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Assignment 1

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Download all python codes from

https://github.com/SAHIL150602/AI1103/blob/main/Assignment1/codes/Assignment.py

and latex-tikz codes from

https://github.com/SAHIL150602/AI1103/blob/main/Assignment1/Assignment1.tex

1 Problem

Question 3.1

How many times a man must toss a coin such that the probability of getting atleast one head is greater than 90%

2 Solution

The probability of getting heads when an unbiased coin is tossed 1 time is $\frac{1}{2}$ and vice versa.

By Binomial distribution the probability of getting k heads is

$$Pr(X = k) = {}^{n}C_{k} \left(\frac{1}{2}\right)^{k} \left(\frac{1}{2}\right)^{n-k}$$
 (1)

$$=\frac{{}^{n}C_{k}}{2^{n}}\tag{2}$$

(3)

So the probability of getting at least one head is P(X > 0).

By binomial distribution we also know that

$$\sum_{i=0}^{n} P(X=i) = 1 \tag{4}$$

So

$$Pr(X \ge 1) + Pr(X = 0) = 1$$
 (5)

$$Pr(X \ge 1) = 1 - Pr(X = 0)$$
 (6)

$$=1-\frac{{}^{n}C_{0}}{2^{n}}\tag{7}$$

$$\Pr(X \ge 1) = 1 - \frac{1}{2^n} \tag{8}$$

the condition given was probability of getting at least one head must be greater than 90%

$$\implies \Pr(X \ge 1) > 0.9$$
 (9)

$$\implies 1 - \frac{1}{2^n} > 0.9 \tag{10}$$

$$\implies \frac{1}{2^n} < 0.1 \tag{11}$$

$$\implies 2^n > 10 \tag{12}$$

Hence n = 4

⇒ The minimum number of times the coin has to be tossed so that the probability of getting atleast one head is greater than 0.9 is 4 times.