

Phase Diagram of Soil

Volume

$$e = \frac{V_v}{V_s}$$

$$n = \frac{V_v}{V}$$

$$S = \frac{V_w}{V_v}$$

Weight

$$\omega = \frac{W_w}{W_s}$$

$$e = \frac{n}{1-n}$$

$$n = \frac{e}{1+e}$$

Se

$$Se = G_s \omega$$

$$\gamma = \frac{W}{V}$$

$$\gamma_d = \frac{W_s}{V}$$

$$\gamma_d = \frac{\gamma}{1+\omega}$$

Unit Weight:

$$\gamma = \frac{(G_s + G_s \omega) \gamma_w}{1+e}$$

When S=0:

$$\gamma_d = \frac{G_s \gamma_w}{1+e}$$

When S=100%:

$$\gamma_{sat} = \frac{(G_s + e) \gamma_w}{1+e}$$

$$\gamma_{sub} = \gamma_{sat} - \gamma_w$$

$$\gamma_{sub} = \frac{(G_s - 1) \gamma_w}{1+e}$$

$$\gamma_{zav} = \frac{G_s \gamma_w}{1 + G_s \omega}$$

Specific Gravity of Solid:

$$G_s = \frac{\gamma_s}{\gamma_w}$$

Bulk Specific Gravity:

$$g = G_s(1 - n)$$

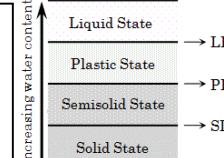
Relative Compaction:

$$R = \frac{\gamma_d}{\gamma_{dmax}}$$

Relative Density/Density Index:

$$D_r = \frac{e_{max} - e}{e_{max} - e_{min}}$$

$$D_r = \frac{\frac{1}{\gamma_{dmin}} - \frac{1}{\gamma_d}}{\frac{1}{\gamma_{dmin}} - \frac{1}{\gamma_{dmax}}}$$



$$SL = \frac{m_1 - m_2}{m_2} - \frac{V_1 - V_2}{m_2} \gamma_w$$

$$SL = \frac{e}{G_s}; SR = \frac{m_2}{V_2 \gamma_w}$$

$$G_s = \frac{1}{SR - SL}$$

$$GI = (F - 35)[0.2 + 0.005(LL - 40)] + 0.01(F - 15)(PI - 10)$$

LI	State
LI < 0	Semisolid
0 < LI < 1	Plastic
LI > 1	Liquid
AC	Class
AC < 0.7	Inactive
0.7 < AC < 1.2	Normal
AC > 1.2	Active

PI	Description
0	Non-plastic
1-5	Slightly plastic
5-10	Low plasticity
10-20	Medium plasticity
20-40	High plasticity
>40	Very High plastic

Permeability

$$v = ki; i = \frac{\Delta h}{L}; v_s = \frac{v}{n}$$

Constant Head Test:

$$k = \frac{QL}{Aht}$$

Falling/Variable Head Test:
 $k = \frac{aL}{At} \ln \frac{h_1}{h_2}$

Hazen Formula: $k = c \cdot D_{10}^{-2}$
 Casagrande: $k = 1.4e^2 k_{0.85}$
 Kozeny-Carman: $k = C_1 \cdot \frac{e^2}{1+e}$
 Samarasinha: $k = C_3 \cdot \frac{e^n}{1+e}$

Stresses in Soil

Effective Stress/
Intergranular Stress:
 $p_E = p_T - p_w$

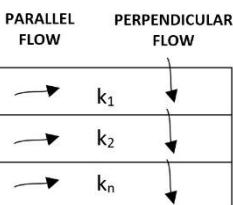
Pore Water Pressure/
Neutral Stress:
 $p_w = \gamma_w h_w$

Total Stress:
 $p_T = \gamma_1 h_1 + \gamma_2 h_2 + \dots + \gamma_n h_n$

NOTE:
Quick condition:
 $p_E = 0$

Capillary Rise:
 $h_{cr} = \frac{C}{eD_{10}}$

Stratified Soil



for Parallel flow:

$$k_{eq} = \frac{h_1 k_1 + h_2 k_2 + \dots + h_n k_n}{H}$$

for Perpendicular flow:

$$k_{eq} = \frac{H}{\frac{h_1}{k_1} + \frac{h_2}{k_2} + \dots + \frac{h_n}{k_n}}$$

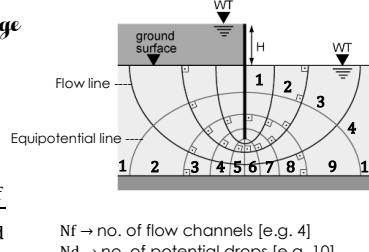
Flow Net / Seepage

Isotropic soil:

$$q = kH \frac{N_f}{N_d}$$

Non-Isotropic soil:

$$q = \sqrt{k_x k_z H} \frac{N_f}{N_d}$$



Lateral Earth Pressure

AT REST: $k_o = 1 - \sin \theta$

ACTIVE PRESSURE: $p_a = \frac{1}{2} k_a \gamma H^2 - 2CH \sqrt{k_a}$

For Inclined:

$$k_a = \cos \beta \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \theta}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \theta}}$$

For Horizontal:

$$k_a = \frac{1 - \sin \theta}{1 + \sin \theta}$$

If there is angle of friction α bet. wall and soil:

$$k_a = \frac{\cos^2 \theta}{\cos \alpha \left[1 + \sqrt{\frac{\sin(\theta + \alpha) \sin \theta}{\cos \alpha}} \right]^2}$$

PASSIVE PRESSURE:

$$p_p = \frac{1}{2} k_p \gamma H^2 + 2CH \sqrt{k_p}$$

For Inclined:

$$k_p = \cos \beta \frac{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \theta}}{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \theta}}$$

For Horizontal:

$$k_p = \frac{1 + \sin \theta}{1 - \sin \theta}$$

If there is angle of friction α bet. wall and soil:

$$k_p = \frac{\cos^2 \theta}{\cos \alpha \left[1 - \sqrt{\frac{\sin(\theta - \alpha) \sin \theta}{\cos \alpha}} \right]^2}$$

Shear strength of soil

$\theta \rightarrow$ angle of failure in shear
 $\phi \rightarrow$ angle of internal friction/shearing resistance
 $C \rightarrow$ cohesion of soil

$$\theta = 45^\circ + \frac{\phi}{2}$$

TRI-AXIAL TEST:

$\sigma_1 \rightarrow$ maximum principal stress

→ axial stress

$\Delta \sigma \rightarrow$ additional pressure

→ deviator stress

→ plunger pressure

$\sigma_3 \rightarrow$ minimum principal stress

→ confining pressure

→ lateral pressure

→ radial stress

→ cell pressure

→ chamber pressure

\odot Normally consolidated:

$$\sin \theta = \frac{r}{\sigma_3 + r}$$

\odot Cohesive soil:

$$\sin \theta = \frac{r}{x + \sigma_3 + r}$$

$$\tan \theta = \frac{c}{x}$$

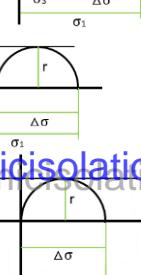
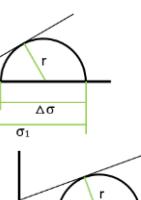
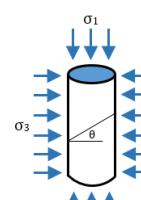
\odot Unconsolidated-undrained test:

$$c = r$$

\odot Unconfined compression test:

$$\sigma_3 = 0$$

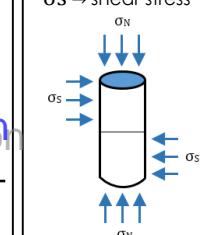
@seismicisolation



DIRECT SHEAR TEST:

$\sigma_N \rightarrow$ normal stress

$\sigma_S \rightarrow$ shear stress



\odot Normally consolidated soil:

$$\tan \theta = \frac{\sigma_S}{\sigma_N}$$

\odot Cohesive soil:

$$\tan \theta = \frac{\sigma_S}{x + \sigma_N} = \frac{c}{x}$$

$$\sigma_S = c + \sigma_N \tan \theta$$

