with thanks to Dr. Steve Bellan and the Alachua County Control Flu Program.

Title: Simplification for generalization – an introduction to modelling infectious disease dynamics

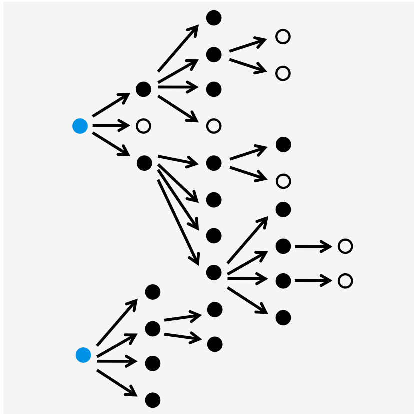
Attribution: Prof. Juliet Pulliam

Source URL: http://github.sacema.org/s4g/Pulliam_DTTC_S4G.pdf

For further information please contact Prof. Juliet Pulliam (pulliam@sun.ac.za).

Simplification for Generalization:

an introduction to modelling infectious disease dynamics



Interest Group in Data Analysis and Modelling, Desmond Tutu TB Centre

April 11, 2017

Juliet R.C. Pulliam, PhD

DST-NRF Centre of Excellence in Epidemiological Modelling and Analysis (SACEMA)

Stellenbosch University

School-located Influenza Vaccination

Alachua County Control Flu Program

- Community-supported
- 2006/07; 2009-Present
- K-8th; Pre-K to 12th
- Live-attenuated vaccine at school
- Inactivated vaccine at provider
- 300 volunteers, 27 community partners
- Recognized by AMA/CDC & IOM

Slide courtesy of CH Tran

Alachua County Control Flu Program

Coverage

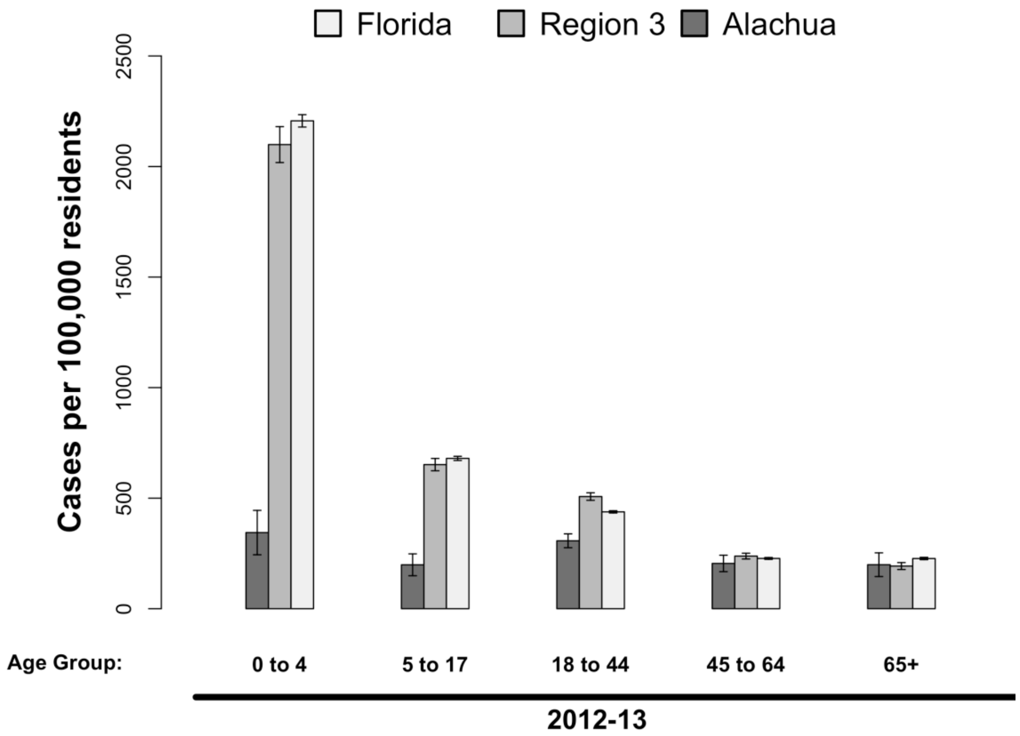
	8 States Averaged[+]	Alachua County						
	08/09	06/07	07/08	08/09	09/10	10/11	11/12	12/13
Preschool	~26%	-	-	-	12%	16%	16%	16%
Elementary	16%	>25%	-	-	67%	67%	63%	65%
Middle	13%	>24%	-	-	43%	41%	43%	49%
High	9%	-	-	-	6%	23%	24%	30%
School-Aged	-	>25%	-	-	42%	48%	47%	50% *(13,579)*

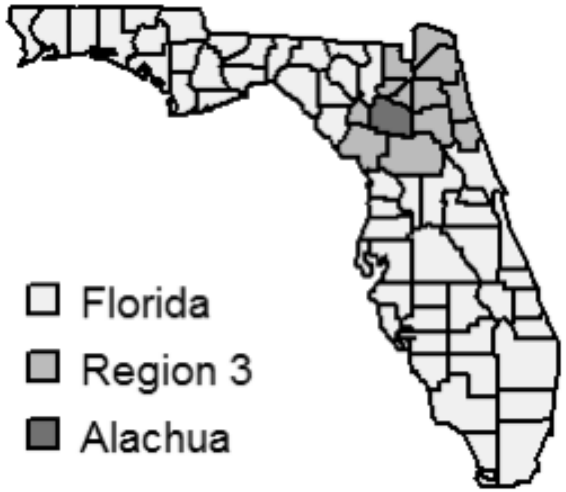
Slide courtesy of CH Tran

Alachua County Control Flu Program

Impact

2012-2013 season





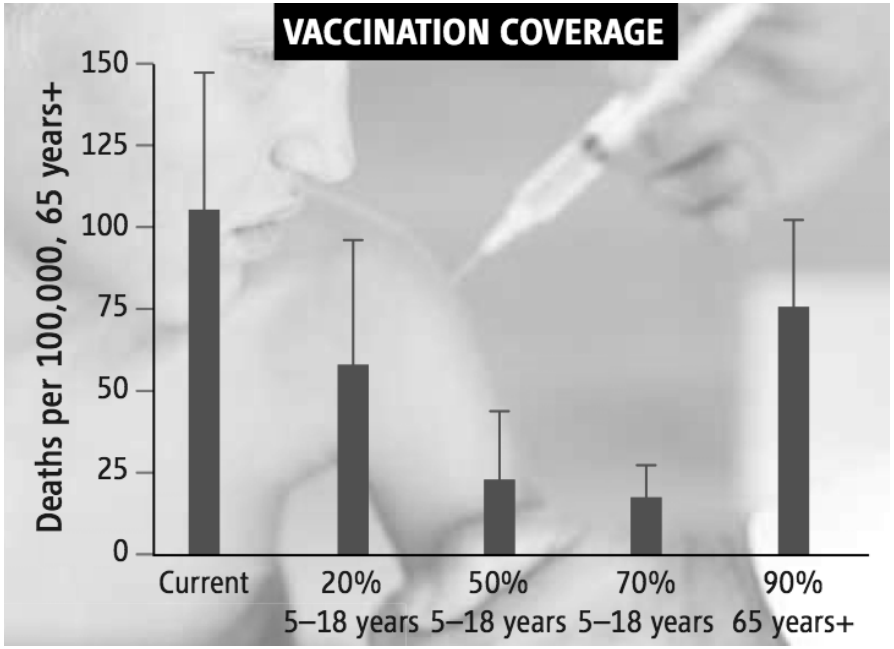
Tran *et al*. 2014

Alachua County Control Flu Program

Why did they think it would work?

Alachua County Control Flu Program

Why did they think it would work?



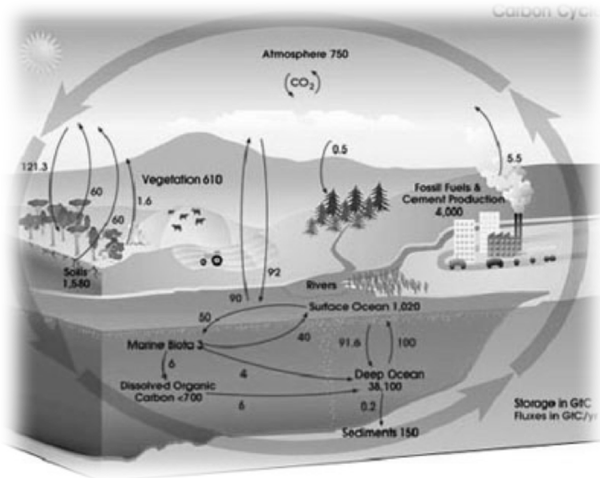
Halloran & Longini 2006 Science

Model-based prediction…

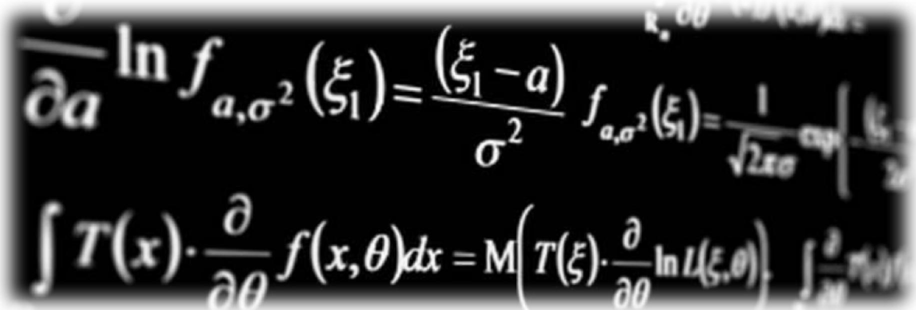
What are models?

- Physical

- Conceptual



- Mathematical



What are dynamical models?

Statistical Models

- Account for bias and random error to find correlations that may imply causality.
- Often the first step to assessing relationships.
- Assume independence of individuals (at some scale).

Dynamical Models

- Systems Approach: Explicitly model multiple mechanisms to understand their interactions.
- Link observed relationships at different scales.
- Explicitly focus on dependence between individuals

Dynamical models

Explicitly account for the dependence between individual outcomes that is inherent in the transmission process for communicable diseases

Can be used to describe the evolution of a system through time – such as changes in disease incidence that result from the interaction between transmission and immunity

Model World

an abstraction of the world that is simple and fully specified, which we construct to help us understand particular aspects of the real world

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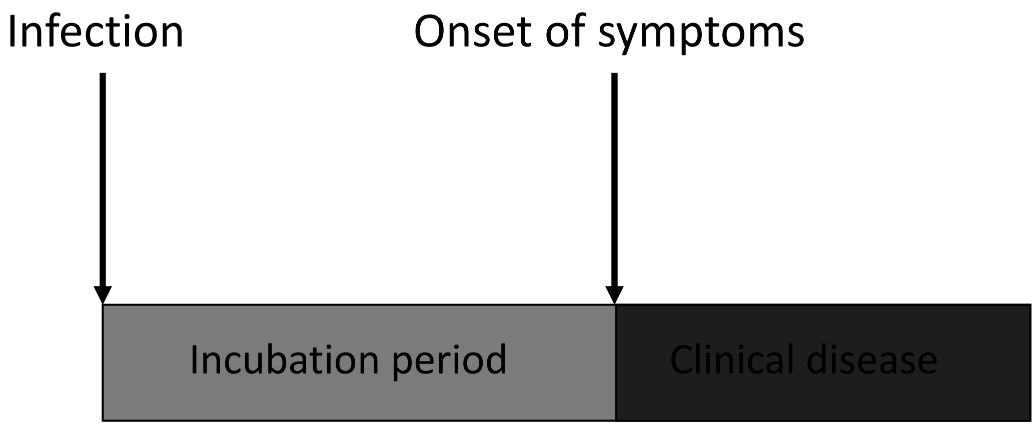
model worlds have their own rules

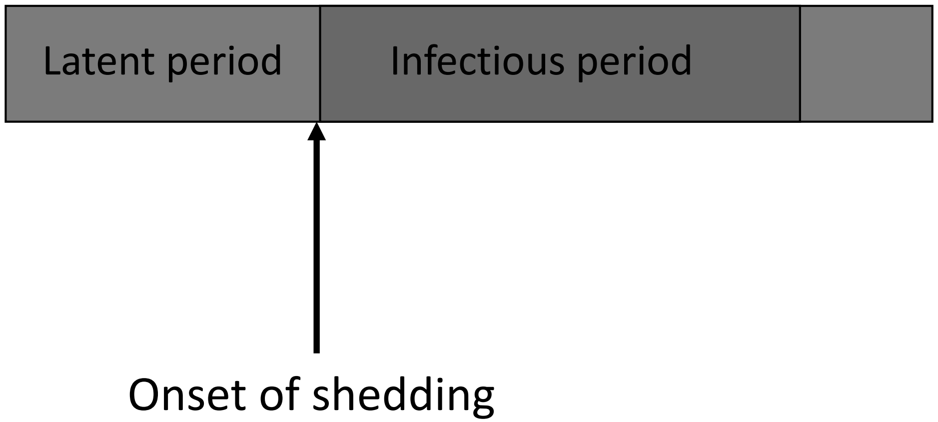
sometimes they reflect reality and sometimes they do not

but if you specify all of your assumptions, you can figure out what things are possible given your assumptions

Natural History of Infection

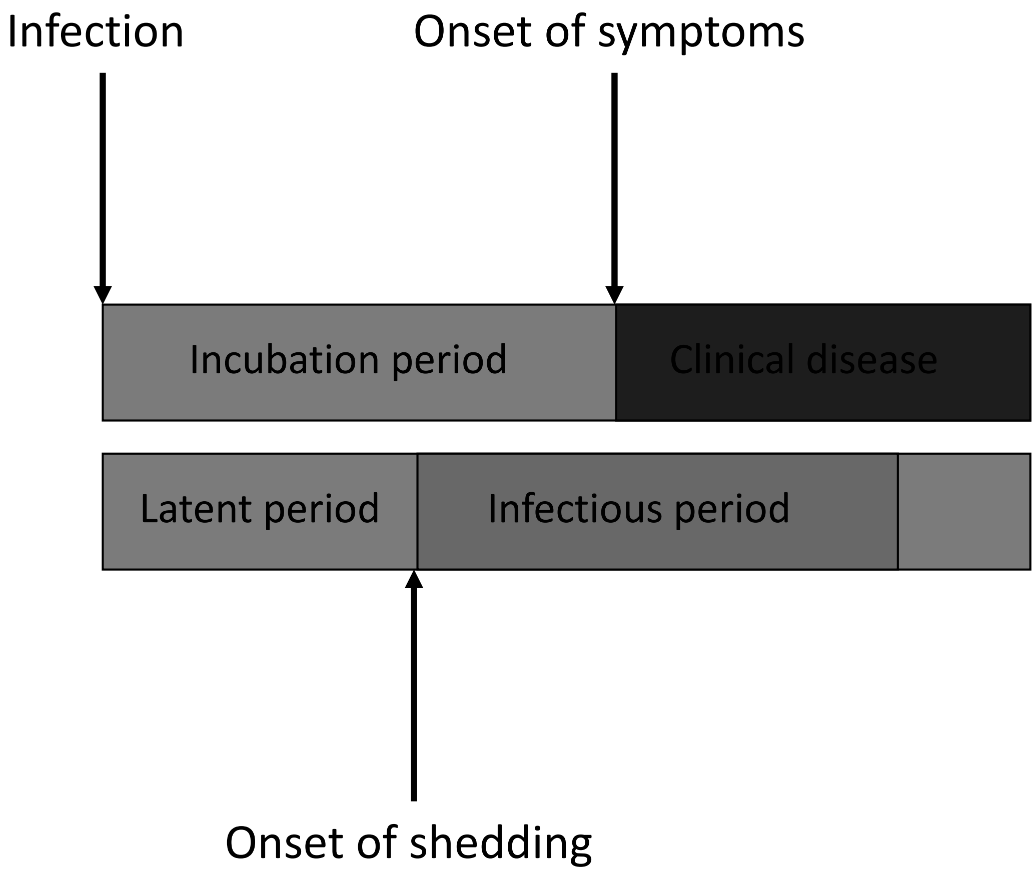


Natural History of Infection



Natural History of Infection

Acute, immunizing infections



<u>Acute</u>

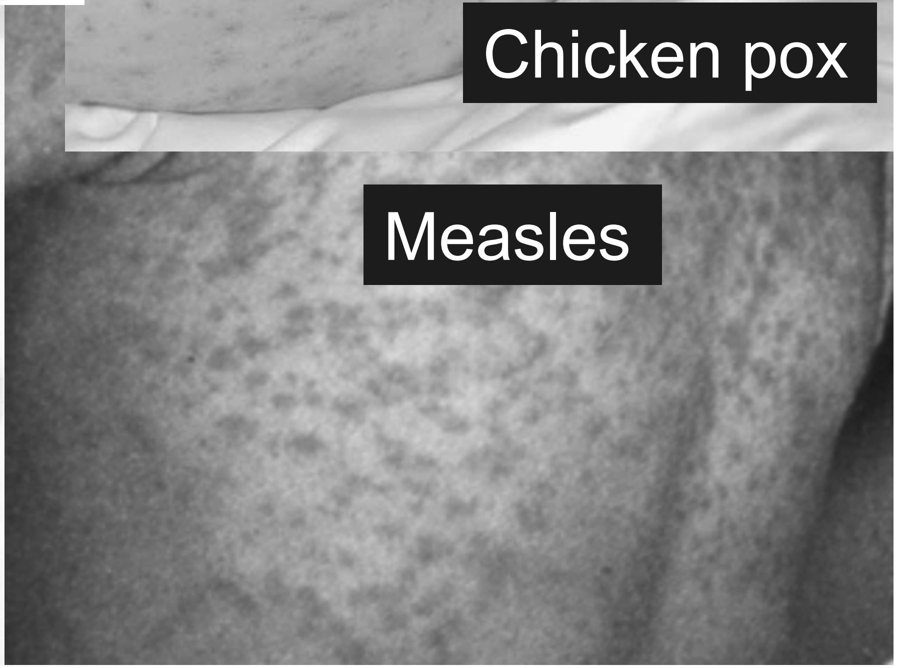
Infection time course
<<<
host lifespan

<u>Immunizing</u>

infection ➔ antibody production

prevents future infection

Examples



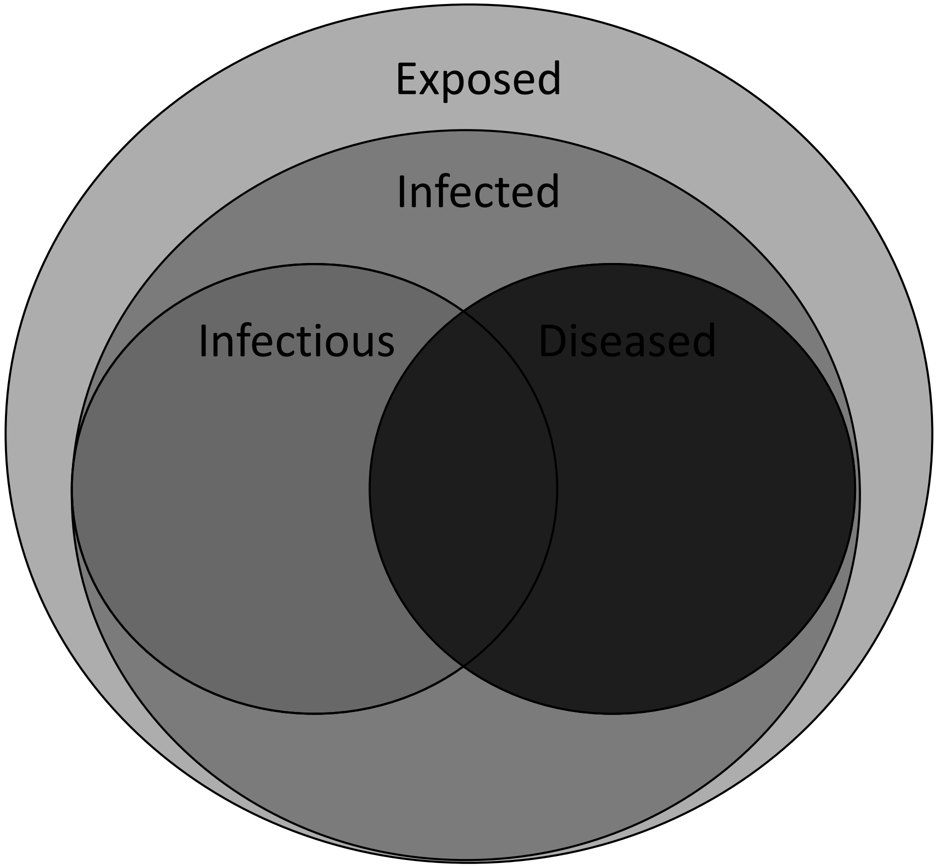
Natural History of Infection

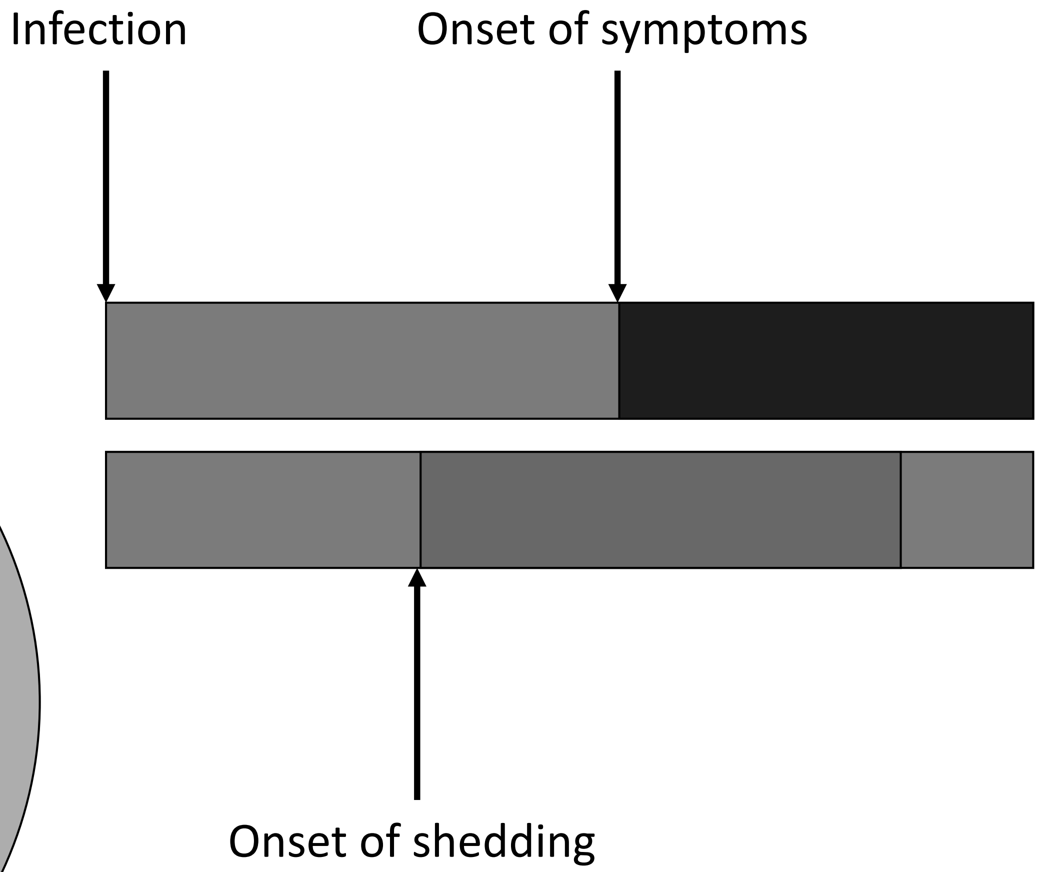
Table 3.1 Incubation, latent and infectious periods (in days) for a variety of viral and bacterial infections. Data from Fenner and White (1970), Christie (1974), and Benenson (1975)

Infectious disease	Incubation period	Latent period	Infectious period
Measles	8–13	6–9	6–7
Mumps	12–26	12–18	4–8
Whooping cough (pertussis)	6–10	21–23	7–10
Rubella	14–21	7–14	11–12
Diphtheria	2–5	14–21	2–5
Chicken pox	13–17	8–12	10–11
Hepatitis B	30–80	13–17	19–22
Poliomyelitis	7–12	1–3	14–20
Influenza	1–3	1–3	2–3
Smallpox	10–15	8–11	2–3
Scarlet fever	2–3	1–2	14–21

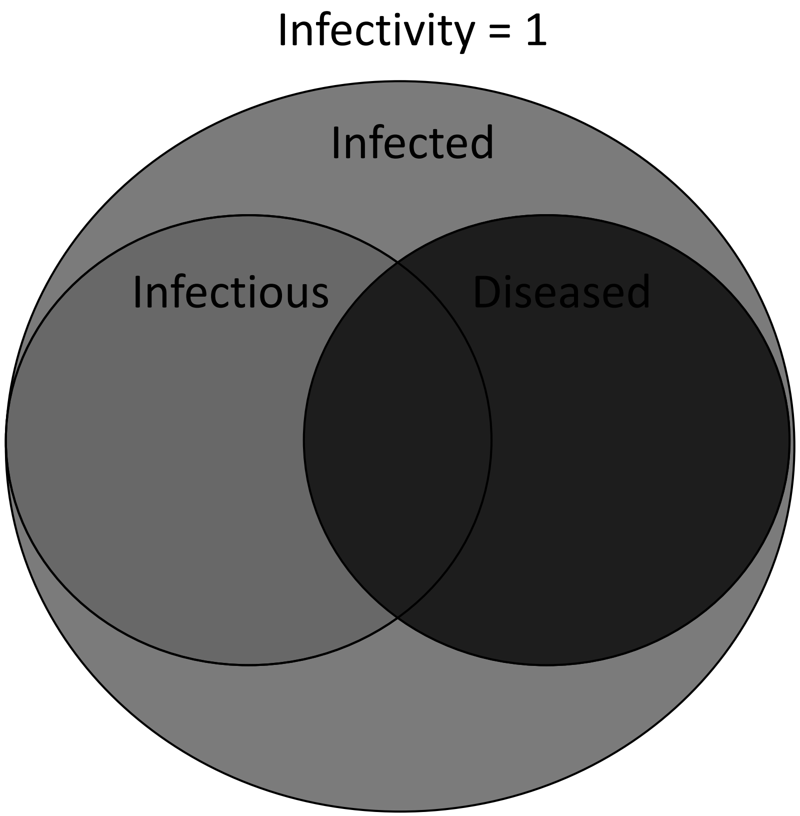
Anderson and May 1982 Science

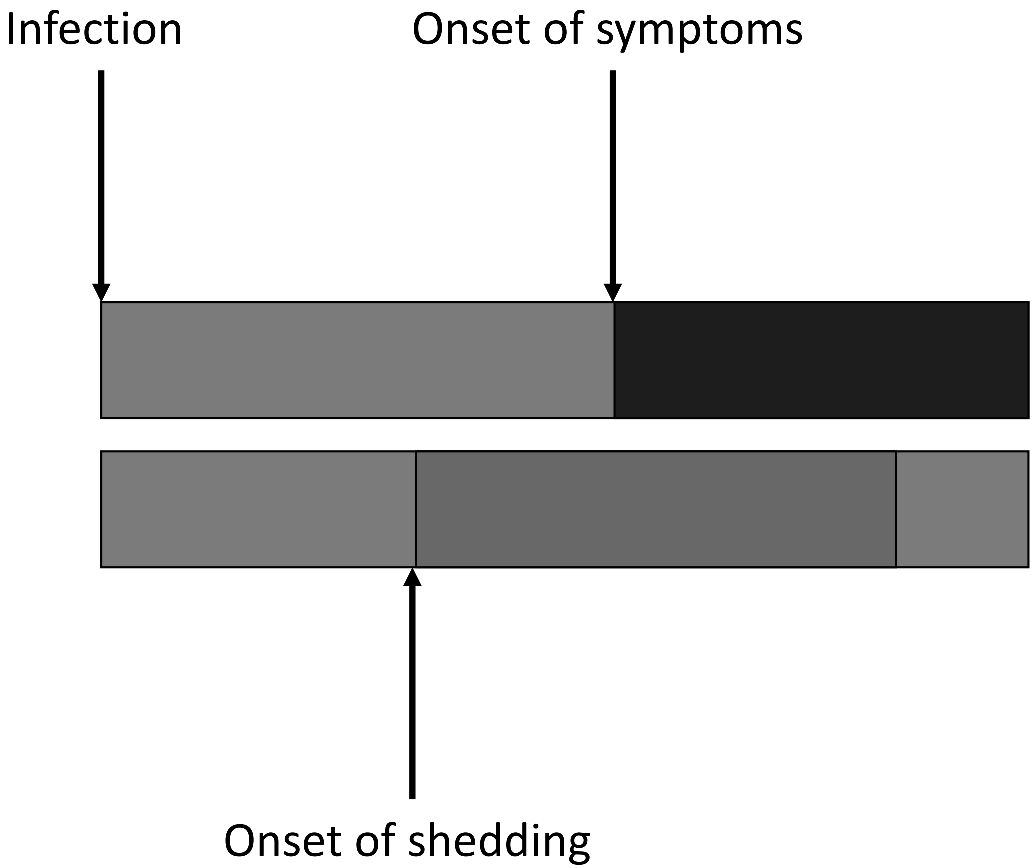
Terminology





A simple view of the world

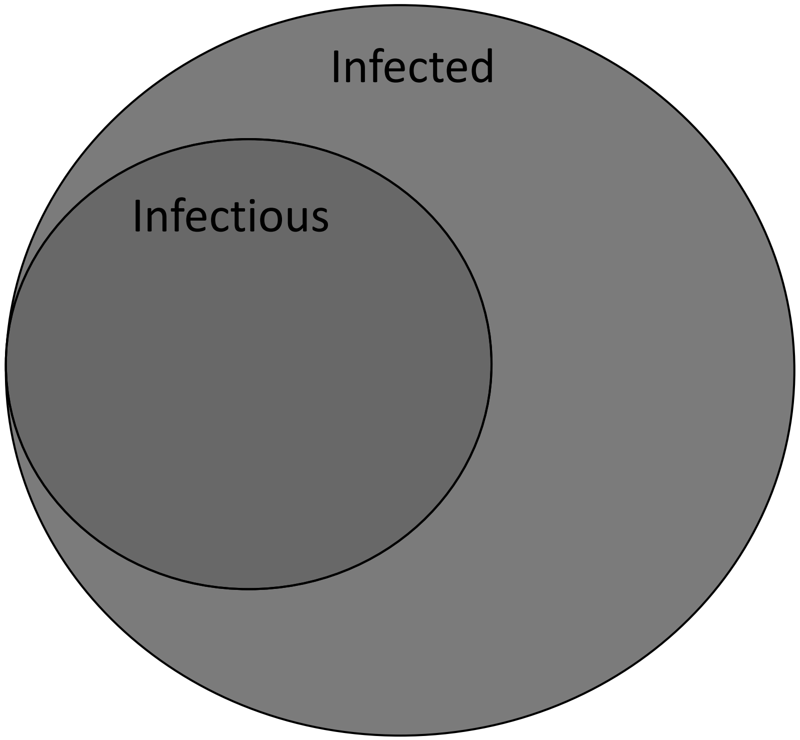


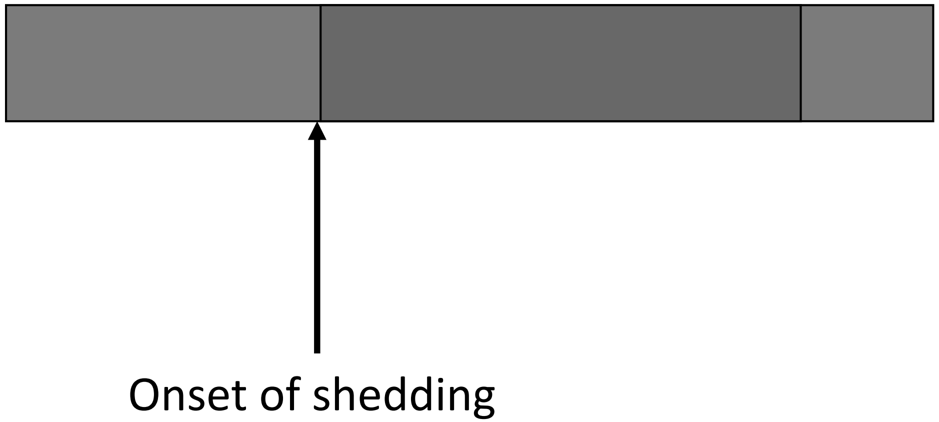


A simpler view of the world

Don't worry about symptoms and disease!

Infectivity = 1





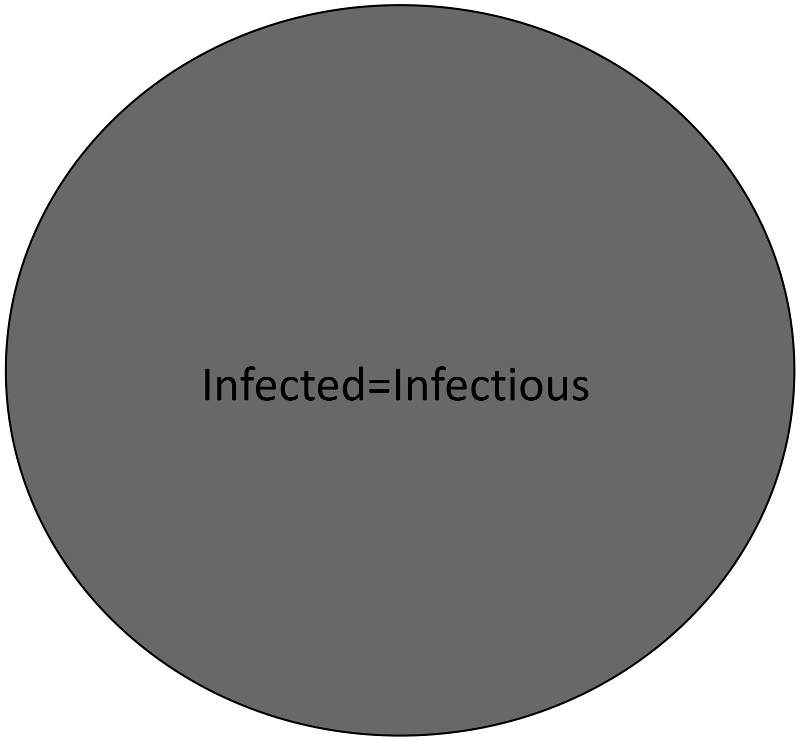
An extremely simple view of the world

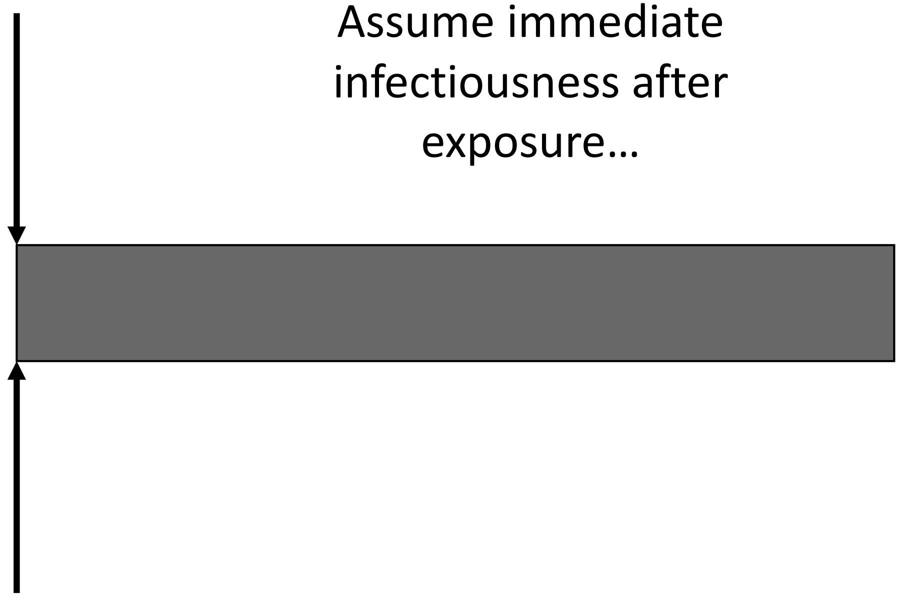
Don’t worry about symptoms and disease!

Infection

Assume immediate infectiousness after exposure…

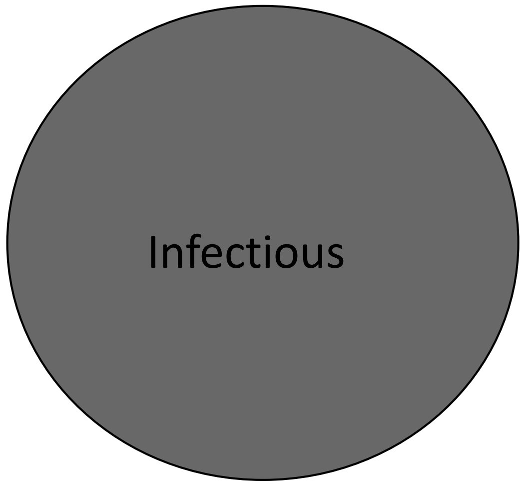
Infectivity = 1



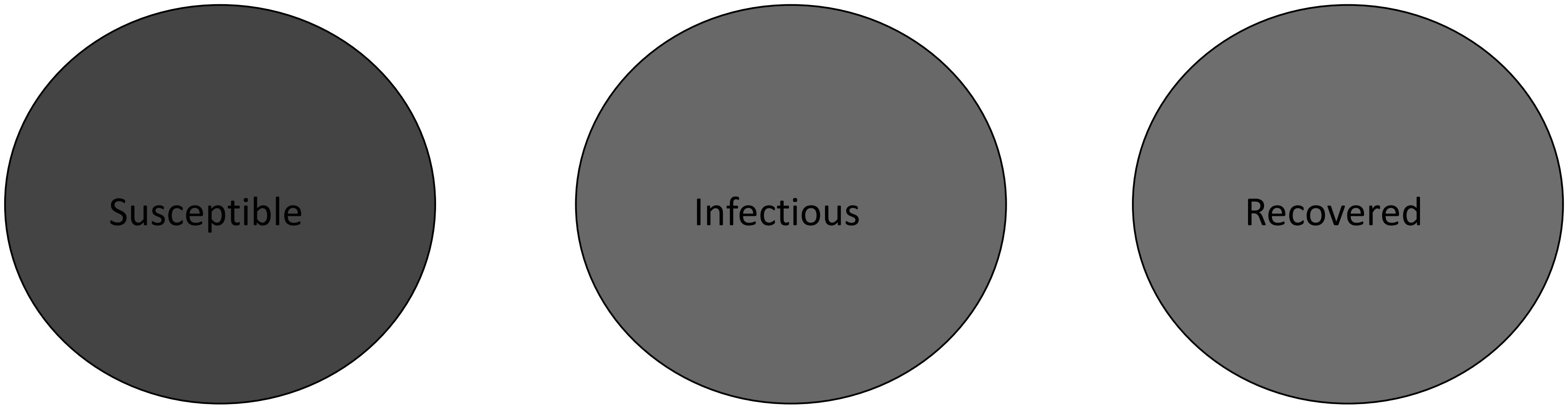


Onset of shedding

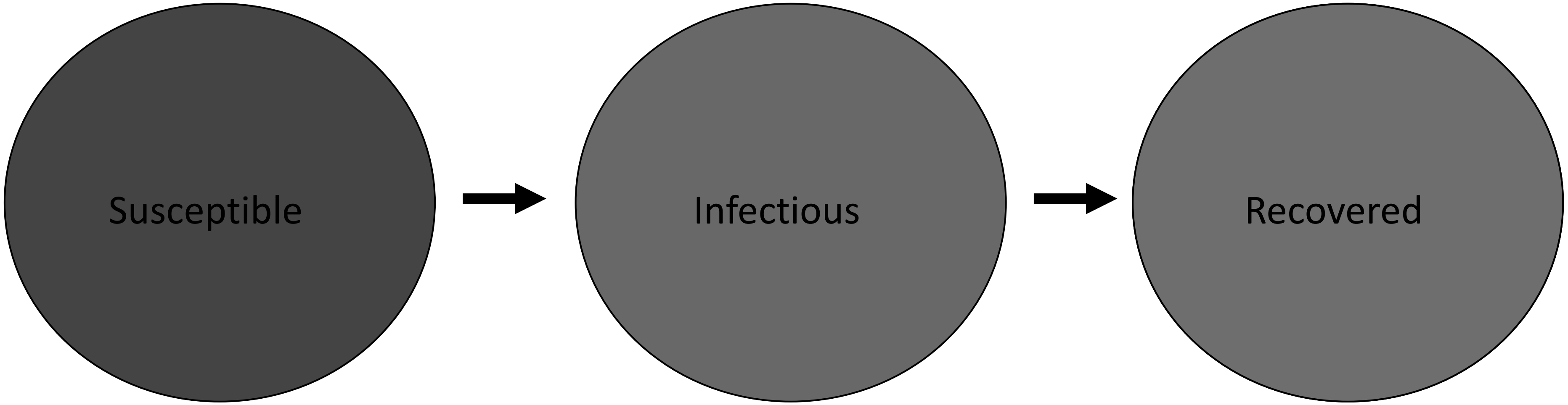
An extremely simple view of the world



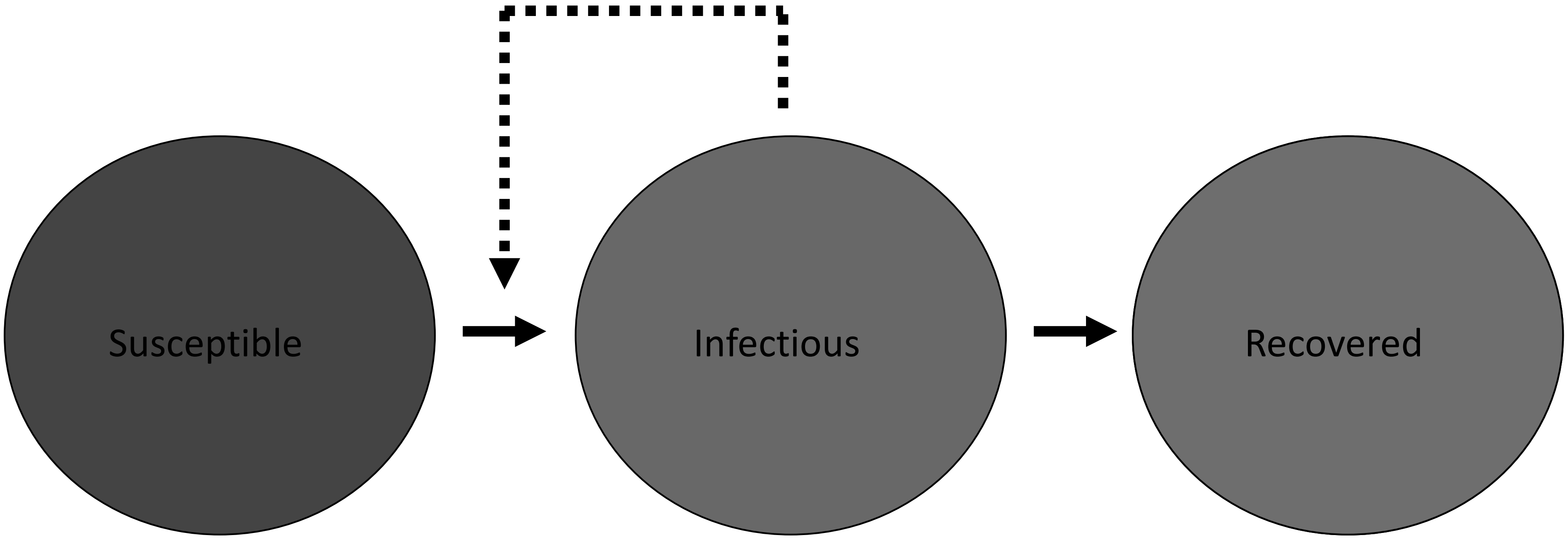
An extremely simple view of the world



An extremely simple view of the world

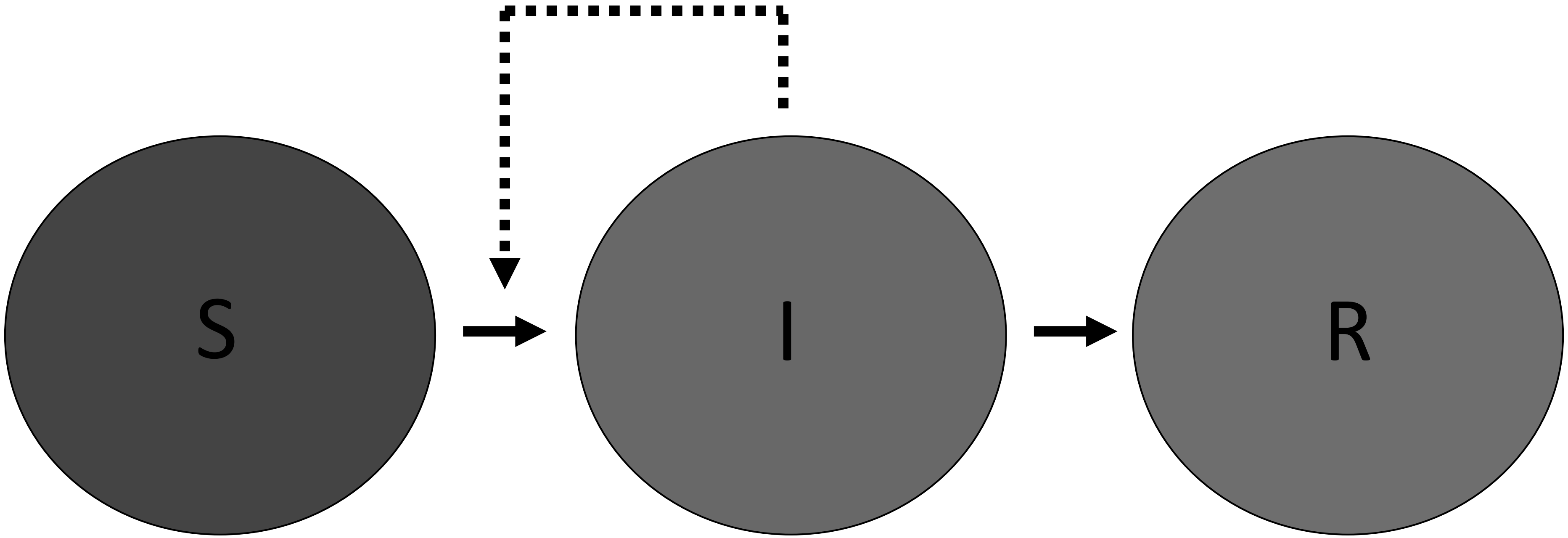


Health-related States

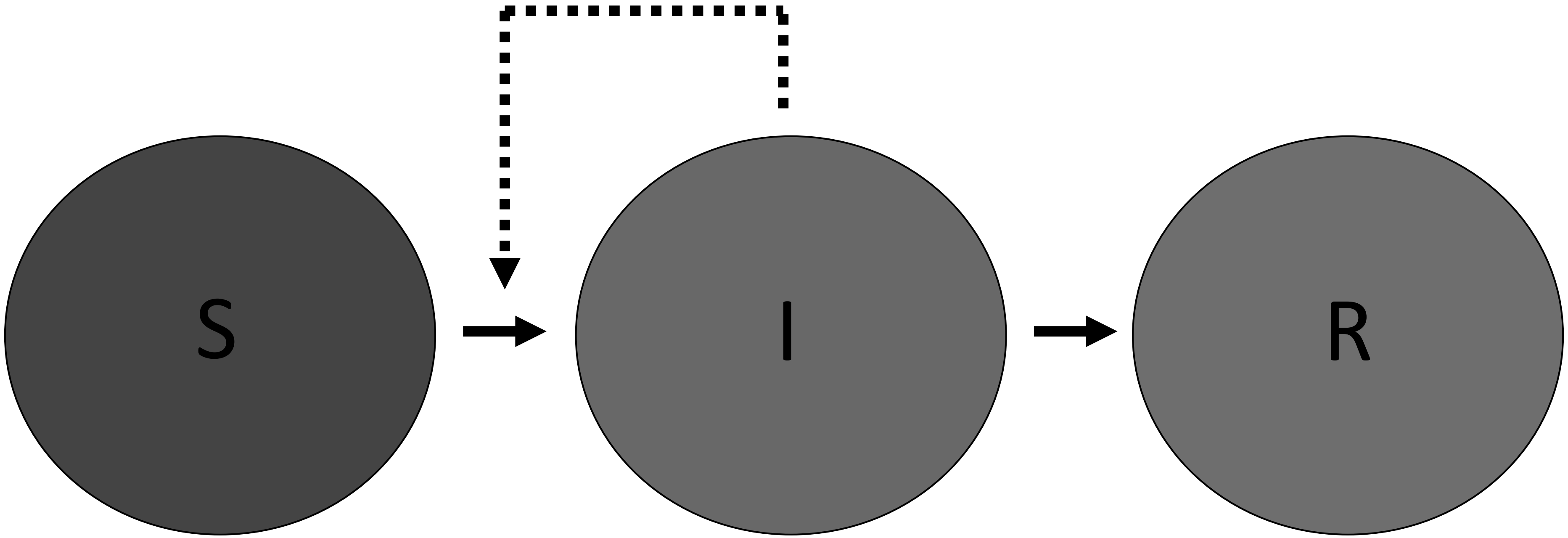


The rate at which susceptible individuals become infected depends on how many infectious people are in the population

State variables

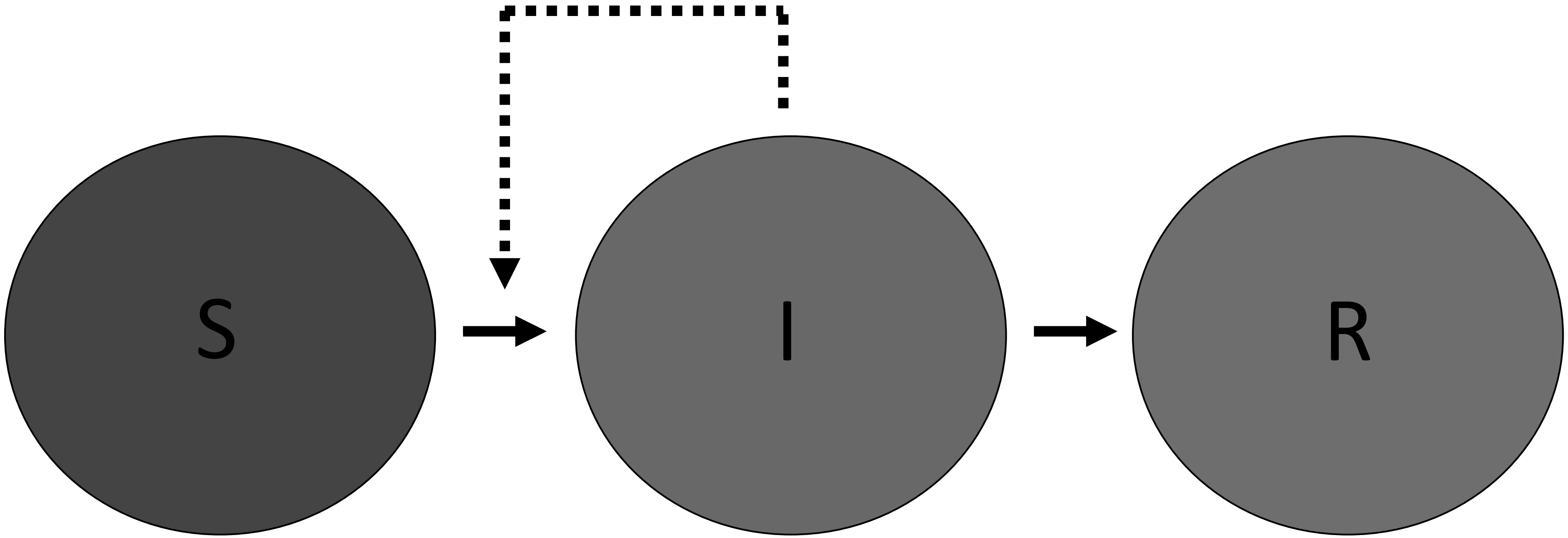


State variables



We can use equations to describe the rate at which individuals flow between states

SIR Model



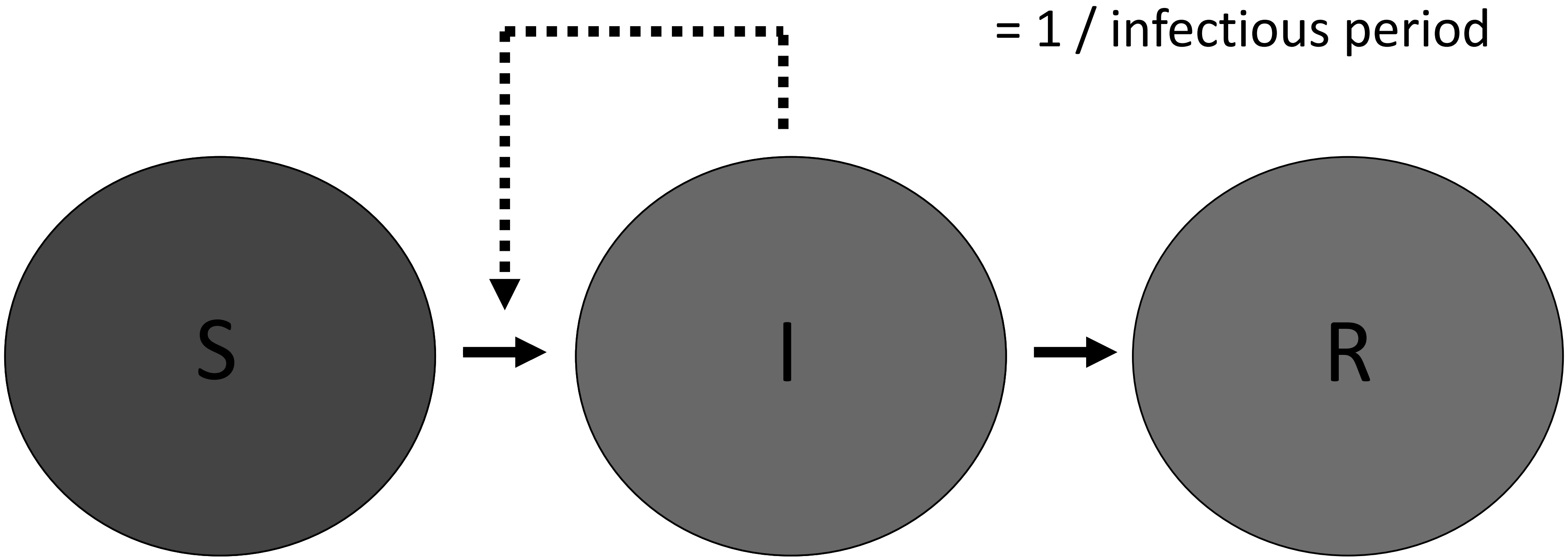
= transmission coefficient

= per capita contact rate * infectivity

= per capita contact rate   (infectivity = 1)

proportion of contacts that are with an infectious individual

SIR Model

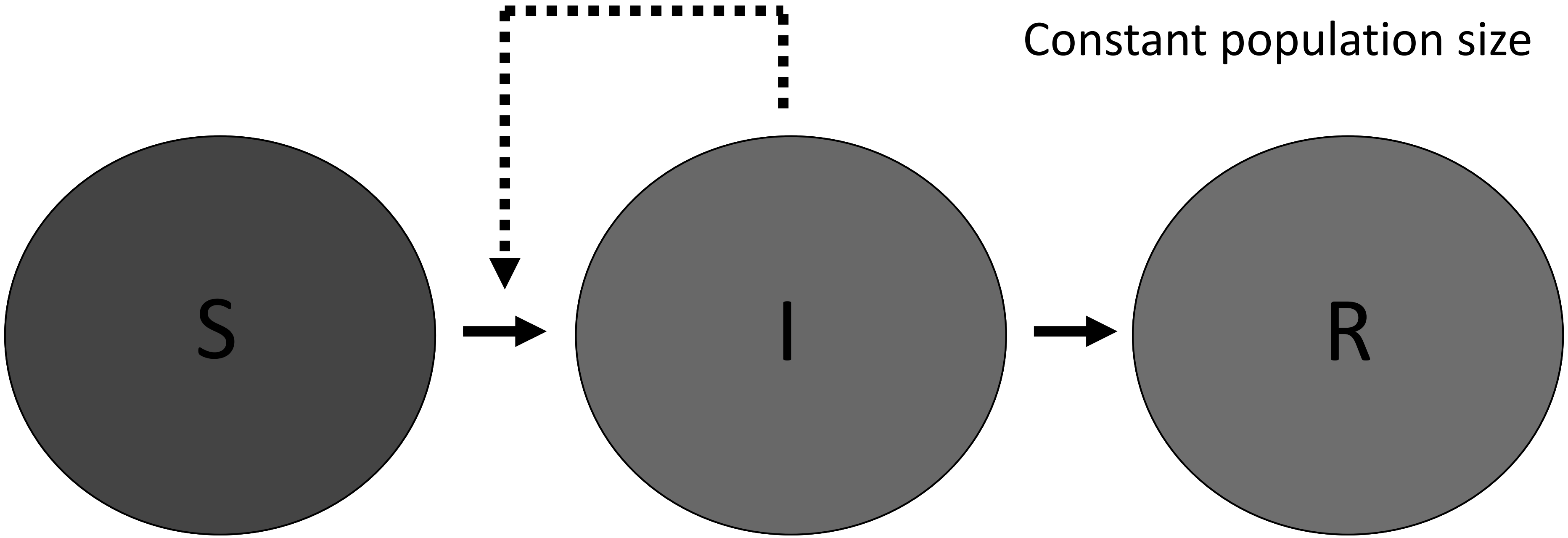


If infectious people recover at a rate of 0.5 / day,

the average time they spend infectious is 1 / 0.5 = 2 days

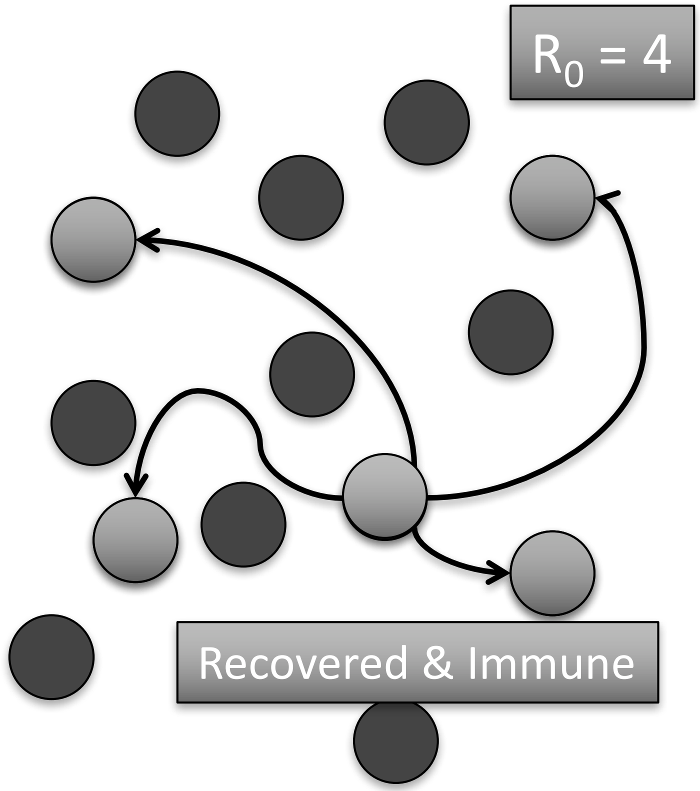
SIR Model

Constant population size



R_0: The Basic Reproductive Number

Average # of secondary infections an infected host produces in a population with no pre-existing immunity



SIR Model

$\xrightarrow{N \text{ large}}$

1

Rate at which an infected individual produces new infections in a naïve population

X

Proportion of new infections that become infectious

X

Average duration of infectiousness

SIR Model

Rate at which an infected individual produces new infections in a naïve population

X

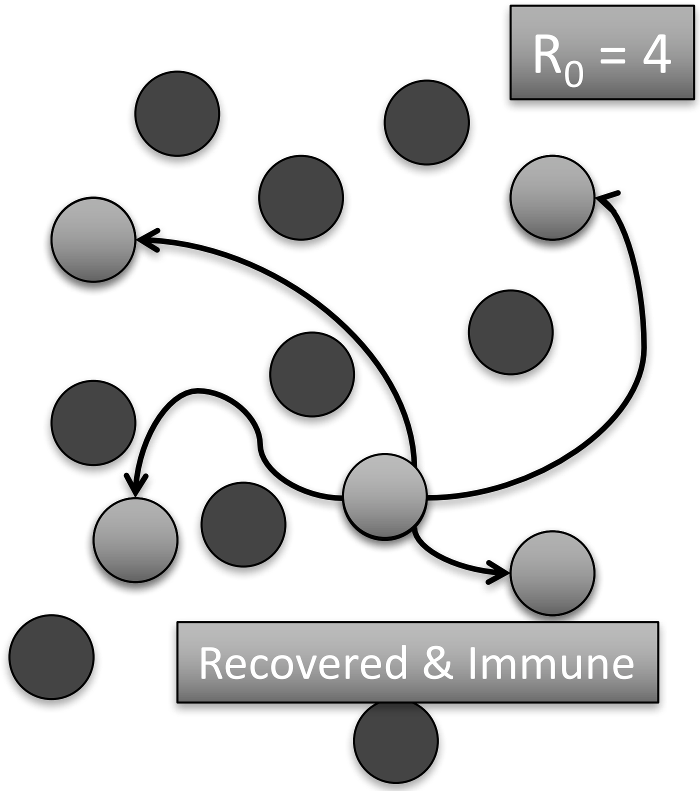
Proportion of new infections that become infectious

X

Average duration of infectiousness

R_0: The Basic Reproductive Number

- Average # of secondary infections an infected host produces in a susceptible population.

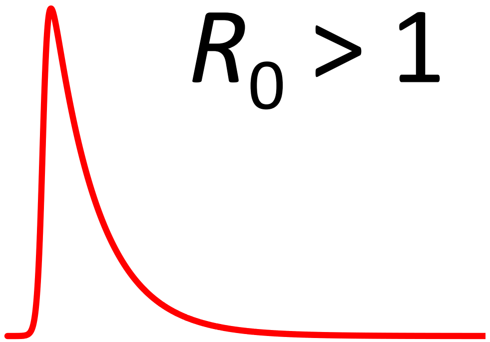


- Threshold criteria:

  If $R_0 < 1$, disease dies out

  If $R_0 > 1$, disease persists

SIR Model: R_0 as a Threshold



$R_0 > 1$

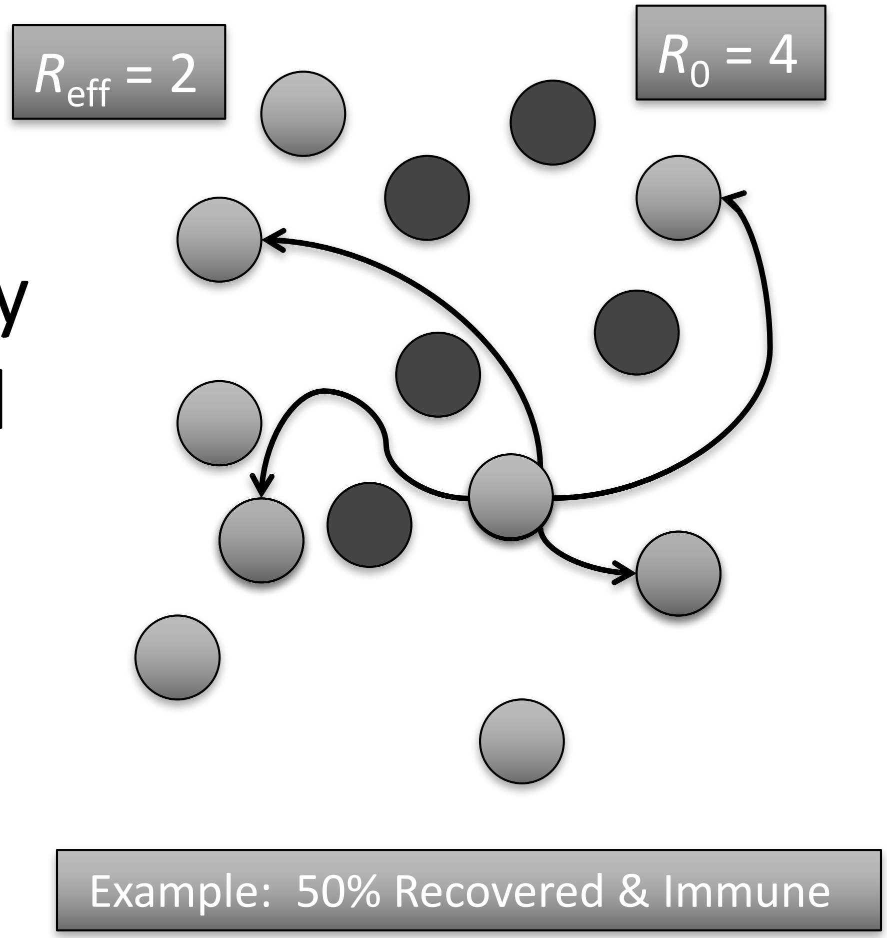
Disease Introduction:

$R_0 \leq 1$

Epidemic occurs if $R_0 > 1$.

R_{eff}: The Effective Reproductive Number

The average # of secondary infections that an infected host produces in a population



R_{eff}: Effective Reproductive Number

Rate at which an infected individual
produces new infections in
a general population

X

1

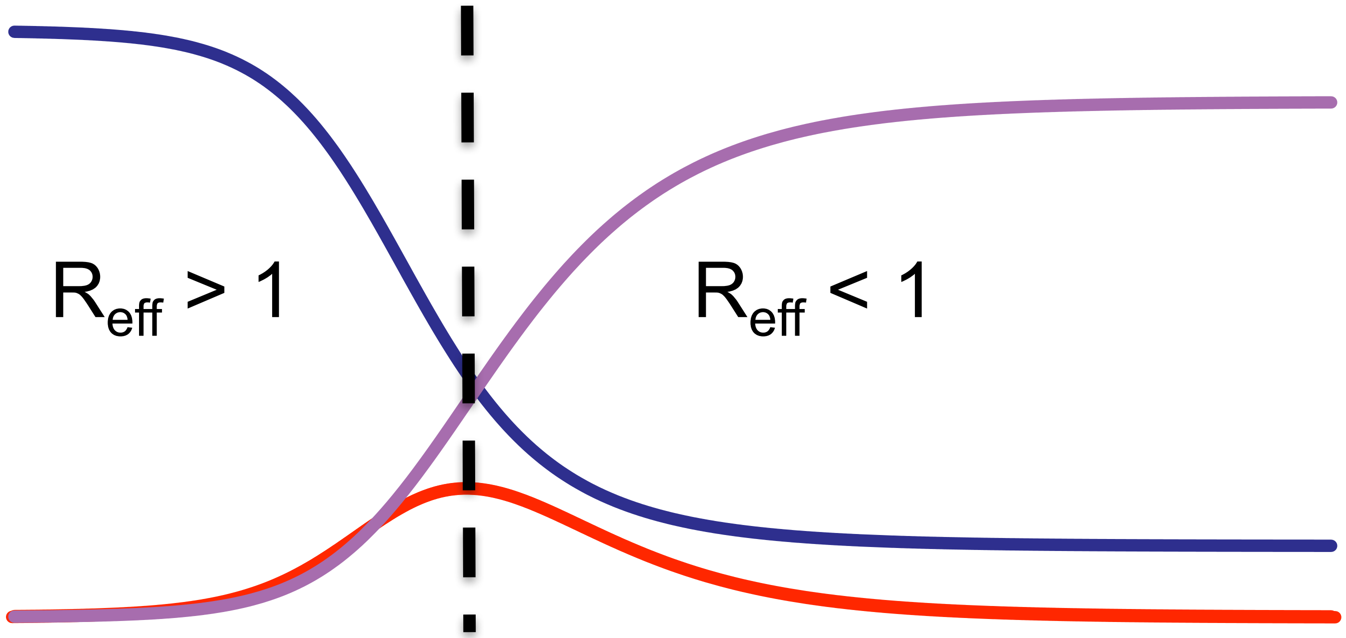
Proportion of new infections that
become infectious

X

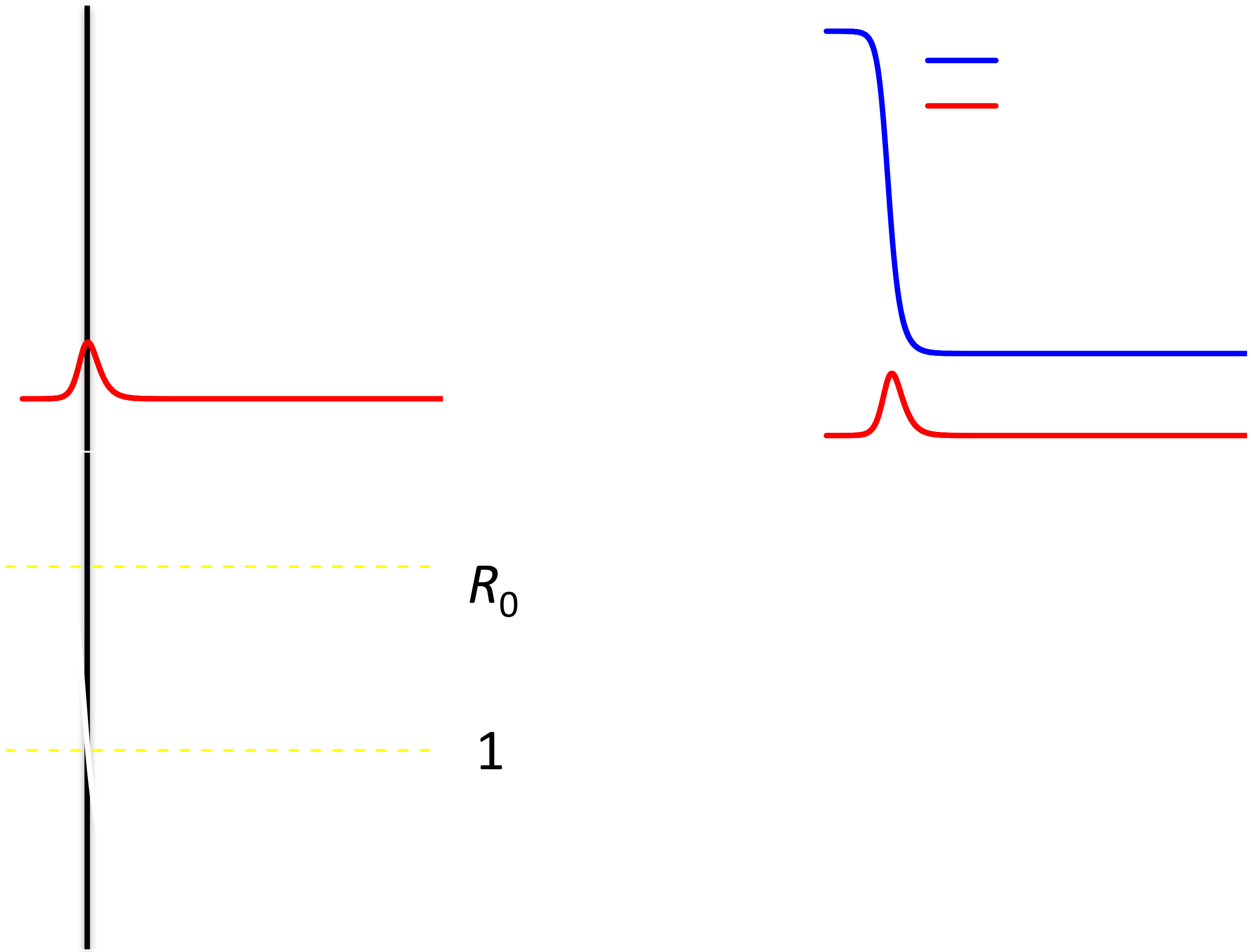
Average duration of infectiousness

Why do epidemics peak?

Death or long-term immunity leads to exhaustion of susceptibles

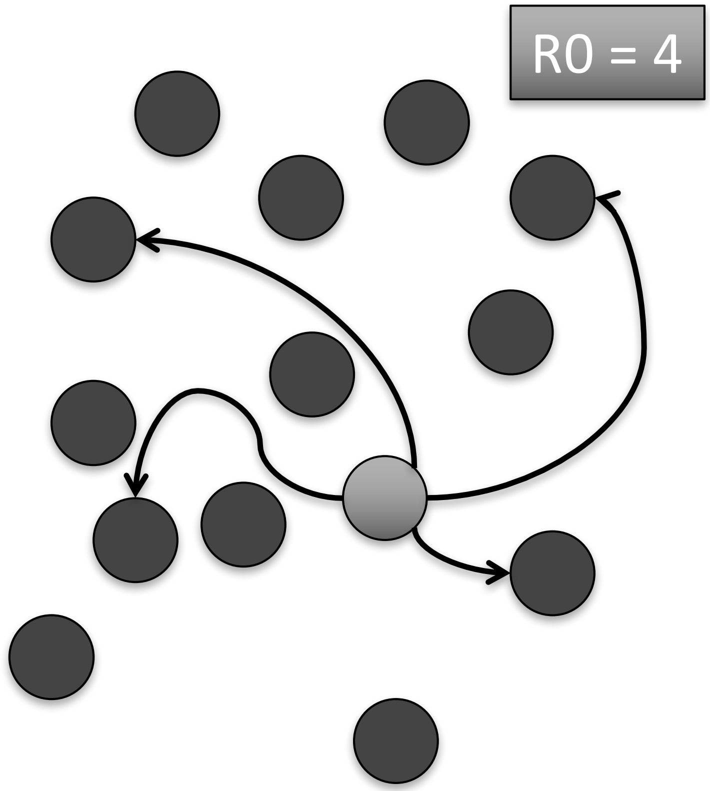


R_{eff}: The Effective Reproductive Number

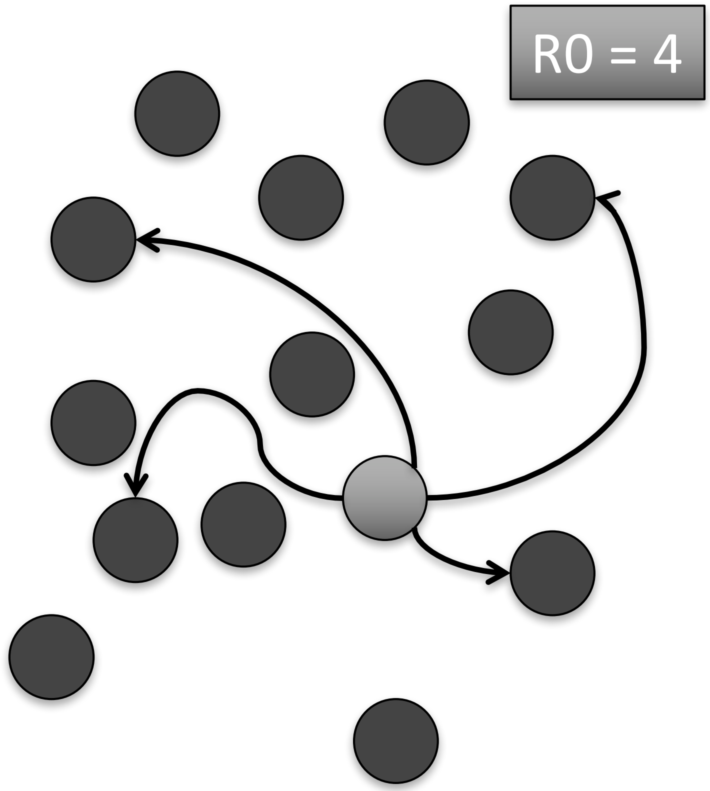


Proportion to Vaccinate

- So what proportion of the population should be vaccinated to prevent pathogen invasion?



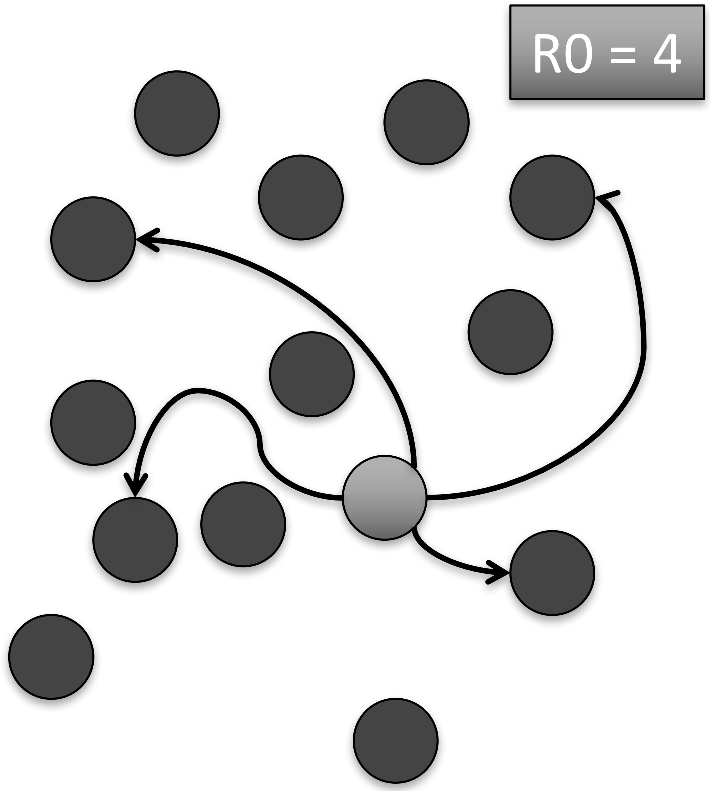
Proportion to Vaccinate



For a disease to die out, $R_{eff} \leq 1$

Proportion to Vaccinate

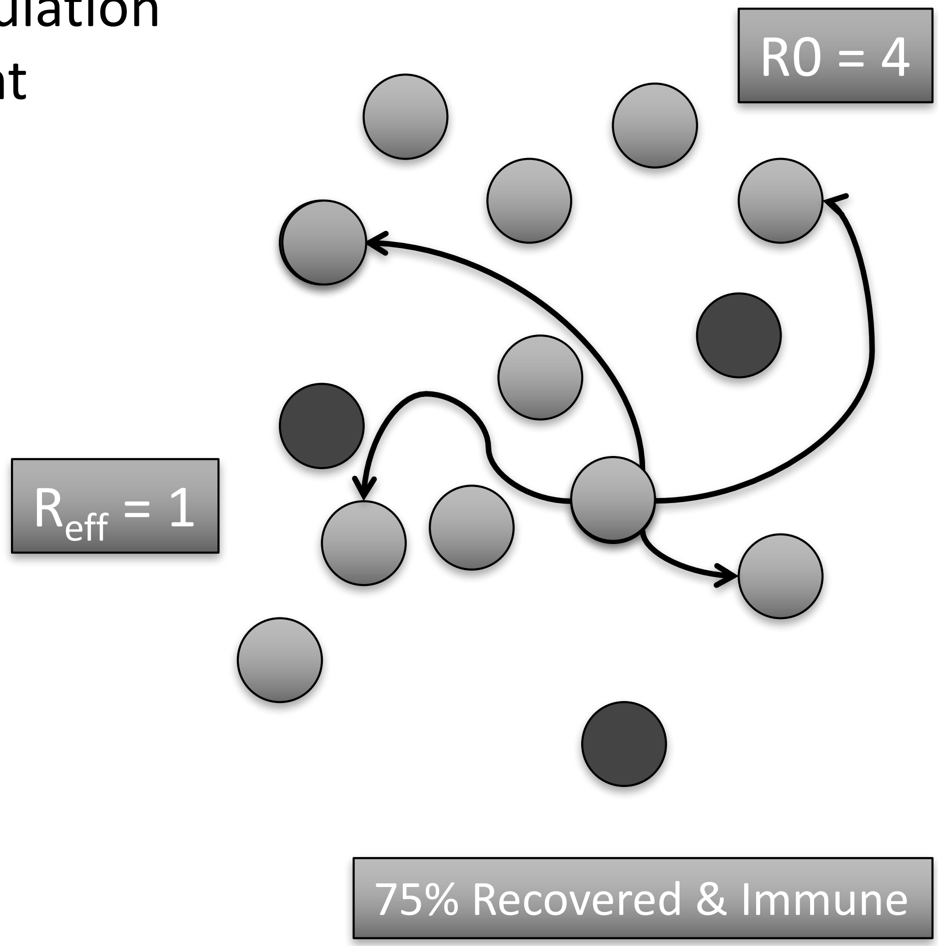
Proportion immune = P_V =
1 – proportion susceptible



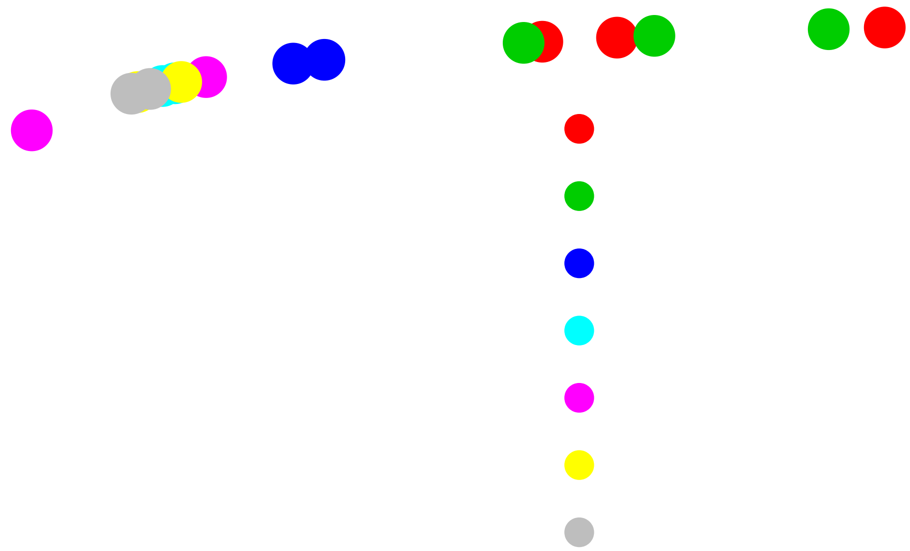
You don't have to vaccinate everyone to eliminate transmission!!!

Proportion to Vaccinate

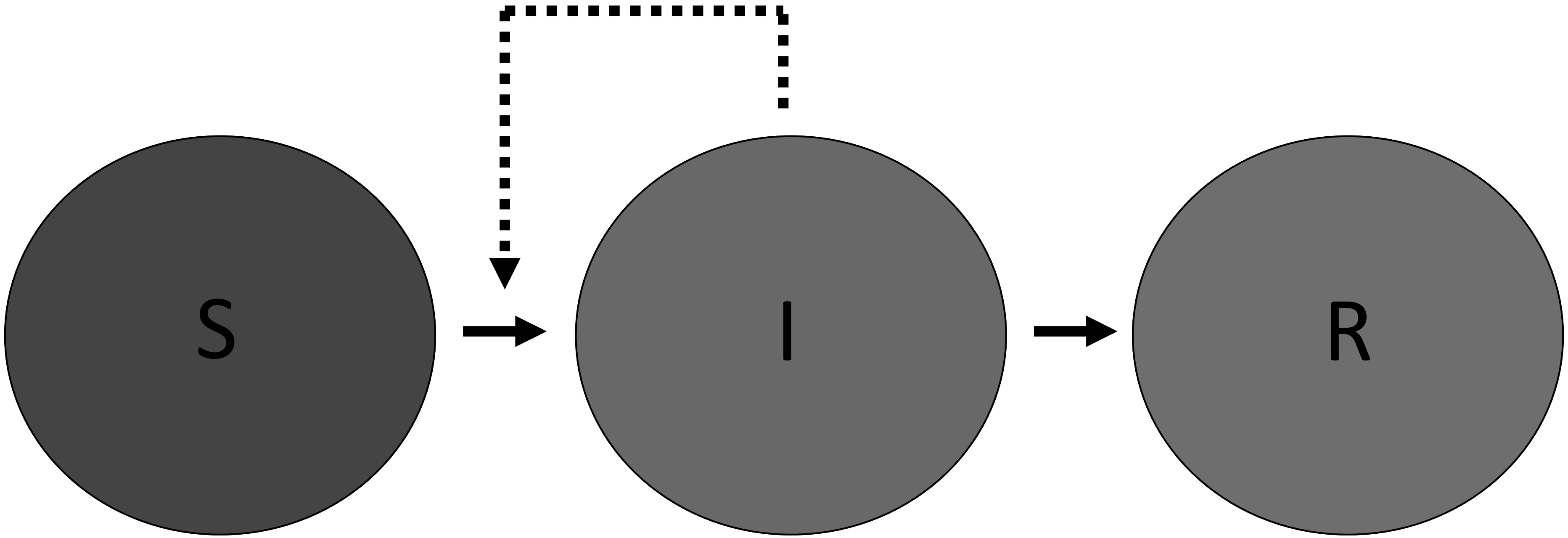
- So what proportion of the population should be vaccinated to prevent pathogen invasion?



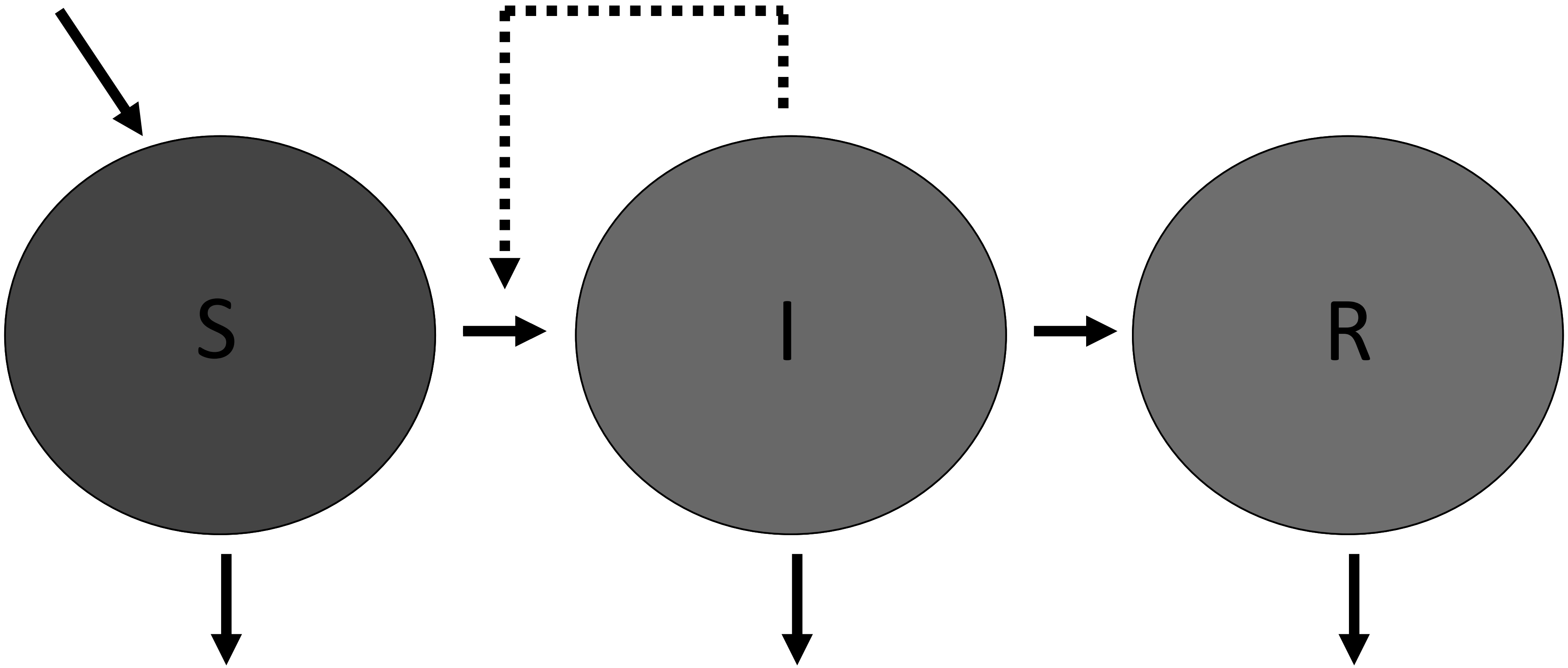
Elimination Thresholds



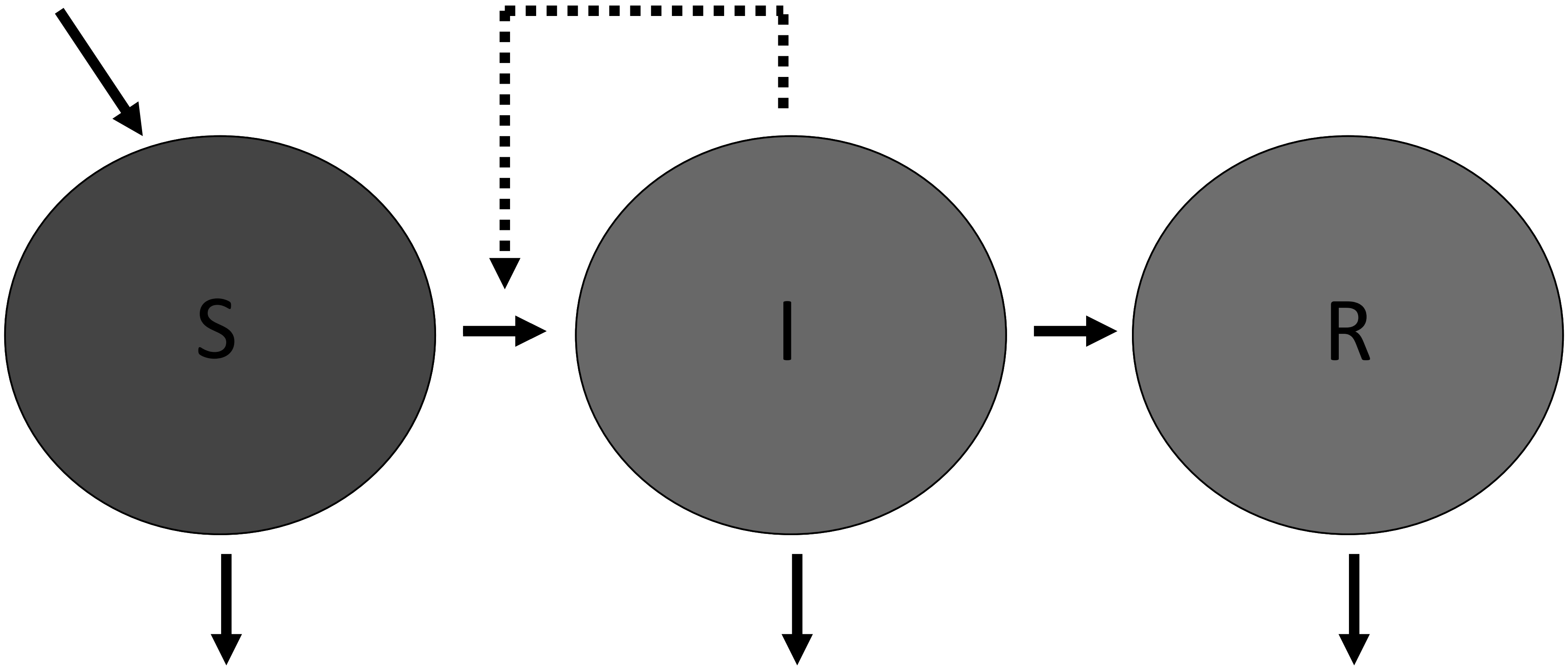
SIR Model



SIR Model with Birth & Death



SIR Model with Birth & Death



SIR Model with Birth & Death

$$\xrightarrow{N \text{ large}}$$

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Rate at which an infected individual produces new infections in a naïve population

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Proportion of new infections that become infectious

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Average duration of infectiousness

SIR Model with Birth & Death

Rate at which an infected individual produces new infections in a naïve population

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Proportion of new infections that become infectious

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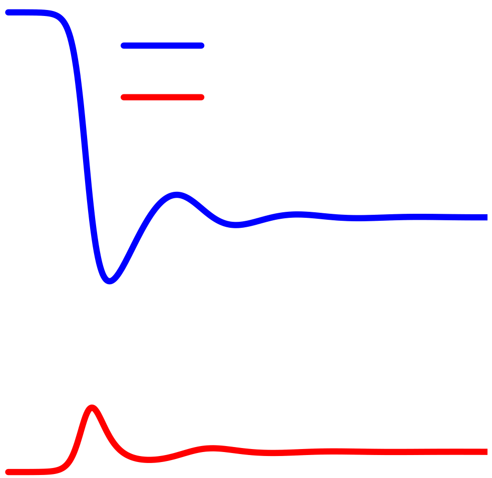
Average duration of infectiousness

SIR Model with Birth & Death

Dynamics upon introduction:

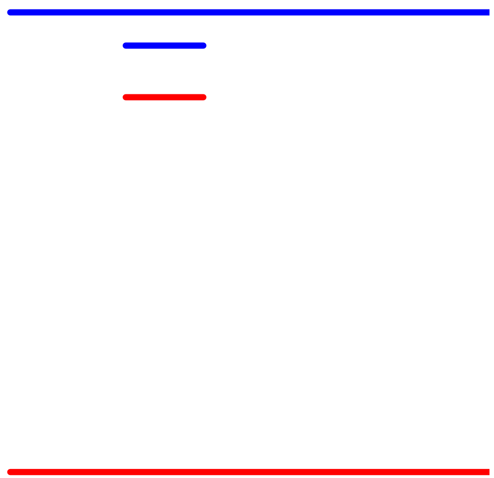
Epidemic if $R_0 > 1$

Endemic state



No epidemic if $R_0 \leq 1$

No endemic state



R_{eff}: Effective Reproductive Number

1

Rate at which an infected individual
produces new infections in
a non-fully susceptible population

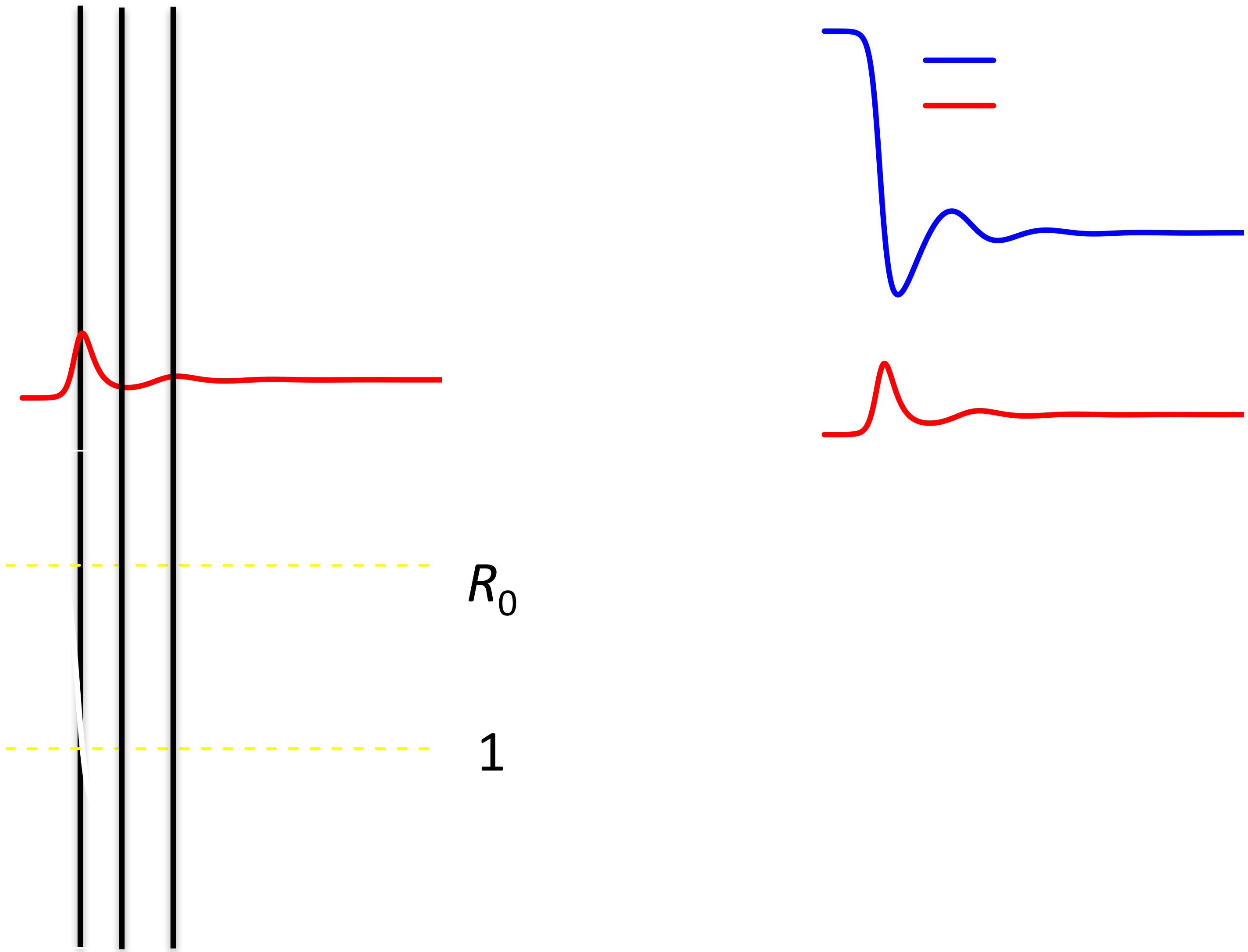
X

Proportion of new infections that
become infectious

X

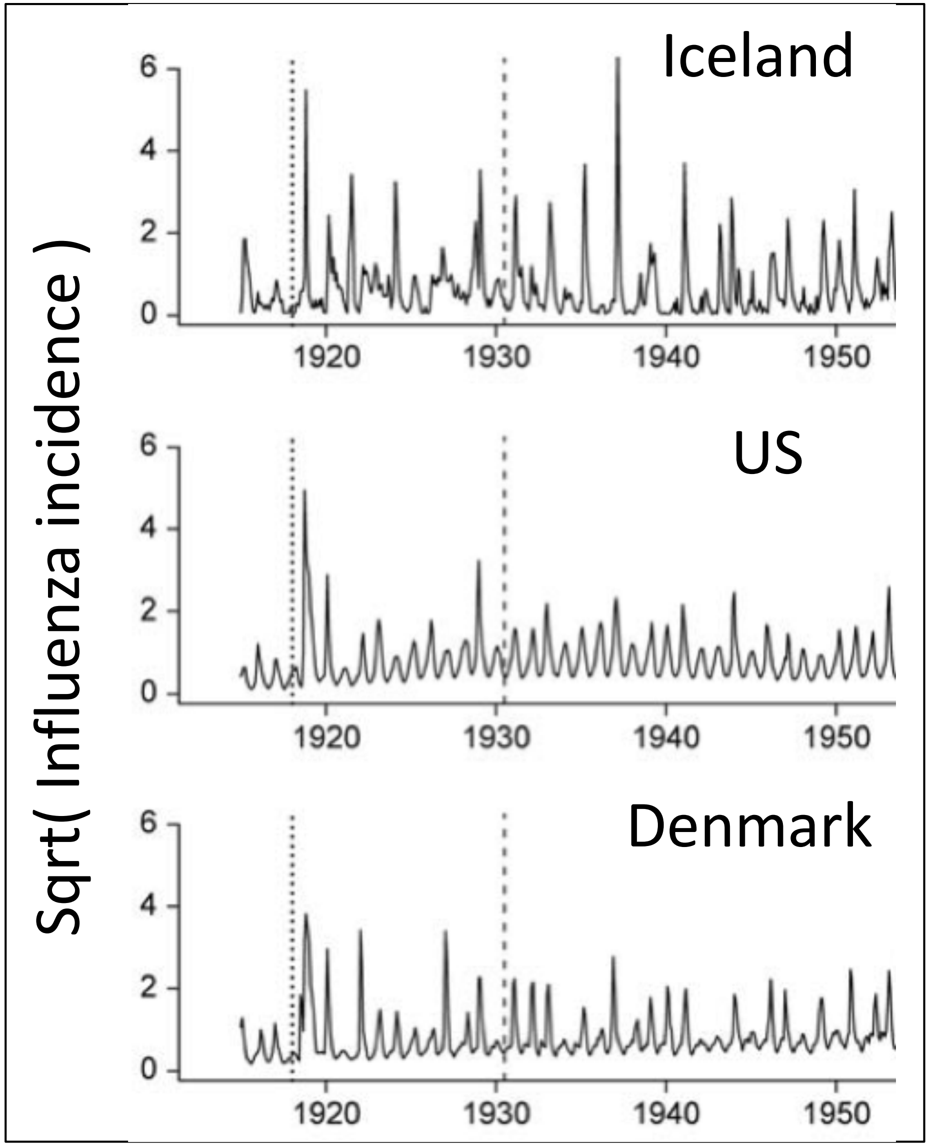
Average duration of infectiousness

R_{eff}: The Effective Reproductive Number



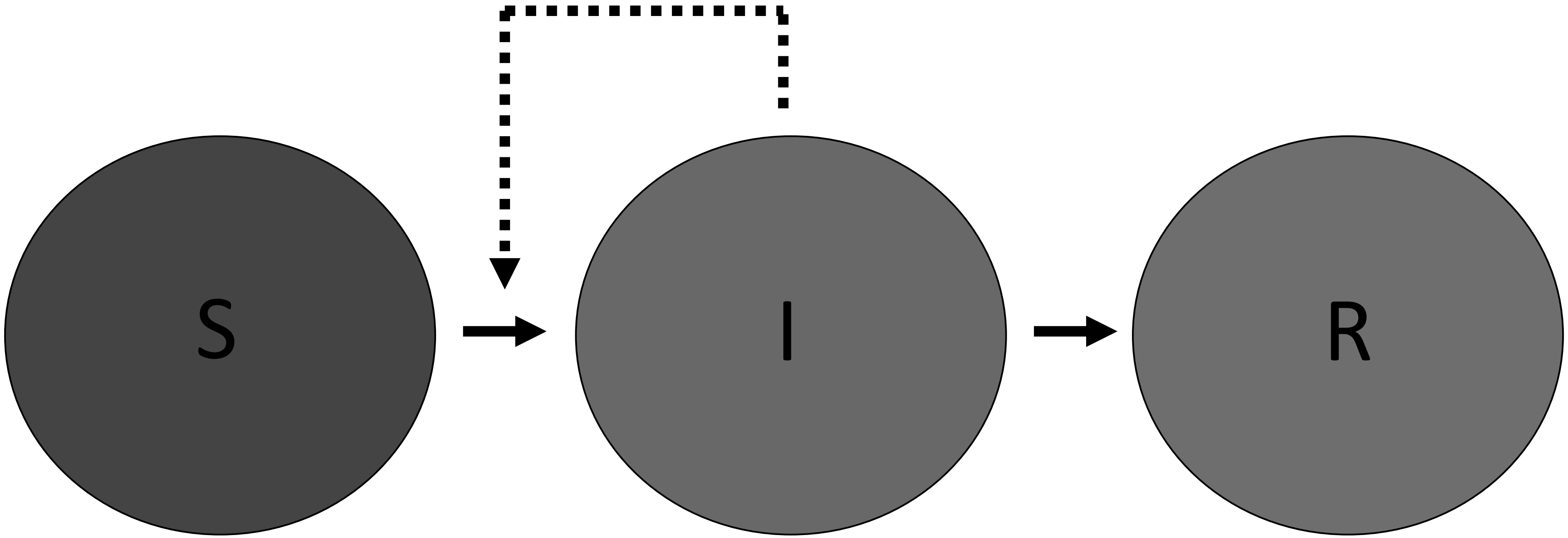
Why do recurrent epidemics happen?

- Susceptibles exhausted from an epidemic
- Disease does not completely die out (or is reintroduced).
- Susceptibles replenished through birth, pathogen evolution, or loss of immunity



Weinberger *et al*. 2012 Am J Epidemiol

State variables



We can use equations to describe the rate at which individuals flow between states

Features of models discussed so far:

Ordinary differential equations

- Deterministic
- Well-mixed
- All individuals are identical (except in disease status)
- Continuous time with exponential waiting times
- State variables are continuous quantities

Extremely simple models…

- Important insights
  - Why and when epidemics peak
  - What determines the endemic level of infection in a population
  - The level of effort needed to eliminate transmission
- Lots of assumptions

Extremely simple models…

- Important insights
  - Why and when epidemics peak
  - What determines the endemic level of infection in a population
  - The level of effort needed to eliminate transmission
- Lots of assumptions

These assumptions rarely hold in the real world…

So, what did the influenza transmission model that motivated the Alachua County SLIV program look like?

- Stochastic
- Contacts based on population structure
  - households
  - neighborhoods
  - work/school groups
- Each individual is a discrete entity with identifying features
- Discrete time

So, what did the influenza transmission model that motivated the Alachua County SLIV program look like?

- Synthetic population
- Influenza outcomes
- Transmission patterns
- Vaccination options

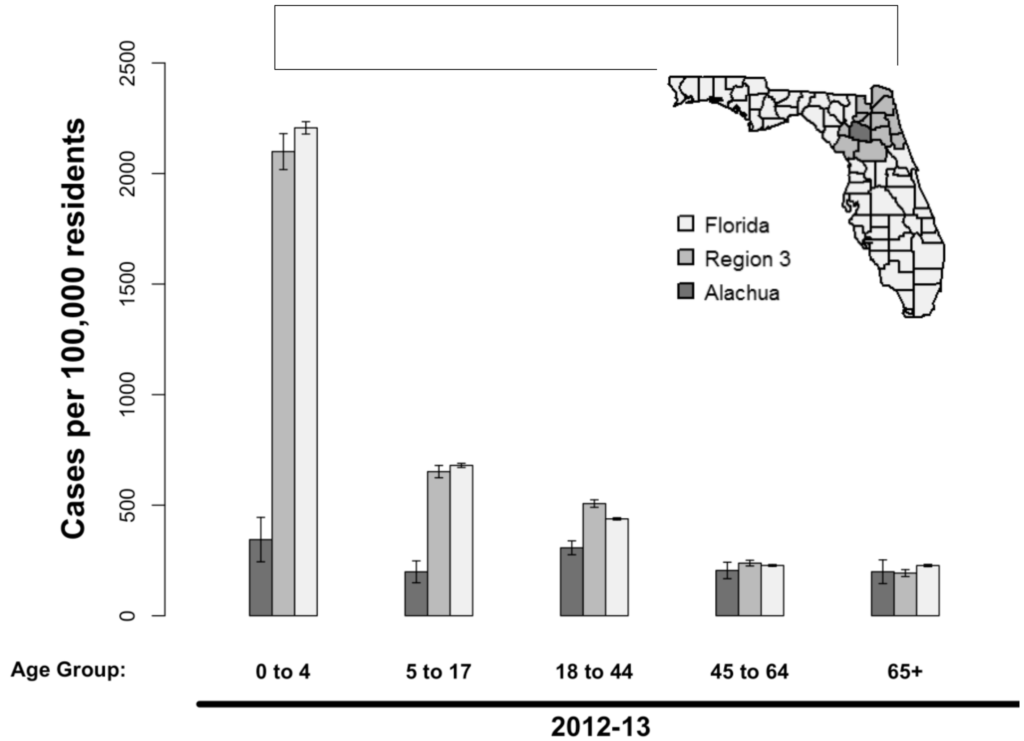
So, what did the influenza transmission model that motivated the Alachua County SLIV program look like?

- Synthetic population
- Influenza outcomes
- Transmission patterns
- Vaccination options

Details:

Weycker *et al.* 2005 *Vaccine*; Halloran *et al*. 2006 *Science*; Germann *et al.* 2006 *PNAS*; Basta *et al*. 2009 *AJE*; Longini 2012 *Pediatrics*

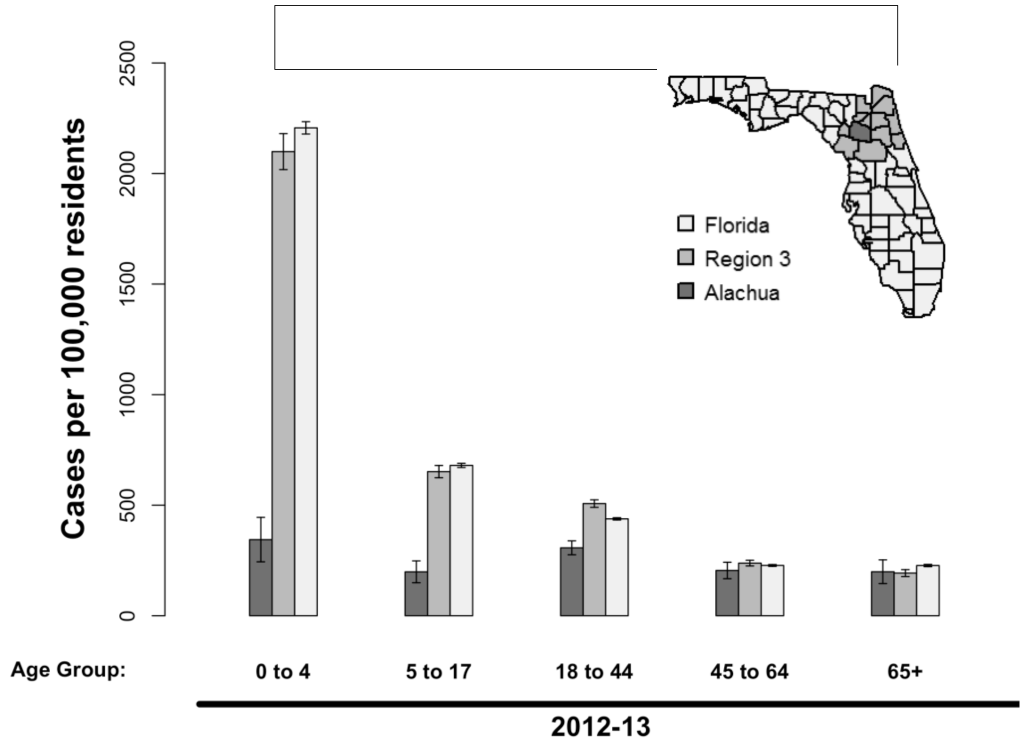
Were the predictions borne out?



Tran *et al*. 2014

- Not entirely

Were the predictions borne out?



Tran *et al*. 2014

- Not entirely
- Is the model still valuable?

Acknowledgements

Alachua County Control Flu Program

University of Florida

- Cuc Tran & Parker Small

For sharing materials used in this presentation

ICI3D Program

Faculty

- Steve Bellan, Jonathan Dushoff, Travis Porco, & Jim Scott
- John Hargrove, Alex Welte, & Brian Williams

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- Gavin Hitchcock (SACEMA)

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Research and Policy for Infectious Disease Dynamics (RAPIDD) Program

FOGARTY

U.S. DEPARTMENT OF HOMELAND SECURITY

NIGMS, National Institutes of Health
Award # R25GM102149 (JRC Pulliam & A Welte)

UF Emerging Pathogens Institute

ICI3D

UF UNIVERSITY of FLORIDA