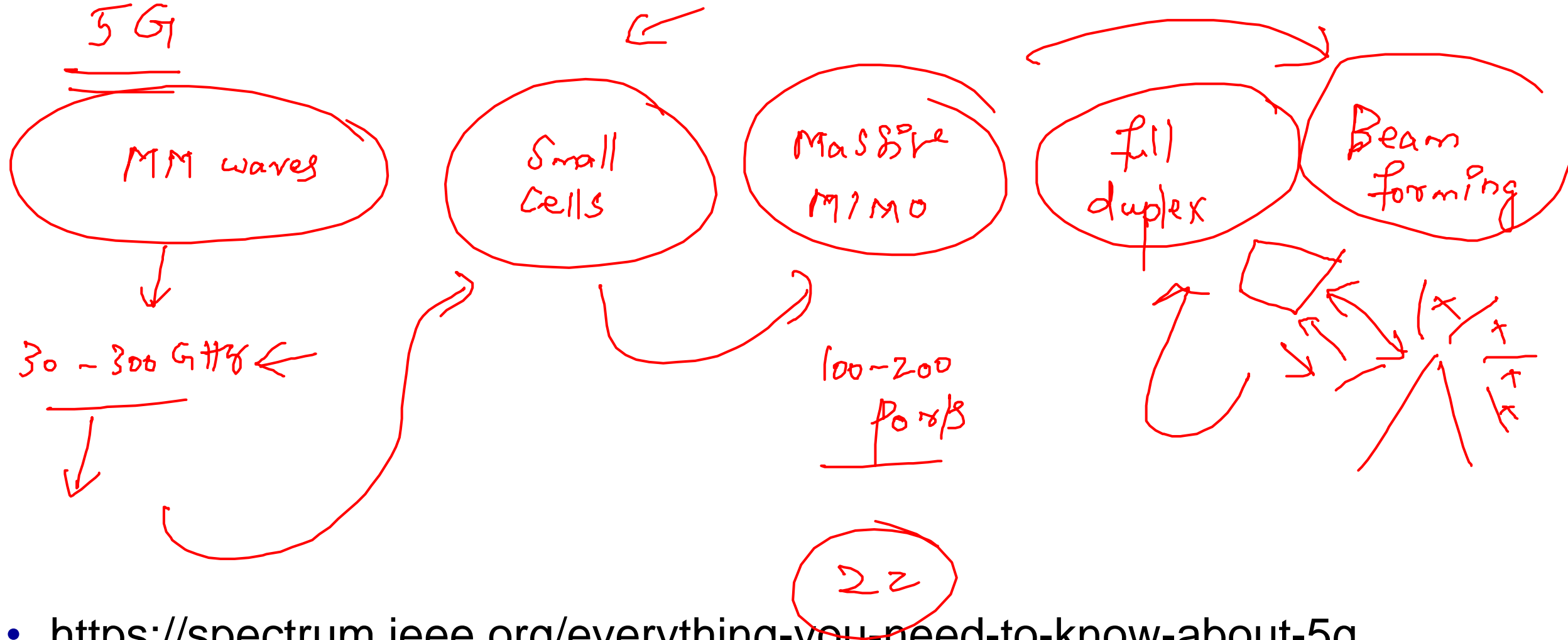


## Unit - II

### 2.5 Super Mesh and Star – Delta Transformation

**Dr.Santhosh.T.K.**



- <https://spectrum.ieee.org/everything-you-need-to-know-about-5g>

## Syllabus

Tool/chest

ohms  
Reduction  
Division  
KVL, KCL  
mesh

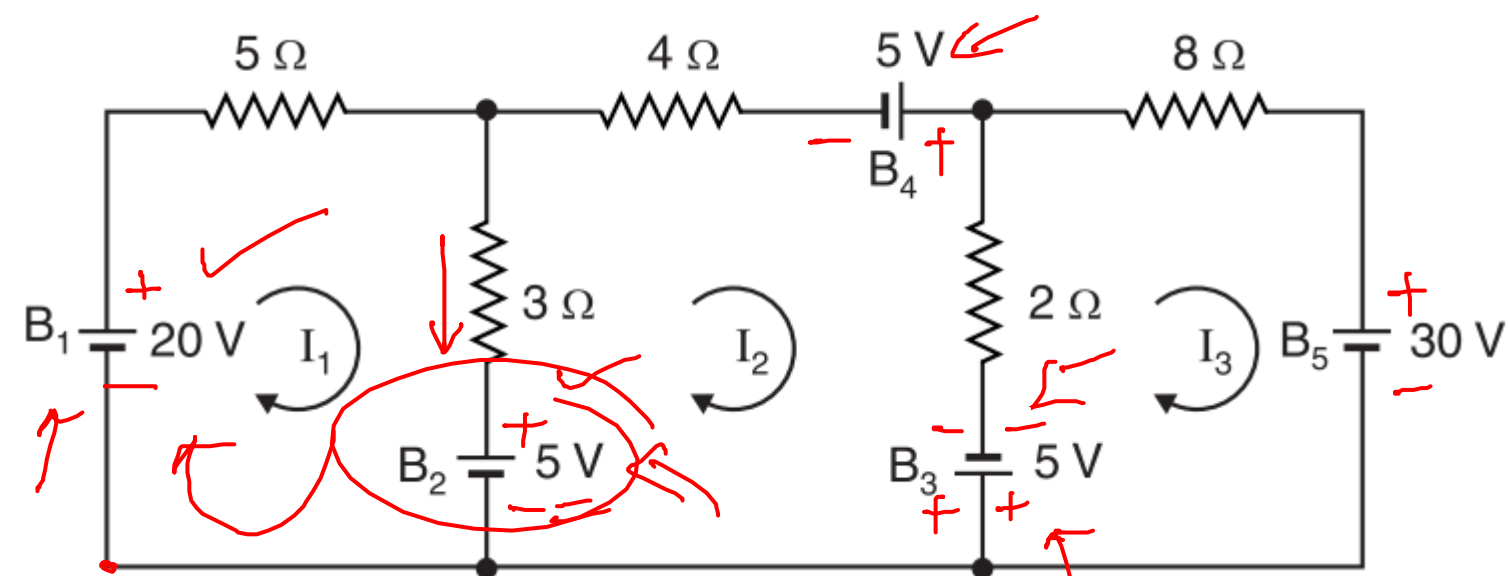
### UNIT – II

14 Periods

**DC Circuit Analysis:** Voltage source and current sources, ideal and practical, Kirchhoff's laws and applications to network solutions using mesh analysis, - Simplifications of networks using series- parallel, Star/Delta transformation, DC circuits-Current-voltage relations of electric network by mathematical equations to analyse the network (Superposition theorem, Thevenin's theorem, Maximum Power Transfer theorem), Transient analysis of R-L, R-C and R-L-C Circuits.

**AC Steady-state Analysis:** AC waveform definitions - Form factor - Peak factor - study of R-L - R-C -RLC series circuit - R-L-C parallel circuit - phasor representation in polar and rectangular form - concept of impedance - admittance - active - reactive - apparent and complex power - power factor, Resonance in R-L-C circuits - 3 phase balanced AC Circuits

Mesh



$$\begin{bmatrix} 8 & -3 & 0 \\ -3 & 9 & -2 \\ 0 & -2 & 10 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} 15 \\ 15 \\ -35 \end{bmatrix}$$

Inspection method

$$V_1 = +20 - 5 = 15V$$

$$V_2 = +5 + 5 + 5 = 15V$$

$$V_3 = -30 - 5 = -35V$$

Current supplied by battery  $B_1 = I_1 = \mathbf{2.56\text{ A}}$

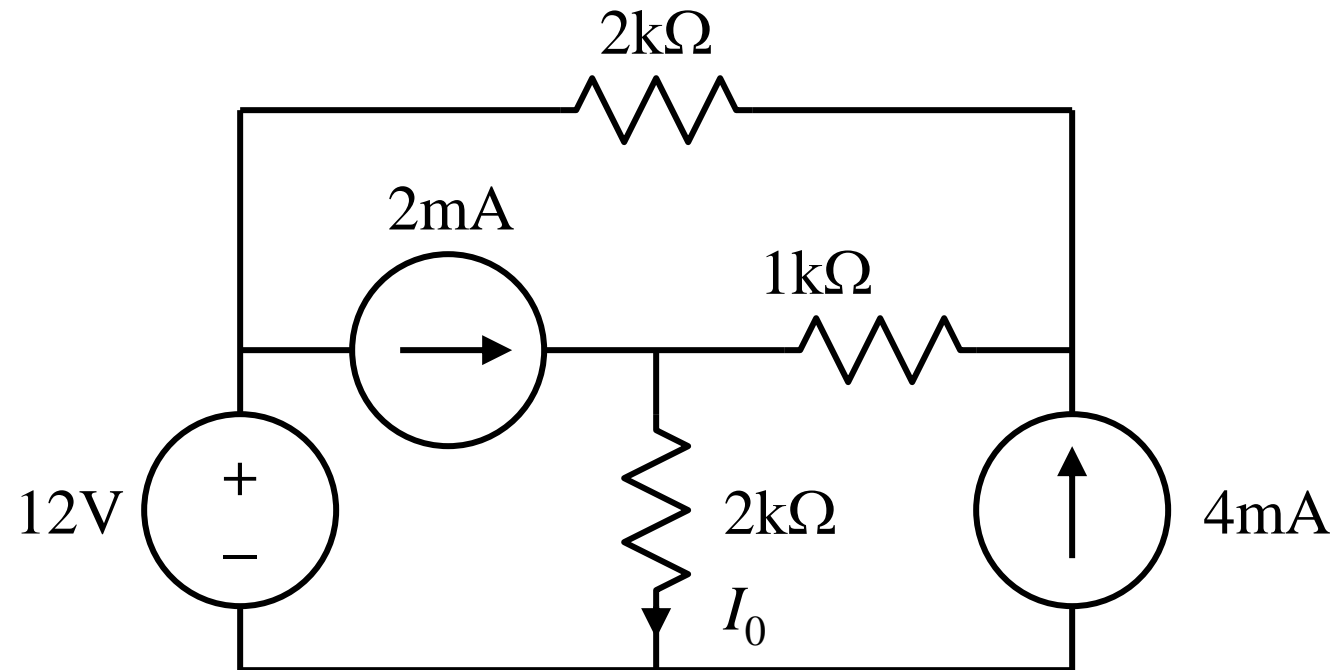
Current supplied to battery  $B_2 = I_1 - I_2 = 2.56 - 1.82 = \mathbf{0.74\text{ A}}$

Current supplied by battery  $B_3 = I_2 + I_3 = 1.82 + 3.13 = \mathbf{4.95\text{ A}}$

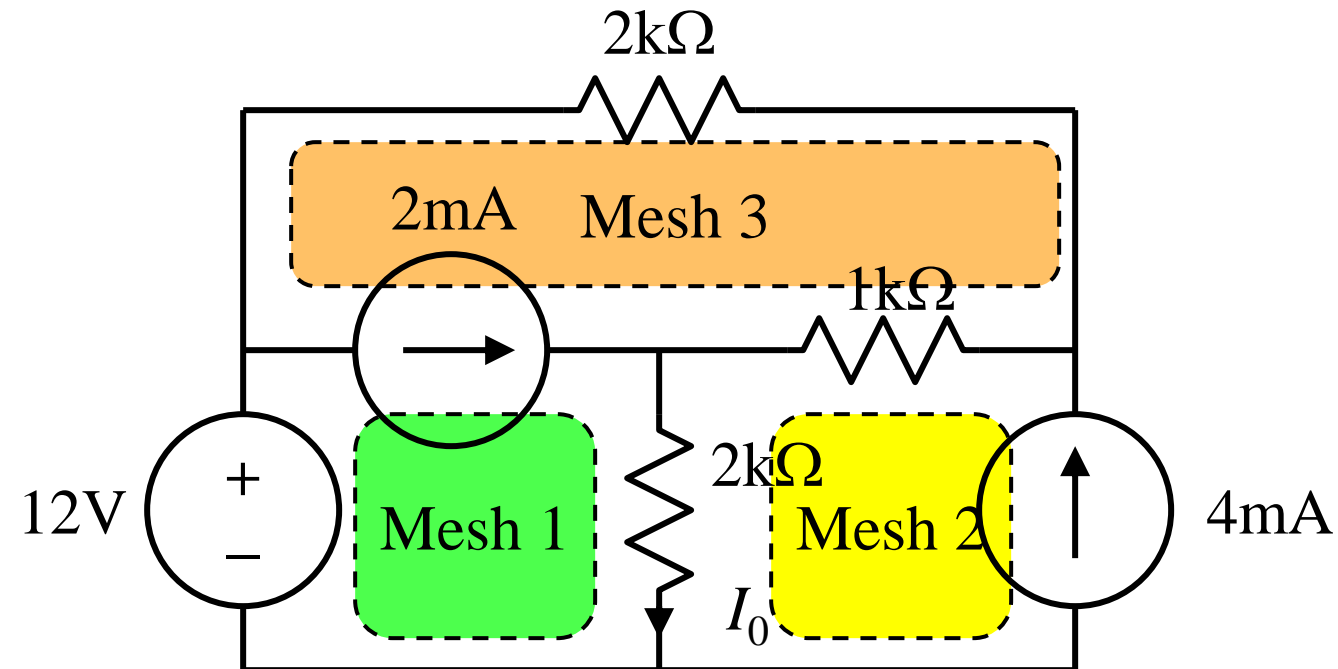
Current supplied by battery  $B_4 = I_2 = \mathbf{1.82\text{ A}}$

Current supplied by battery  $B_5 = I_3 = \mathbf{3.13\text{ A}}$

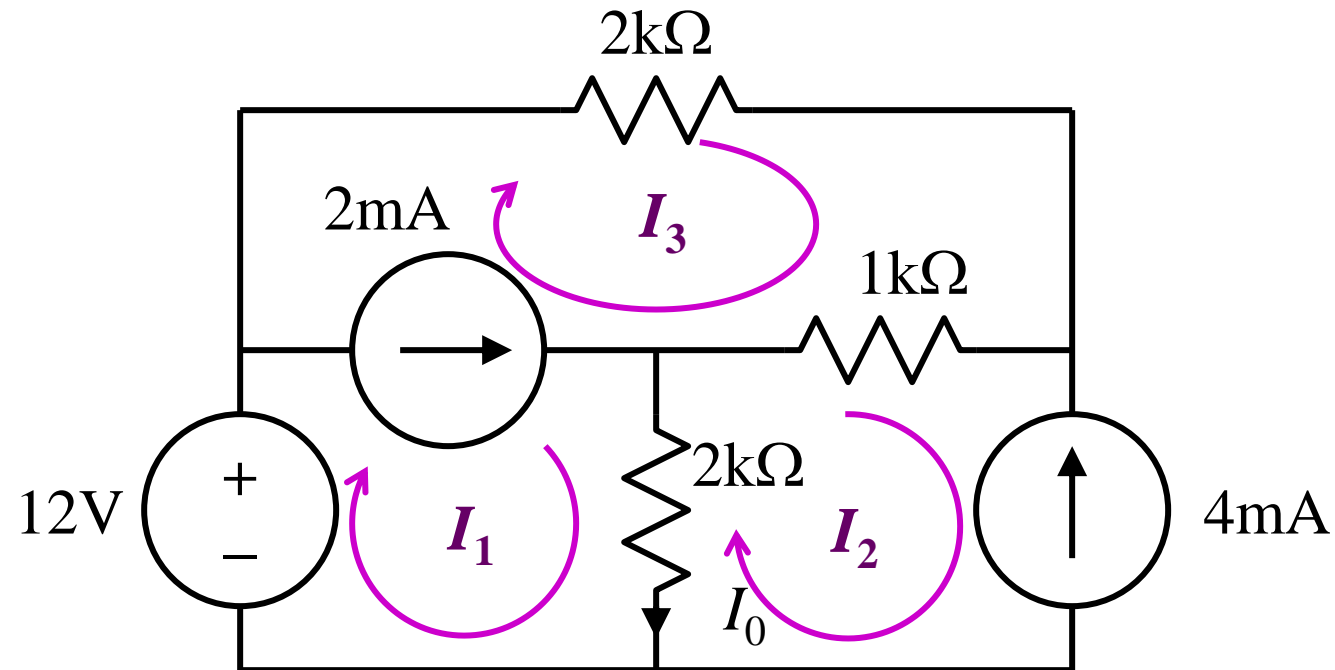
## Another Example



# 1. Identify Meshes



## 2. Assign Mesh Currents

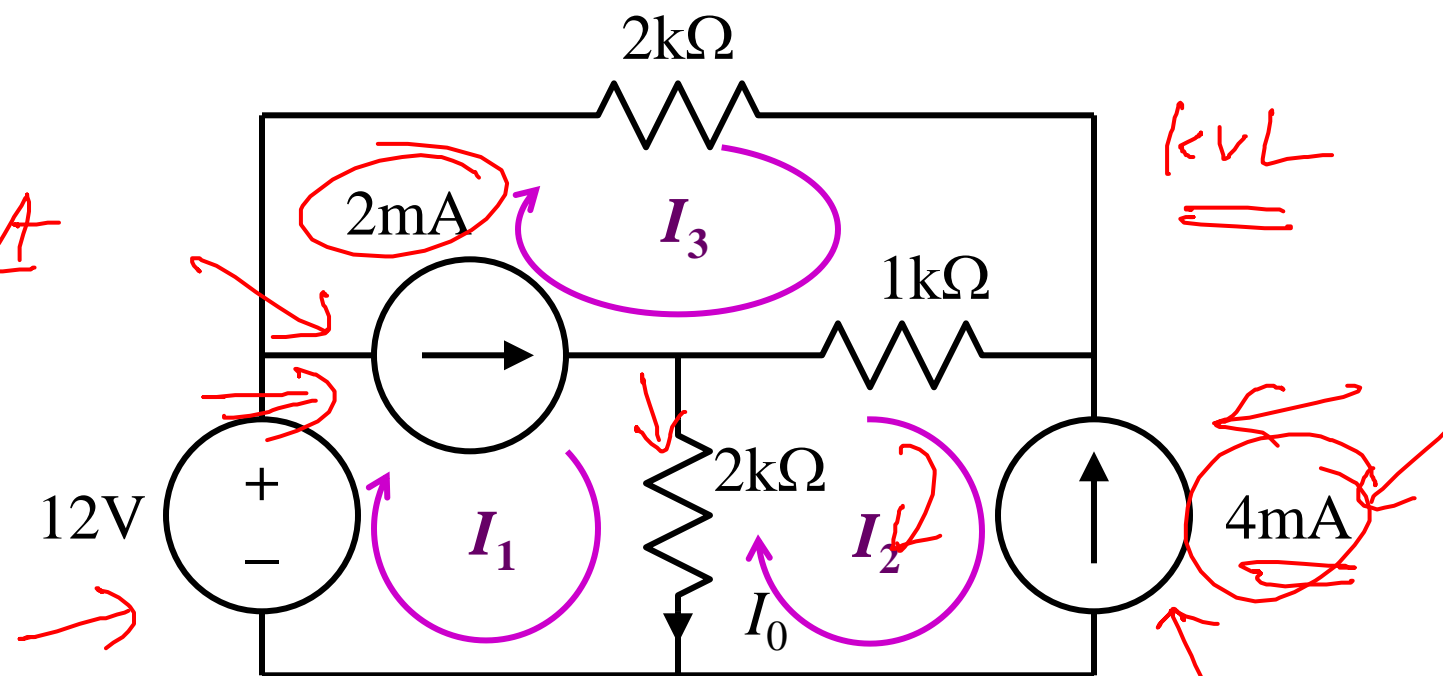


# Current Sources

- The current sources in this circuit will have whatever voltage is necessary to make the current correct
- We can't use KVL around any mesh because we don't know the voltage for the current sources

- What to do?

$I_1 =$   
 $I_2 = -4mA$   
 $I_3 =$   
 $2mA \rightarrow I_1 - I_3 = 2mA$





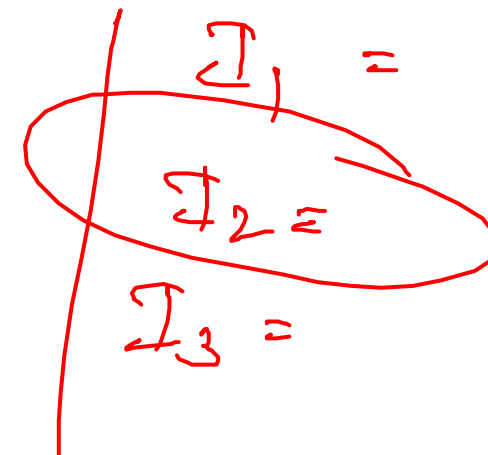
# Current Sources

- The 4mA current source sets  $I_2$ :

$$I_2 = -4 \text{ mA}$$

- The 2mA current source sets a *constraint* on  $I_1$  and  $I_3$ :

$$I_1 - I_3 = 2 \text{ mA} \quad \text{--- (1)}$$



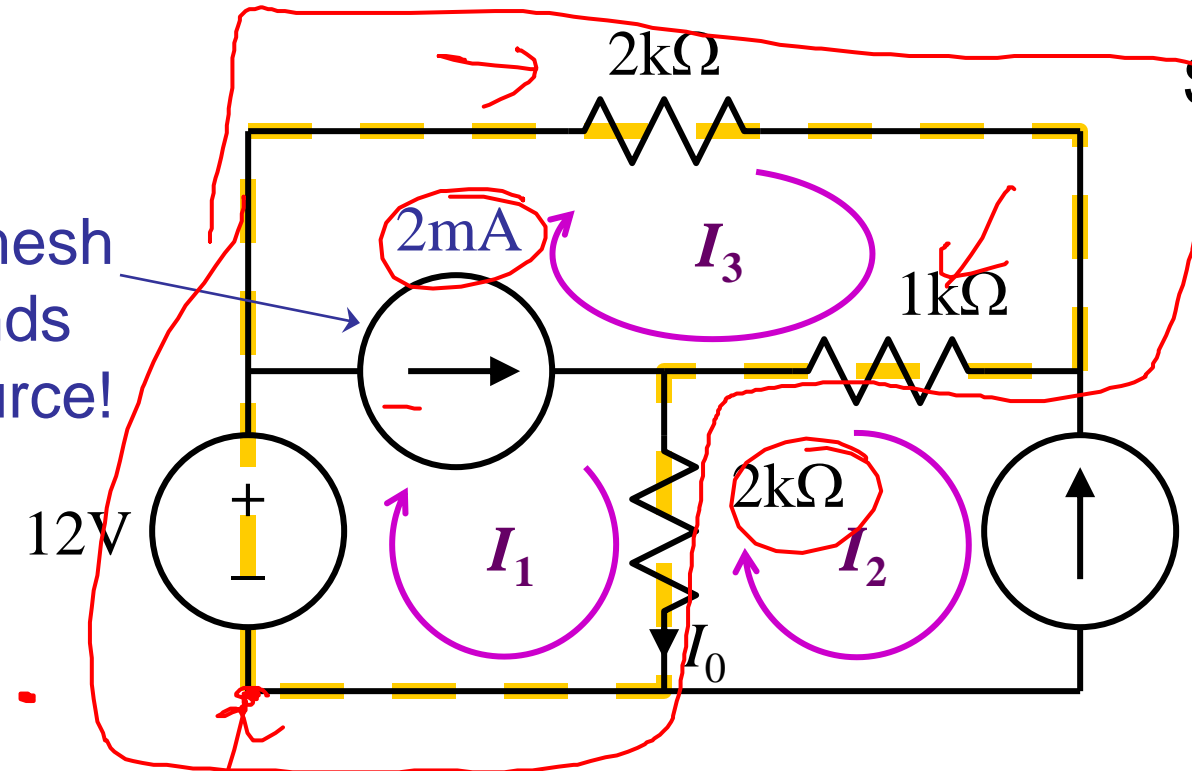
$I_1 =$   
 $I_2 =$   
 $I_3 =$

- We have two equations and three unknowns. Where is the third equation?

# The Supermesh!

The Supermesh surrounds this source!

The Supermesh does not include this source!



4mA → mesh 2

KVL  $+12 - 2k(I_3) - 1k(I_3 - I_2) - 2k(I_1 - I_2) = 0 \leftarrow$

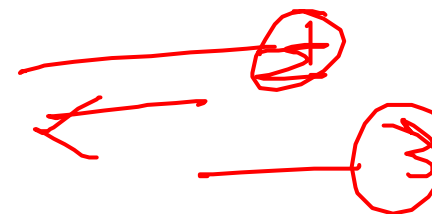
### 3. KVL Around the Supermesh

$$-12V + I_3 2k\Omega + (I_3 - I_2)1k\Omega + (I_1 - I_2)2k\Omega = 0$$

$$I_3 2k\Omega + (I_3 - I_2)1k\Omega + (I_1 - I_2)2k\Omega = 12V$$


$$I_2 = -4mA \quad \text{--- (1)}$$

$$I_1 - I_3 = 2mA \quad \text{--- (2)}$$



# Matrix Notation

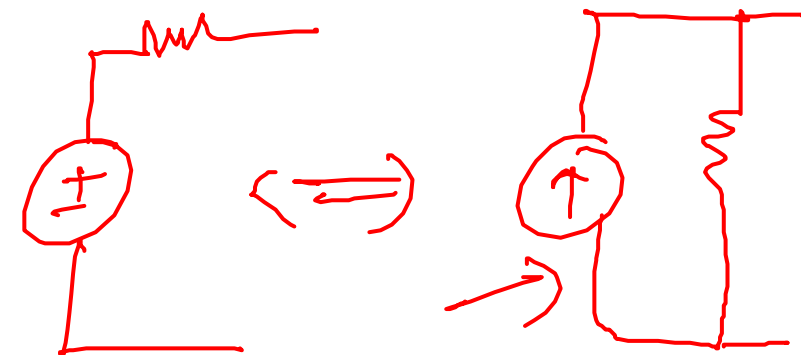
- The three equations can be combined into a single matrix/vector equation

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & -1 \\ 2\text{k}\Omega & -1\text{k}\Omega - 2\text{k}\Omega & 2\text{k}\Omega + 1\text{k}\Omega \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} -4\text{mA} \\ 2\text{mA} \\ 12\text{V} \end{bmatrix}$$


# Solution

$$\begin{aligned} I_1 &= 1.2 \text{ mA} \\ I_2 &= -4 \text{ mA} \\ I_3 &= -0.8 \text{ mA} \end{aligned}$$

$$I_0 = I_1 - I_2 = 5.2 \text{ mA}$$



Mesh → KVL → ✓

Current Sources →

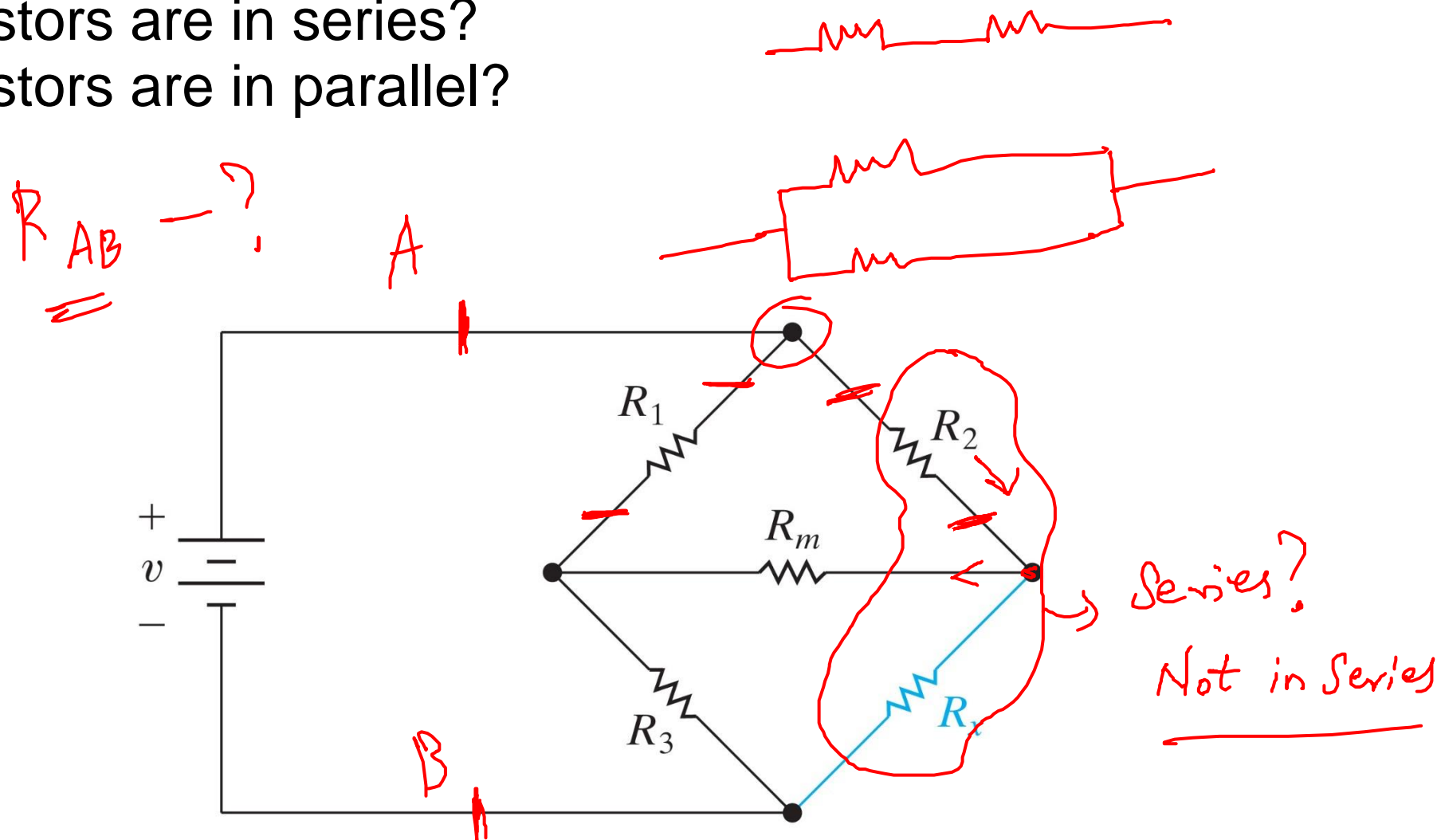
Source transformation ✓

Redaction →

Supermesh ↙

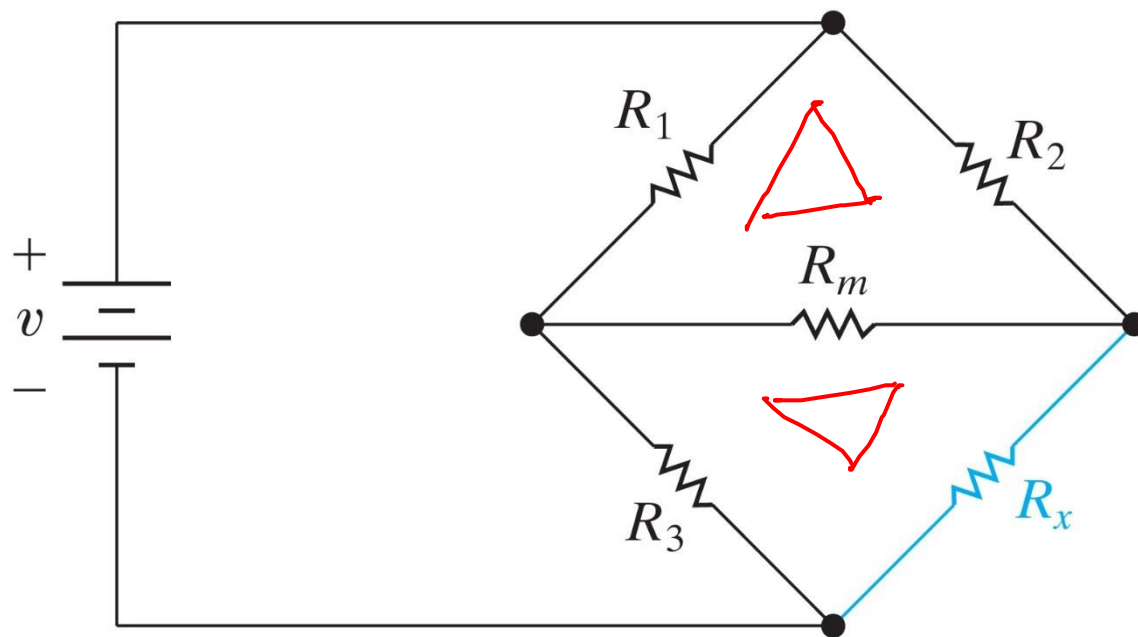
# Back to the Bridge

- Which resistors are in series?
- Which resistors are in parallel?



# Delta ( $\Delta$ ) Connection

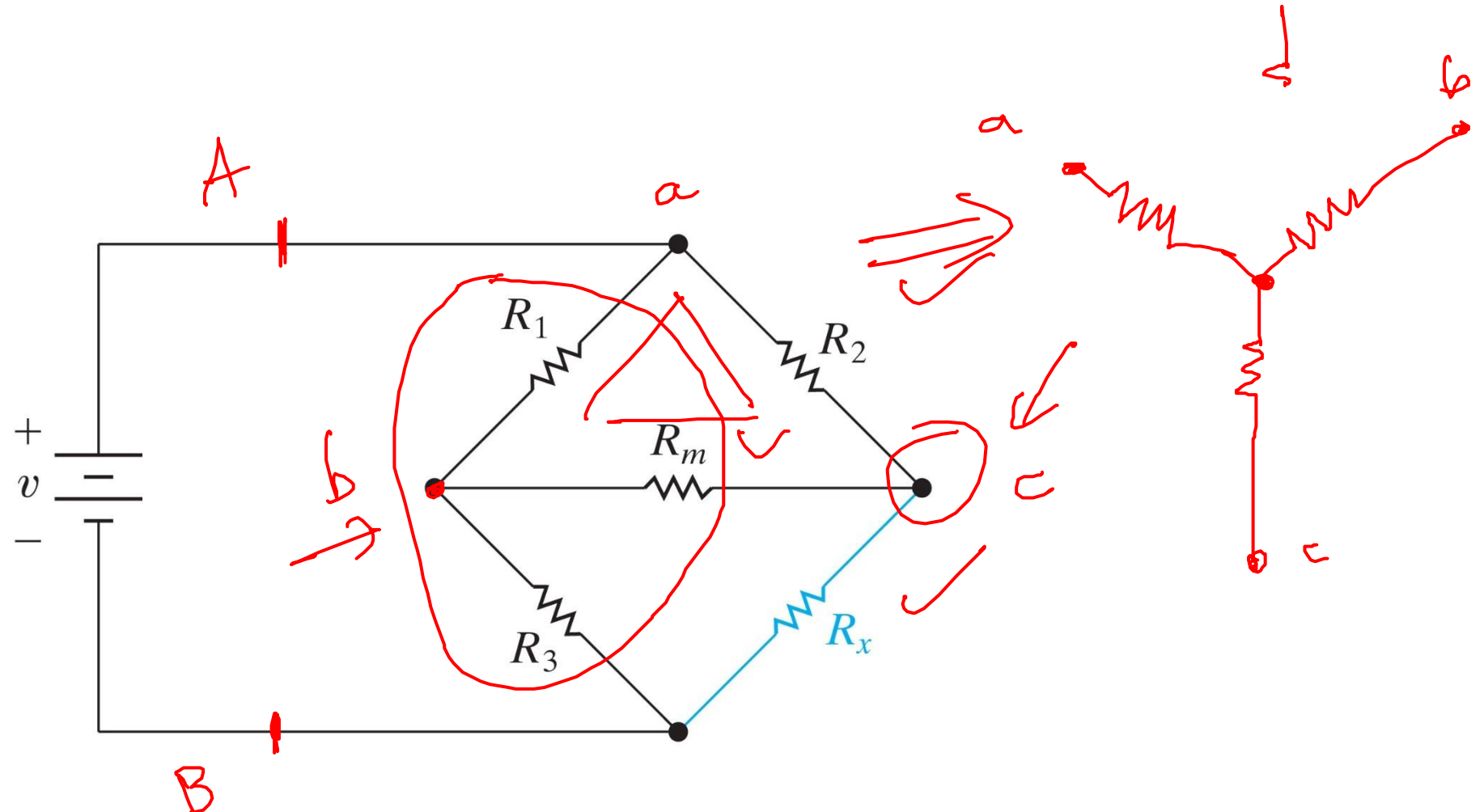
- Resistors  $R_1$ ,  $R_2$ , and  $R_m$  (or  $R_3$ ,  $R_m$ , and  $R_x$ ) are in a Delta ( $\Delta$ ), or pi ( $\pi$ ) connection.



*Star*

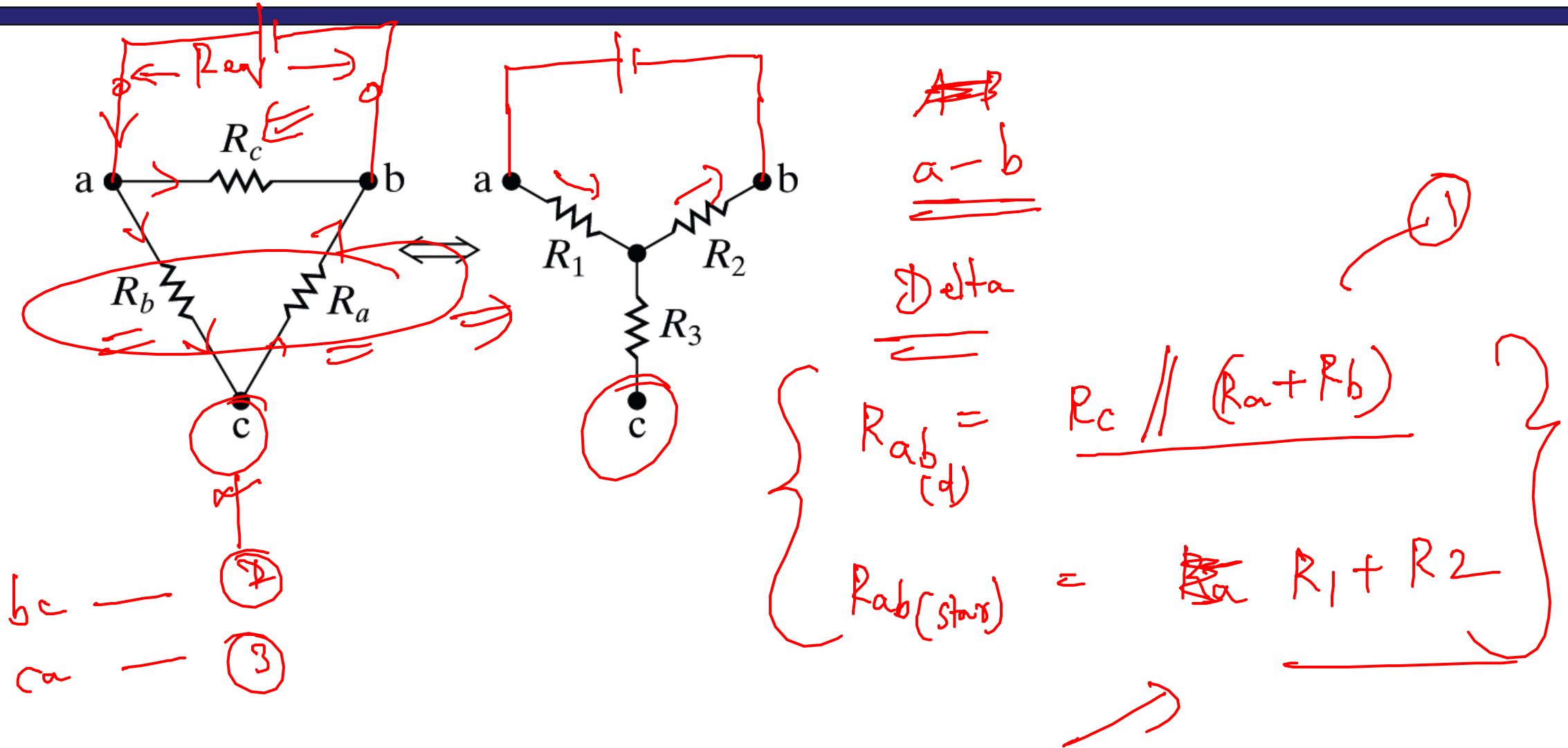
# Wye (Y) Connection

- Resistors  $R_1$ ,  $R_m$ , and  $R_3$  (or  $R_2$ ,  $R_m$ , and  $R_x$ ) are in a wye (Y), or tee (T) connection.



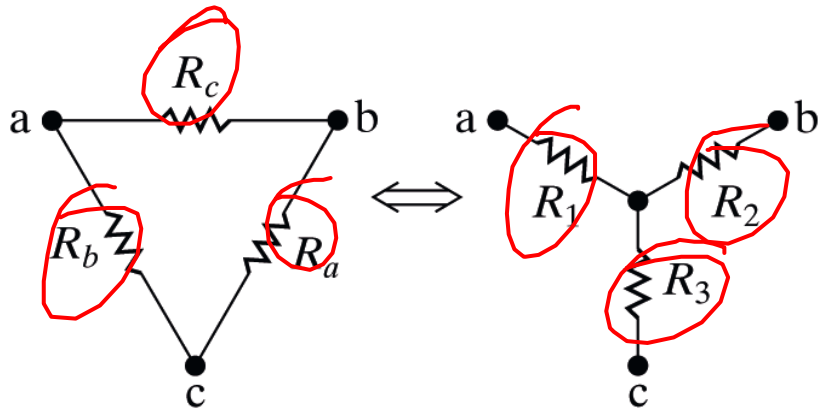


# Δ – Y Conversion



# $\Delta - Y$ Conversion (continued)

- The resistance between the terminal pairs must be the same for both circuits



*delta*

*$R_c \parallel R_a + R_b$*

$$R_{ab} = \frac{R_c (R_a + R_b)}{R_a + R_b + R_c} = R_1 + R_2 \quad \text{--- (1)}$$

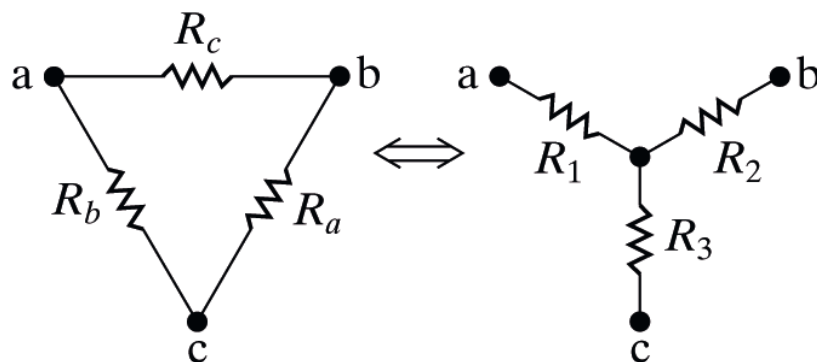
$$R_{bc} = \frac{R_a (R_b + R_c)}{R_a + R_b + R_c} = R_2 + R_3 \quad \text{--- (2)}$$

$$R_{ca} = \frac{R_b (R_c + R_a)}{R_a + R_b + R_c} = R_1 + R_3 \quad \text{--- (3)}$$

# Δ – Y Conversion (continued)

- After some algebraic manipulation

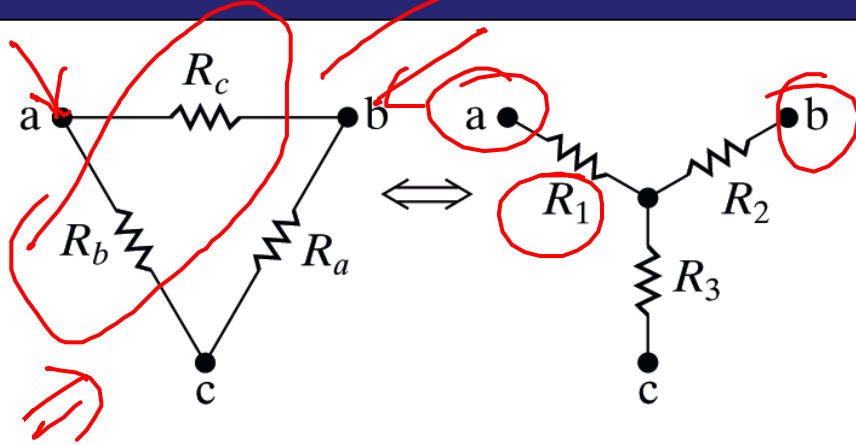
Delta – Star Conversion



$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c}$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$



$$R_a = 1\Omega$$

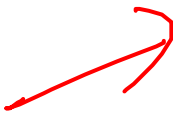
$$R_b = 1\Omega$$

$$R_c = 1\Omega$$

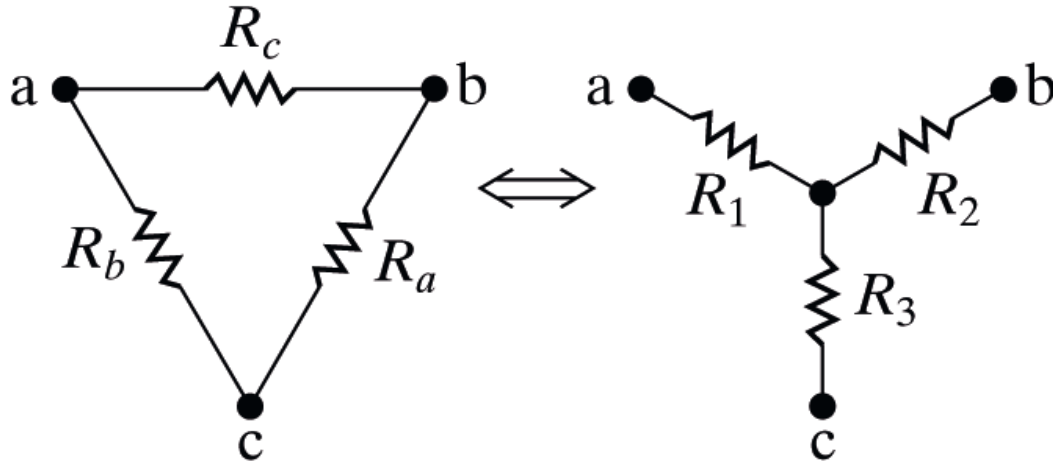
$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c} = \frac{1}{3} \Omega$$

$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c} = \frac{1}{3} \Omega$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c} = \frac{1}{3} \Omega$$

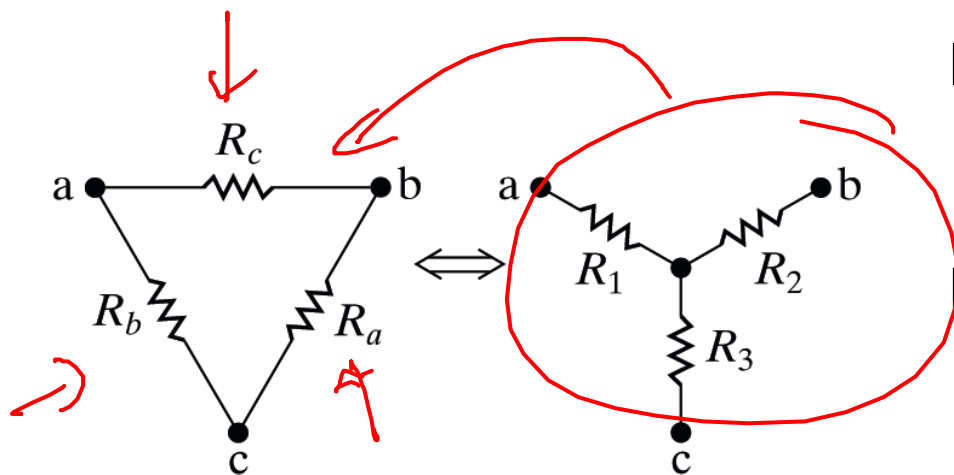


# Y – $\Delta$ Conversion



# Y – Δ Conversion (continued)

- The resistance between the terminal pairs must be the same for both circuits



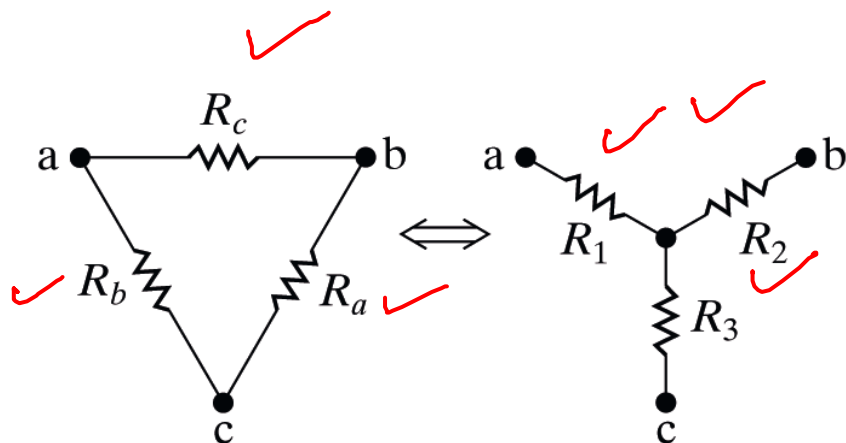
$$R_{ab} = \frac{R_c(R_a + R_b)}{R_a + R_b + R_c} = R_1 + R_2$$

$$R_{bc} = \frac{R_a(R_b + R_c)}{R_a + R_b + R_c} = R_2 + R_3$$

$$R_{ca} = \frac{R_b(R_c + R_a)}{R_a + R_b + R_c} = R_1 + R_3$$

# Y – Δ Conversion (continued)

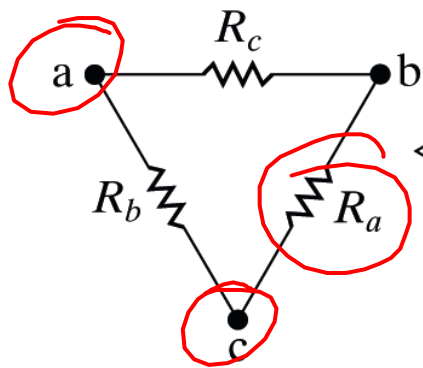
- After some algebraic manipulation



$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

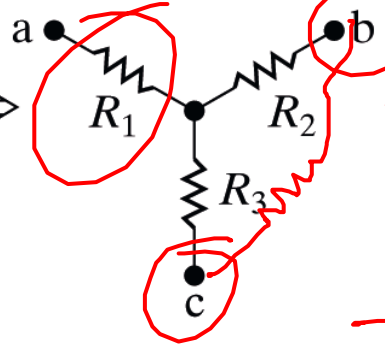
$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$



$$R_1 = 1\Omega$$

$$R_2 = 2\Omega$$

$$R_3 = 3\Omega$$



$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$= \frac{11}{1} \Omega$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$= \frac{11}{2} \Omega$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

$$= \frac{11}{3} \Omega$$



# Summary

