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|------|------------------------|
| Step | Algorithm: |
| 1a | |
| 4 | where |
| 2 | |
| 3 | while do |
| 2,3 | \wedge |
| 5a | where |
| 6 | |
| 8 | |
| 5b | |
| 7 | |
| 2 | |
| | endwhile |
| 2,3 | $\wedge \neg(\quad)$ |
| 1b | |

| | |
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| Step | Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$ |
| 1a | $C = \widehat{C}$ |
| 4 | $A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}, B \rightarrow \begin{pmatrix} B_T \\ B_B \end{pmatrix}$ where A_T has 0 rows, B_T has 0 rows |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| 3 | while $m(A_T) < m(A)$ do |
| 2,3 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge m(A_T) < m(A)$ |
| 5a | Determine block size b $\begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ A_1 \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \rightarrow \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix}$ where A_1 has b rows, B_1 has b rows |
| 6 | $C = A_0^T B_0 + B_0^T A_0 + \widehat{C}$ |
| 8 | $C := A_1^T B_1 + B_1^T A_1 + \widehat{C}$ |
| 5b | $\begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ A_1 \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix}$ |
| 7 | $C = A_0^T B_0 + B_0^T A_0 + A_1^T B_1 + B_1^T A_1 + \widehat{C}$ |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| | endwhile |
| 2,3 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge \neg(m(A_T) < m(A))$ |
| 1b | $[C] = \text{Syr2k_lt}(A, B, \widehat{C})$ |

Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$

$$A \rightarrow \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix}, B \rightarrow \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix}$$

where A_T has 0 rows, B_T has 0 rows

while $m(A_T) < m(A)$ **do**

Determine block size b

$$\begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ \frac{A_0}{A_1} \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix} \rightarrow \begin{pmatrix} B_0 \\ \frac{B_0}{B_1} \\ B_2 \end{pmatrix}$$

where A_1 has b rows, B_1 has b rows

$$C := A_1^T B_1 + B_1^T A_1 + \hat{C}$$

$$\begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ \frac{A_0}{A_1} \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ \frac{B_0}{B_1} \\ B_2 \end{pmatrix}$$

endwhile

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| Step | Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$ |
| 1a | $C = \hat{C}$ |
| 4 | where |
| 2 | |
| 3 | while do |
| 2,3 | \wedge |
| 5a | Determine block size |
| | where |
| 6 | |
| 8 | |
| 5b | |
| 7 | |
| 2 | |
| | endwhile |
| 2,3 | $\wedge \neg($ |
| 1b | $[C] = \text{Syr2k_lt}(A, B, \hat{C})$ |

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| Step | Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$ |
| 1a | $C = \widehat{C}$ |
| 4 | where |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| 3 | while do |
| 2,3 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge$ |
| 5a | Determine block size |
| | where |
| 6 | |
| 8 | |
| 5b | |
| 7 | |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| | endwhile |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge \neg($) |
| 1b | $[C] = \text{Syr2k_lt}(A, B, \widehat{C})$ |

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| Step | Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$ |
| 1a | $C = \widehat{C}$ |
| 4 | where |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| 3 | while $m(A_T) < m(A)$ do |
| 2,3 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge m(A_T) < m(A)$ |
| 5a | Determine block size |
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| 5a | <p>Determine block size</p> <p>where</p> |
| 6 | |
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| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
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| 5b | $\begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ A_1 \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ B_B \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix}$ |
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| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| | endwhile |
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| 7 | $C = A_0^T B_0 + B_0^T A_0 + A_1^T B_1 + B_1^T A_1 + \widehat{C}$ |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| | endwhile |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge \neg(m(A_T) < m(A))$ |
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| 7 | $C = A_0^T B_0 + B_0^T A_0 + A_1^T B_1 + B_1^T A_1 + \widehat{C}$ |
| 2 | $C = A_T^T B_T + B_T^T A_T + \widehat{C}$ |
| | endwhile |
| 2,3 | $C = A_T^T B_T + B_T^T A_T + \widehat{C} \wedge \neg(m(A_T) < m(A))$ |
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| Step | Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$ |
| | |
| | $A \rightarrow \begin{pmatrix} A_T \\ \overline{A_B} \end{pmatrix}, B \rightarrow \begin{pmatrix} B_T \\ \overline{B_B} \end{pmatrix}$ <p>where A_T has 0 rows, B_T has 0 rows</p> |
| | |
| | while $m(A_T) < m(A)$ do |
| | |
| | <p>Determine block size b</p> $\begin{pmatrix} A_T \\ \overline{A_B} \end{pmatrix} \rightarrow \begin{pmatrix} \overline{A_0} \\ \overline{A_1} \\ \overline{A_2} \end{pmatrix}, \begin{pmatrix} B_T \\ \overline{B_B} \end{pmatrix} \rightarrow \begin{pmatrix} \overline{B_0} \\ \overline{B_1} \\ \overline{B_2} \end{pmatrix}$ <p>where A_1 has b rows, B_1 has b rows</p> |
| | |
| | $C := A_1^T B_1 + B_1^T A_1 + \widehat{C}$ |
| | $\begin{pmatrix} A_T \\ \overline{A_B} \end{pmatrix} \leftarrow \begin{pmatrix} \overline{A_0} \\ \overline{A_1} \\ \overline{A_2} \end{pmatrix}, \begin{pmatrix} B_T \\ \overline{B_B} \end{pmatrix} \leftarrow \begin{pmatrix} \overline{B_0} \\ \overline{B_1} \\ \overline{B_2} \end{pmatrix}$ |
| | |
| | |
| | endwhile |
| | |
| | |

Algorithm: $[C] := \text{SYR2K_LT_BLK_VAR5}(A, B, C)$

$$A \rightarrow \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix}, B \rightarrow \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix}$$

where A_T has 0 rows, B_T has 0 rows

while $m(A_T) < m(A)$ **do**

Determine block size b

$$\begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ \frac{A_0}{A_1} \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix} \rightarrow \begin{pmatrix} B_0 \\ \frac{B_0}{B_1} \\ B_2 \end{pmatrix}$$

where A_1 has b rows, B_1 has b rows

$$C := A_1^T B_1 + B_1^T A_1 + \hat{C}$$

$$\begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ \frac{A_0}{A_1} \\ A_2 \end{pmatrix}, \begin{pmatrix} B_T \\ \frac{B_T}{B_B} \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ \frac{B_0}{B_1} \\ B_2 \end{pmatrix}$$

endwhile