Digital Logic Design Daily Practice Problems Day -5

- 60. The Boolean expression AC + BC is equivalent to
 - (A) $\overline{AC} + \overline{BC} + \overline{AC}$
 - (B) $\overline{BC} + AC + B\overline{C} + \overline{ACB}$
 - (C) $AC + B\overline{C} + \overline{B}C + ABC$
 - (D) ABC+ABC+ABC+ABC

61. The simplified form of the Boolean expression

$$Y = (\overline{A}.BC + D)(\overline{A}.D + \overline{B}.\overline{C})$$
 can be written as

(A)
$$\overline{A}.D + \overline{B}.\overline{C}.D$$
 (B) $AD + B.\overline{C}.D$

(C)
$$(\overline{A} + D)(\overline{B}.C + \overline{D})$$
 (D) $A.\overline{D} + BC.\overline{D}$

62. If P. Q. R are Boolean variables, then

$$(P + \overline{Q})(P.\overline{Q} + P.R)(\overline{P}.\overline{R} + \overline{Q})$$

Simplifies to

$$(C) P.Q + R$$

$$(D) P.R + Q$$

63. The simplified SOP (Sum of Product) form of the Boolean expression.

$$(P + \overline{Q} + \overline{R}).(P + \overline{Q} + R).(P + Q + \overline{R})$$

 $(A)(\overline{PQ} + \overline{R})$ $(B)P + \overline{Q}\overline{R}$

(C)
$$(\overline{PQ}+R)$$
 (D) $(PQ+R)$

64 Consider the following Boolean expression:

$$F = (X + Y + Z)(\overline{X} + Y)(\overline{Y} + Z)$$

Which of the following Boolean expressions is/are equivalent to F?

(a)
$$X\overline{Y} + Y\overline{Z} + \overline{X}\overline{Y}\overline{Z}$$

(b)
$$(\overline{X} + \overline{Y} + \overline{Z})(X + \overline{Y})(Y + \overline{Z})$$

(c)
$$(X + \overline{Z})(\overline{Y} + \overline{Z})$$

65. A Boolean function F of three variables X, Y and Z is given as

$$F(X, Y, Z) = (X' + Y + Z) \cdot (X + Y' + Z') \cdot (X' + Y + Z') \cdot (X' Y' Z' + X' Y Z' + X Y Z')$$

Which one of the following is true?

- (a) $F(X, Y, Z) = (X + Y + Z') \times (X' + Y' + Z')$
- (b) $F(X, Y, Z) = (X' + Y) \times (X + Y' + Z')$
- (c) F(X, Y, Z) = X'Z' + YZ'
- (d) F(X, Y, Z) = X' Y' Z + X Y Z

- A switching function f(A,B,C,D) = A'B'CD+A'BC'D+A'BCD+AB'C'D+AB'CD can also be written as
 - (a) Σ m (1,3,5,7,9) (b) Σ m (3,5,7,9,11) (c) Σ m (3,5,9,11,13) (d) Σ m (5,7,9,11,13)

- 67. The switching function $f(A,B,C,D) = \Sigma m$ (5,9,11,14) can be written as
 - (a) A' B C' D+A B' C' D+A B' CD+ABCD' (b) A' B' C' D + AB' C' D + A' B' CD + ABCD'
 - (b) A' BC' D + A' BC' D' + AB' C D' + ABCD (d) None

68. The switching function f(A,B,C) = (A+B'+C)(A'+B'+C)(A+B'+C') can also be written as (a) $\Sigma m(2,3,6)$ (b) $\Sigma m(0,1,4,5,7)$ (c) $\Sigma m(1,2,5,6,7)$ (d) $\Sigma m(0,2,4,6)$

69. The other canonical form of $f(A,B,C) = \sum m(0,1,5,7)$ is

(a) $\prod M(2,3,4,6)$ (b) $\prod M(2,4,6,8)$ (c) $\prod M(2,5,6,7)$ (d) $\prod M(1,3,5,7)$

- If a three variable switching function is expressed as the product of maxterns by f(A,B,C) =70. Π M(0,3,5,6) then it can also be expressed as the sum of minterms by
 - (a) Σ m(0,3,5,6)

- (b) $\Pi M(1,2,4,7)$ (c) $\Sigma m(1,2,4,7)$
- (d) $\Pi M (1,2,4,7)$

71. The logic expression F = XY+XZ'+YZ is known as
(a) SSOP form (b) SOP form (c) POS form (d) SPOS form

The logic expression F = (x+y+z)(x+y')(y+z')(x+z) is known as

(a) SOP form

(b) SSOP form

(c) SPOS form

(d) POS form

73. The logic expression $F = \Sigma$ m (0,3,6,7,10,12,15) is equivalent to

(a)
$$F = \Pi M(0,3,6,7,10,12,15)$$

(b)
$$F = \Pi M(1,2,4,5,8,9,11,13,14)$$

(c)
$$F = \Sigma m(0,1,5,6,7,12,15)$$

(d)
$$F = \Sigma m (1,2,4,5,8,9,11,13,14)$$

Identify number of literals in the given Boolean function F = x' yz + xyz + xy' z(a) 5 (b) 4 (c) 3 (d) 6

- 75. A minterm is nothing but
 - (a) Standard sum term

- (b) Standard product term
- (c) May be standard sum term or product term
- (d) None

- 76. A maxterm is nothing but a
 - (a) Standard sum term

- (b) Standard product term
- (c) May be standard sum term or product term
- (d) None

- 77. The Boolean function expressed in standard sum of products form or standard product of sums form is called
 - (a) Canonical form
- (b) Conical form

(c) Both 1 and 2

(d) None

78. The complement of

$$F(x, y, z) = \prod M(2, 4, 5, 7)$$
 is

- (a) Σ m (0, 1, 3, 6)
- (c) Σ m (0, 1, 2, 3)

- (b) Σ m (2, 4, 5, 7)
- (d) Σ m (0, 5, 6, 7)

There are four Boolean variables x_1 , x_2 , x_3 and x_4 . The following function are defined on sets of them

f $(x_3, x_2, x_1) = \sum m (3, 4, 5)$ g $(x_4, x_3, x_2) = \sum m (1, 6, 7)$ h $(x_4, x_3, x_2, x_1) = fg$ Then h (x_4, x_3, x_2, x_1) is (a) $\sum m (3, 12, 13)$ (b) $\sum m (3, 6)$ (c) $\sum m (3, 12)$ d) 0 80. Given $F_1 = \prod M (0, 4, 5, 6)$ and

 $F_2 = \prod M \{0, 3, 4, 6, 7\}$. The maxterm expansion for F_1 F_2 is given by

(a) $\prod M$ (3, 5, 7)

- (b) $\prod M(1, 2)$
- (c) $\prod M (0, 3, 4, 5, 6, 7)$ (d) $\prod M (0, 3, 5, 7)$

- Consider the following Boolean function, f(A,B,C) = A + ABC. Which of the following represents the function in the sum of minterms?
 - (a) $\sum m$ (2, 3, 6, 7)

(b) Σ m (4, 5, 6, 7)

(c) Σ m (1, 4, 5, 6)

(d) None of these

GATE (ECE 2005)

Α	В	С	f
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	0

(a) B
$$(A + C)(\bar{A} + \bar{C})$$

(b)
$$B(A + \bar{C})(\bar{A} + C)$$

(c)
$$\bar{B}(A+C)(\bar{A}+C)$$

(d)
$$\bar{B}(A+C)(\bar{A}+\bar{C})$$

- 83. What is the function $y = A + \overline{B}C$ in product of sum (POS) form (where A is MSB and C is LSB)
 - (a) $\pi M(1,4,5,6,7)$
 - (b) $\pi M(0,1,2,3)$
 - (c) $\pi M(0,2,3)$
 - (d) $\pi M(0,3,4)$

- The max terms expansion of f (ABCD) = $A + B\bar{C} + AB\bar{D} + ABCD$
 - (a) $\pi M(4,5,8,9,10,11,12,13,14,15)$
 - (b) $\pi M(0,1,2,3,6,9)$
 - (c) $\pi M(0,1,2,3,6,7,8,9,10,11)$
 - (d) $\pi M(0,1,2,3,6,7)$

The Boolean expression

$$F(X,Y,Z) = \overline{X}Y\overline{Z} + X\overline{Y}\overline{Z} + XY\overline{Z} + XYZ$$

converted into the canonical product of sum (POS) form is

(A)
$$(X+Y+Z)(X+Y+\overline{Z})(X+\overline{Y}+\overline{Z})(\overline{X}+Y+\overline{Z})$$

(B)
$$(X+\overline{Y}+Z)(\overline{X}+Y+\overline{Z})(\overline{X}+\overline{Y}+Z)(\overline{X}+\overline{Y}+\overline{Z})$$

(C)
$$(X+Y+Z)(\overline{X}+Y+\overline{Z})(X+\overline{Y}+Z)(\overline{X}+\overline{Y}+\overline{Z})$$

(D)
$$(X + \overline{Y} + \overline{Z})(\overline{X} + Y + Z)(\overline{X} + \overline{Y} + Z)(X + Y + Z)$$

A function of Boolean variables X, Y and Z is expressed in terms of the min-terms as $F(X,Y,Z) = \sum (1,2,5,6,7)$

Which one of the product of sums given below is equal to the function F(X, Y, Z)?

(a)
$$(\overline{X} + \overline{Y} + \overline{Z}).(\overline{X} + Y + Z).(X + \overline{Y} + \overline{Z})$$

(b)
$$(X + Y + Z)$$
. $(X + \overline{Y} + \overline{Z})$. $(\overline{X} + Y + Z)$

(c)
$$(\overline{X} + \overline{Y} + Z)$$
. $(\overline{X} + Y + \overline{Z})$. $(X + \overline{Y} + Z)$. $(X + Y + \overline{Z})$. $(X + Y + Z)$

(d)
$$(X + Y + \overline{Z})$$
. $(\overline{X} + Y + Z)$. $(\overline{X} + Y + \overline{Z})$. $(\overline{X} + \overline{Y} + Z)$. $(\overline{X} + \overline{Y} + \overline{Z})$

87. Consider the following Sum of Products expression, F.

$$F = ABC + \overline{AB}C + A\overline{B}C + \overline{AB}C + \overline{AB}C$$

The equivalent Product of Sums expression is

(a)
$$F = (A + \overline{B} + C)(\overline{A} + B + C)(\overline{A} + \overline{B} + C)$$

(b)
$$F = (A + B + \overline{C})(A + B + C)(\overline{A} + \overline{B} + \overline{C})$$

(c)
$$F = (\overline{A} + B + \overline{C})(A + \overline{B} + \overline{C})(A + \overline{B} + C)$$

(d)
$$F = (\overline{A} + \overline{B} + C)(A + B + \overline{C})(A + B + C)$$

88. The minterm expansion of f

- (A) $m_2 + m_4 + m_6 + m_7$
- (B) $m_0 + m_1 + m_3 + m_5$
- (C) $m_0 + m_1 + m_6 + m_7$
- (D) $m_2 + m_3 + m_4 + m_5$

89. A function F (A, B, C) defined by three Boolean variables A, B and C when expressed as sum of products is given by:

$$F = \overline{A}. \overline{B}. \overline{C} + \overline{A}. B. \overline{C} + A. \overline{B}. \overline{C}$$

Where, \overline{A} , \overline{B} , and \overline{C} and the complements of the respective variables. The product of sums (POS) form of the function F is

- (a) $F = (A + B + C).(A + \overline{B} + C).(\overline{A} + B + C)$
- (b) $F(\overline{A} + \overline{B} + \overline{C}).(\overline{A} + B + \overline{C}).(A + \overline{B} + \overline{C})$
- (c) $F = (A + B + \overline{C}).(A + \overline{B} + \overline{C}).(\overline{A} + B + \overline{C}).(\overline{A} + \overline{B} + C).(\overline{A} + \overline{B} + \overline{C})$
- (d) $F = (\overline{A} + \overline{B} + C).(\overline{A} + B + C).(A + \overline{B} + C).(A + B + \overline{C}).(A + B + C)$

- The product of sum expression of a Boolean function F (A, B, C) of three variables is given by F(A, B, C) = (A + B + \(\bar{C}\)). (A + \(\bar{B}\) + \(\bar{C}\)). (\(\bar{A}\) + B + C). (\(\bar{A}\) + \(\bar{B}\) + \(\bar{C}\)) The canonical sum of product expression of F(A, B, C) is given by
 - (a) $\overline{ABC} + \overline{ABC} + A\overline{BC} + ABC$
 - (b) $\overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC}$
 - (c) $AB\overline{C} + A\overline{B}\overline{C} + \overline{A}BC + \overline{A}\overline{B}\overline{C}$
 - (d) $\overline{ABC} + \overline{ABC} + AB\overline{C} + ABC$