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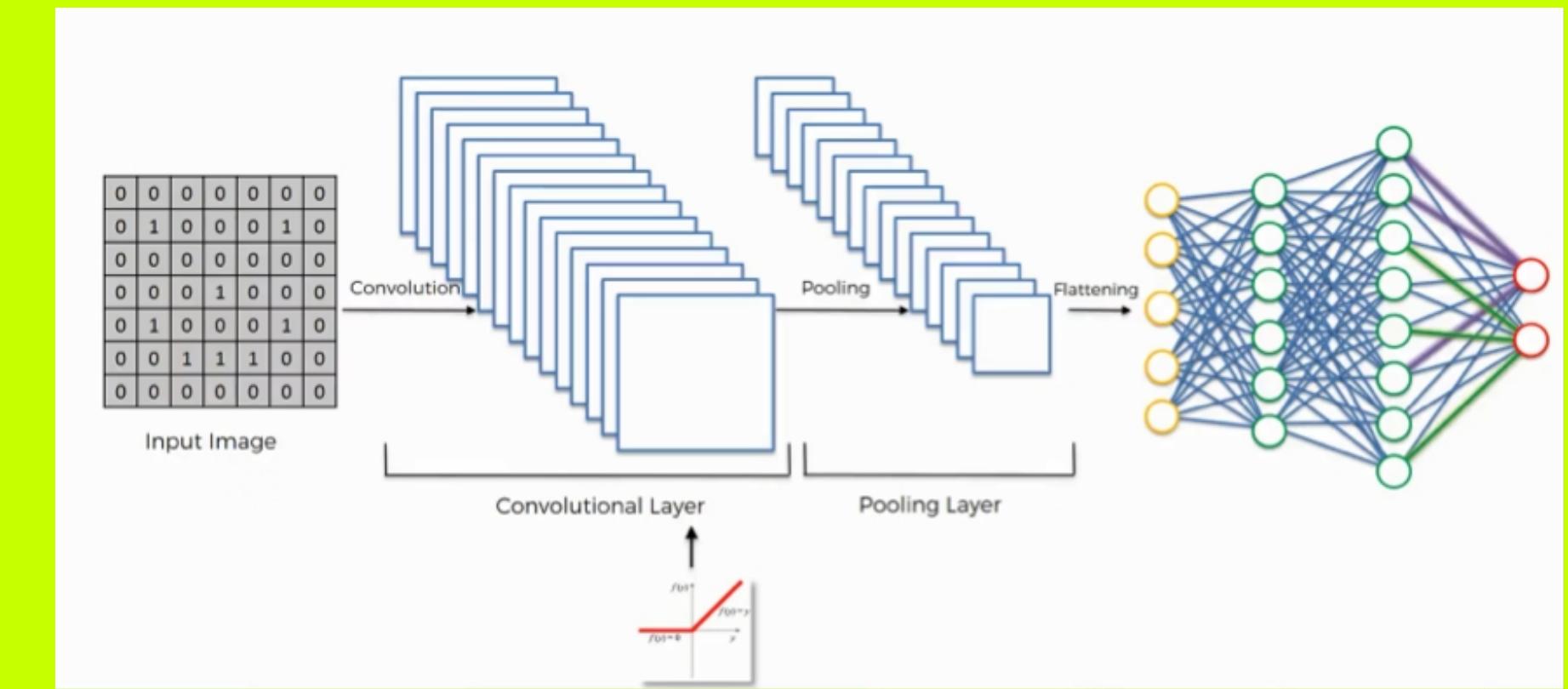
CB.EN.U4AIE22011

MFC - 4

ASSIGNMENT - 1

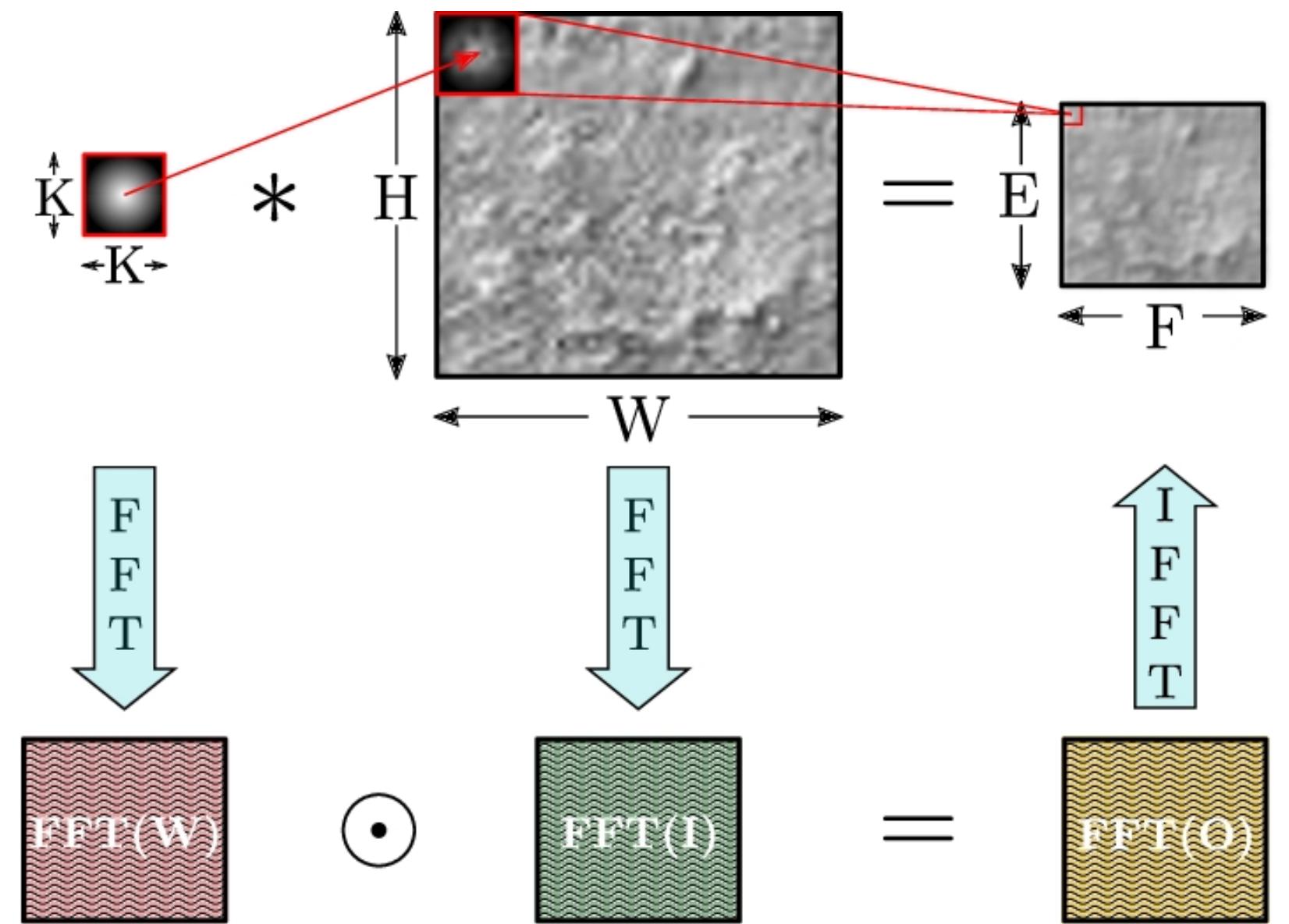
Topic

SUBSTITUTE FOR CONVOLUTIONAL LAYER



Convolution layer
Substituted with -

FFT LAYER



But for this assignment, DFT was used

How?

Using 2-Dimensional DFT Algorithm

(or)

$$\hat{h}(k, l) = \sum_{n=0}^{N-1} \sum_{m=0}^{M-1} e^{-i(\omega_k n + \omega_l m)} h(n, m)$$

$$h(n, m) = \frac{1}{NM} \sum_{k=0}^{N-1} \sum_{l=0}^{M-1} e^{i(\omega_k n + \omega_l m)} \hat{h}(k, l)$$

Can also use 1D DFT Algorithm

$$X(k) = \sum_{n=0}^{N-1} x(t_n) e^{-2i\pi k t_n / N}$$

How did we know???

PROOF

Wednesday

Convolution

$$(f * g)(t) = \int_{-\infty}^{\infty} f(\tau)g(t-\tau)d\tau$$

\rightarrow Fourier

$$F(f * g) = \int_{-\infty}^{\infty} (f * g) \cdot e^{j2\pi ft} dt$$
$$F(f * g) = \int_{-\infty}^{\infty} \left(\int_{-\infty}^{\infty} f(\tau)g(t-\tau) \cdot e^{j2\pi ft} d\tau \right) dt$$
$$F\{f(\tau) \cdot g(t-\tau)\} = F\{f\} \cdot F\{g\}$$
$$F\{f * g\} = \int_{-\infty}^{\infty} (F\{f\} \cdot F\{g\}) dt$$

Steps

1. Take an image and a filter/kernel to perform convolution.
2. Pad the filter with zeros to match its shape with the image.
3. Apply FFT or DFT on the image and the filter.
4. Multiply both, $\text{FFT}\{\text{image}\}$ and $\text{DFT}\{\text{filter}\}$ (element wise).
5. Apply IFFT or IDFT on the the output.
6. Zero bit would've shifted to the left. So pull it back and place it in the center.
7. "Convolved" output is ready to pass into the next layer.

Overview



-1	0	+1
-2	0	+2
-1	0	+1

DFT

f

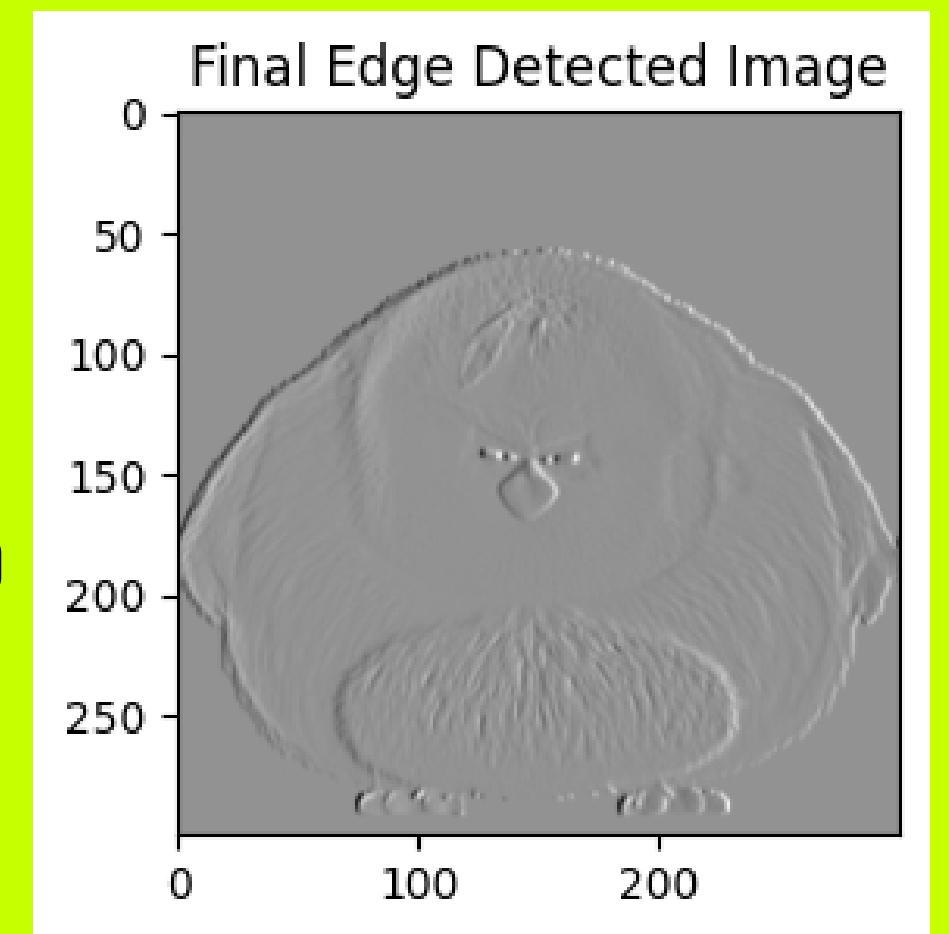
$f * g$

IDFT

(after shifting zero)

DFT

g



Code

DFT2D

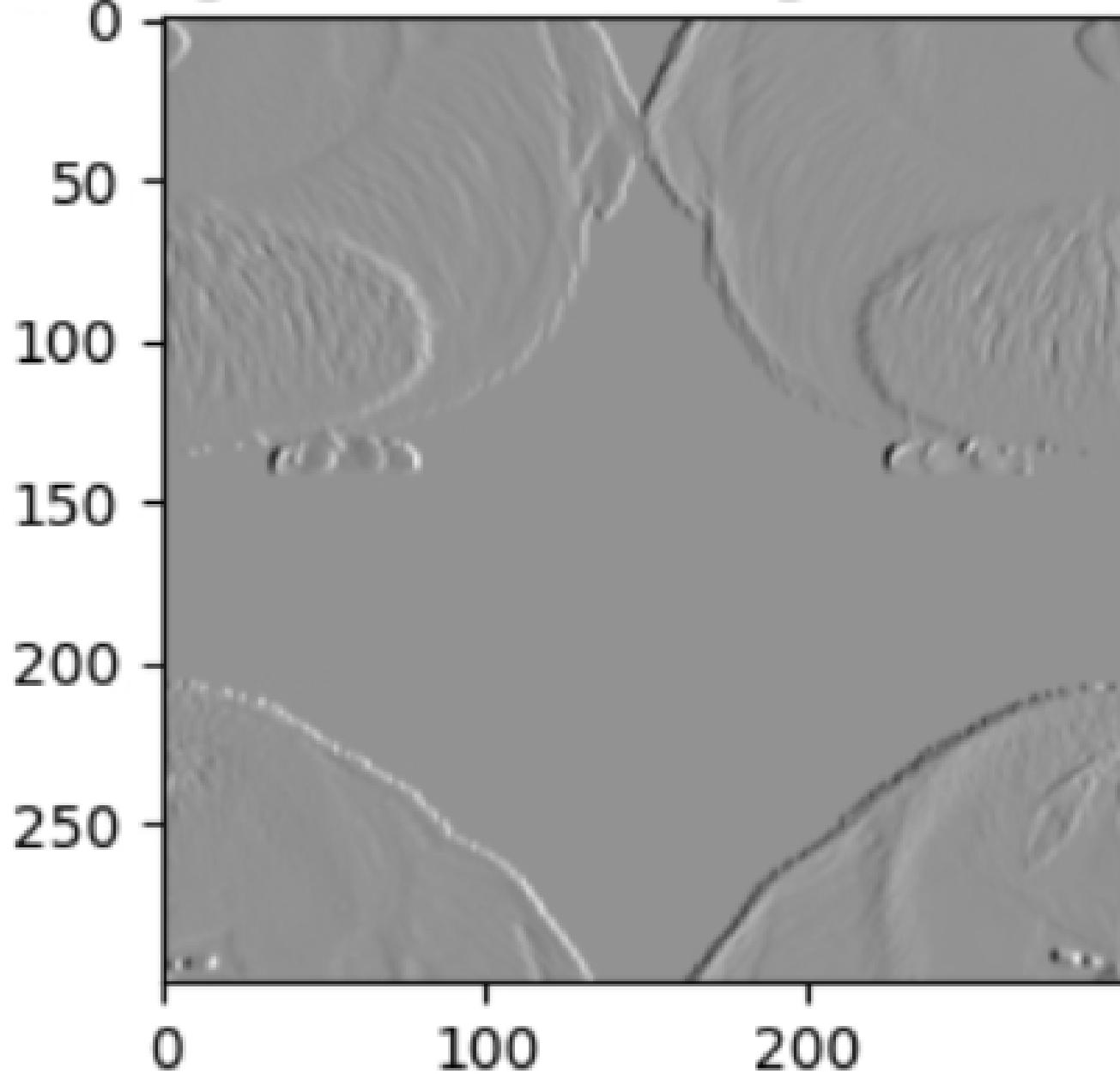
```
def Dft2(ip):
    row, col = ip.shape
    op = np.zeros_like(ip, dtype=complex)
    for k in range(row):
        if (k+1)%100==0:print(k)
        y = np.arange(col)
        bas1 = np.exp(-2j * np.pi * k * np.arange(row) / row)
        for l in range(col):
            bas2 = np.exp(-2j * np.pi * l * y / col)
            bas = np.outer(bas1, bas2)
            print(bas.shape,bas1.shape,bas2.shape,ip.shape)
            op[k,l] = np.sum(ip*bas)
    return op
```

IDFT2D

```
def IDft2(ip):
    op=np.zeros_like(ip,dtype=complex)
    row, col = ip.shape
    for k in range(row):
        bas1=np.exp(2j*np.pi*np.arange(row)*k/row)
        for l in range(col):
            bas2=np.exp(2j*np.pi*np.arange(col)*l/col)
            bas=np.outer(bas1,bas2)
            op[k,l]=(np.sum(ip*bas))/(row*col)
    return op
```

Output

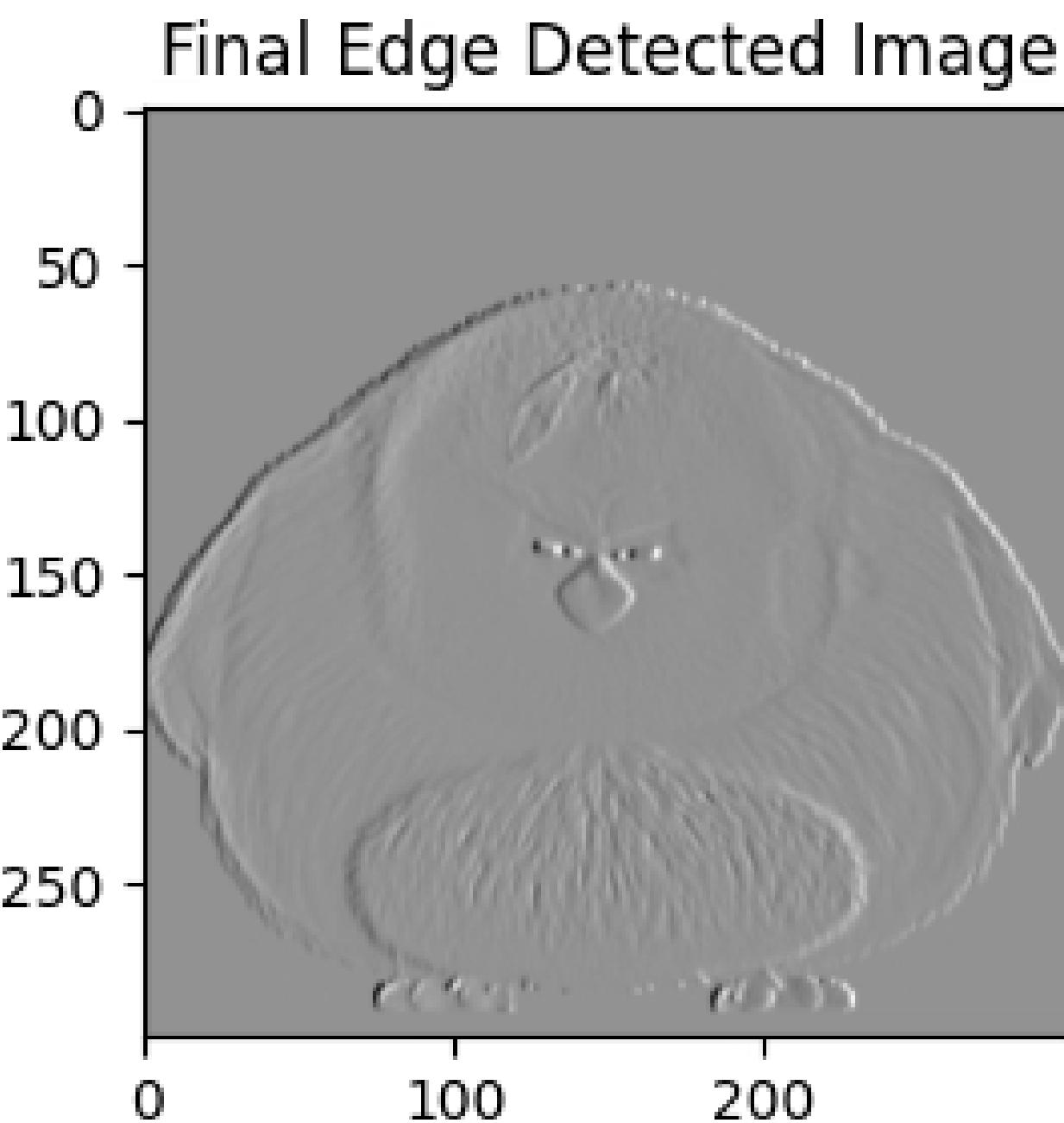
IDFT Edge Detected Image(!shifting zero)



Shifts zero

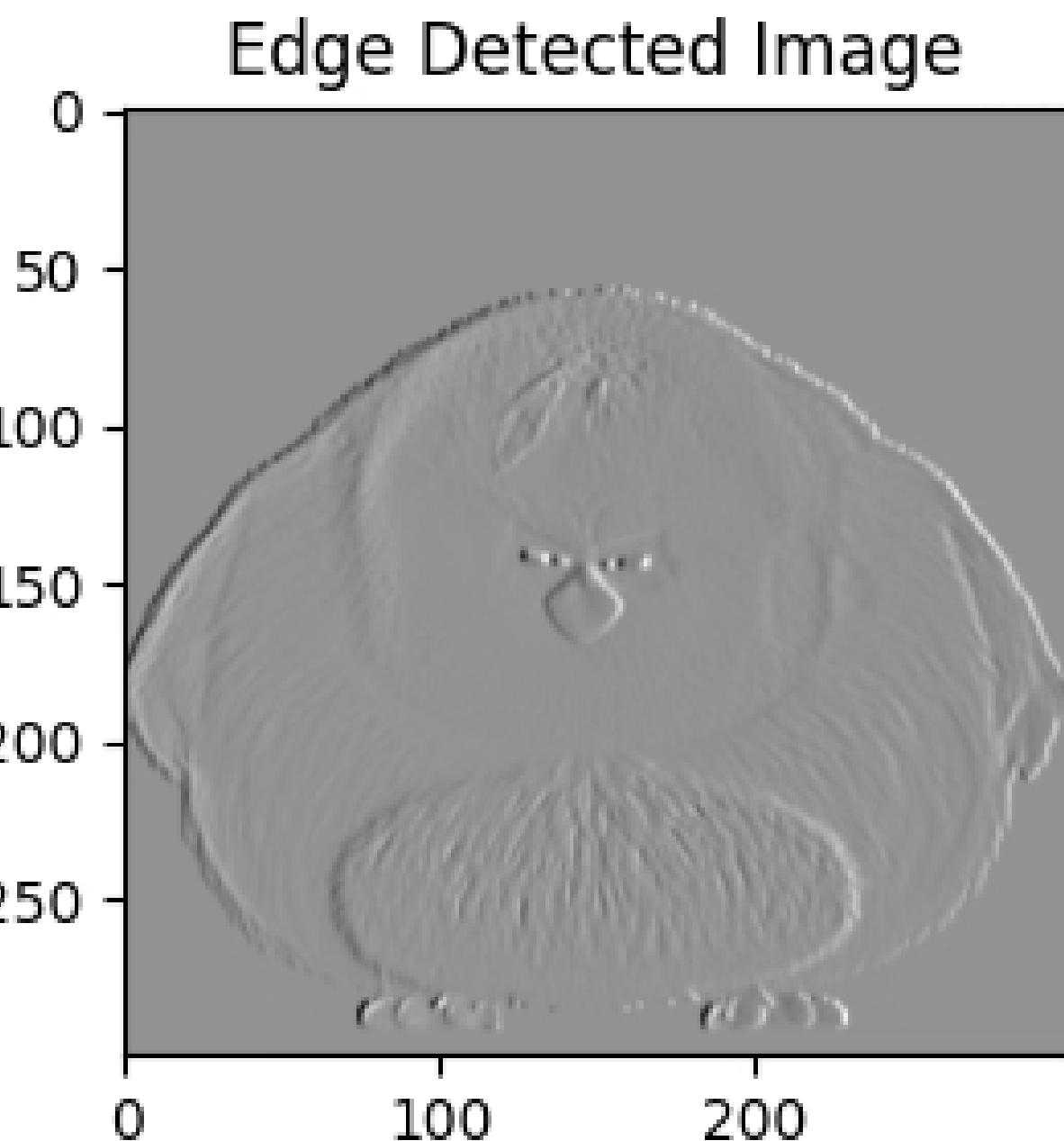
```
from math import ceil  
r=ceil(op.shape[0]/2)  
c=ceil(op.shape[1]/2)  
zer=np.zeros(op.shape)  
  
zer[0:r,0:c]=op[r:,c:]  
zer[r:,c:]=op[0:r,0:c]  
zer[0:r,c:]=op[r:,0:c]  
zer[r:,0:c]=op[0:r,c:]  
plt.figure(figsize=(3,3))  
plt.imshow(zer,cmap='gray')  
plt.title('Final Edge Detected Image')  
plt.show()
```

Output



Output and Code using inbuilt

```
f1=np.fft.fftn(img)
k1=np.fft.fftn(k1)
op=f1*k1
op=np.fft.ifftn(op)
plt.figure(figsize=(3,3))
plt.title('Original Image')
plt.imshow(np.real(op),cmap='gray')
```



Done

THE END