Chapter 1

Fun with Floats

Floats are inexact by nature and this can confuse programmers. In this chapter we present an introduction to this problem. The basic message is that Floats are what they are inexact but fast numbers.

1.1 Never test equality on floats

The first basic principle is to never compare float equality. Let's take a simple case: the addition of two floats may not be equal to the float representing their sum. For example 0.1 + 0.2 is not equal to 0.3.

```
(0.1 + 0.2) = 0.3 returns false
```

We can see that we are in presence of two different numbers by looking at the hexadecimal values.

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The method storeString also conveys that we are in presence of two different numbers.

```
(0.1+0.2) storeString
returns '0.3000000000000004'
0.3 storeString
returns '0.3'
```

About Scaled Decimals. Scaled Decimals are exact numbers so they exhibit the behavior you expected.

```
0.1s2 + 0.2s2 = 0.3s2
returns true
```

Analyzing 13/10

1.3 is represented in machine as

Or if you prefer:

As you can see, this is quite different from 13/10. However, you can test (13/10) as Float = 1.3 and that happens to be true, but that won't always be true. In particular the inverse it not. So we are sure that if you compare floats using simple equality there is a high chance that you will get burned back. Again scaled decimal return correct and consistent behavior.

```
(13/10) asFloat = 1.3
returns true

1.3 = (13/10).
returns false
```

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```
1.3s1 = (13/10).
returns true

1.3s2*1.3s2 = 1.69s2.
returns true

1.3 * 1.3 = 1.69.
returns false
```

Stéf ► add a word on closeTo: ◄

1.2 Study of a simple example

While float equality is known to evil, you have to pay attention to other aspects of floats. Let us illustrate that point with the following example.

```
2.8011416510246336 roundTo: 0.01
-> 2.8000000000000003

2.8 truncateTo: 0.01
-> 2.8000000000000000
```

Yes nice example to exhibit in school

This again happens even if performed exactly (then rounded to nearest Float) (2.8 asTrueFraction roundTo: 0.01 asTrueFraction) asFloat

As soon as you write 0.01 instead of (1/100) or (0.01s2), the worm is in the fruit.

Once more, Floats are inexact

```
0.01 \sim = 0.01s2
```

The name absPrintExactlyOn:base: is lying, it does not print exactly, but it prints the shortest decimal representation than will be rounded to the same Float when read back.

To print it exactly, you need to use printShowingDecimalPlaces: indeed. As every finite Float is a represented internally as a Fraction with a denominator being a power of 2, every finite Float has a decimal representation with a finite number of decimals digits (just multiply numerator and denominator with adequate power of 5, and you'll get the digits).

So try:

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You see that even if you try to execute the operation without rounding error, then convert it back to Float, you get the error:

```
(2.8011416510246336 asTrueFraction roundTo: 0.01 asTrueFraction) asFloat -> 2.800000000000003
```

When you perform the roundTo: operations in Float inexact arithmetic, you may accumulate more rounding errors, so the result may vary.

If you want to round to an exact hundredth, then use exact arithmetic and try:

2.8011416510246336 roundTo: 0.01s2

1.3 Fun with Inexact representations

Pour enfoncer le clou, let's play a bit more with inexact representations:

```
{
  ((2.8 asTrueFraction roundTo: 0.01 asTrueFraction) - (2.8 predecessor)) abs -> -1.
  ((2.8 asTrueFraction roundTo: 0.01 asTrueFraction) - (2.8)) abs -> 0.
  ((2.8 asTrueFraction roundTo: 0.01 asTrueFraction) - (2.8 successor)) abs -> 1.
} detectMin: [:e | e key ]

returns
  0.0->1
```

you get 0.0->1, which mean that: (2.8 asTrueFraction roundTo: 0.01 asTrueFraction) asFloat = (2.8 successor)

But remember that

```
(2.8 asTrueFraction roundTo: 0.01 asTrueFraction) \sim= (2.8 successor)
```

It must be interpreted as the nearest Float to (2.8 asTrueFraction roundTo: 0.01 asTrueFraction) is (2.8 successor).

If you want to know how far it is, then get an idea with:

```
((2.8 asTrueFraction roundTo: 0.01 asTrueFraction) - (2.8 successor) asTrueFraction) asFloat -2.0816681711721685e-16
```

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Floats are inexact numbers.