

limit 知 continuity判定的起义区别:

limatc:

ce(domb), 但不需要cedomb),且《通证明的指在的 continuity at a:

a e dom (f),但不需要 a e (dom (f)),且 significate to a 的

```
Def f在某个综上 continuous

if f is continuous on V b ∈ B (C dom(f))

则称f is continuous on 整7 dom(f)

则终f is continuous (连续函数)
```

More general def of continuity in metric space topological spaces (even topological space) $f; X \rightarrow Y$ is ctn if $f^{-1}[V]$ is open in X for every open set $V \subseteq Y$

19是 dom (月中, 并不是每个点都是 lim. pt.
而我们现在约 rigorous def 定则是 吧 Mind isolated point 都说作在约束 ctn. 63.

review: metric space X 中,ASX 那么X\A'为A的所在isolated pt.的练。 (YXEX, X型We lim. pt of A, 要以是isolated pt. of A)

国而りcedom(f): if c & (dom(f))' => f在cst-ctn, とelse: f在cst-ctn if limf(s)=f(c)

Thm UF4& are equiv.

(i) f在a处ctn.

(ii) limfor) = f(a) or a is an isolated pt of dom(f)

(iii) Y seq. (an) in dom(f) s.t. (an)—>a, 都 lim fran)=f(a)

(iv) V open nbh Vz (f(a)), 3 open nbd Uz(a) s.t. (实际就是def的复造、使用open set) f[ANU] SV

第三条路存搬:①如果 A ∈ (dom(f)). 那么directly follow from

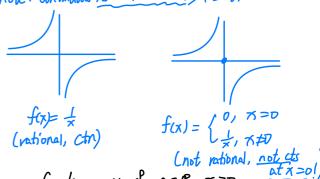
(lim f(an)=l iff ∀(an)→c, f(an)→l)
②如果 a ∉ (dom(f)), 即: a & dom(f) bb → t iso lated pt.

那么dom(f)中任何 (conv. to a bi seq 一定是eventually const. (a) bb (hw3)

ex The following functions are continuous:

(2) rational functions (specially: polynomials)

note: continuous 完定义在domain to Fadomain 上的表示表



(3) power functions: y=xp, p=R, x>0

(4) exponential function: y =a, a > D

(5) logarithmic function

(6) trig/inverse trig functions

(7) y= /x1

