Math 3002: Problem Set 2

1. Rewrite each equation in the standard form of linear equations. Then solve each differential equation, showing and justifying all work:

(a)

$$y' = \frac{x - y\cos(x)}{\sin(x)}$$

(b)

$$y' = \frac{y + x^2}{2x}$$

(c)

$$xy' = x\sin(x) + y$$

(hint: integration by parts gives $\int x \sin(x) dx = \sin(x) - x \cos(x) + c$)

(d)

$$x^2y' + xy = 12x^2$$

(e) For each differential equation above, write the corresponding homogeneous version (i.e., replace b(x) with 0, using the notation from class), and find the solution of these homogeneous equations. Recognize anything?

2. Find a solution to the following differential equations:

(a)

$$y' - 3y = 6$$

(b)

$$y' - 3y = x$$

(c) If $y_a(x)$ is your solution from part (a), and $y_b(x)$ is your solution for part (b), define a new function

$$z(x) = y_a(x) + y_b(x)$$

Find a differential equation which z(x) solves.

Can you relate this question to question 1(e)?