Cálculo de Programas

Licenciatura em Engenharia Informática

Ficha 10

Indique quais das seguintes funções não podem ser codificadas usando catamorfismos ou anamorfismos. Justifique a sua resposta. Codifique as funções identificadas usando hilomorfismos. Identifique os tipos intermédios e desenhe os respectivos diagramas. Pode codificar os genes no estilo *point-wise*.

```
\mathsf{msort} :: \mathsf{Ord} \ a \Rightarrow [a] \to [a]
msort[] = []
\mathsf{msort}\, [x] = [x]
\mathsf{msort}\ l = \mathbf{let}\ (x,y) = \mathsf{split}\ l
                   in merge (msort x, msort y)
\mathsf{split} :: [a] \to ([a], [a])
\mathsf{split}\,[\,] = ([\,],[\,])
\operatorname{split}(h:t) = \operatorname{let}(x,y) = \operatorname{split} t
                     in (y, h:x)
\mathsf{merge} :: \mathsf{Ord}\ a \Rightarrow ([\,a\,],[\,a\,]) \rightarrow [\,a\,]
merge ([], ys) = ys
merge(xs,[]) = xs
\mathsf{merge}\;(x:xs,y:ys) \mid x < y \, = x : \mathsf{merge}\;(xs,y:ys)
                              |x \geqslant y = y : \mathsf{merge}(x : xs, ys)
isort :: Ord a \Rightarrow [a] \rightarrow [a]
isort [] = []
isort(h:t) = insert(h, isort t)
insert :: Ord a \Rightarrow (a, [a]) \rightarrow [a]
insert (x, []) = [x]
insert (x, y : ys) \mid x < y = x : y : ys
                        |x \geqslant y = y : \mathsf{insert}(x, ys)
bsort :: Ord a \Rightarrow [a] \rightarrow [a]
\mathsf{bsort}\,\,[\,] = [\,]
\mathsf{bsort}\ l\ = \ \mathbf{let}\ (x,m) = \mathsf{bubble}\ l
                in x: bsort m
bubble :: Ord a \Rightarrow [a] \rightarrow (a, [a])
\mathsf{bubble}\,[x] = (x,[\,])
\mathsf{bubble}\;(x:l) = \mathbf{let}\;(y,m) = \mathsf{bubble}\;l
                         in if x < y then (x, y : m) else (y, x : m)
```