

# Matrix Theory EE5609 - Assignment 1

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**Abstract**—This document provides a solution for the problem of finding slopes of two lines, slope of one line being double of the slope of another line. and tangent of the angle between them is  $1/3$ .

## I. PROBLEM STATEMENT

The slope of a line is double of the slope of another line. If the tangent of the angle between them is  $1/3$ , find the slopes of the lines.

## II. SOLUTION

Two vectors are considered to be passing through origin. Where  $m_1$  and  $m_2$  are slopes of the vectors  $\mathbf{m}_1$  and  $\mathbf{m}_2$  respectively. Let  $m_1 = m$ . Given  $m_2 = 2m$

These vectors can be represented as below:-

$$\mathbf{m}_1 = \begin{pmatrix} 1 \\ m \end{pmatrix} \quad \mathbf{m}_2 = \begin{pmatrix} 1 \\ 2m \end{pmatrix} \quad (1)$$

The dot product of the vectors is given by:-

$$\mathbf{m}_1^T \mathbf{m}_2 = \|\mathbf{m}_1\| \|\mathbf{m}_2\| \cos \theta \quad (2)$$

Given that

$$\tan \theta = \frac{1}{3} \quad (3)$$

By Pythagorus theorem, we can obtain

$$\cos \theta = \frac{3}{\sqrt{10}} \quad (4)$$

Therefore,

$$\cos \theta = \frac{\mathbf{m}_1^T \mathbf{m}_2}{\|\mathbf{m}_1\| \|\mathbf{m}_2\|} \quad (5)$$

$$\frac{3}{\sqrt{10}} = \frac{1 \times 1 + m \times 2m}{\sqrt{1+m^2} \sqrt{1+4m^2}} \quad (6)$$

Applying square on both sides:-

$$9 \times (1+m^2)(1+4m^2) = 10(1+2m^2)^2 \quad (7)$$

$$4m^4 - 5m^2 + 1 = 0 \quad (8)$$

$$m_1 = m = 1, -1, \frac{1}{2}, -\frac{1}{2} \quad (9)$$

Substituting the value of  $m_1$  we get value of  $m_2 = 2, -2, 1, -1$ .

## III. CONCLUSION

The slopes  $m_1$  and  $m_2$  of vectors  $\mathbf{m}_1$  and  $\mathbf{m}_2$  for the said conditions are: -

$$\begin{pmatrix} 1 \\ 2 \end{pmatrix}, \begin{pmatrix} -1 \\ -2 \end{pmatrix}, \begin{pmatrix} \frac{1}{2} \\ 1 \end{pmatrix}, \begin{pmatrix} -\frac{1}{2} \\ -1 \end{pmatrix}$$