

$$(B+C) + (-B) = C$$

EC point addition
加上反元素

DLP

$\{(g, g^\alpha) \rightarrow \alpha, g \text{ is generator is } \mathbb{Z}_q \text{ (同樣意義 } \alpha P, \text{ 不同表示方法)}\}$

Verify (vk, m, σ)

$$\sigma_2 \cdot \sigma_1 = ?$$

$$(H(m) + \alpha u)P = H(m)P + u(\alpha P) \quad \Rightarrow \text{代表所有人都可以驗證}$$

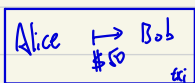
$\downarrow vk$
 $\hookrightarrow H(\sigma_1, vk, m)$

if $\sigma_2 \cdot \sigma_1 == H(m)P + u(\alpha P) : \text{return True}$

else : return False

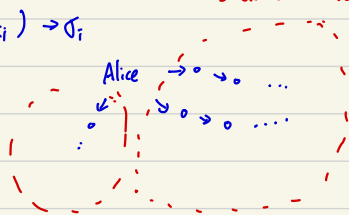
$$\sigma_1 = rP$$

$\sigma_2 = r^{-1} (H(m) + \alpha \cdot u) \Rightarrow \alpha \text{ 相同的機率很低, 所以幾乎只有自己做得出來}$



Sign $(sk_{Alice}, tx_i) \rightarrow \sigma_i$

Block Chain Network



如果兩筆交易剛好用了同一個，那麼就可以得知該人的 α ，導致帳號被盜

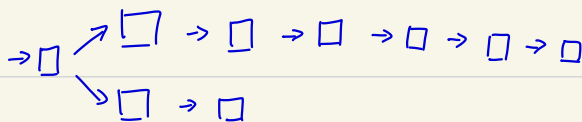
所以現在都用冷錢包，多個錢包，用了就丟，就不用到同一個 α

When r 用到相同， σ_1 就會相同

$$\sigma_2 = r^{-1} (H(m) + \alpha \cdot u)$$

\Rightarrow 則可得 α 值 (極度危險!!)

$$\sigma_2 = r^{-1} (H(m) + \alpha \cdot u)$$



長鏈：以 Bitcoin 為例，A tx is complete if tx is with 6 confirmations (包含自己)
短鏈：自根無視，上面的交易不在鏈上

正常來說，大家都跟著最快的鏈做題目

Byzantine Generals Problem (1982 Lamport et al.)

- ① 假設 n 個將軍，有一個發指令的將軍，
- ② 而此時他要發 (0 or 1) 的指令給所有將軍

1. 所有的好人都會往相同的方向

2. 如果發指令將軍是好人，所有好人都會聽他的
(CG)

Example. We can know CG is 100% loyal,

Byzantine Broadcast become trivial

Example We can know CG is 100% traitor

就 retreat 就好了

BB Problem Definition

- Entities: ^{generals} nodes, ^{sender} sender
(node 1 is the sender)
- $[n] = \{1, \dots, n\}$ denotes the set of all nodes

- Honest nodes

- Corrupted nodes (a subset of nodes)

對於
Controlled by an adversary

- ① send / transmit arbitrary messages

- ② share info or coordinated attack

- ③ stop

- ④ incorrect stop

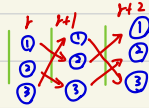
[Static Corruption model
Adversary decides corrupted nodes at beginning]

Synchronous network

If an honest node send a msg

in round r to an honest recipient

the recipient gets it at the beginning of $r+1$



Def of BB

Consistency : If two honest nodes output b_1, b_2 , then $b_1 = b_2$

Validity : If S is honest with input b
then all honest nodes output b'
s.t. $b' = b$