will bite the player's hand. The event of picking a venomous snake, or equivalently, a venomous snake's bite will earn the player zero points. On the other hand, the event of picking a non-venomous snake, or equivalently, a non-venomous snake's bite will earn the player one point.					
	Let X denote Player 1's pick and let Y denote Player 2's pick. Suppose Player 1 is the first to pick out a snake.					
	The expected value of Player 1's pick is: $E(X) = $					
	(Express your answer as a fraction or round your answer to two decimal places.)					
	The expected value of Player 2's pick is: $E(Y) = $					
	(Express your answer as a fraction or round your answer to two decimal places.)					
	Which of the following statements describes the relationship between $E(X)$ and $E(Y)$ in this example?					
	$\bigcirc$ <b>A.</b> E(X) and E(Y) are independent of each other. Their values do not reflect anything about their relationship.					
	$\bigcirc$ <b>B.</b> E(Y) is greater than E(X) as there is a greater possibility that Player 1 picks up a venomous snake.					
	○ C. E(X) is greater than E(Y) because Player 1 has an advantage of picking first.					
	$\bigcirc$ <b>D.</b> E(X) and E(Y) are equal, so the order in which the players pick a snake is irrelevant.					
	Answers 2					
	5					
$\frac{2}{5}$						
	D. E(X) and E(Y) are equal, so the order in which the players pick a snake is irrelevant.					
	ID: Concept Exercise 2.3.2					

27. The table gives the joint probability distribution of the number of sports an individual plays (X) and the number of times she may get injured while playing (Y).

	X=1	X = 2	X=3
Y=4	0.12	0.08	0.15
Y=3	0.05	0.05	0.06
Y=2	0.10	0.03	0.15
Y=1	0.15	0.04	0.02

	The covariance between $X$ and $Y$ , $\sigma_{XY}$ , is
	(Round your answer to two decimal places. Enter a minus sign if your answer is negative.)
	The correlation between $X$ and $Y$ , $corr(X, Y)$ , is
	(Round your answer to two decimal places. Enter a minus sign if your answer is negative.)
	An increase in the number of sports an individual plays will tend to (1) the number of times she may get injured while playing.
	(1) increase
	O decrease
	Answers 0.23
	0.22
	(1) increase
	ID: Concept Exercise 2.3.3
28.	Suppose that $Y_1,, Y_n$ are i.i.d. random variables with a $N(\mu_Y, \sigma_Y^2)$ distribution. How would the probability density of $\overline{Y}$ change as the sample size $n$ increases?
	Hint: Think about the law of large numbers.
	$\bigcirc$ <b>A.</b> As the sample size increases, the variance of $\overline{Y}$ decreases. So, the distribution of $\overline{Y}$ becomes highly concentrated around $\mu_{Y}$ .
	$\bigcirc$ <b>B.</b> As the sample size increases, the variance of $\overline{Y}$ increases. So, the distribution of $\overline{Y}$ becomes highly concentrated around $\mu_{Y}$ .
	$\bigcirc$ <b>C.</b> As the sample size increases, the variance of $\overline{Y}$ increases. So, the distribution of $\overline{Y}$ becomes less concentrated around $\mu_{Y}$ .
	$\bigcirc$ <b>D.</b> As the sample size increases, the variance of $\overline{Y}$ decreases. So, the distribution of $\overline{Y}$ becomes less concentrated around $\mu_{\overline{Y}}$ .
	Answer: A. As the sample size increases, the variance of $\overline{Y}$ decreases. So, the distribution of $\overline{Y}$ becomes highly concentrated around $\mu_Y$ .
	ID: Review Concept 2.5

29. Suppose that  $Y_1$ , ...,  $Y_n$  are i.i.d. random variables with the probability distribution given in the figure below.



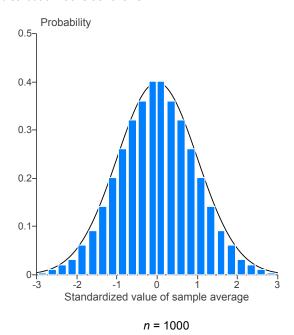
n = 25

Suppose further that you want to calculate Pr  $(\overline{Y} \le 0.1)$ .

Would it be reasonable to use the normal approximation if n = 25?

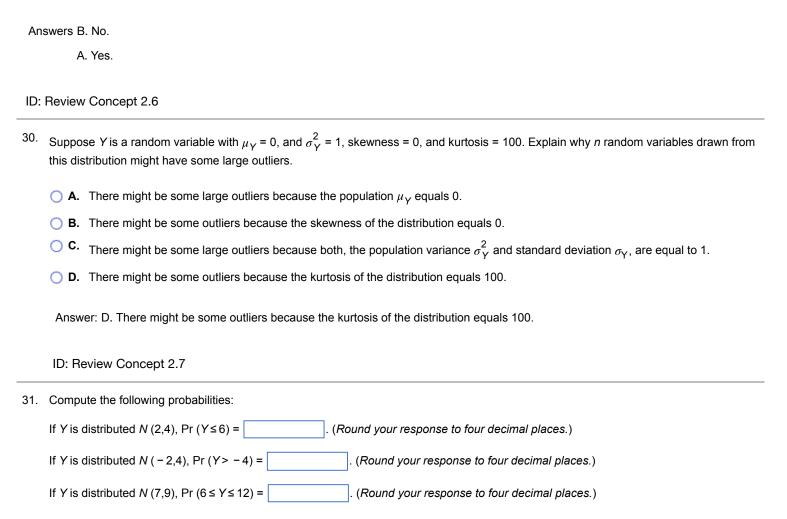
- OA. Yes.
- O B. No.

Now suppose that with n = 1000 the distribution looks as follows.



Would it be reasonable to use the normal approximation now?

- O A. Yes.
- O B. No.



Answers 0.9772

0.8413

0.5818

32. The following table contains data on the joint distribution of age (*Age*) and average hourly earnings (*AHE*) for 25 to 34 year-old full-time workers with an educational level that exceeds a high school diploma in 2012. Download the data from the table by clicking the *download table* icon . A detailed description of the variables used in the dataset is available here. Use a statistical package of your choice to answer the following questions.

Compute the marginal distribution of Age.

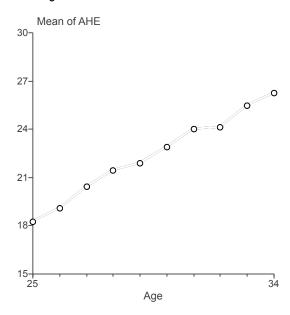
Marginal distribution of Age									
				Age (years)					
	25	26	27	28	29	30	31	32	
									1

(Round your response to four decimal places)

Compute the mean of AHE for Age = 34; that is, compute,  $E(AHE \mid Age = 34)$ .

(Round your response to four decimal places)

Below is the plot of the mean of AHE versus Age.



Are average hourly earnings and age related?

_							
$\cap$ $\wedge$	NΙΩ	the mean	of AHF ar	$\Delta \Lambda \Delta \Delta$	not coom	to he	ralatad

B. Yes, the mean of AHE and Age appear to be positively related.

O. Yes, the mean of AHE and Age appear to be negatively related.

Use the law of iterated expectations to compute the mean of AHE; that is compute E(AHE).

(Round your response to four decimal places)

Compute the variance of AHE; that is compute var(AHE).

(Round your response to four decimal places)

Compute the covariance between AHE and Age; that is compute cov(AHE, Age).

(Round your response to four decimal places)

Compute the correlation between AHE and Age; that is compute corr(AHE, Age).
corr(AHE, Age) =
(Round your response to four decimal places)
Answers 0.0754
0.0797
0.0947
0.0953
0.0983
0.1105
0.1109
0.1134
0.1134
0.1085
26.2457
B. Yes, the mean of AHE and Age appear to be positively related.
22.6914
154.1000
6.7205
0.1932
ID: Empirical Exercise 2.1
33. Assume that Y is normally distributed $N(\mu, \sigma^2)$ . Moving from the mean $(\mu)$ 1.96 standard deviations to the left and 1.96 standard deviations to the right, then the area under the normal p.d.f. is:
<b>A.</b> 0.33.
○ <b>B.</b> 0.05.
○ <b>C.</b> 0.95.
<b>D.</b> 0.67.
Answer: C. 0.95.
ID: Test B Ex 2.4.5

4.	$X_1, X_2, X_3$ , and $X_4$ are normally distributed random variables: $X_1 \sim N(0,0), X_2 \sim N(0,1), X_3 \sim N(1,0)$ , and $X_4 \sim N(1,1)$ .
	The variable(s) which follow(s) a standard normal distribution is (are) (1)
	$Y_1$ , $Y_2$ , and $Y_3$ are normally distributed random variables. Use the normal cumulative distribution function to answer the following questions.
	If $Y_1 \sim N(5,9)$ , $Pr(Y_1 \le 5.5) =$
	If $Y_2 \sim N(15,25)$ , $Pr(Y_2 > 10) =$
	If $Y_3 \sim N(30,16)$ , $Pr(20 \le Y_3 \le 40) =$
	(Round your answers to four decimal places.)
	Out of the above, the variable(s) which has (have) a skewness value of zero and a kurtosis value of 3 is (are) (2)
	(1) $\bigcirc$ $X_1$ $\bigcirc$ all of the above (2) $\bigcirc$ $X_1$ $\bigcirc$ all of the above
	$\bigcirc$ $\chi_2$ $\bigcirc$ none of the above $\bigcirc$ $\chi_2$ $\bigcirc$ none of the above
	$\bigcirc X_3$ $\bigcirc X_3$
	$\bigcirc X_4$
	Answers (1) X <sub>2</sub>
	0.5662
	0.8413
	0.9876
	(2) all of the above
	ID: Concept Exercise 2.4.1

35.	In a given population for beverage drinkers, an individual's per kg expenditure on tea ( <i>T</i> ) and their per kg expenditure on coffee ( <i>C</i> ) have a bivariate normal distribution with covariance 0.15. An individual's per kg expenditure on tea is distributed with mean \$2.85 and variance 0.16. An individual's per kg expenditure on coffee is distributed with mean \$2.42 and variance 0.09.
	If each individual in the population drinks 2 kg of tea and 1 kg of coffee, the mean total expenditure on beverages is \$ with a variance of
	If <i>T</i> and <i>C</i> have a bivariate normal distribution with covariance zero, the mean total expenditure on beverages is \$ with a variance of
	If X and Y have a bivariate distribution with covariance zero, this implies that the variables show (1)
	(1) skewness
	O independence
	consistency
	Answers 8.12
	1.33
	8.12
	0.73
	(1) independence
	ID: Concept Exercise 2.4.2

36. Let *A*, *B*, *C*, *D*, *E*, and *F* be independent standard normal random variables. Identify the distributions that will be followed by the variables *P*, *Q*, and *R*.

Variable	Distribution
$P = A^2 + B^2 + C^2$	(1)
$Q = \frac{F}{\sqrt{\left(D^2 + E^2\right)/2}}$	(2)
$R = \frac{\left(A^2 + B^2 + C^2\right)/3}{\left(D^2 + E^2\right)/2}$	(3)

	$\left(D^2 + E^2\right)/2$	(0)		
Compute the following probabilities.  threetwo  Group 1: (Round your answers to three de	cimal places.)			
If X is distributed $\chi^2_{30}$ , $Pr(X > 50.89) =$				
If X is distributed $t_{30}$ , $Pr(X > 2.04) =$				
<b>Group 2:</b> (Round your answers to two decomposition of the following of the following that $X$ is distributed $\chi^2_{20}$ , $\Pr(X > 37.57) = 1$ If $X$ is distributed $F_{20,\infty}$ , $\Pr(X > 1.88) = 1$	imal places.)			
<b>Group 3:</b> (Round your answers to three de If X is distributed $F_{7,\infty}$ , $\Pr(X \le 2.01) =$ If X is distributed $t_7$ , $\Pr(X \le 2.36) =$	cimal places.)			
<b>Group 4:</b> (Round your answers to two decided of $X$ is distributed $F_{10,2}$ , $Pr(X \le 19.40) = $ If $X$ is distributed $F_{2,10}$ , $Pr(X \le 2.92) = $	imal places.)			
<b>Group 5</b> : (Round your answers to three de If X is distributed $N(0,1)$ , $Pr(X > 1.86) =$ If X is distributed $t_8$ , $Pr(X > 1.86) =$				
The probabilities of (4) are	e equal because (5)			
<ul> <li>(1)  F distribution (2)</li> <li>Normal distribution</li> <li>t distribution</li> <li>Chi – squared distribution</li> </ul>	<ul><li>Chi – squared distribution</li><li>t distribution</li><li>Normal distribution</li><li>F distribution</li></ul>	ution (3) (	Chi – square F distributio Normal dist t distributior	ribution
(4) Group 5 Group 1 Group 4 Group 2 Group 3				
(5) O the $F$ – distribution is symmetric O the $t$ – distribution is always appro O if $X \sim t_n$ , then $X \sim F_{1,n}$ O $F_{m,\infty}$ distribution is the distributio O the distribution of $\chi^2_m$ is the same as	n of $\chi_m^2/m$		stribution	

	(2) t distribution
	(3) F distribution
	0.01
	0.025
	0.01
	0.01
	0.95
	0.975
	0.95
	0.90
	0.031
	0.05
	(4) Group 2
	(5) $F_{m,\infty}$ distribution is the distribution of $\chi^2_m/m$
D:	Concept Exercise 2.4.3
7.	In any year, the weather can inflict storm damage to a home. From year to year, the damage is random. Let $Y$ denote the dollar value of damage in any given year. Suppose that in 95% of the years $Y = 0$ , but in 5% of the years $Y = 19,163$ .
	The mean of the damage in any year is \$ . (Round your response to two decimal places.)
	The standard deviation of the damage in any year is \$ (Round your response to two decimal places.)
	Consider an "insurance pool" of 100 people whose homes are sufficiently dispersed so that, in any year, the damage to different homes can be viewed as independently distributed random variables. Let $\overline{Y}$ denote the average damage to these 100 homes in a year.
	$E(\overline{Y})$ , the expected value of the average damage $\overline{Y}$ , is \$
	The probability that $\overline{Y}$ exceeds \$2,000 is $\overline{}$ . (Round your response to four decimal places.)
	Answers 958.15
	4,176.48
	958.15
	0.0064
	ID: Exercise 2.18
_	

Answers (1) Chi – squared distribution

38.	In any year, a person can suffer from a minor fracture. From year to year, the number of people seeking treatment for such fractures is random. Let $Y$ denote the treatment expenditure for a minor fracture in any given year. Suppose that in 90% of the years $Y = \$0$ , but in 10% of the years $Y = \$4,000$ .						
	The mean treatment expenditure for a minor fracture in any year is \$ , and the standard deviation of the treatment						
	expenditure for a minor fracture in any year is \$						
	(Round your answers to two decimal places.)						
	Consider a group of 400 people whose lives, homes, and occupations are sufficiently dispersed so that, in any year, the treatment						
	expenditure for a minor fracture of different persons can be viewed as independently distributed random variables. Let $\overline{Y}$ denote the average treatment expenditure for a minor fracture of these 400 persons in a year.						
	The expected value of the average treatment expenditure for a minor fracture, $E(\overline{Y})$ , in any year is \$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \						
	deviation of the average treatment expenditure for a minor fracture in any year is \$						
	(Round your answers to two decimal places.)						
	The probability that for 400 people $\overline{Y}$ exceeds \$400 is						
	(Round your answer to four decimal places.)						
	Answers 400						
	1,200						
	400						
	60						
	0.5						
	ID: Concept Exercise 2.6.1						
39.	A software firm has 120 employees. The average time spent by these employees on social networking sites in a day during office hours is 55 minutes. Suppose a random sample of 70 employees is selected from the firm, and their average time spent on social networking sites is calculated.						
	Considering that the time spent by any two employees is independent of each other, which of the following statements are true? (Check all that apply.)						
	<ul> <li>■ A. The mean time spent by these randomly selected 70 employees will approximately be 55 minutes as the sample size is large.</li> </ul>						
	■ B. In this case, the sample mean is likely to be consistent for the population mean.						
	C. In this case, the sample mean is likely to be not consistent for the population mean.						
	□ <b>D.</b> The mean time spent by these randomly selected 70 employees may not be 55 minutes as the sample size is small.						
	Answer: A.						
	The mean time spent by these randomly selected 70 employees will approximately be 55 minutes as the sample size is large. , B. In this case, the sample mean is likely to be consistent for the population mean.						
	ID: Concept Exercise 2.6.2						

40.	Which of the following statements best describes what the central limit theorem states?	
	O A.	Under general conditions, when $n$ is large, $\overline{Y}$ will be near $\mu_Y$ with very high probability.
	○ В.	Under general conditions, the mean of $Y$ is the weighted average of the conditional expectation of $Y$ given $X$ , weighted by the probability distribution of $X$ .
	O C.	Under general conditions, when $n$ is large, the distribution of $\overline{Y}$ is well approximated by a normal distribution even if $Y_i$ are not themselves normally distributed.
	O D.	Under general conditions, when $n$ is large, the distribution of $\overline{Y}$ is well approximated by a standard normal distribution even if $Y_i$ are not themselves normally distributed.
	Answ	er: C.  Under general conditions, when $n$ is large, the distribution of $\overline{Y}$ is well approximated by a normal distribution even if $Y_i$ are not themselves normally distributed.

ID: Concept Exercise 2.6.3