RELACIÓN PID ACADÉMICO PID-ISA

Representaciones PID

$$G_r = PID_{ACD} = K \frac{(s+a)(s+b)}{s}$$

$$PID_{ISA}(s) = K_c \left(1 + \frac{1}{T_i \cdot s} + T_d \cdot s \right)$$

Relaciones entre Representaciones

$$\mathbf{p} \qquad Gr = \frac{U(s)}{E(s)} = kc$$

PI
$$Gr = kc + \frac{kc}{Ti \cdot s} = kc \frac{\left(s + \frac{1}{Ti}\right)}{s}$$
 $Gr = k \frac{\left(s + a\right)}{s}$

PD
$$Gr = kc + s \cdot kc \cdot Td = kc(1 + s \cdot Td)$$
 $Gr = k(s+b)$

PID
$$Gr = kc + \frac{kc}{Ti \cdot s} + s \cdot kc \cdot Td = kc \left(1 + \frac{1}{Ti \cdot s} + s \cdot Td\right) = kc \frac{\left(Td \cdot s^2 + s + \frac{1}{Ti}\right)}{s}$$
 $Gr = k \frac{(s+a)(s+b)}{s}$