

11. Suppose that $\log_2 3 = a/b$ where $a, b \in \mathbb{Z}^+$ and $b \neq 0$. Then $2^{a/b} = 3$, so $2^a = 3^b$. This violates the fundamental theorem of arithmetic. Hence, $\log_2 3$ is irrational. **13.** 3, 5, and

7 are primes of the desired form. **15.** 1, 7, 11, 13, 17, 19, 23,

29 **17.** a) Yes b) No c) Yes d) Yes **19.** Suppose that n

of the first $n - 1$ primes. **49.** Because every second integer

is divisible by 2, the product is divisible by 2. Because every third integer is divisible by 3, the product is divisible by 3. Therefore, the product has both 2 and 3 in its prime factorization and is therefore divisible by $3 \cdot 2 = 6$. **51.** $n = 1601$ is