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HW#1 Asymptotic Notation Exercise

Definitions:

- a) Define Big O notation in your own words.

Big O defines the upper bound of a function

- b) Define Big Omega (Ω) notation in your own words.

Big Ω defines the lower bound of a function

- c) Define Big Theta (Θ) notation in your own words.

Big Θ defines both the lower and upper bound

- d) How does Big Theta relate to Big O and Big Omega?

It consists of both the lower and upper bound

Classifications:

- a) Is $f(n) = 2n + 5$ in $O(n)$? Explain.

Yes, because the highest order term in the function is $2n$, therefore Big O is, $O(n)$.

- b) Is $f(n) = n^2 + 3n$ in $\Omega(n)$? Explain.

No, because $3n$ becomes negligible compared to n^2 , because of that the function isn't in $\Omega(n)$.

- c) Is $f(n) = 3n^2 + 2n + 1$ in $\Theta(n^2)$? Explain.

Yes, because the function grows exactly like n^2 .

- d) Is $f(n) = 2^n + n^2$ in $O(2^n)$? Explain.

Yes, because 2^n dominates the function, so $f(n) = O(2^n)$

Rules for Combining Functions:

- a) If $f(n)$ is in $O(g(n))$ and $h(n)$ is in $O(g(n))$, is $f(n) + h(n)$ in $O(g(n))$? Explain.

Yes, because both f and h are bounded by g

- b) If $f(n)$ is in $O(g(n))$, is $c \cdot f(n)$ in $O(g(n))$ for any constant c ? Explain.

Yes, because multiplying by a constant doesn't change

- c) If $f(n)$ is in $O(g(n))$ and $h(n)$ is in $O(k(n))$, is $f(n) \cdot h(n)$ in $O(g(n) \cdot k(n))$? Explain.

Yes, because if 2 functions are bounded by different multiples, it will result in a bound that combines both

Comparing Functions:

a) Rank the following functions in order of increasing growth rate:

$$2^n > n^2 > n \log n > n > \log n$$

(Handwritten ranking with functions: $2^n, \log n, n, 2^n, n \log n$ above the terms)

b) Given $f(n) = n^3$ and $g(n) =$, which function grows faster as n approaches infinity?

$$n^3?$$

5. True or False:

a) If $f(n)$ is in $O(g(n))$, then $f(n)$ is also in $\Omega(g(n))$. *True*

b) If $f(n)$ is in $\Theta(g(n))$, then $f(n)$ is also in $O(g(n))$ and $\Omega(g(n))$. *True*

c) If $f(n)$ is in $O(g(n))$ and $f(n)$ is in $\Omega(g(n))$, then $f(n)$ is in $\Theta(g(n))$. *False*