

CS331
Haskell Tutorial 01
Basic of Haskell

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Outline

- Introduction: Installing, Invoking, Hello world
- Functional programming
 - Basic
- Typed
- Isomorphic
- Currying, Composition
- Lazy Evaluation

Installing Haskell: GHC and Cabal

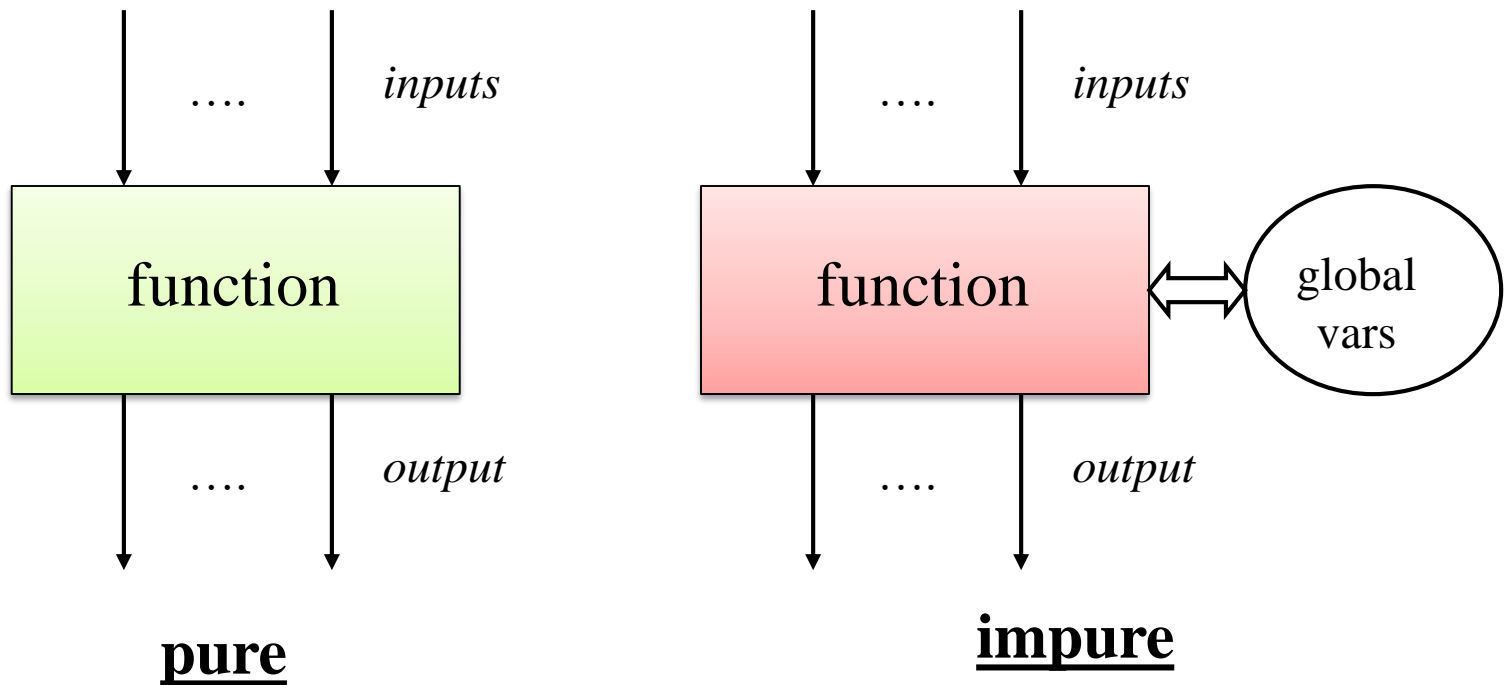
- Ubuntu
 - `sudo add-apt-repository ppa:hvr/ghc`
 - `sudo apt-get update`
 - `sudo apt-get install -y cabal-install ghc`
- Windows in command mode
 - `Start-Process powershell -Verb runAs`
 - `Set-ExecutionPolicy Bypass -Scope Process -Force;`
`[System.Net.ServicePointManager]::SecurityProtocol =`
`[System.Net.ServicePointManager]::SecurityProtocol -bor 3072; iex ((New-Object`
`System.Net.WebClient).DownloadString('https://chocolatey.org/install.ps1'))`
 - Download https://get.haskellstack.org/stable/windows-x86_64-installer.exe
 - **choco install haskell-dev**
- Issue command: `ghci` or `ghc`

GHC and Cabal

- GHC (Glasgow Haskell Compiler, version **10**) is the version of Haskell I am using
 - GHCi is the REPL
 - Just enter **ghci** at the command line
- \$ghci
 - Prelude> "Hello, World!"
 - Prelude> putStrLn "Hello World"
- Create object file: put putStrLn "Hello World" in file hw.hs
 - \$ghc -o hello hw.hs
 - \$./hello

Functions

- Function is a black box that converts input to output. A basis of software component.



Using Haskell

- You can do arithmetic at the prompt:
 - Prelude> `2 + 2`
4
- You can call functions at the prompt:
 - Prelude> `sqrt 10`
3.16228
- The GHCi documentation says that functions must be loaded from a file:
 - Prelude > `:l "test.hs"`
Reading file "test.hs":
- But you can define them in GHCi with `let`
 - `let double x = 2 * x`

Lexical issues

- Haskell is case-sensitive
 - Variables begin with a lowercase letter
 - Type names begin with an uppercase letter
- Indentation matters (braces and semicolons can also be used, but it's not common)
- There are two types of comments:
 - `--` (two hyphens) to end of line
 - `{ -` multi-line `{ -` these may be nested `- }` `- }`

Semantics of Haskell

- The best way to think of a Haskell program is as a single mathematical expression
 - In Haskell you do not have a sequence of “statements”, each of which makes some changes in the state of the program
 - Instead you evaluate an expression, which can call functions
- Haskell is a **functional programming** language

Functional Programming (FP)

- Functions are **first-class objects**. That is, they are **values**, just like other objects are values, and can be treated as such. Functions can be
 - assigned to variables, passed as parameters to **higher-order functions**, returned as results of functions
 - There is some way to write **function literals**
- Functions should *only* transform their inputs into their outputs
 - A function should have no **side effects**
 - It should not do any input/output
 - It should not change any **state** (any external data)

Functional Programming (FP)

- Given the same inputs, a function should produce the same outputs, every time--it is deterministic
- If a function is side-effect free and deterministic, it has **referential transparency**—all calls to the function could be replaced in the program text by the result of the function
 - But we need random numbers, date and time, input and output, etc.

Types

- Haskell is strongly typed...
- But type declarations are seldom needed, because Haskell does **type inferencing**
- Primitive types: **Int**, **Float**, **Char**, **Bool**
- Lists: **[2, 3, 5, 7, 11]**
 - All list elements must be the same type
- Tuples: **(1, 5, True, 'a')**
 - Tuple elements may be different types

Bool Operators

- `Bool` values are `True` and `False`
 - Notice how these are capitalized
- “And” is infix `&&`
- “Or” is infix `||`
- “Not” is prefix `not`
- Functions have types
 - “Not” is type `Bool -> Bool`
 - “And” and “Or” are type `Bool -> Bool -> Bool`

Arithmetic on Integers

- `+` `-` `*` `/` `^` are infix operators
 - Add, subtract, and multiply are type $(\text{Num } a) \Rightarrow a \rightarrow a \rightarrow a$
 - Divide is type $(\text{Fractional } a) \Rightarrow a \rightarrow a \rightarrow a$
 - Exponentiation is type $(\text{Num } a, \text{Integral } b) \Rightarrow a \rightarrow b \rightarrow a$
- `even` and `odd` are prefix operators
 - They have type $(\text{Integral } a) \Rightarrow a \rightarrow \text{Bool}$
- `div`, `quot`, `gcd`, `lcm` are also prefix
 - They have type $(\text{Integral } a) \Rightarrow a \rightarrow a \rightarrow a$

Floating-Point Arithmetic

- $+$ $-$ $*$ $/$ $^$ are infix operators, with the types specified previously
- \sin , \cos , \tan , \log , \exp , $\sqrt{}$, \log , \log_{10}
 - These are prefix operators, with type
 - $(\text{Floating } a) \Rightarrow a \rightarrow a$
- π
 - Type Float
- truncate
 - Type $(\text{RealFrac } a, \text{Integral } b) \Rightarrow a \rightarrow b$

Operations on Chars

- These operations require `import Data.Char`
- `ord` is `Char -> Int`
- `chr` is `Int -> Char`
- `isPrint`, `isSpace`, `isAscii`, `isControl`, `isUpper`, `isLower`, `isAlpha`, `isDigit`, `isAlphaNum` are all `Char -> Bool`
- A string is just a list of `Char`, that is, `[Char]`
 - `"abc" == ['a', 'b', 'c']`

Polymorphic Functions

- `==` `/=`
 - Equality and inequality tests are type
`(Eq a) => a -> a -> Bool`
- `<` `<=` `>=` `>`
 - These comparisons are type
`(Ord a) => a -> a -> Bool`
- `show` will convert almost anything to a string
- Any operator can be used as infix or prefix
 - `(+) 2 2` is the same as `2 + 2`
 - `100 `mod` 7` is the same as `mod 100 7`

Simple Functions

- Functions are defined using =
 - `Prelude> avg x y = (x + y) / 2`
- `:type` or `:t` tells you the type
 - `Prelude>:t avg`
`avg: (Fractional a) => a -> a -> a`

Example of Functions

- Double a given input.

```
square :: Int -> Int
Prelude>square x = x*x
Prelude>square 5
```

- Conversion from fahrenheit to celcius

```
fahr_to_celcius :: Float -> Float
Prelude> fahr_to_celcius temp = (temp - 32)/1.8
Prelude> :t fahr_to_celcius
```

- A function with multiple results - quotient & remainder

```
divide :: Int -> Int -> (Int,Int)

divide x y = (div x y, mod x y)
```

Expression-Oriented

- Instead of imperative commands/statements, the focus is on expression.
- Instead of *command/statement* :
`if e1 then stmt1 else stmt2`
- We use conditional *expressions* :
`if e1 then e2 else e3`

Expression-Oriented

- An example function:

```
fact    :: Integer -> Integer
fact n  = if n=0 then 1
          else n * fact (n-1)
```

- Can use pattern-matching instead of conditional

```
fact 0      = 1
fact n      = n * fact (n-1)
```

- Alternatively:

```
fact n      = case n of
  0 -> 1
  a -> a * fact (a-1)
```

Conditional → Case Construct

- Conditional;

```
if e1 then e2 else e3
```

- Can be translated to

```
case e1 of  
  True  -> e2  
  False -> e3
```

- Case also works over data structures
(without any extra primitives)

```
length xs = case xs of  
  [] -> 0;  
  y:ys -> 1+(length ys)
```

↖
Locally bound variables

Lexical Scoping

- Local variables can be created by **let** construct to give nested scope for the name space.

Example:

```
let      y = a+b
      f x = (x+y)/y
in f c + f d
```

- For scope bindings over guarded expressions, we require a **where** construct instead:

```
f x y      | x>z= ...
          | y==z      = ...
          | y<z= ....
where z=x*x
```

Layout Rule

- Haskell uses two dimensional syntax that relies on declarations being “lined-up columnwise”

```
let  y      = a+b  
    f x    = (x+y)/y  
in f c + f d
```

is being parsed as:

```
let  { y      = a+b  
      ; f x    = (x+y)/y }  
in f c + f d
```

- Rule : Next character after keywords **where/let/of/do** determines the starting columns for declarations.
Starting *after* this point continues a declaration, while starting *before* this point terminates a declaration.

Expression Evaluation

- Expression can be computed (or evaluated) so that it is reduced to a value. This can be represented as:

$$e \rightarrow \dots \rightarrow v$$

- We can abbreviate above as:

$$e \rightarrow^* v$$

- A concrete example of this is:

$$\text{inc } (\text{inc } 3) \rightarrow \text{inc } (4) \rightarrow 5$$

- Type preservation theorem says that:

if $e :: t \ \&\#x2190^* \ v$, it follows that $v :: t$

Values and Types

- As a purely functional language, all computations are done via evaluating *expressions* (syntactic sugar) to yield *values* (normal forms as answers).
- Each expression has a *type* which denotes the set of possible outcomes.
- $v :: t$ can be read as value v has type t .
- Examples of *typings*, associating a value with its corresponding type are:

5	:: Integer
'a'	:: Char
[1,2,3]	:: [Integer]
('b', 4)	:: (Char, Integer)
"cs5"	:: String (same as [Char])

Built-In Types

- They are not special:

```
data Char      = 'a' | 'b' | ...
data Int       = -65532 | ... | -1 | 0 | 1 | ... | 65532
data Integer   = ... | -2 | -1 | 0 | 1 | 2 | ...
```

- Tuples are also built-in.

```
data (a,b)      = M2 (a,b)
data (a,b,c)     = M3 (a,b,c)
data (a,b,c,d)   = M4 (a,b,c,d)
```

- List type uses an infix operator:

```
data [a]         = [] | a : [a]
```

`[1,2,3]` is short hand for `1 : (2 : (3 : []))`

User-Defined Algebraic Types

- Can describe enumerations:

```
data Bool      = False | True
data Color     = Red   | Green | Blue | Violet
```

- Can also describe a tuple

```
data Pair      = P2 Integer Integer
data Point a   = Pt a a
```

 *type variable*

- **Pt** is a data constructor with type **a -> a -> Point a**

```
Pt 2.0 3.1      :: Point Float
Pt 'a' 'b'      :: Point Char
Pt True False   :: Point Bool
```

Recursive Types

- Some types may be recursive:

```
data Tree a = Leaf a | Branch (Tree a) (Tree a)
```

- Two data constructors:

```
Leaf    :: a -> Tree a  
Branch :: Tree a -> Tree a -> Tree a
```

- An example function over recursive types:

```
fringe :: Tree a -> [a]
```

```
fringe (Leaf x)          = [x]  
fringe (Branch left right) = (fringe left) ++  
                             (fringe right)
```

Polymorphic Types

- Support types that are universally quantified in some way over all types.
- $\lambda c. [c]$ denotes a family of types, for every type c , the type of lists of c .
- Covers `[Integer]`, `[Char]`, `[Integer->Integer]`, etc.
- Polymorphism help support *reusable* code, e.g

```
length      ::  $\lambda a. [a] \rightarrow \text{Integer}$   
length []   = 0  
length (x:xs) = 1 + length xs
```

```
Prelude> :t length
```

Polymorphic Types

- This polymorphic function can be used on list of any type..

```
length [1,2,3]           )      2
length ['a', 'b', 'c']   )      3
length [[1],[],[3]]      )      3
```

- More examples :

```
head      :: [a] -> a
head (x:xs) = x
```

```
tail      :: [a] -> [a]
tail (x:xs) = xs
```

- Note that head/tail are partial functions, while length is a total function?

Principal Types

- Some types are more general than others:

$[Char] \leq 8 a. [a] \leq 8 a. a$

- An expression's *principal type* is the *least general type* that contains all instances of the expression.
- For example, the *principal type* of `head` function is $[a] \rightarrow a$, while $[b] \rightarrow a$, $b \rightarrow a$, a are correct but too general but $[Integer] \rightarrow Integer$ is too specific.
- Principal type can help supports software reusability with accurate type information.

Functions and its Type

- Method to increment its input

```
inc x = x+1
```

- Or through lambda expression (anonymous functions)

```
(\ x -> x+1)
```

- They can also be given suitable function typing:

```
inc           :: Num a => a -> a  
(\x -> x+1)   :: Num a => a -> a
```

- Types can be *user-supplied* or *inferred*.

Anonymous Functions

- Anonymous functions are used often in Haskell, usually enclosed in parentheses
- $\backslash x\ y \rightarrow (x + y) / 2$
 - the \backslash is pronounced “lambda”
 - It’s just a convenient way to type λ
 - the x and y are the formal parameters
- Functions are first-class objects and can be assigned
 - $\text{avg} = \backslash x\ y \rightarrow (x + y) / 2$

Functions and its Type

- Some examples

```
(\x -> x+1) 3.2  →
```

```
(\x -> x+1) 3  →
```

```
Prelude> (\x -> x+1) 3
```

- User can restrict the type, e.g.

```
inc    :: Int -> Int
```

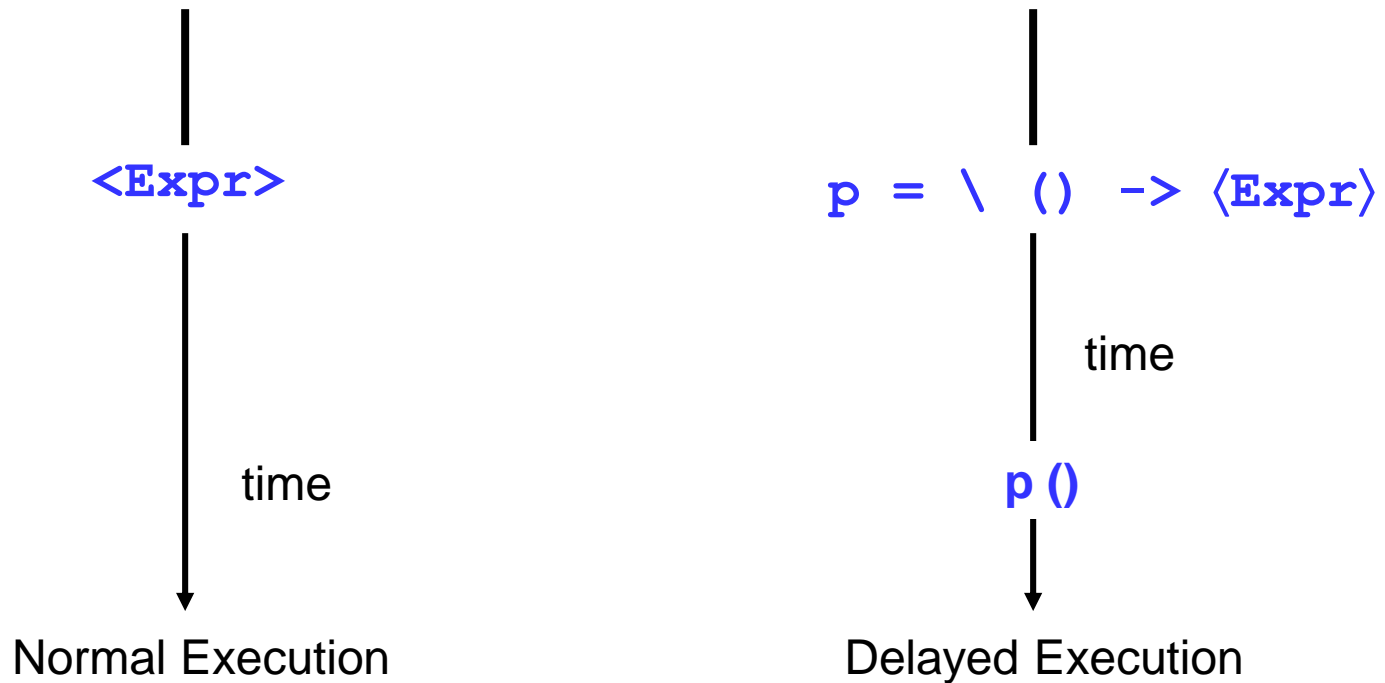
- In that case, some examples may be wrongly typed.

```
inc 3.2  →
```

```
inc 3  →
```

Function Abstraction

- Function abstraction is the ability to convert any expression into a function that is evaluated at a later time.



Higher-Order Functions

- **Higher-order programming** treats functions as first-class,
 - Allowing them to be passed as parameters, returned as results or stored into data structures.
- This concept supports generic coding,
 - and allows programming to be carried out at a more abstract level.
- Genericity can be applied to a function
 - by letting specific operation/value in the function body to become parameters.

Functions

- Functions can be written in two main ways:

```
add                :: Integer -> Integer -> Integer
add x y           = x+y
```

```
add2               :: (Integer,Integer) -> Integer
add2 (x,y)         = x+y
```

- The first version allows a function to be returned as result after applying a single argument.

```
inc                :: Integer -> Integer
inc                = add 1
```

- The second version needs all arguments. Same effect requires a lambda abstraction:

```
inc                = \ x -> add2 (x,1)
```

Functions

- Functions can also be passed as parameters. Example:

```
map           :: (a->b) -> [a] -> [b]
map f []      = []
map f (x:xs)  = (f x) : (map f xs)
```

- Such higher-order function aids code reuse.

```
map (add 1) [1, 2, 3]    ) [2, 3, 4]
map add [1, 2, 3]        ) [add 1, add 2, add 3]
```

- Alternative ways of defining functions:

```
add           = \ x -> \ y -> x+y
add           = \ x y -> x+y
```