

$$5.) \quad A = \begin{bmatrix} \cos(\theta) & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$$

$$A^{-1} = \frac{\text{adj}(A)}{\det(A)}$$

$$\begin{aligned} \det(A) &= (\cos\theta)(\cos\theta) - (-\sin\theta)(\sin\theta) \\ &= \cos^2\theta + \sin^2\theta \\ &= \underline{\underline{1}} \end{aligned}$$

$$\text{adj}(A) = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$$

$$A^{-1} = \frac{\text{adj}(A)}{\det(A)} = \text{adj}(A) = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$$

$$A^T = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$$

$$\Rightarrow \boxed{A^{-1} = A^T}$$