

MEASUREMENT I



1. What is **Physics**? (2mk)

Physics is the study of matter and its relation to energy.

2. Differentiate fundamental quantities from derived quantities and give an example of each

Fundamental quantities are quantities that cannot be obtained from physical quantities e.g Length, mass, time etc. while derived quantities are quantities that are obtained by either division or multiplication of basic physical quantities e.g Area, Volume, density etc

3. State what the following branches of physics deals with:

(i) Mechanics

This branch deals majorly with motions under the influence of forces. Under this branch, we look into details the aspects of linear, circular and oscillatory motions as well as motion of fluids.

(ii) Electricity and magnetism

This branch looks at the interaction between electric fields and magnetic fields and the applications of such interactions.

(iii) Thermodynamics

This branch looks at how heat as a form of energy is transformed to/from other forms of energy

(iv) Geometric optics

This branch takes a keen look at the behavior of light in various media.

(v) Waves

It deals with the study of the propagation of energy through space.

(vi) Atomic physics

This area of study is targeted at the behavior of particles of the nucleus and the accompanying energy changes.

4. State and explain **two** basic laboratory safety rule

- a. *Locations of electrical switches, firefighting equipment, first aid kit, gas supply and water supply systems must be noted.*
- b. *Windows and doors should be kept open while working in the laboratory.*
- c. *Any instructions given must be followed carefully. NEVER attempt anything while in doubt.*
- d. *There should no eating, drinking or chewing in the laboratory.*
- e. *Ensure that all electrical switches, gas and water taps are turned off when not in use.*
- f. *When handling electrical apparatus, hands must be dry.*
- g. *Never plug in foreign materials into electrical sockets.*
- h. *Shirts and blouses must be tucked in and long hair tied up.*
- i. *Keep floors and working surfaces dry. Any spillage should be wiped off immediately.*
- j. *All apparatus must be cleaned and returned to correct location of storage after use.*
- k. *Laboratory equipment should not be taken out of laboratory unless authorized.*
- l. *Any waste after an experiment must be disposed of immediately.*
- m. *Hands must be washed before leaving the laboratory*

5. State the **SI** units of the following quantities (3mk)

Length = ...*Metre(m)*.....

Mass =*Kilograms(kg)*.....

Temperature =*Kelvin(k)*.....

6. Name two branches of physics. (2mk)

1. *Mechanics*
2. *Thermodynamics*
3. *Geometric optics*
4. *Waves*
5. *Electricity and magnetism*
6. *Atomic physics*

7. Name two career opportunity in physics. (2mk)
- Bachelor of education (science)*
 - Bachelor of Science (civil engineering)*
 - Bachelor of medicine*
 - Bachelor of architecture*
 - Bachelor of technology (production engineering)*
 - Diploma in computer science*
8. State the relationship between physics and the following subjects.
- (i) Biology (1mk)
Knowledge of lenses studied in physics has led to the manufacture of microscopes used in the study of the cell and diseases.
- (ii) Geography (1mk)
Accurate use of weather instruments like thermometer, wind vane, rain gauges etc. require physics knowledge.
Concepts like heat transfer by convection which explain the formation of convectional rainfall and pressure variation can be best explained in physics.

LENGTH AND AREA

1. Convert the following values into **SI** units

(i) **86400cm²**

(1mk)

$$1M^2 \text{-----} 10000cm^2$$

$$86400cm/10000 = 8.64m^2$$

(iii) **204000cm³**

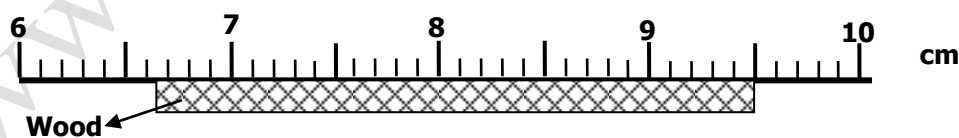
(1mk)

$$2040000cm^3/1000000 = 0.204m^3$$

2. A student measured the length of a wire four times using a meter rule and obtained the following readings: **18.6cm; 18.5cm; 18.6cm; and 18.5cm**. Determine the length the student should record. (2mk)

$$\frac{18.6+18.5+18.6+18.5}{4} = 18.55cm$$

3. The figure below shows a section of a meter rule used to measure length of a piece of wood.

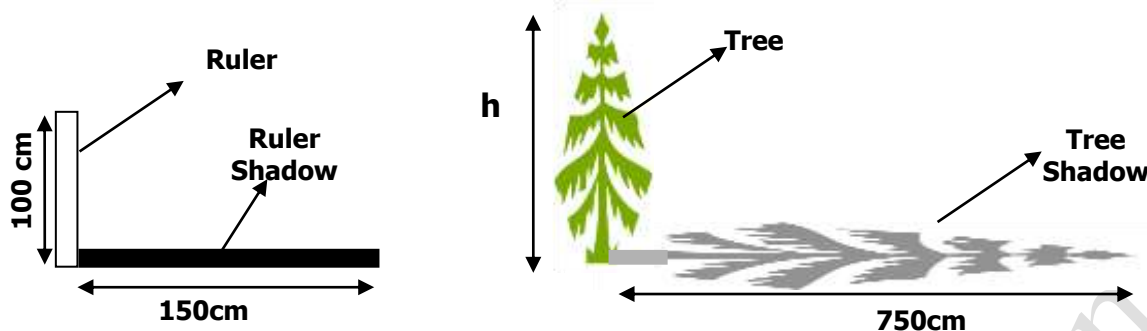


Find the length of the wood

(2mk)

$$9.5 - 6.7 = 1.8cm$$

4. In an experiment to estimate the height of a tree using its shadow, a ruler of height **100cm** is placed next to the tree as shown below. If the ruler and the tree forms shadows of **150cm** and **750cm** respectively.



Calculate the height **h** of the tree.

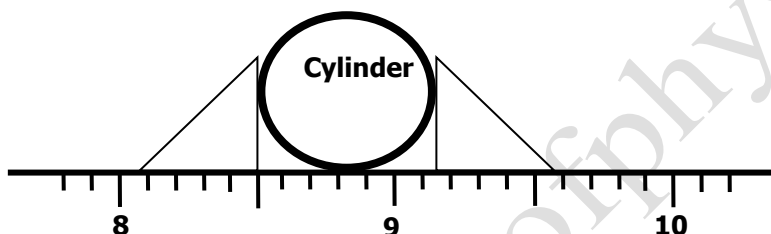
(3mk)

$$\frac{\text{height of the tree, } x}{\text{height of the rod}} = \frac{\text{length of shadow of tree}}{\text{length of shadow of rod}}$$

$$\frac{x}{100} = \frac{750}{150}$$

$$x = 500\text{cm} = 5.0\text{m}$$

5. A Figure below is an arrangement of two set squares and a rule being used to determine the external diameter of a cylinder.



- (a) State the accuracy of the rule.

(1mk)

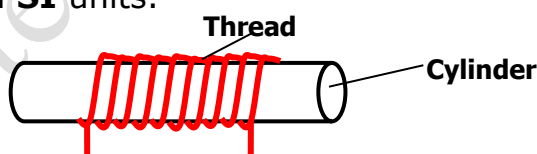
$$0.1\text{cm} = 1\text{mm}$$

- (b) What is the radius of the cylinder?

(2mk)

$$9.1 - 8.5 = 0.6\text{cm}$$

6. A thin wire was wound **10** times closely over a boiling tube. The total length of the wire wound around was found to be **440mm**. Calculate the radius of the boiling tube in **SI** units.



$$\text{no of turns} = 10\text{times}$$

$$\text{length of the wire} = 440\text{mm}$$

$$\text{radius of the boiling tube} =$$

$$10\text{turns} = 440\text{mm}$$

$$1\text{turn} = x$$

$$440/10 = 44\text{mm}$$

$$D = 44/\pi = 14$$

$$R = 14/2 = 7\text{cm}$$

7. A thin wire was wound **30** times closely over a boiling tube. The total length of the windings was found to be **9.3 mm**. Calculate the radius of the wire.

no of turns = 30times

length of the wire = 9.3mm

radius of the boiling tube =

30turns = 9.3mm

1turn = x

9.3/30 = 0.31mm

D = 0.31/π = 0.09864

R = 0.09864/2 = 0.04932cm

8. A length of 550cm of them thread wraps around a cylindrical tin exactly 25times. Calculate the radius of the cylinder (2mks)

no of turns = 25times

length of the wire = 550mm

radius of the boiling tube =

25turns = 550mm

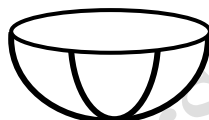
1turn = x

550/25 = 22mm

D = 22/π = 7

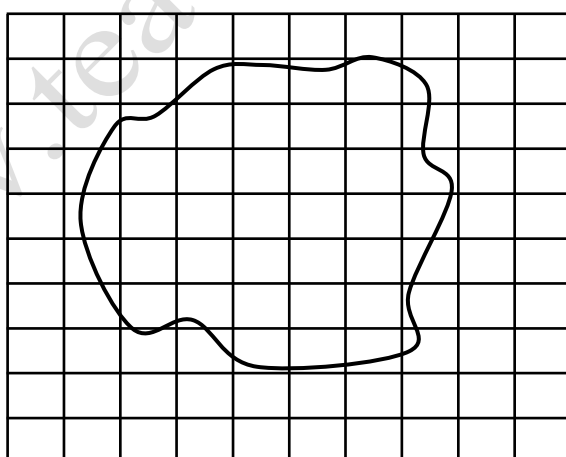
R = 7/2 = 3.5cm

9. The figure below shows a half spherical bowl of radius **3cm**. calculate its volume.



$$V = \frac{4}{3}\pi r^3 = \frac{2}{3} \times \pi \times 3^3 = 56.57\text{cm}^3$$

10. The figure below shows the map of a school compound. Each square is equivalent to **1cm²**. Calculate the total area covered by the school on the map. (3mk)



○ $\text{Area} = \left(\text{number of complete squares} + \frac{1}{2} \times \text{number of incomplete squares} \right) \text{area of one square}$

Full squares = 22squares cm²

1/2 squares = 21/2 = 10.5squares cm²

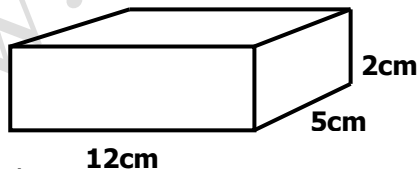
Total area = 22 + 10.5 = 32.5cm²

11. Express the area of land of **0.0025km²** in **S.I** units and in standard form

0.0025km² x 1000000m² = 2500m² = 2.5 x 10³m²

VOLUME

1. Define volume and give its **SI** units.
Volume refers to the amount of space occupied by matter.
*The SI unit of volume is **the cubic meter (m^3)***
2. Find the volume of a spherical ball of radius **3cm**. **(3mk)**
 $V = \frac{4}{3}\pi r^3 = \frac{4}{3} \times \pi \times 3^3 = 113.1 \text{ cm}^3$
3. Calculate the volume of a Cuboid that measures **4cm** by **5cm** by **3cm** in **SI** Units.
 $V = l \times w \times h$
 $0.04\text{m} \times 0.05\text{m} \times 0.03\text{m} = 6 \times 10^{-5} \text{ m}^3$
4. Find the capacity of a cylinder of radius **70cm** and height **20cm** in litres.
 $\frac{22}{7} \times 70 \times 70 \times 20 = 308000 \text{ cm}^3$
 $308000/1000 = 308\text{l}$
5. A sphere of radius **6cm** is moulded into a thin cylindrical wire of length **32cm**. Calculate the radius of the wire in SI Units.
 $V = \frac{4}{3}\pi r^3 = \frac{4}{3} \times \pi \times 6^3 = 905.1 \text{ cm}^3$
 $V = \pi r^2 h = \frac{22}{7} \times r^2 \times 32 = 100.6 r^2$
 $R^2 = 905.1/100.6 = 8.9970 \text{ cm}^2$
 $R = 2.9995 \text{ cm} = 0.029995 \text{ m}$
6. A solid Cuboid of dimensions **11cm x 14cm x 5cm** is melted in to a cylindrical solid of diameter **28 cm**. calculate the height of the cylinder
Volume of cuboid = $l \times w \times h$
 $11 \times 14 \times 5 = 770 \text{ cm}^3$
 $V = \pi r^2 h = \frac{22}{7} \times 14 \times 14 \times h = 616h$
Volume of cuboid = volume of cylinder
 $H = 770/616 = 1.25 \text{ cm}$
7. A cylinder of height **25cm** is completely melted and a sphere of the same radius made. Determine the radius of the sphere in metres and express your answer in **standard form**. **(3mk)**
 $\text{Volume of cylinder} = \pi r^2 h = \pi r^2 (25) = 25\pi r^2$
 $\text{Volume of sphere} = \frac{4}{3}\pi r^3$
 $25\pi r^2 = \frac{4}{3}\pi r^3$
 $25 = \frac{4}{3}r$
 $R = 18.75 \text{ cm} = 0.1875 \text{ m} = 1.875 \times 10^{-1} \text{ m}$
8. The figure below shows a block of mass **360g**.



Calculate the

- (i) Volume of the block.

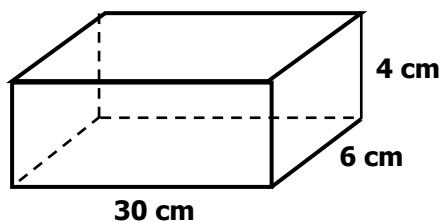
$$\text{Volume of cuboid} = l \times w \times h$$

$$12 \times 5 \times 2 = 120 \text{ cm}^3$$

- (ii) Density of the block in **SI** unit.

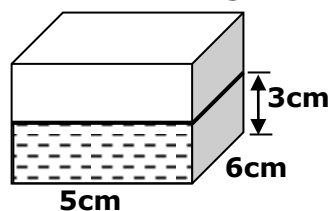
$$\text{Density} = \text{mass/volume} = 360/120 = 3 \text{ g/cm}^3 = 3000 \text{ kg/m}^3$$

9. The diagram below shows a brick of mass **120g**. The brick measures **30cm x 6cm x 4cm**. Calculate the density of the brick



$$\text{Density} = \text{mass/volume} = 120/720 = 0.167\text{g/cm}^3 = 167\text{kg/m}^3$$

10. The figure below shows Perspex container with a base of sides **5** by **6** cm carrying water to a height of **3cm**.



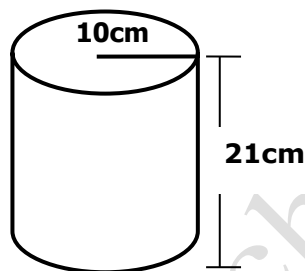
When pebble is immersed into the water, the level rise to **10 cm**. what is the volume of the pebble?

$$\text{Initial volume of water} = 5 \times 6 \times 3 = 90\text{cm}^3$$

$$\text{Final volume of water} = 5 \times 6 \times 10 = 300\text{cm}^3$$

$$300 - 90 = 210\text{cm}^3$$

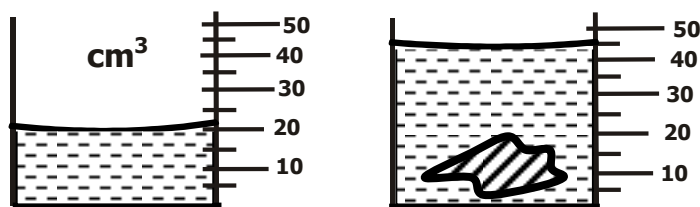
11. The figure below shows a cylinder of radius **10cm** and height **21cm**. Calculate its capacity in litres.



$$V = \pi r^2 h = 22/7 \times 10 \times 10 \times 21 = 6600\text{cm}^3$$

$$6600/1000 = 6.6\text{litres}$$

12. The figure below shows the change in volume of a liquid in a measuring cylinder when an irregular solid is immersed in it. Given that the mass of the solid is **75g**, determine the density of the solid in SI units.



$$\text{Initial volume of water} = 20\text{cm}^3$$

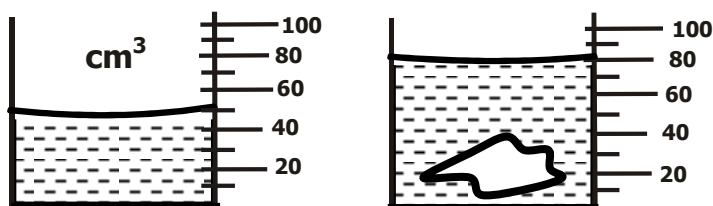
$$\text{Final volume of water} = 45\text{cm}^3$$

$$45 - 20 = 25\text{cm}^3$$

$$\text{Mass of solid} = 75\text{g}$$

$$\text{Density} = \text{mass/volume} = 75/25 = 3\text{g/cm}^3 = 3000\text{kgm}^{-3}$$

- 13.** The figure below shows the change in volume of a liquid in a measuring cylinder when an irregular solid is immersed in it. Given that the density of the solid is **4g/cm³**, determine the mass of the solid in SI units. (4mk)



Initial volume of water = 50cm³

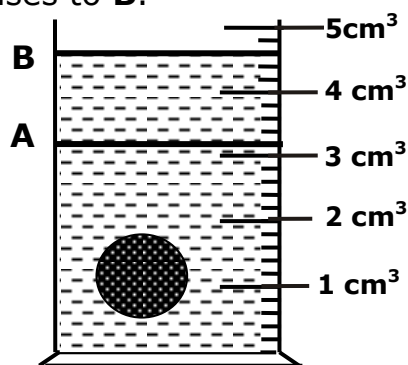
Final volume of water = 80cm³

80 – 50 = 30cm³

Mass of solid = density x volume

Mass = 4x30 = 120g = 0.12kg

- 14.** The figure below shows a measuring cylinder which contains water initially at a level **A**. A spherical solid of mass **11g** is immersed in the water, the level rises to **B**.



Determine the diameter of the spherical ball

(2mk)

Initial volume of water = 3.2cm³

Final volume of water = 4.6cm³

Volume of spheres = 4.6 – 2.3 = 1.4cm³

Mass of the spherical = 11g

Volume of sphere = 4/3πr³

1.4 = 4/3πr³

1.4 = 88/21r³

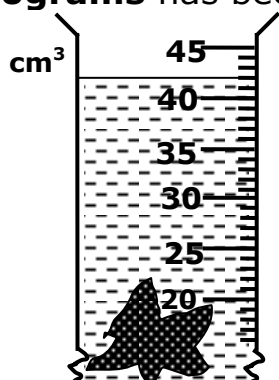
29.4 = 88r³

R³ = 0.3341

R = 0.6939

Diameter = 1.3878cm

- 15.** Fig shows a measuring cylinder into which an irregular stone of mass **60grams** has been immersed.



If the initial reading before immersing was **27cm³**. Find the density of the stone. (2mk)

$$\text{Initial reading} = 27\text{cm}^3$$

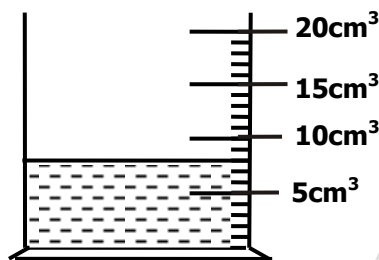
$$\text{Final reading} = 42\text{cm}^3$$

$$\text{Volume of the stone} = 42 - 27 \\ 15\text{cm}^3$$

$$\text{Mass of the stone} = 60\text{g}$$

$$\text{Density} = \text{mass/volume} = 60/15 = 4\text{g/cm}^3$$

- 16.** The figure below shows water placed in a measuring cylinder calibrated in **cm³**?



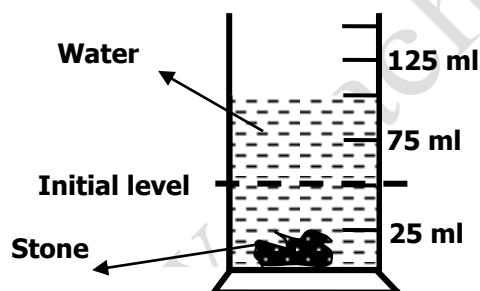
An object of mass **50.1g** and density **16.7g/cm³** is lowered gently into the water. Indicate on the diagram the new level. (2mk)

$$\text{Density} = \text{mass/volume}$$

$$16.7 = 60/v$$

$$V = 3\text{cm}^3$$

- 17.** The figure below shows the level of water in a measuring cylinder after a stone of mass **100 g** is immersed in the water. The initial level of the water is shown with a dotted line. Determine the density of the stone. (3mk)



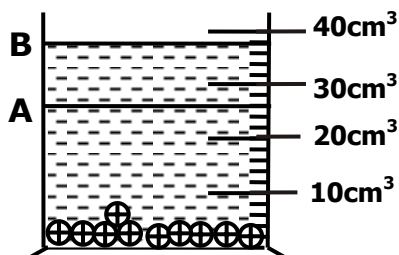
$$\text{Initial reading} = 50\text{cm}^3$$

$$\text{Final reading} = 100\text{cm}^3$$

$$\text{Volume of the stone} = 100 - 50 \\ 50\text{cm}^3$$

$$\text{Density} = \text{mass/volume} = 100/50 = 2\text{g/cm}^3$$

- 18.** Ten glass marbles, each of mass 6.0 g, were gently lowered into a measuring cylinder containing water to the level marked **A**. The water level rose to the level marked **B** as shown in Fig below. Determine the density of the glass. (3mk)



Initial reading = 26cm³

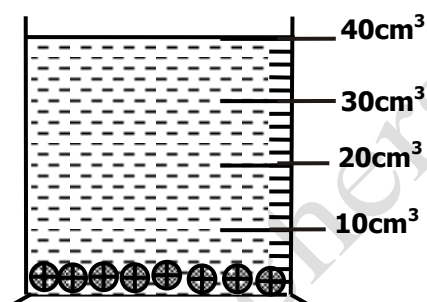
Final reading = 38cm³

*Volume of ten glass marble = 38 – 26
12cm³*

Volume of each glass marble = 12/10 = 1.2cm³

Density = mass/volume = 6/1.2 = 5g/cm³

- 19.** The figure below shows a cylinder with water and **8** lead pellets each of volume **1.5cm³**.



Indicate on the diagram the level of water if the pellets are removed. (2 mk)

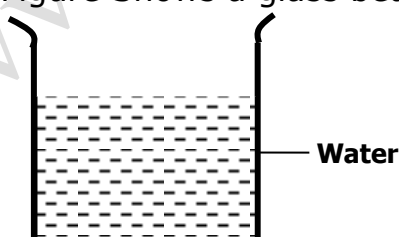
Volume of 1 pellet = 1.5cm³

Volume of 8 pellet = 1.5 x 8cm³ = 12cm³

Final volume = 40

Initial volume = final volume - Volume of 8 pellet = 40 – 12 = 28cm³

- 20.** Figure Shows a glass beaker of cross sectional area 10.5cm²



When a metal block of mass **250 g** is immersed into the water, the level of water rises by **3.5 cm**. determine the density of the metal block. Express your answer in S.I unit (3mk)

$$\text{Volume} = A \times h$$

$$10.5 \times 35 = 36.75\text{cm}^3$$

$$\text{Mass of the metal block} = 250\text{g}$$

$$\text{Density} = \text{mass/volume}$$

$$250/36.75 = 6.8\text{g/cm}^3$$

$$1\text{g/cm}^3 = 1000\text{kg/m}^3$$

$$6.8\text{g/cm}^3 = ?$$

$$6.8 \times 1000 = 6800\text{kg/m}^3$$

BURETTE

- 1. 1600 cm³** of fresh water of density **1 g/cm³** are mixed with **1400cm³** of seawater of density **1.25g/cm³**. Determine the density of the mixture.

$$\text{Density of the mixture} = \text{total mass of the mixture}/\text{total volume of mixture}$$

$$\text{Mass of fresh water} = \text{density} \times \text{volume}$$

$$1\text{g} \times 1600\text{cm}^3 = 1600\text{g}$$

$$\text{Mass of salt water} = \text{density} \times \text{volume}$$

$$1.25\text{g} \times 1400\text{cm}^3 = 11750\text{g}$$

$$\text{Density} = \frac{1600+11750}{1600+1400} = 3350/3000 = 0.1117\text{g/cm}^3$$

- 1.** The water level in a burette is **27cm³**. If **88** drops of water fall from the burette and the average volume of one drop is **0.25cm³** what is the final water level in the burette?

$$\text{Initial level of water in burette} = 27\text{cm}^3$$

$$\text{No of drops added} = 88$$

$$\text{Volume of each drop} = 0.25\text{cm}^3$$

$$\text{Total volume added} = 88 \times 0.25 = 22\text{cm}^3$$

$$\text{Final burette reading} = 27 - 22 = 5\text{cm}^3$$

- 2.** The initial level of water in a burette was **32cm³**. Some **20** drops of water each of volume **0.4cm³** are **added**. Find its final reading.

$$\text{Initial level of water in burette} = 32\text{cm}^3$$

$$\text{No of drops added} = 20$$

$$\text{Volume of each drop} = 0.4\text{cm}^3$$

$$\text{Total volume added} = 20 \times 0.4 = 8\text{cm}^3$$

$$\text{Final burette reading} = 32 - 8 = 24\text{cm}^3$$

- 2. 1600 cm³** of fresh water of density **1 g/cm³** are mixed with **1400cm³** of seawater of density **1.25g/cm³**. Determine the density of the mixture.

$$\text{Density of the mixture} = \text{total mass of the mixture}/\text{total volume of mixture}$$

$$\text{Mass of fresh water} = \text{density} \times \text{volume}$$

$$1\text{g} \times 1600\text{cm}^3 = 1600\text{g}$$

$$\text{Mass of salt water} = \text{density} \times \text{volume}$$

$$1.25\text{g} \times 1400\text{cm}^3 = 11750\text{g}$$

$$\text{Density} = \frac{1600+11750}{1600+1400} = 3350/3000 = 0.1117\text{g/cm}^3$$

- 3.** The initial level of water in a burette was **26cm³**. Some **10** drops of water each of volume **0.5cm³** are allowed to **drop out**. Find its final reading.

$$\text{Initial level of water in burette} = 26\text{cm}^3$$

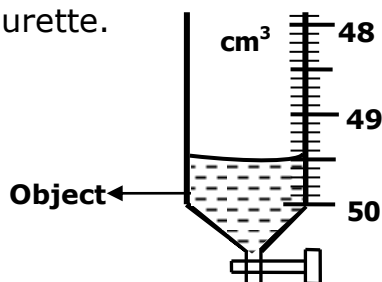
$$\text{No of drops added} = 10$$

$$\text{Volume of each drop} = 0.5\text{cm}^3$$

$$\text{Total volume added} = 10 \times 0.5 = 5\text{cm}^3$$

$$\text{Final burette reading} = 26 + 5 = 31\text{cm}^3$$

4. A ball bearing of volume 1.8cm^3 was dropped into water contained in the burette shown in figure below. Determine the final reading of water in the burette. (2mks)

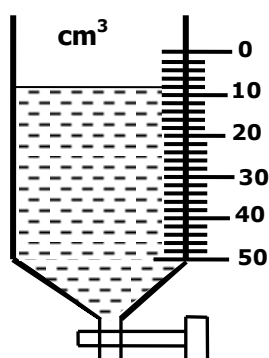


Volume of the ball bearing = 1.8cm^3

Initial reading = 49.5cm^3

Final reading = $49.5 - 1.8 = 47.7\text{cm}^3$

5. The figure below shows the reading on a burette after 55 drops of a liquid have been used.



If the initial reading was at **0cm** mark, determine the volume of one drop.

Burette reading = 8cm^3

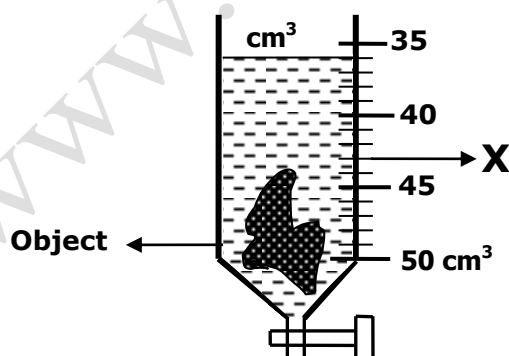
Initial burette reading = 0cm^3

Volume of water added = $8 - 0 = 8\text{cm}^3$

Total volume of 55 drops = 8cm^3

Volume of 1 drop = $8/55 = 0.145\text{cm}^3$

6. The figure below shows a burette initially filled with water to the level marked **X**. An object of density 1.5gcm^{-3} is immersed into it and the level rose as shown. Determine the mass of the object (3mk)



Initial reading at x = 43cm^3

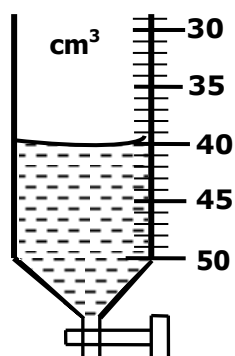
Final reading = 36cm^3

Volume of the object = $43 - 36 = 7\text{cm}^3$

Density of the object = 1.5g/cm^3

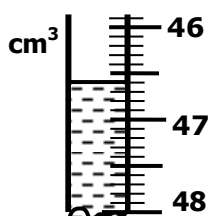
Mass = density \times volume = $1.5 \times 7 = 10.5\text{g}$

7. The figure below shows a section of a measuring instrument.



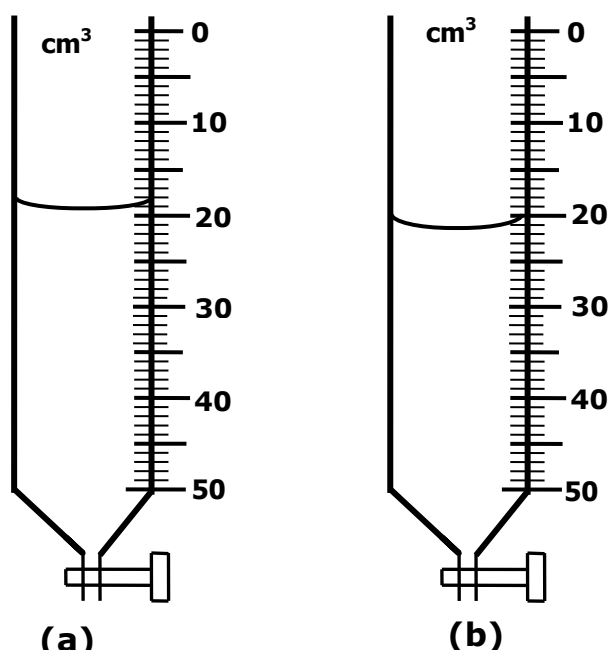
- (i) Name the measuring instrument shown above **(1mk)**
Burette
- (ii) What is the volume of water in it? **(1mk)**
Initial volume = 40 cm³
Final volume = 50 cm³
Volume of water in the burette = 50 – 40 = 40 cm³
- (iii) Some **24** drops of water each of volume **0.5cm³** are **added** to the instrument above. Find the final reading of the instrument.
Total volume of drops added = 24 x 0.5 = 12 cm³
Final reading = 40 - 12 = 28 cm³

8. In an experiment to measure the density of a liquid, a student filled a burette with a liquid to the 0cm³ mark. The figure below shows a section of the burette showing the level of the liquid after 93.2g of the liquid had been run out.



- (i) Take the reading of the burette **46.6 cm³** **(1mk)**
- (ii) Determine the density of the liquid. **(3mk)**
Mass of the liquid 93.2g
Volume of the liquid = 46.6 – 0 = 46.6 cm³
Density = mass/volume = 93.2/46.6 = 2g/ cm³

9. The figure (a) below shows the initial reading of a burette used to measure the volume of oil. After 50 drops of oil were run out, the final reading was as shown in (b). Determine the volume of one drop of oil (2mk)



Initial volume = 19 cm^3

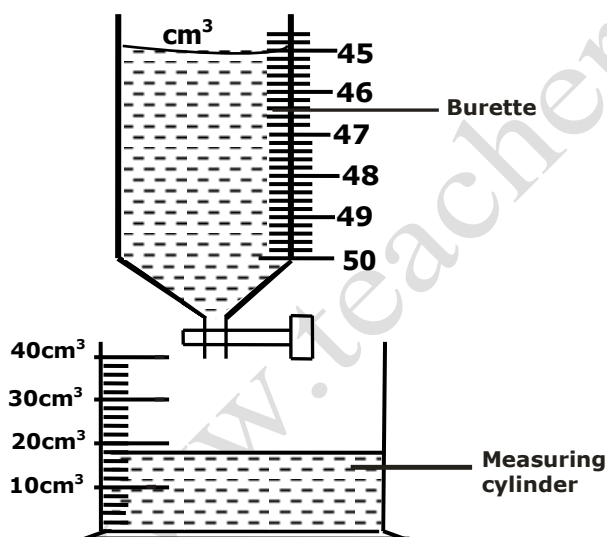
Final volume = 21 cm^3

Volume of oil = $21 - 19 = 2 \text{ cm}^3$

Volume of 1 drops = $2/50 = 0.04 \text{ cm}^3$

(3mk)

10. Figure below shows a measuring cylinder containing some water.

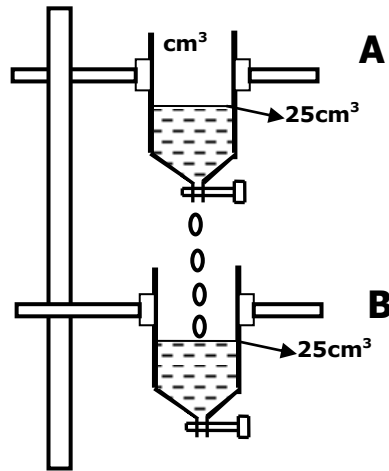


(i) New reading 5 cm^3 (1 mk)

(ii) New reading $19 + 3 = 21 \text{ cm}^3$ (1mk)

Another 3 cm^3 of water was added to the cylinder from a burette delivering volume from 0 cm^3 to 50 cm^3 . Record in the spaces provided the new reading indicated on each vessel.

- 11.** Two burettes **A** and **B** were arranged as shown below. Burette **A** leaked into **B** at the rate of **10** drops per minute. If the initial reading on both burettes was **25cm³**. What would be their reading at the end of one hour if **B** does not leak? Volume of one drop of water is **2.0 x 10⁻⁸m³**. (3mks)



A leak to B at the rate of 10drops

1min = 10drops

No of drops in 1hour

60x10 = 600drops

Volume of all drops = 600 x 2.0 x 10⁻⁵m³ = 1.2 x 10⁻⁵m³ = 12cm³

Final reading in A = 25 + 12 = 37cm³

Final reading in B = 13cm³

- 12.** In an experiment to measure the radius of a wire a student cut the wire into **100** identical pieces of length **7mm** and dipped the pieces completely into a burette with initial level of liquid at **49.5cm³** mark. If the final level was at **0cm³**. Determine the radius of the wire giving your answer to two decimal places (3mks)

Initial reading = 49.5

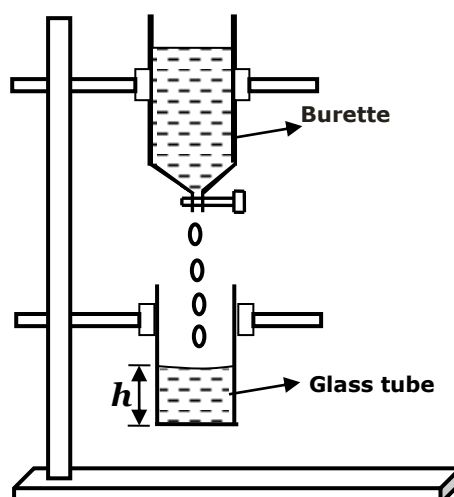
Final reading = 0cm³

Volume of 100 pieces of wire = 49.5

Volume of 1 piece 49.5/100 = 0.495cm³

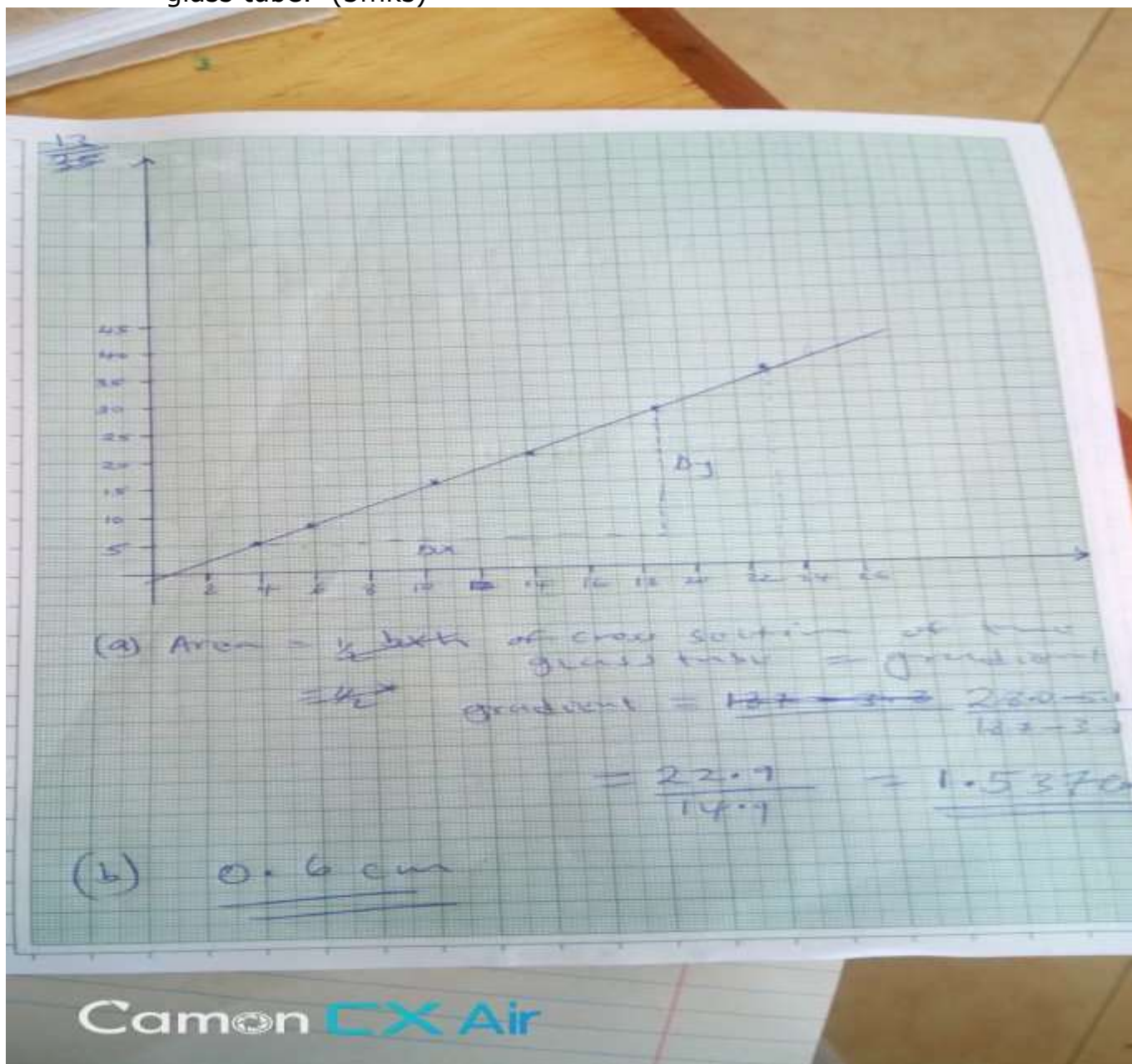
$R^2 = 0.495 \times \frac{7}{22} \times \frac{10}{7} = 0.225$. $r = \sqrt{0.225} = 0.474cm$

- 13.** The diagram fig below shows an arrangement that a certain student set up in a physics lab without the consent of the teacher. He allowed some volume of water into the glass tube and measured the corresponding height **h** of water in the tube using a ruler. He tabulated his data as below.



Burette reading cm^3	5.1	8.2	15.4	21.5	28.0	35.6
Height h , cm	3.8	5.8	10.5	14.5	18.7	23.2

- (a) Draw a graph of the burette reading against height h of the water in the glass tube. (5mks)



(ii) Use your graph above to determine the area of cross section of the glass tube. (3mks)

(iii) Use your graph to determine how far the zero mark of the ruler is from the end placed on the base of the stand. (2mks)

DENSITY

3. Define density and give its **SI** units.

Density is defined as mass per unit volume.

SI units kilograms per cubic metre (kg/m^3)

4. The density of concentrated Sulphuric acid is 1.8gcm^{-3} . Calculate the volume of **3.6kg** of the acid.

Volume = mass/ density = $3.6 \times 1000^3 / 1.8 = 2000\text{g}$ Or 2kg

5. A block of metal of mass **72g** measures **2cm x 4cm x 6 cm**, calculate the density of the metal in **SI** unit.
Density = mass/volume = (2x4x6)/48 = 1.5g/cm³ x 1000 = 1500kg/m³
6. Determine the density in **SI units** of a solid whose mass is **40g** and whose dimensions in cm are **30 x 4 x 3** **(2mk)**
Volume = 30x4x3 = 360cm³
Mass = 40g
Density = 40/360 = 0.1111g/cm³ = 111.1kg/m³
7. A cuboid has dimensions **12cm** by **10cm** by **15cm**. its weight is **72N**. Determine the density of the material the cuboid is made of. **(3mks)**
Volume = 12 x 10 x 15 = 180 cm³
W = mg
Mass = 72/10 = 7.2kg
Density = mass/volume = 7200/180 = 4g/cm³ = 4000kg/m³
8. The mass of an empty density bottle is **20g**. When the bottle is full of paraffin it weighs **60g** and when full of water weighs **70g**. Calculate the density of paraffin in SI units. **(4mk)**
Mass of paraffin = 60 - 20 = 40g
Mass of water 70 - 20 = 50g
Volume of water = 50/1g/cm³ = 50 cm³
Volume of water = volume of paraffin = 50 cm³
Density of paraffin = m/v = 40/50 = 0.8g/cm³ = 800kg/m³
9. An empty density bottle has a mass of **50g**. Its mass is **100g** when filled with water and **120g** when filled with liquid **K**. Calculate the density of liquid **K** in **SI** units.
Mass of water = 100 - 50 = 50g
Mass of water 120 - 50 = 70g
Volume of water = 50/1g/cm³ = 50 cm³ (density of water = 1g/cm³)
Volume of density bottle = volume of liquid K = 50 cm³
Density of liquid K = m/v = 70/50 = 1.4g/cm³ = 1400kg/m³
10. The mass of a density bottle is **20g** when empty, **70g** when full of water and **50g** when full of ethanol. Calculate the density of ethanol in **SI** units.
Mass of water = 70 - 20 = 50g
Mass of ethanol 50 - 20 = 30g
Volume of water = 50/1g/cm³ = 50 cm³ (density of water = 1g/cm³)
Density of liquid ethanol = m/v = 30/50 = 0.6g/cm³ = 600kg/m³
11. A density bottle has a mass of **45g** when full of paraffin and a mass of **50g** when full of water if the empty bottle weighs **25g**, calculate the relative density of paraffin.
Mass of paraffin = 45 - 25 = 20g
Mass of water 50 - 25 = 25g
Volume of water = 25/1g/cm³ = 25 cm³
Volume of water = volume of paraffin = 25 cm³
Density of paraffin = m/v = 20/25 = 0.8g/cm³ = 800kg/m³
12. The mass of an empty density bottle is **20g**. When the bottle is full of paraffin it weighs **60g** and when full of water weighs **70g**. Calculate the density of paraffin in **SI** units.
Mass of paraffin = 60 - 20 = 40g
Mass of water 70 - 20 = 50g
Volume of water = 50/1g/cm³ = 50 cm³
Volume of water = volume of paraffin = 50 cm³
Density of paraffin = m/v = 40/50 = 0.8g/cm³ = 800kg/m³

13. The mass of a density bottle is **20g** when empty **70g** when full of water and **695g** when full of another liquid. Calculate the

(i) density of the other liquid (take density of water as **1g/cm³**)

$$\text{Mass of water} = 70 - 20 = 50\text{g}$$

$$\text{Mass of liquid} = 695 - 20 = 675\text{g}$$

$$\text{Volume of water} = 50/1\text{g/cm}^3 = 50\text{ cm}^3$$

$$\text{Volume of water} = \text{volume of liquid} = 50\text{ cm}^3$$

$$\text{Density of liquid} = m/v = 675/50 = 13.5\text{g/cm}^3 = 13500\text{kg/m}^3$$

(ii) Mass of **20cm³** of the liquid

(2mk)

$$\text{Mass} = \text{density} \times \text{volume}$$

$$13.5 \times 20 = 270\text{g}$$

14. The mass of a density bottle of volume **50cm³** is **10.0g** when empty. Aluminium turnings are poured into the bottle and the total mass is **60.0g**. Water is then added into the turnings till the bottle is full. If the total mass of the bottle and its contents is **90.0g**, calculate the density of the aluminium turnings. **(3mk)**

$$\text{Mass of aluminium turnings} = 60 - 10 = 50\text{g}$$

$$\text{Mass of liquid} = 90 - 60 = 30\text{g}$$

$$\text{Volume of water} = 30/1\text{g/cm}^3 = 30\text{ cm}^3$$

$$\text{Volume of aluminium turnings} = 50 - 30 = 20\text{cm}^3$$

$$\text{Density} = m/v = 50/20 = 2.5\text{g/cm}^3 = 2500\text{kg/m}^3$$

15. An empty density bottle has a mass of **23g**. When completely filled with water its mass is **39.0g**. What will be its mass if it is completely filled with an acid of relative density **1.25**? (Take the density of water as **1.0gcm⁻³**)

$$\text{Mass of water} = 39 - 23 = 16\text{g}$$

$$\text{Density of acid} = 1.25\text{g/cm}^3$$

$$\text{Volume of water} = \text{mass/volume} = 16/1\text{g/cm}^3 = 16\text{cm}^3$$

$$\text{Mass of acid} = 1.25 \times 16 = 20\text{cm}^3$$

16. An empty density bottle has a mass of **30g**. When completely filled with water its mass is **70g**. What will be its mass if it is completely filled with an acid of relative density **1.6**?

$$\text{Mass of water} = 70 - 30 = 40\text{g}$$

$$\text{Volume of water} = m/d = 40/1 = 40\text{cm}^3$$

$$\text{Volume of water} = \text{volume of acid}$$

$$\text{Mass of acid} = 1.6 \times 40 = 64\text{cm}^3$$

17. **200cm³** of water of density **1g/cm³** is mixed with **300cm³** of milk of density **2g/cm³**. Calculate

(i) The total volume of the mixture

$$200 + 300 = 500\text{ cm}^3$$

(ii) The total mass of the mixture

$$\text{Mass of water} = \text{density} \times \text{volume}$$

$$1\text{g/cm}^3 \times 200\text{ cm}^3 = 200\text{g}$$

$$\text{Mass of milk} = \text{density} \times \text{volume}$$

$$2\text{g/cm}^3 \times 300\text{ cm}^3 = 600\text{g}$$

$$\text{Total mass of mixture} = 200\text{g} + 600\text{g} = 800\text{g}$$

(iii) The density of the mixture in **SI** units.

$$\text{Density of mixture} = \text{total mass mixture} / \text{total volume of mixture}$$

$$800/500 = 1.6\text{g/cm}^3 = 1600\text{kg/m}^3$$

- 18.** 1000cm^3 of water density 1g/cm^3 mixed with 2000cm^3 of saturated salt solution of density 1.3g/cm^3 . Calculate
- The total volume of the mixture
 $1000 + 2000 = 3000\text{cm}^3$
 - The total mass of the mixture
Mass of water = density x volume
 $1\text{g/cm}^3 \times 1000\text{cm}^3 = 1000\text{g}$
Mass of saturated salt = density x volume
 $1.3\text{g/cm}^3 \times 2000\text{cm}^3 = 2600\text{g}$
Total mass of mixture = 1000g + 2600g = 3600g
 - The density of the mixture in SI units.
Density of mixture = total mass mixture/total volume of mixture
 $3600/3000 = 1.2\text{g/cm}^3 = 1200\text{kg/m}^3$
- 19.** An alloy is made by mixing 80cm^3 of copper of density 9g/cm^3 with 120cm^3 of aluminium of density 3g/cm^3 . Determine the
- Total volume of the alloy.
 $80 + 120 = 200\text{cm}^3$
 - Total mass of the alloy
Mass of copper = density x volume
 $9\text{g/cm}^3 \times 80\text{cm}^3 = 720\text{g}$
Mass of aluminium = density x volume
 $3\text{g/cm}^3 \times 120\text{cm}^3 = 360\text{g}$
Total mass of mixture = 720g + 360g = 1080g
 - Density of the alloy in SI units.
Density of alloy = total mass mixture/total volume of mixture
 $1080/200 = 5.4\text{g/cm}^3 = 5400\text{kg/m}^3$
- 20.** 100cm^3 of water of density 1g/cm^3 is mixed with 400cm^3 of ethanol of density 800kg/m^3 . Calculate
- The total volume of the mixture
 $100 + 400 = 500\text{cm}^3$
 - The total mass of the mixture
Mass of water = density x volume
 $1\text{g/cm}^3 \times 100\text{cm}^3 = 100\text{g}$
Mass of ethanol = density x volume
 $0.8\text{g/cm}^3 \times 400\text{cm}^3 = 320\text{g}$
Total mass of mixture = 100g + 320g = 420g
 - The density of the mixture in SI units.
Density of mixture = total mass mixture/total volume of mixture
 $420/500 = 0.84\text{g/cm}^3 = 840\text{kg/m}^3$
- 21.** 400cm^3 of alcohol of density 800kg/m^3 is mixed with 600cm^3 of water of density 1000kg/m^3 . Calculate the density if the mixture in SI units.
Density of mixture = total mass of mixture/total volume of mixture
 $= \frac{(400 \times 0.8) + (600 \times 1)}{400 + 600} = 920/1000 = 0.92\text{g/cm}^3 = 920\text{kg/m}^3$
- 22.** An alloy is made by mixing 180cm^3 iron metal of density 2000kg/m^3 with 120cm^3 of lead metal of density 4g/cm^3 . Calculate the density of the alloy.
Density of mixture = total mass of mixture/total volume of mixture
 $= \frac{(180 \times 2) + (120 \times 4)}{180 + 120} = 840/300 = 2.8\text{g/cm}^3 = 2800\text{kg/m}^3$

- 23.** 400cm^3 of alcohol of density 800kg/m^3 is mixed with 600cm^3 of water of density 1g/cm^3 . Calculate the density if the mixture in **SI** units.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(400 \times 0.8) + (600 \times 1)}{400 + 600} = 920/1000 = 0.92\text{g/cm}^3 = 920\text{kg/m}^3$$
- 24.** 1600cm^3 of fresh water of density 1g/cm^3 are mixed with 1400cm^3 of seawater of density 1.25g/cm^3 . Determine the density of the mixture.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(1600 \times 1) + (1400 \times 1.25)}{1600 + 1400} = 3350/3000 = 1.117\text{g/cm}^3 = 1117\text{kg/m}^3$$
- 25.** A liquid of density 800kg/m^3 has a mass of 3.2g . Calculate its volume in **SI** unit.
Volume = mass/density = $3.25/0.8 = 4\text{cm}^3$
- 26.** 100cm^3 of water of density 1g/cm^3 is mixed with 200cm^3 of ethanol of density 0.79g/cm^3 . Calculate the density of the mixture in SI units.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(100 \times 1) + (200 \times 0.79)}{100 + 200} = 258/300 = 0.86\text{g/cm}^3 = 860\text{kg/m}^3$$
- 27.** 500cm^3 of fresh water of density 1000kg/m^3 mixed with 1000cm^3 of sea water density 1020kg/m^3 . Calculate the density of the mixture in SI units.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(500 \times 1) + (1000 \times 1.02)}{500 + 1000} = 1520/1500 = 1.013\text{g/cm}^3 = 1013\text{kg/m}^3$$
- 28.** An alloy is made by mixing 80cm^3 of copper of density 8.9g/cm^3 with 120cm^3 of aluminium of density 2.7g/cm^3 . Determine the density of the alloy in SI units.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(80 \times 8.9) + (120 \times 2.7)}{80 + 120} = 1036/200 = 5.18\text{g/cm}^3 = 5180\text{kg/m}^3$$
- 29.** An alloy is made by mixing 180cm^3 iron metal of density 2000kg/m^3 with 120cm^3 of lead metal of density 4g/cm^3 . Calculate the density of the alloy.
Density of alloy = total mass of mixture/total volume of mixture

$$= \frac{(180 \times 2) + (120 \times 4)}{180 + 120} = 840/300 = 2.8\text{g/cm}^3 = 2800\text{kg/m}^3$$
- 30.** 400cm^3 of alcohol of density 800kg/m^3 is mixed with 600cm^3 of water of density 1g/cm^3 . Calculate the density if the mixture in **SI** units.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(400 \times 0.8) + (600 \times 1)}{400 + 600} = 920/1000 = 0.92\text{g/cm}^3 = 920\text{kg/m}^3$$
- 31.** 100cm^3 of sea water of density 1150kg/m^3 is mixed with 100cm^3 of fresh water of density 1000kg/m^3 . Determine density of the mixture.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(100 \times 1.15) + (100 \times 1)}{100 + 100} = 215/200 = 1.075\text{g/cm}^3 = 1075\text{kg/m}^3$$
- 32.** 1600cm^3 of fresh water of density 1g/cm^3 are mixed with 1400cm^3 of seawater of density 1.25g/cm^3 . Determine the density of the mixture.
Density of mixture = total mass of mixture/total volume of mixture

$$= \frac{(1600 \times 1) + (1400 \times 1.25)}{1600 + 1400} = 3350/3000 = 1.117\text{g/cm}^3 = 1117\text{kg/m}^3$$

- 33.** An alloy contains **40%** by mass of lead and **60%** by mass of tin. Determine the density of the alloy in kgm^3 . (density of lead = **1.4g/cm^3** and density of tin = **7.3g/cm^3**) (3mks)
- 34.** $X\text{cm}^3$ of substance **A** which has a density of **800kg/m^3** is mixed with **100cm^3** of water with a density of **1000kg/m^3** . The density of the mixture is **960kg/m^3** . Determine the value of **X**.

Density of mixture = total mass of mixture/total volume of mixture

$$0.96 = \frac{(y \times 0.8) + (100 \times 1)}{y + 100}$$

$$0.96 = \frac{0.8y + 100}{y + 100}$$

$$0.96(y + 100) = 0.8y + 100$$

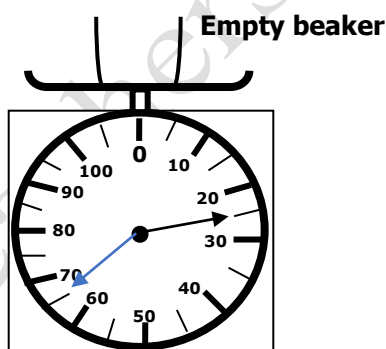
$$Y = 25\text{cm}^3$$

MASS

- 35.** A butcher has a beam balance and masses **0.5 kg** and **2 kg**. How would he measure **1.5 kg** of meat on the balance at once?

Place a mass of 2kg on one side and 0.5kg mass on the other side . place a piece of meat which have a mass relatively greater than 1.5kg on the same side as 0.5kg mass. Reduce the meat bit by bit until the beam balances and end up with 1.5kg mass meat.

- 36.** The figure below shows an empty beaker placed on the top of a pan calibrated in grammes. **50ml** of alcohol of density **0.8g/cm^3** was added to the beaker. Show on the diagram the new pointer position. (3mk)



$$1\text{l} = 1000\text{ml}$$

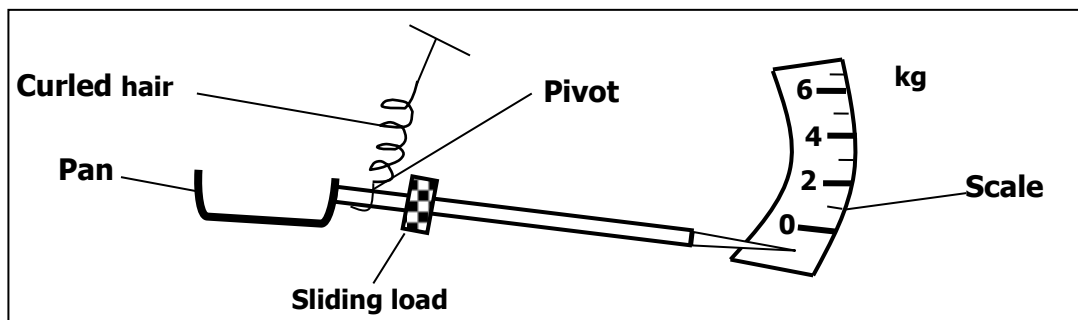
$$? = 50\text{ml}$$

$$0.05\text{ml}$$

$$\text{Mass} = \text{density} \times \text{volume} = 0.8 \times 50 = 40\text{g}$$

$$\text{New reading } 25\text{g} + 40\text{g} = 65\text{g}$$

37. Figure below shows the arrangement of a sensitive spring balance.



How would you adjust the position of the sliding load to reset its reading to zero?
(1 mk)

Moving the sliding load towards the pan.