

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
const long long PRIME = 2305843009213693951LL; prime)
```

```
// Modular exponentiation
```

```
long long modPow(long long a, long long b, long long p = PRIME) {
```

```
    long long res = 1;
```

```
    a %= p;
```

```
    while (b > 0) {
```

```
        if (b & 1) res = (__int128)res * a % p;
```

```
        a = (__int128)a * a % p;
```

```
        b >>= 1;
```

```
    }
```

```
    return res;
```

```
}
```

```
// Modular inverse
```

```
long long modInverse(long long a, long long p = PRIME) {
```

```
    return modPow(a, p - 2, p);
```

```
}
```

```
// Lagrange interpolation
```

```
long long lagrangeInterpolation(long long target, const vector<pair<long long, long long>>&  
shares, long long p = PRIME) {
```

```
    long long total = 0;
```

```

int k = shares.size();
for (int i = 0; i < k; i++) {
    long long xi = shares[i].first;
    long long yi = shares[i].second;
    long long num = 1, den = 1;
    for (int j = 0; j < k; j++) {
        if (i == j) continue;
        long long xj = shares[j].first;
        num = (__int128)num * (target - xj + p) % p;
        den = (__int128)den * (xi - xj + p) % p;
    }
    long long li = (__int128)num * modInverse(den, p) % p;
    total = (total + yi * li) % p;
}
return (total + p) % p;
}

// Convert value string in given base to decimal
long long baseToDecimal(const string &s, int base) {
    long long result = 0;
    for (char c : s) {
        int digit;
        if (isdigit(c)) digit = c - '0';
        else if (isalpha(c)) digit = 10 + (tolower(c) - 'a');
        else continue;
        if (digit >= base) throw invalid_argument("Digit out of range for base");
    }
}

```

```

        result = result * base + digit;
    }
    return result;
}

```

```

int main() {

```

```

    int n = 10, k = 7;

```

```

    vector<pair<long long,long long>> shares = {
        {1, baseToDecimal("13444211440455345511", 6)},
        {2, baseToDecimal("aed7015a346d635", 15)},
        {3, baseToDecimal("6aeeb69631c227c", 15)},
        {4, baseToDecimal("e1b5e05623d881f", 16)},
        {5, baseToDecimal("316034514573652620673", 8)},
        {6, baseToDecimal("2122212201122002221120200210011020220200", 3)},
        {7, baseToDecimal("20120221122211000100210021102001201112121", 3)},
        {8, baseToDecimal("20220554335330240002224253", 6)},
        {9, baseToDecimal("45153788322a1255483", 12)},
        {10, baseToDecimal("1101613130313526312514143", 7)}
    };

```

```

    // Reconstruct majority secret

```

```

    map<long long, int> freq;

```

```

    vector<int> idx(n);

```

```

    fill(idx.begin(), idx.begin() + k, 1);

```

```

do {
    vector<pair<long long,long long>> subset;

    for (int i = 0; i < n; i++) if (idx[i]) subset.push_back(shares[i]);

    long long secret = lagrangeInterpolation(0, subset);

    freq[secret]++;
} while (prev_permutation(idx.begin(), idx.end()));

```

```

// Find most frequent secret

```

```

long long true_secret = -1;

```

```

int best = -1;

```

```

for (auto &kv : freq) {

```

```

    if (kv.second > best) {

```

```

        best = kv.second;

```

```

        true_secret = kv.first;

```

```

    }

```

```

}

```

```

cout << "Recovered Secret: " << true_secret << "\n";

```

```

// Detect wrong shares

```

```

vector<pair<long long,long long>> wrong;

```

```

for (auto &sh : shares) {

```

```

    vector<pair<long long,long long>> others;

```

```

    for (auto &s : shares) if (s != sh) others.push_back(s);

```

```

    if ((int)others.size() >= k-1) {

```

```

        vector<pair<long long,long long>> testSubset(others.begin(), others.begin() + (k-1));
        testSubset.push_back(sh);
        long long expected = lagrangeInterpolation(sh.first, testSubset);
        if (expected != sh.second) wrong.push_back(sh);
    }
}

cout << "Wrong Shares: ";
if (wrong.empty()) cout << "None\n";
else {
    for (auto &sh : wrong) cout << "(" << sh.first << "," << sh.second << ") ";
    cout << "\n";
}

return 0;
}

```