Def D congruent modulo f. (In both) 2F75-f7 = f100. Diff $p(x) \in F(x)$. 2f = g(x), $h(x) \in F[x]$, 2f = g(x), $h(x) \in F[x]$, 2f = g(x) = h(x) (if f = h(x) = h(x)

Thm (2) 5-2

Făfield. $p(x) \in F(x) \# 0$. $\sharp f(x) = g(x) \mod p(x)$ $h(x) = k(x) \mod p(x)$ (1) $f(x) + h(x) = g(x) + k(x) \mod p(x)$ (2) $f(x) h(x) = g(x) k(x) \mod p(x)$

Def ② congruence class 飯梯 residue class)

F(x) 中 fh th (congruent to g(x) mod p(x)) ft polynomials

ft set 写作 [g(x)] xxx 就(g),

Pr: [g(x)] p(x) = {g(x) | g(x) \in F(x)| and | g(x) = f(x) | mod p(x)|}

Thm② 5·3 (其比 Thm 2·3.) $f(x) = g(x) \mod p(x) \qquad (不知道为什么在这个 hm, 实际就是 def iff [fex]_p(x) = [g(x)]_{p(x)} \qquad 66 注意到)$

Corollary ② 5.4 (美比 corollary 2.4)
两个 congruence class modulo pin)
either [disjoint] or [identica]

(2) 全分的企业 OF 和FIN 中所有 degree In the polynomial 的 set

P: S= (of) U(foveFEN) degree In the construction of the construction of

三 FEN 中海ケ p(n) bis congruent class 注: 都是S 中東ケ polynomial bis congruent class. 就像 Zn 中海ケ 在 offerent polynomial 都有 congruence class 都有

是(v,1,...,n-1) 中東于int his distinct congruence class.

congruence class, 且这个5억每个elem 的 congruence

class 都distinct, 也并是一个元子给表一个congruent data,

covering every congruence class.

Def 3

The set of all congruence classes modulo p(x) on F(x) is denoted by:

F(x)/(p(x)) &

 $5 \ Zn \not\equiv tt$. $Zn \not\equiv Z \not\Rightarrow n \land congruence classes$.

To $F[x]/(p(x)) \not\equiv F[x] \not\Rightarrow j \not\equiv J[S] \not\uparrow (j \not\equiv infinite. S = \{o_F\} \lor \{f(x) \in F[x)\} \ degfty \leq n \}$ congruent classes. $F(x)/(p(x)) = \{f(n)\}_{p(x)} \mid f(n) \in S \}$

Thm \bigcirc 5-6 (ap Thm 5-2, 5-3 &-h 1 kit) $\begin{array}{ll}
\text{ is } [f(\pi)]_{p(x)} = [g(\pi)]_{p(x)}, [h(\pi)]_{p(x)} = [k(\pi)]_{p(x)} \\
& \in F(\pi)/(p(\pi)).
\end{array}$ $\begin{array}{ll}
\text{ is } [f(\pi) + h(\pi)] = [g(\pi) + k(\pi)]_{p(\pi)} \\
\text{ is } [f(\pi) + h(\pi)]_{p(\pi)} = [g(\pi) + k(\pi)]_{p(\pi)}
\end{array}$

Def 4 + 10 × in FED/(P(x))

+: [f(x)] + [g(x)] = [f(x) + s(x)] p(x)

 $X: [f(x)]_{p(x)} = [f(x) \cdot g(x)]_{p(x)} = [f(x) \cdot g(x)]_{p(x)}$

Thm 55.7

2 F& field. p(x) & F[x] EBS nonconst polynomial.

= FCX/(p(x)) \$ -t commutative ring.

A F(X)/(p(x)) - it is -t subring F*

which is isomorphic to F.

这是一种结结地。实际上下至FEX/(pax). Flage是 FEXX/(pax)的 subring.

Thm (8) 5.8

至Fish field. p(x) 为FLX)上的nonconst polynomial.

FLX/(p(x)) 为一个commutative ring。且Fith—不subring。

(给定-4 field F, 新加总是微构造的-4厘长的 ring,) 包括包含-4 subning、FLD、FLD/p(D)都是。

Thm 19 5.9

Få field. pan = Fin at anst.

Definition of Fixi/pxi of the mit.