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## Matrix Theory EE5609 - Assignment 3 Find if a triangle is isosceles triangle.

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23-Sep-2020
AI20RESCH14001

Abstract—This document provides a solution for finding if a traingle is isosceles given two equal altitudes of the triangle

## I. PROBLEM STATEMENT

BE and CF are two equal altitudes of a triangle ABC. Prove that the triangle ABC is isosceles.

## II. SOLUTION

Given that BE and CF are two equal altitudes of a triangle ABC.

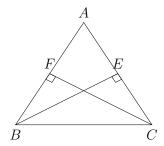


Fig. 1: Triangle with equal altitudes on two sides

Given that,

$$\|(\mathbf{B} - \mathbf{E})\| = \|(\mathbf{C} - \mathbf{F})\|$$

$$(1)$$

$$\|(\mathbf{B} - \mathbf{A})\| + \|(\mathbf{A} - \mathbf{E})\| = \|(\mathbf{C} - \mathbf{A})\| + \|(\mathbf{A} - \mathbf{F})\|$$

$$(2)$$

$$||(\mathbf{B} - \mathbf{A})|| + ||(\mathbf{A} - \mathbf{B})|| + ||(\mathbf{B} - \mathbf{E})|| = ||(\mathbf{C} - \mathbf{A})|| + ||(\mathbf{A} - \mathbf{C})|| + ||(\mathbf{C} - \mathbf{F})||$$
(3)

$$\|(\mathbf{B} - \mathbf{A})\| + \|(\mathbf{A} - \mathbf{B})\| =$$
  
 $\|(\mathbf{C} - \mathbf{A})\| + \|(\mathbf{A} - \mathbf{C})\|$  (4)

$$2 \times \|(\mathbf{B} - \mathbf{A})\| = 2 \times \|(\mathbf{C} - \mathbf{A})\|$$
 (5)

$$\|(\mathbf{B} - \mathbf{A})\| = \|(\mathbf{C} - \mathbf{A})\| \tag{6}$$

Therefore, the sides AB and AC of the  $\triangle ABC$  are of the same magnitude. Hence  $\triangle ABC$  is an isosceles triangle with equal sides AB and AC.