

$$1. \quad L(G) = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}^+$$

对于句子 000, 最左推导:

$$N \Rightarrow ND \Rightarrow NDD \Rightarrow DDD \Rightarrow 0DD \Rightarrow 00D \Rightarrow 000$$

最右推导:

$$N \Rightarrow ND \Rightarrow NO \Rightarrow NDO \Rightarrow NOO \Rightarrow DOO \Rightarrow 000$$

$$2. \quad G_1: 2 \text{ 型}. \quad L(G_1) = \{a0^n \mid n \geq 0 \cup b0^{2n} \mid n \geq 0\}$$

$$G_2: 2 \text{ 型}. \quad L(G_2) = \{a^n c b^n \mid n \geq 0\}$$

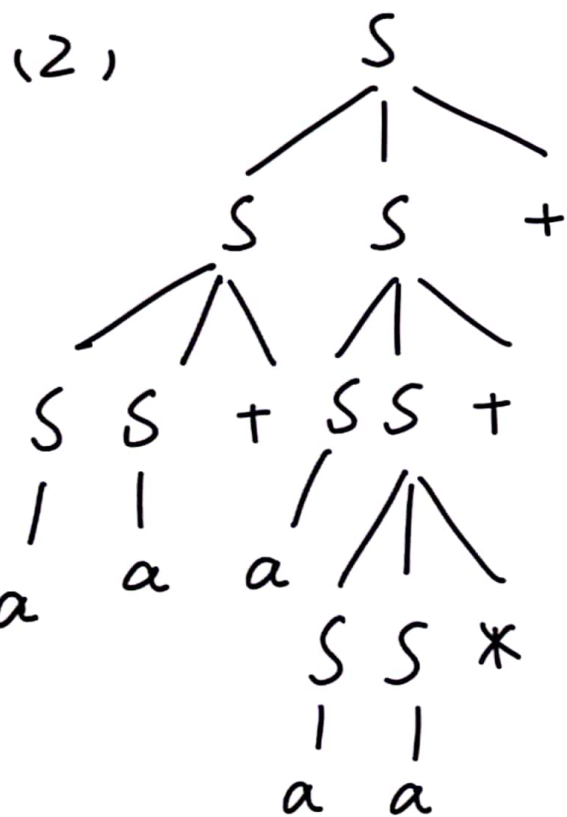
$$G_3: 3 \text{ 型}. \quad L(G_3) = \{a^{2^{n+1}} \mid n \geq 0\}$$



3. 1) $(10|01)^+$

(2) 101010、101001、100110、100101、
011010、011001、010110、010101

4. 1) \$1



(3)

$L(G(S)) = \{ \text{以 } a \text{ 作为运算对象, 包含 } + \text{ 和 } * \text{ 运算符的递归表达式} \}$



5. (1) 对于 $G(N)$ 有: $N \Rightarrow E \Rightarrow 0$
 $N \Rightarrow D \Rightarrow 0$

对于 $G(S)$ 有: $S \Rightarrow S(S)S \Rightarrow S(S)S(S)S \Rightarrow ()()$

$S \Rightarrow S(S)S \Rightarrow S(S)S(S)S \Rightarrow ()()$

(2) $G(N)$: $N \rightarrow ND \mid D$
 $D \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$

$G(S)$: $S \rightarrow S(S) \mid \varepsilon$



$$6. (1) \quad S \rightarrow aBa$$

$$B \rightarrow bB \mid \varepsilon$$

$$(2) \quad S \rightarrow Sc \mid D$$

$$D \rightarrow aDb \mid ab$$

$$(3) \quad S \rightarrow Sb \mid D$$

$$D \rightarrow ab \mid aDb$$

$$(4) \quad S \rightarrow AA$$

$$A \rightarrow aAb \mid \varepsilon$$

$$(5) \quad S \rightarrow aSb \mid A$$

$$A \rightarrow bAa \mid \varepsilon$$

$$(6) \quad S \rightarrow a \mid b \mid c \mid aSa \mid bSa \mid cSc \mid \varepsilon$$

