

Supervised Learning: Classification

Noah Simon & Ali Shojaie

July 17-19, 2019
Summer Institute for Statistics of Big Data
University of Washington

Classification

- ▶ Regression involves predicting a continuous-valued response.

Classification

- ▶ Regression involves predicting a continuous-valued response.
- ▶ Classification involves predicting a categorical / qualitative response:
 - ▶ Cancer versus Normal
 - ▶ Tumor Type 1 versus Tumor Type 2 versus Tumor Type 3

Classification

- ▶ Regression involves predicting a continuous-valued response.
- ▶ Classification involves predicting a categorical / qualitative response:
 - ▶ Cancer versus Normal
 - ▶ Tumor Type 1 versus Tumor Type 2 versus Tumor Type 3
- ▶ Classification problems tend to occur even more frequently than regression problems in biomedical applications.

Classification

- ▶ Regression involves predicting a continuous-valued response.
- ▶ Classification involves predicting a categorical / qualitative response:
 - ▶ Cancer versus Normal
 - ▶ Tumor Type 1 versus Tumor Type 2 versus Tumor Type 3
- ▶ Classification problems tend to occur even more frequently than regression problems in biomedical applications.
- ▶ Just like regression,
 - ▶ Classification cannot be blindly performed in high-dimensions **because you will get zero training error but awful test error**;
 - ▶ Properly estimating the test error is crucial; and
 - ▶ There are a few tricks to extend classical classification approaches to high-dimensions, which we have already seen in the regression context!

Classification

- ▶ Categorical / qualitative variables take values in an unordered set: e.g.
 $\text{eye color} \in \{\text{brown}, \text{blue}, \text{green}\}$
 $\text{email} \in \{\text{spam}, \text{not spam}\}.$
- ▶ We want to build a function that takes as input the feature vector X and predicts the value for Y .
- ▶ Often we are more interested in estimating the **probability** that X belongs to a given category.
- ▶ For example: we might want to know the probability that someone will develop diabetes, rather than to predict whether or not they will develop diabetes.

Can't We Just Use Linear Regression?

- Classify an emergency room patient on the basis of her symptoms to one of three conditions:

$$Y = \begin{cases} 1 & \text{if stroke;} \\ 2 & \text{if drug overdose;} \\ 3 & \text{if epileptic seizure.} \end{cases}$$

- If we apply linear regression, then the results will depend on the choice of coding . . . and the coding implies an ordering among the medical conditions.
- A classification approach is more appropriate.

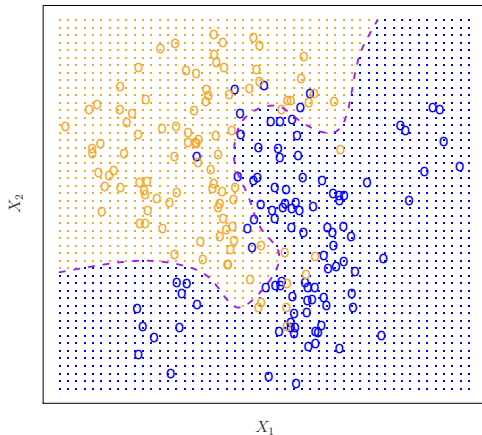
Classification

- ▶ There are many approaches out there for performing classification.
- ▶ We will discuss three: *k*-nearest neighbors, logistic regression, and support vector machines.

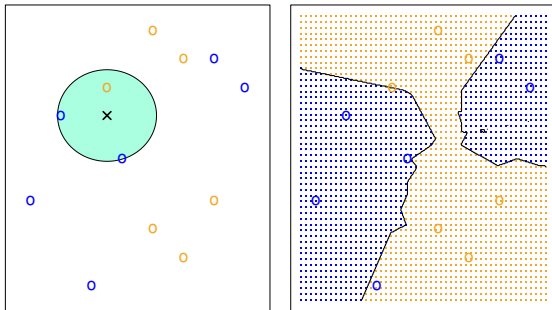
K -Nearest Neighbors

- ▶ Can I take a totally non-parametric (model-free) approach to classification?
- ▶ **K -nearest neighbors:**
 1. Identify the K observations whose X values are closest to the observation at which we want to make a prediction.
 2. Classify the observation of interest to the most frequent class label of those K nearest neighbors.

K-Nearest Neighbors

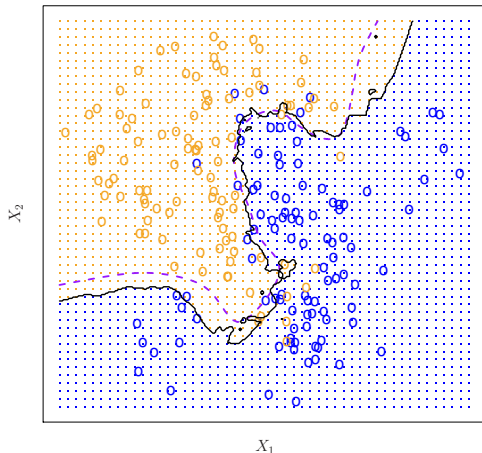


K-Nearest Neighbors



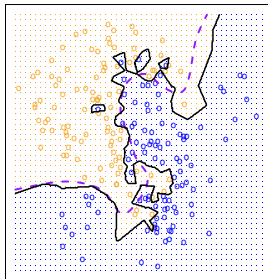
K-Nearest Neighbors

KNN: K=10

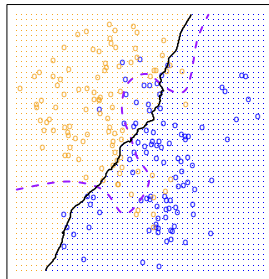


K-Nearest Neighbors

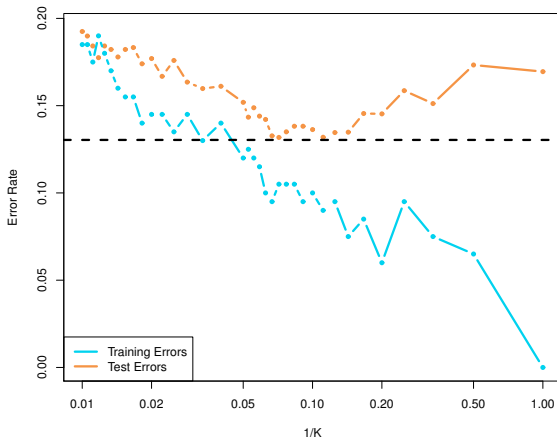
KNN: K=1



KNN: K=100



K-Nearest Neighbors



K-Nearest Neighbors

- ▶ Simple, intuitive, model-free.
- ▶ Good option when p is very small.
- ▶ Curse of dimensionality: when p is large, no neighbors are “near”. All observations are close to the boundary.
- ▶ **Do not use in high dimensions!**

Logistic Regression

- ▶ Logistic regression is the straightforward extension of linear regression to the classification setting.

Logistic Regression

- ▶ Logistic regression is the straightforward extension of linear regression to the classification setting.
- ▶ For simplicity, suppose $y \in \{0, 1\}$: a two-class classification problem.

Logistic Regression

- ▶ Logistic regression is the straightforward extension of linear regression to the classification setting.
- ▶ For simplicity, suppose $y \in \{0, 1\}$: a two-class classification problem.
- ▶ The simple linear model $y = X\beta + \epsilon$ doesn't make sense for classification.

Logistic Regression

- ▶ Let $p(X) = \Pr(Y = 1|X)$.
- ▶ Suppose we want to use **biomarker level** to predict **probability of cancer**.
- ▶ Logistic regression uses the form

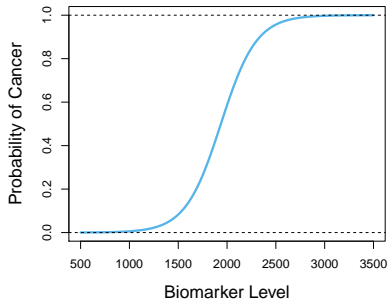
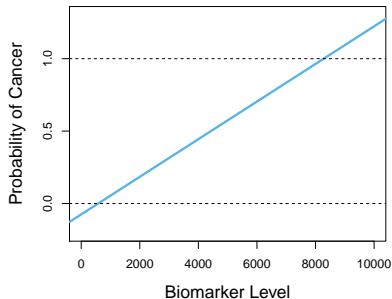
$$p(X) = \frac{e^{\beta_0 + \beta_1 X}}{1 + e^{\beta_0 + \beta_1 X}}.$$

- ▶ $p(X)$ will lie between 0 and 1.
- ▶ Furthermore,

$$\log \left(\frac{p(X)}{1 - p(X)} \right) = \beta_0 + \beta_1 X.$$

- ▶ This function of $p(X)$ is called the **logit** or **log odds**.

Why Not Linear Regression?



- ▶ Left: linear regression.
- ▶ Right: logistic regression.

Multiple Logistic Regression

- Just like before:

$$p(X) = \frac{e^{\beta_0 + \beta_1 X_1 + \dots + \beta_p X_p}}{1 + e^{\beta_0 + \beta_1 X_1 + \dots + \beta_p X_p}}.$$

- And just like before:

$$\log \left(\frac{p(X)}{1 - p(X)} \right) = \beta_0 + \beta_1 X_1 + \dots + \beta_p X_p.$$

Example in R

```
xtr <- matrix(rnorm(1000*20),ncol=20)
beta <- c(rep(1,10),rep(0,10))
ytr <- 1*((xtr%*%beta + .2*rnorm(1000)) >= 0)
mod <- glm(ytr~xtr,family="binomial")
print(summary(mod))
```

Five Ways to Extend Logistic to High Dimensions

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection
2. Forward Stepwise Logistic Regression

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection
2. Forward Stepwise Logistic Regression
3. Ridge Logistic Regression

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection
2. Forward Stepwise Logistic Regression
3. Ridge Logistic Regression
4. Lasso Logistic Regression

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection
2. Forward Stepwise Logistic Regression
3. Ridge Logistic Regression
4. Lasso Logistic Regression
5. Principal Components Logistic Regression

Five Ways to Extend Logistic to High Dimensions

1. Variable Pre-Selection
2. Forward Stepwise Logistic Regression
3. Ridge Logistic Regression
4. Lasso Logistic Regression
5. Principal Components Logistic Regression

How to decide which approach is best, and which tuning parameter value to use for each approach? **Cross-validation** or **validation set approach**.

What is an appropriate validation measure?

For classification without a probability or score:

- Misclassification rate:

$$\frac{\text{\#test samples misclassified}}{\text{total \# of test samples}}$$

What is an appropriate validation measure?

For probabilistic classification

- ▶ Can still use misclassification rate.
- ▶ Like in continuous regression could use SSE:

$$\sum_{i \in \text{test}} (y_i - \hat{p}_i)^2$$

- ▶ Often preferable to use “predictive [log]likelihood”:

$$-\log \left[\prod_{i \in \text{test}} \hat{p}_i^{y_i} (1 - \hat{p}_i)^{1-y_i} \right]$$

- ▶ Can also use ROC-curve-based metric (eg. AUC)

Remember though; all of these must be conducted on a **separate validation set**.

Example in R: Lasso Logistic Regression

```
xtr <- matrix(rnorm(1000*20),ncol=20)
beta <- c(rep(1,5),rep(0,15))
ytr <- 1*((xtr%*%beta + .5*rnorm(1000)) >= 0)
cv.out <- cv.glmnet(xtr, ytr, family="binomial", alpha=1)
plot(cv.out)
```


Let's Try It Out in R!

Chapter 4 R Lab

Skip part on LDA & QDA

www.statlearning.com

Bayes-based classifiers

Suppose rather than knowing $P(y = j|x)$...

we have information on $f_j(x) = P(x|y = j)$, the feature distribution within each class

How do we use this to make predictions?

Bayes-based classifiers

Suppose rather than knowing $P(y = j|x)$...

we have information on $f_j(x) = P(x|y = j)$, the feature distribution within each class

How do we use this to make predictions?

Using Bayes Theorem:

$$P(y = j|x) = \frac{f_j(x)\pi_j}{\sum_k f_k(x)\pi_k}$$

here $\pi_k = P(y = k)$ is the prior probability of class k .

Estimating the Rule

To apply Bayes Theorem

$$P(y = j|x) = \frac{f_j(x)\pi_j}{\sum_k f_k(x)\pi_k}$$

we need

- ▶ $f_k(x)$ for $k = 1, \dots, K$
- ▶ π_k for $k = 1, \dots, K$

Estimating the π_k

π_k is generally simple to estimate

- ▶ If your data are a random sample; then can use the sample proportion

$$\hat{\pi}_k = \frac{\# \{y_i = k\}}{n}$$

- ▶ Otherwise can use outside information (eg. historical data)

If you change population proportions; it is easy to adjust the rule.

Estimating the $f_k(x)$

Estimate of $f_k(x) = P(x|y = k)$ is more difficult.

This is a **density estimation** problem.

The tools we discuss for this break down into 3 general categories

- ▶ flexible, non-parametric estimates
- ▶ parametric estimates
- ▶ shrunken parametric estimates

The above are ordered (more-or-less) by where they fall on bias/variance spectrum:

more flexible \rightarrow less bias/more variance

Parametric $f_k(x)$ Estimate

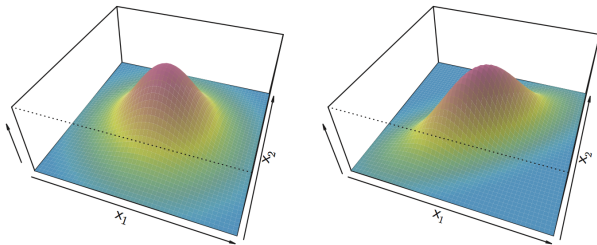
Most well known estimator of this type is **Linear/Quadratic Discriminant Analysis**:

Here we assume that $f_k(x)$ is **Gaussian density**, $N(\mu_k, \Sigma_k)$

Parametric $f_k(x)$ Estimate

Most well known estimator of this type is **Linear/Quadratic Discriminant Analysis**:

Here we assume that $f_k(x)$ is **Gaussian density**, $N(\mu_k, \Sigma_k)$



Discriminant Analysis

There are three main types of unpenalized discriminant analysis:

- ▶ Quadratic (QDA)
- ▶ Linear (LDA)
- ▶ Diagonal (DDA)

These make different assumptions on the covariance structure:

- ▶ QDA makes no assumptions
- ▶ LDA assumes a pooled variance $\Sigma = \Sigma_k$ for all k
- ▶ DDA assumes a pooled variance; and further that Σ is diagonal (i.e. **no correlation among covariates!**)

Discriminant Analysis

Why would we choose DDA over QDA?

Remember, *flexibility* comes at a price!

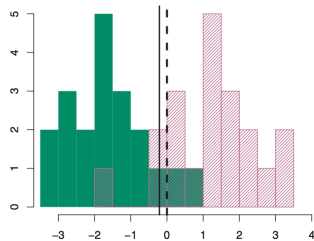
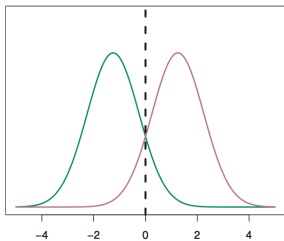
QDA will have the least bias; but has many more parameters to estimate

Often good estimates of the correlation don't improve classifications much

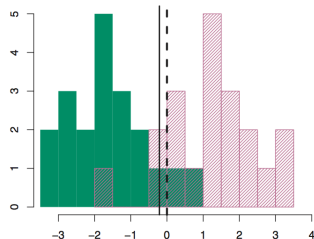
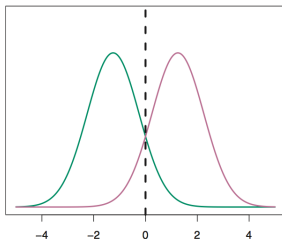
DDA takes into account the scale of each feature, but trades a bit of bias for potentially a large reduction in variance

LDA for $p = 1$

LDA for $p = 1$



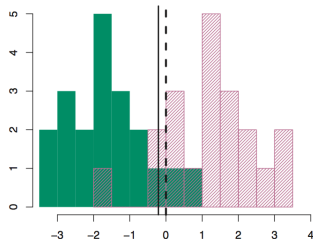
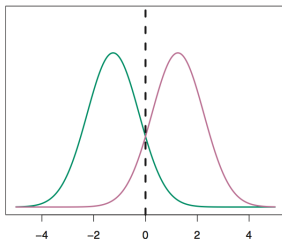
LDA for $p = 1$



- To make this work, we need to estimate the parameters. The ML estimates are given by $\hat{\pi}_k = n_k/n$ and

$$\hat{\mu}_k = \frac{1}{n_k} \sum_{i:y_i=k} x_i \quad \hat{\sigma}^2 = \frac{1}{n-K} \sum_{k=1}^K \sum_{i:y_i=k} (x_i - \hat{\mu}_k)^2$$

LDA for $p = 1$



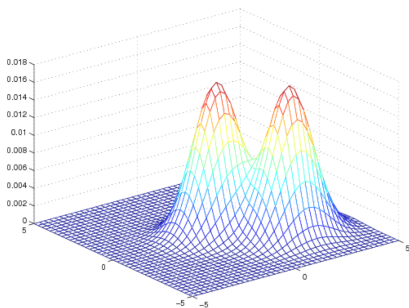
- To make this work, we need to estimate the parameters. The ML estimates are given by $\hat{\pi}_k = n_k/n$ and

$$\hat{\mu}_k = \frac{1}{n_k} \sum_{i:y_i=k} x_i \quad \hat{\sigma}^2 = \frac{1}{n-K} \sum_{k=1}^K \sum_{i:y_i=k} (x_i - \hat{\mu}_k)^2$$

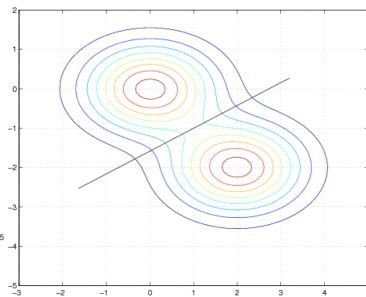
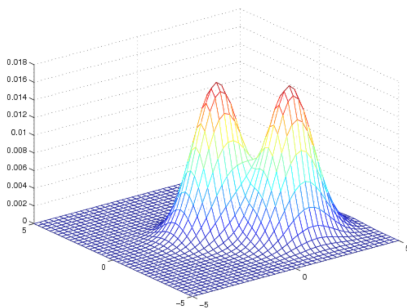
- The picture is very similar if $K > 2$...or if $p > 1$

LDA for $p > 1$

LDA for $p > 1$

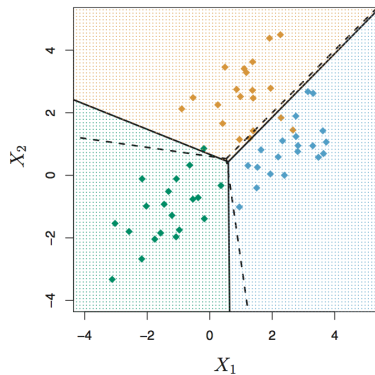
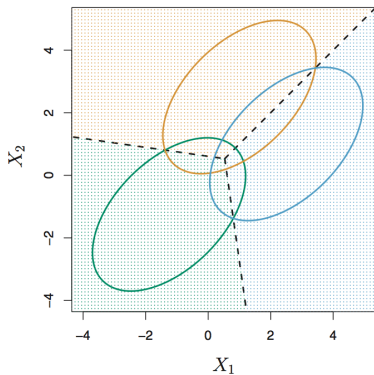


LDA for $p > 1$



LDA for $p > 1$

LDA for $p > 1$

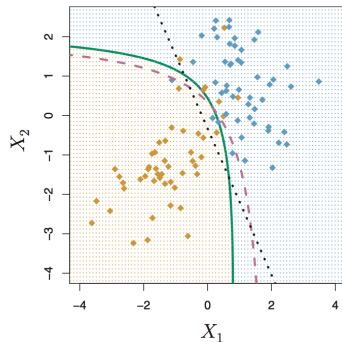
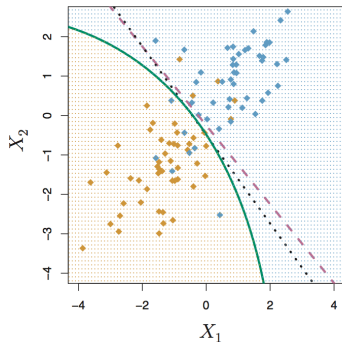


QDA vs LDA

The level-curves for each class look identical with LDA;

QDA allows for different classes to have differently shaped ellipsoids...

Results in non-linear decision boundaries (quadratic in fact)



DDA

For DDA...

- ▶ level curves are spheres (not ellipsoids).
- ▶ decision boundaries are still linear
- ▶ sometimes called *naive bayes* (that doesn't mean it's bad though!)
- ▶ with $\pi_k = \frac{1}{K}$ for all k , and equal variances (ie. $\Sigma = \sigma I$); this is just the *nearest centroid* classifier

-DA vs logistic regression

Discriminant Analysis model can actually be rewritten as multinomial logistic models:

Beginning with

$$P(y = j|x) = \frac{f_j(x)\pi_j}{\sum_k f_k(x)\pi_k}$$

and

$$f_k(x) \propto \exp \left[-\frac{1}{2} (x - \mu_k)^\top \Sigma_k^{-1} (x - \mu_k) \right]$$

substituting and simplifying we get

$$P(y = j|x) = \frac{e^{\eta_j}}{\sum_k e^{\eta_k}}$$

-DA vs logistic regression

$$P(y = j|x) = \frac{e^{\eta_j}}{\sum_k e^{\eta_k}}$$

where

$$\eta_k = \beta_0 + x^\top \beta + x^\top \Sigma_k^{-1} x$$

This is just a multinomial logistic model with quadratic terms and interactions.

In particular for LDA (where $\Sigma_k = \Sigma$ is pooled) we have cancellation and get

$$\eta_k = \beta_0 + x^\top \beta$$

Simply a linear logistic model.

Shrunken Parametric Estimates

Sometimes the optimal bias/variance tradeoff is between two parametric classes.

For example: We may not have the data to estimate completely different covariance matrices for each class (i.e. QDA); but we may not want to use identical covariance matrices.

In this case we can take a weighted combination of our estimates. This is called **regularized discriminant analysis**.

This is a type of *shrunken parametric estimator*.

Regularized Discriminant Analysis

For shrinking between QDA/LDA we use:

$$\hat{\Sigma}_k^{RDA} = \lambda \hat{\Sigma}_k^{LDA} + (1 - \lambda) \hat{\Sigma}_k^{QDA}$$

For shrinking between LDA and Naive Bayes we use

$$\hat{\Sigma}^{RDA} = \lambda \hat{\Sigma}^{LDA} + (1 - \lambda) \hat{\Sigma}^{NB}$$

λ is a tuning parameter, and is generally selected via CV

DA in High Dimensions

All of the Discriminant Analysis techniques discussed so far use **all** the features.

For high dimensional problems this will lead to over-fitting

One popular solution is to shrink each class-mean estimate $\hat{\mu}_k$ towards the overall mean $\hat{\mu}$ using element-wise soft-thresholding

This method is called **Nearest Shrunken Centroids** (though it should probably more appropriately be “nearest shrunken DDA”)

Nearest Shrunk Centroids (PAM)

Steps to the method:

1. Calculate our pooled, diagonal estimate of Σ ; let s_j be the sd. estimate of gene j
2. Calculate the within class mean $\hat{\mu}_{jk}$ for each gene j , class k , and overall mean $\hat{\mu}_{j\cdot}$.
3. Set $\hat{\mu}_{jk}^{PAM}$ to be the shrunk difference:

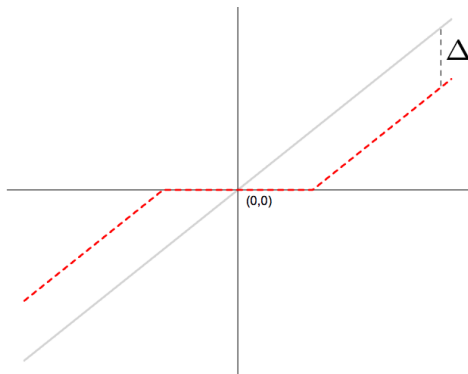
$$\hat{\mu}_{jk}^{PAM} = \hat{\mu}_{j\cdot} + s_j * SHRINK_{\Delta} \left(\frac{\hat{\mu}_{jk} - \hat{\mu}_{j\cdot}}{s_j} \right)$$

where $SHRINK_{\Delta}$ is the *Soft Thresholding Function*

Soft Thresholding

The soft thresholding shrinks its argument towards 0 — if it hits 0; then it stops!

Can be thought of as the continuous version of usual *thresholding*



Other Regularized DA Methods

- Recall that in PAM, $\hat{\mu}_{jk}$'s are **soft thresholded** towards the common mean $\hat{\mu}_j$.

Other Regularized DA Methods

- ▶ Recall that in PAM, $\hat{\mu}_{jk}$'s are **soft thresholded** towards the common mean $\hat{\mu}_j$.
- ▶ Alternatively, μ_{jk} 's can be **penalized**
 - ▶ **towards zero**, using a **lasso penalty**

$$\sum_j \sum_k |\mu_{jk}|,$$

Other Regularized DA Methods

- ▶ Recall that in PAM, $\hat{\mu}_{jk}$'s are **soft thresholded** towards the common mean $\hat{\mu}_j$.
- ▶ Alternatively, μ_{jk} 's can be **penalized**
 - ▶ **towards zero**, using a **lasso penalty**

$$\sum_j \sum_k |\mu_{jk}|,$$

- ▶ or **towards each other**, using a **fused lasso penalty**

$$\sum_j \sum_{k,k'} |\mu_{jk} - \mu_{jk'}|.$$

Both of these are implemented in R-package `penalizedLDA`.

Other Regularized DA Methods

- ▶ Recall that in PAM, $\hat{\mu}_{jk}$'s are **soft thresholded** towards the common mean $\hat{\mu}_j$.
- ▶ Alternatively, μ_{jk} 's can be **penalized**
 - ▶ **towards zero**, using a **lasso penalty**

$$\sum_j \sum_k |\mu_{jk}|,$$

- ▶ or **towards each other**, using a **fused lasso penalty**

$$\sum_j \sum_{k,k'} |\mu_{jk} - \mu_{jk'}|.$$

Both of these are implemented in R-package `penalizedLDA`.

- ▶ Another option, which is especially helpful when using QDA is to **penalize the covariance matrices** Σ_k (or their inverses).

Support Vector Machines

- Developed in around 1995.

Support Vector Machines

- ▶ Developed in around 1995.
- ▶ Touted as “overcoming the curse of dimensionality.”

Support Vector Machines

- ▶ Developed in around 1995.
- ▶ Touted as “overcoming the curse of dimensionality.”
- ▶ Does not automatically overcome the curse of dimensionality!!!

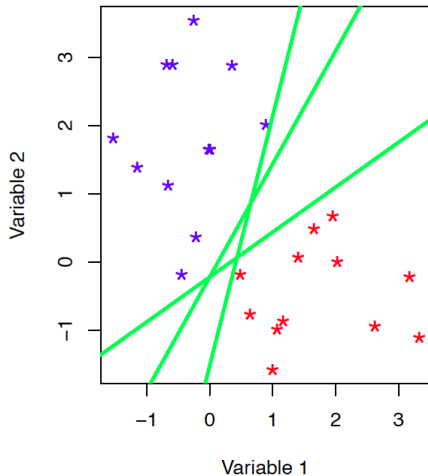
Support Vector Machines

- ▶ Developed in around 1995.
- ▶ Touted as “overcoming the curse of dimensionality.”
- ▶ Does not automatically overcome the curse of dimensionality!!!
- ▶ Fundamentally and numerically very similar to logistic regression.

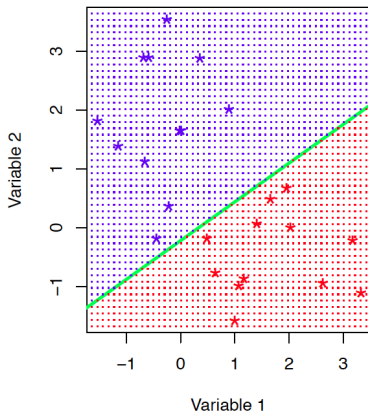
Support Vector Machines

- ▶ Developed in around 1995.
- ▶ Touted as “overcoming the curse of dimensionality.”
- ▶ Does not automatically overcome the curse of dimensionality!!!
- ▶ Fundamentally and numerically very similar to logistic regression.
- ▶ But, it is a nice idea.

Separating Hyperplane

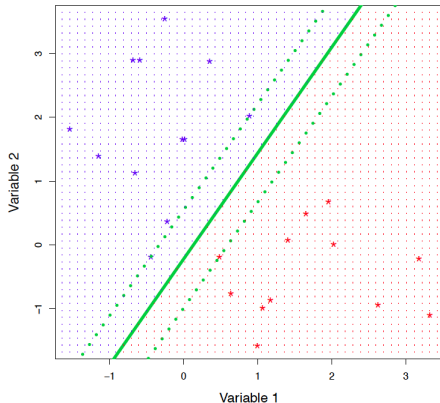


Classification Via a Separating Hyperplane



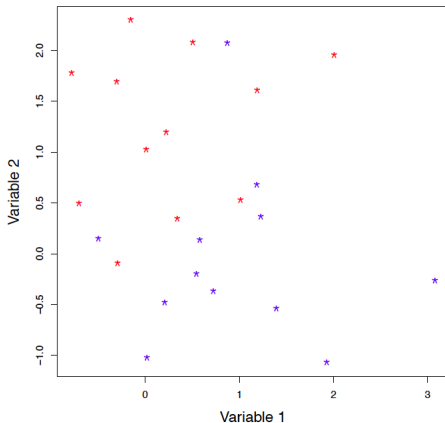
Blue class if $\beta_0 + \beta_1 X_1 + \beta_2 X_2 > c$; red class otherwise

Maximal Separating Hyperplane

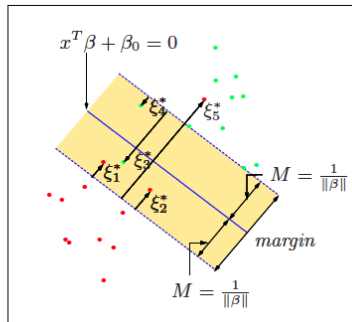
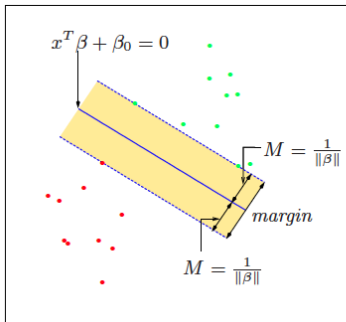


Note that only a few observations are **on the margin**: these are the **support vectors**.

What if There is No Separating Hyperplane?



Support Vector Classifier: Allow for Violations



Support Vector Machine

- ▶ The support vector machine is just like the support vector classifier, but it elegantly allows for non-linear expansions of the variables: “non-linear kernels”.

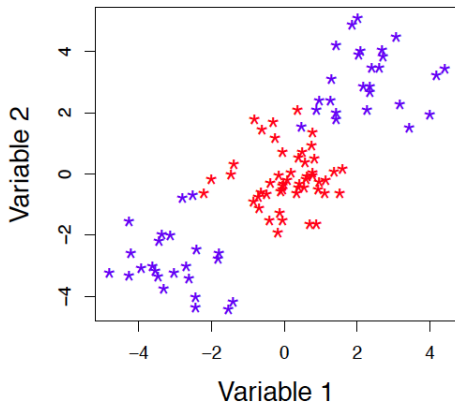
Support Vector Machine

- ▶ The support vector machine is just like the support vector classifier, but it elegantly allows for non-linear expansions of the variables: “non-linear kernels”.
- ▶ However, linear regression, logistic regression, and other classical statistical approaches can also be applied to non-linear functions of the variables.

Support Vector Machine

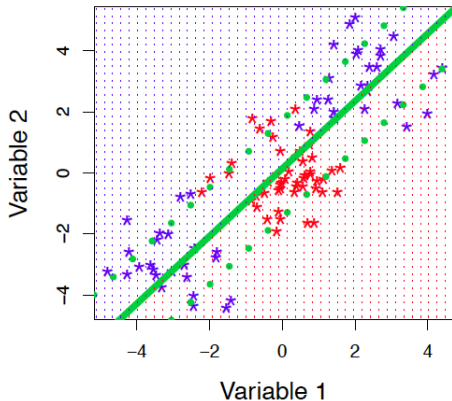
- ▶ The support vector machine is just like the support vector classifier, but it elegantly allows for non-linear expansions of the variables: “non-linear kernels”.
- ▶ However, linear regression, logistic regression, and other classical statistical approaches can also be applied to non-linear functions of the variables.
- ▶ For historical reasons, SVMs are more frequently used with non-linear expansions as compared to other statistical approaches.

Non-Linear Class Structure



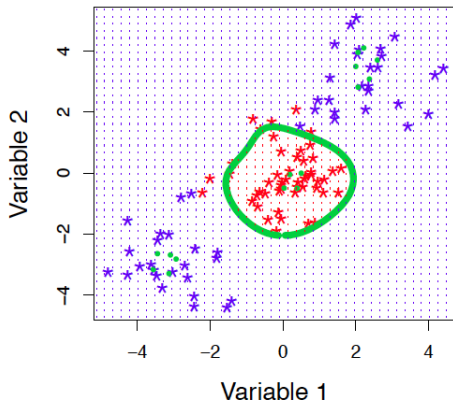
This will be hard for a linear classifier!

Try a Support Vector Classifier



Uh-oh!!

Support Vector Machine



Much Better.

Is A Non-Linear Kernel Better?

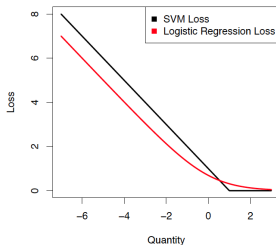
Is A Non-Linear Kernel Better?

- Yes, if the true decision boundary between the classes is non-linear, and you have enough observations (relative to the number of features) to accurately estimate the decision boundary.

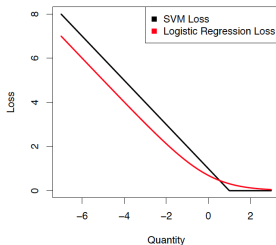
Is A Non-Linear Kernel Better?

- ▶ **Yes**, if the true decision boundary between the classes is non-linear, and you have enough observations (relative to the number of features) to accurately estimate the decision boundary.
- ▶ **No**, if you are in a very high-dimensional setting such that estimating a non-linear decision boundary is hopeless.

Support Vector Classifier Versus Logistic Regression

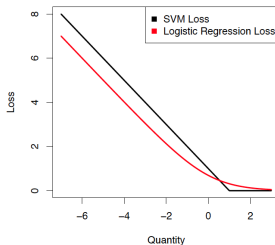


Support Vector Classifier Versus Logistic Regression



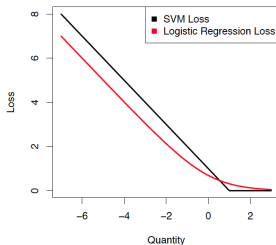
- Bottom Line: Support vector classifier and logistic regression aren't that different!

Support Vector Classifier Versus Logistic Regression



- ▶ Bottom Line: Support vector classifier and logistic regression aren't that different!
- ▶ Neither they nor any other approach can overcome the “curse of dimensionality”.

Support Vector Classifier Versus Logistic Regression



- ▶ Bottom Line: Support vector classifier and logistic regression aren't that different!
- ▶ Neither they nor any other approach can overcome the “curse of dimensionality”.
- ▶ SVM uses a non-linear kernel... but could do that with logistic or linear regression too!

In High Dimensions...

In High Dimensions...

- In SVMs, a tuning parameter controls the amount of flexibility of the classifier.

In High Dimensions...

- ▶ In SVMs, a tuning parameter controls the amount of flexibility of the classifier.
- ▶ This tuning parameter is like a **ridge penalty**, both mathematically and conceptually. The SVM decision rule involves all of the variables.

In High Dimensions...

- ▶ In SVMs, a tuning parameter controls the amount of flexibility of the classifier.
- ▶ This tuning parameter is like a **ridge penalty**, both mathematically and conceptually. The SVM decision rule involves all of the variables.
- ▶ Can get a **sparse SVM** using a **lasso penalty**; this yields a decision rule involving only a subset of the features.

In High Dimensions...

- ▶ In SVMs, a tuning parameter controls the amount of flexibility of the classifier.
- ▶ This tuning parameter is like a **ridge penalty**, both mathematically and conceptually. The SVM decision rule involves all of the variables.
- ▶ Can get a **sparse SVM** using a **lasso penalty**; this yields a decision rule involving only a subset of the features.
- ▶ Logistic regression and other classical statistical approaches could be used with non-linear expansions of features. But this makes high-dimensionality issues worse.

Let's Try It Out in R!

Chapter 9 R Lab

www.statlearning.com

Batch Effects

Batch Effects

- In any sort of omics experiment, need to be very aware of **batch effects**, induced by non-biological factors such as inter-machine or inter-lab or inter-operator variability, time of day, day of week, position of ceiling fan,

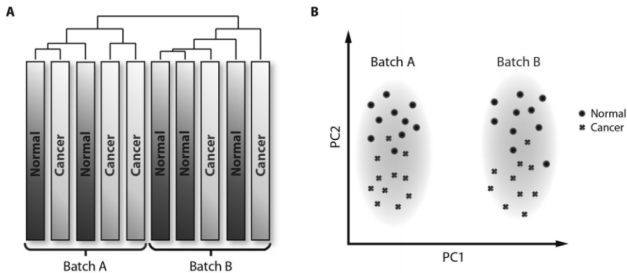
Batch Effects

- ▶ In any sort of omics experiment, need to be very aware of **batch effects**, induced by non-biological factors such as inter-machine or inter-lab or inter-operator variability, time of day, day of week, position of ceiling fan,
- ▶ It has been shown many many times that batch effects can be much stronger than biological effects of interest!

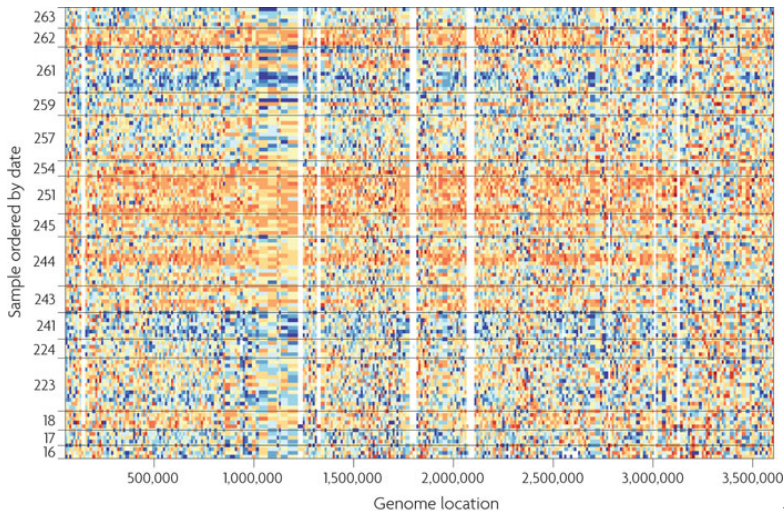
Batch Effects

- ▶ In any sort of omics experiment, need to be very aware of **batch effects**, induced by non-biological factors such as inter-machine or inter-lab or inter-operator variability, time of day, day of week, position of ceiling fan,
- ▶ It has been shown many many times that batch effects can be much stronger than biological effects of interest!
- ▶ Batch effects can make your data nonsense . . .

Batch Effects



Batch Effects in Practice



Steps to Reduce Batch Effects

Steps to Reduce Batch Effects

- ▶ Randomize sample run times: e.g. don't run cases first and controls second.

Steps to Reduce Batch Effects

- ▶ Randomize sample run times: e.g. don't run cases first and controls second.
- ▶ Avoid any extraneous sources of variation, e.g. due to change in person running the experiment.

Steps to Reduce Batch Effects

- ▶ Randomize sample run times: e.g. don't run cases first and controls second.
- ▶ Avoid any extraneous sources of variation, e.g. due to change in person running the experiment.
- ▶ It is often better to train a classification or regression method using **multiple data sets collected at different institutions, rather than using a single data set.**

Steps to Reduce Batch Effects

- ▶ Randomize sample run times: e.g. don't run cases first and controls second.
- ▶ Avoid any extraneous sources of variation, e.g. due to change in person running the experiment.
- ▶ It is often better to train a classification or regression method using **multiple data sets collected at different institutions, rather than using a single data set.**
- ▶ **Need to validate any results obtained on independent data sets from a different institution.**

Steps to Reduce Batch Effects

- ▶ Randomize sample run times: e.g. don't run cases first and controls second.
- ▶ Avoid any extraneous sources of variation, e.g. due to change in person running the experiment.
- ▶ It is often better to train a classification or regression method using **multiple data sets collected at different institutions, rather than using a single data set.**
- ▶ **Need to validate any results obtained on independent data sets from a different institution.**

Batch effects are almost inevitable. But you can do your best to design an experiment and analyze the data in such a way that batch effects do not compromise the results obtained.

Subtypes of Breast Cancer

Subtypes of Breast Cancer

- In the past 10 years, global gene expression analyses have identified at least 4 subtypes of breast cancer: Luminal A, Luminal B, Her2-enriched, and basal-like.

Subtypes of Breast Cancer

- ▶ In the past 10 years, global gene expression analyses have identified at least 4 subtypes of breast cancer: Luminal A, Luminal B, Her2-enriched, and basal-like.
- ▶ Subgroups differ with respect to risk factors, incidence, baseline prognoses, responses to therapies.

Subtypes of Breast Cancer

- ▶ In the past 10 years, global gene expression analyses have identified at least 4 subtypes of breast cancer: Luminal A, Luminal B, Her2-enriched, and basal-like.
- ▶ Subgroups differ with respect to risk factors, incidence, baseline prognoses, responses to therapies.
- ▶ Want to be able to determine the subtype for a new patient with breast cancer.

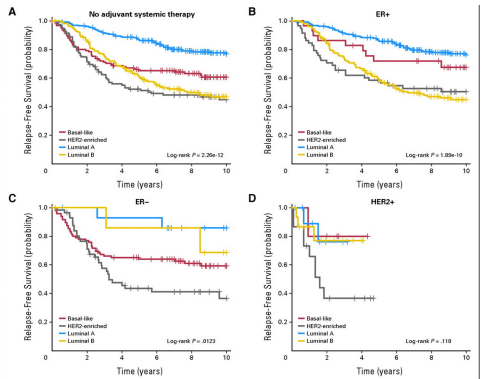
Subtypes of Breast Cancer

- ▶ In the past 10 years, global gene expression analyses have identified at least 4 subtypes of breast cancer: Luminal A, Luminal B, Her2-enriched, and basal-like.
- ▶ Subgroups differ with respect to risk factors, incidence, baseline prognoses, responses to therapies.
- ▶ Want to be able to determine the subtype for a new patient with breast cancer.
- ▶ Controversy over the best classifier for this task:
 - ▶ PAM50 classifier involves 50 genes.
 - ▶ More recent proposal involving three genes.

Subtypes of Breast Cancer

- ▶ In the past 10 years, global gene expression analyses have identified at least 4 subtypes of breast cancer: Luminal A, Luminal B, Her2-enriched, and basal-like.
- ▶ Subgroups differ with respect to risk factors, incidence, baseline prognoses, responses to therapies.
- ▶ Want to be able to determine the subtype for a new patient with breast cancer.
- ▶ Controversy over the best classifier for this task:
 - ▶ PAM50 classifier involves 50 genes.
 - ▶ More recent proposal involving three genes.
- ▶ Moving target: nobody knows the “true” subtype!
- ▶ Prat et al., Breast Cancer Res Treat, 2012

Why Do We Care About Subtypes?



Citation: Parker et al, Journal of Clinical Oncology, 2009

Proteomics for Ovarian Cancer

Proteomics for Ovarian Cancer

- ▶ Ovarian cancer is the leading cause of gynecologic cancer deaths in the USA.

Proteomics for Ovarian Cancer

- ▶ Ovarian cancer is the leading cause of gynecologic cancer deaths in the USA.
- ▶ Much interest in detecting the cancer at an earlier stage.

Proteomics for Ovarian Cancer

- ▶ Ovarian cancer is the leading cause of gynecologic cancer deaths in the USA.
- ▶ Much interest in detecting the cancer at an earlier stage.
- ▶ In 2002, Petricoin and Liotta – investigators from FDA and NCI – reported in The Lancet that mass spectrometry analysis of circulating serum proteins can be used to discriminate between healthy patients and those with ovarian cancer.

Proteomics for Ovarian Cancer

- ▶ Ovarian cancer is the leading cause of gynecologic cancer deaths in the USA.
- ▶ Much interest in detecting the cancer at an earlier stage.
- ▶ In 2002, Petricoin and Liotta – investigators from FDA and NCI – reported in The Lancet that mass spectrometry analysis of circulating serum proteins can be used to discriminate between healthy patients and those with ovarian cancer.
- ▶ Great enthusiasm in the popular press and general public.

Proteomics for Ovarian Cancer

- ▶ Ovarian cancer is the leading cause of gynecologic cancer deaths in the USA.
- ▶ Much interest in detecting the cancer at an earlier stage.
- ▶ In 2002, Petricoin and Liotta – investigators from FDA and NCI – reported in The Lancet that mass spectrometry analysis of circulating serum proteins can be used to discriminate between healthy patients and those with ovarian cancer.
- ▶ Great enthusiasm in the popular press and general public.
- ▶ Plans were made to begin marketing a test based on the reported diagnostic.

Not So Fast!!

- ▶ Independent researchers took a look at the data, which was publicly available, and discovered:
 - ▶ **inadvertent changes in protocol mid-experiment:** i.e. major batch effects.
 - ▶ problems with instrument calibration.
 - ▶ difference in processing between tumor and normal samples.

Not So Fast!!

- ▶ Independent researchers took a look at the data, which was publicly available, and discovered:
 - ▶ **inadvertent changes in protocol mid-experiment**: i.e. major batch effects.
 - ▶ problems with instrument calibration.
 - ▶ difference in processing between tumor and normal samples.
- ▶ In summary: the observed differences between cancer and normal proteomic patterns were attributable to “artifacts of sample processing, not the underlying biology of cancer.”

Gene Expression Signatures for Cancer Treatment

Gene Expression Signatures for Cancer Treatment

- In the early 2000's, Joe Nevins, Anil Potti, and other researchers at Duke University began developing expression-based predictors of response to chemotherapy.

Gene Expression Signatures for Cancer Treatment

- ▶ In the early 2000's, Joe Nevins, Anil Potti, and other researchers at Duke University began developing expression-based predictors of response to chemotherapy.
- ▶ Many (dozens of!) very promising and very high-profile papers were published in Nature Medicine, The Lancet, Journal of Clinical Oncology, and more.

Gene Expression Signatures for Cancer Treatment

- ▶ In the early 2000's, Joe Nevins, Anil Potti, and other researchers at Duke University began developing expression-based predictors of response to chemotherapy.
- ▶ Many (dozens of!) very promising and very high-profile papers were published in Nature Medicine, The Lancet, Journal of Clinical Oncology, and more.
- ▶ Several clinical trials were initiated, using these predictors to direct therapy for cancer patients.

Gene Expression Signatures for Cancer Treatment

- ▶ In the early 2000's, Joe Nevins, Anil Potti, and other researchers at Duke University began developing expression-based predictors of response to chemotherapy.
- ▶ Many (dozens of!) very promising and very high-profile papers were published in Nature Medicine, The Lancet, Journal of Clinical Oncology, and more.
- ▶ Several clinical trials were initiated, using these predictors to direct therapy for cancer patients.
- ▶ This research was hailed as a major breakthrough in cancer treatment, and researchers from all over the world tried to use these sorts of techniques in their own labs.

Upon Closer Inspection....

- Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):

Upon Closer Inspection....

- ▶ Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):
 - ▶ Off-by-one errors in gene lists

Upon Closer Inspection....

- ▶ Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):
 - ▶ Off-by-one errors in gene lists
 - ▶ The same heatmap displayed in multiple (unrelated) papers

Upon Closer Inspection....

- ▶ Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):
 - ▶ Off-by-one errors in gene lists
 - ▶ The same heatmap displayed in multiple (unrelated) papers
 - ▶ Genes not measured on the array were reported as being part of the predictor obtained, and as providing evidence for biological plausibility

Upon Closer Inspection....

- ▶ Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):
 - ▶ Off-by-one errors in gene lists
 - ▶ The same heatmap displayed in multiple (unrelated) papers
 - ▶ Genes not measured on the array were reported as being part of the predictor obtained, and as providing evidence for biological plausibility
 - ▶ Reversal of sensitive/resistant labels

Upon Closer Inspection....

- ▶ Using the fact that some of the data were publicly available, independent researchers discovered the following errors (among many others):
 - ▶ Off-by-one errors in gene lists
 - ▶ The same heatmap displayed in multiple (unrelated) papers
 - ▶ Genes not measured on the array were reported as being part of the predictor obtained, and as providing evidence for biological plausibility
 - ▶ Reversal of sensitive/resistant labels
- ▶ A shocking paper published by Baggerly and Coombes in Annals of Applied Statistics, detailing all of the errors made: “One theme that emerges is that the most common errors are simple (e.g., row or column offsets); conversely, it is our experience that the most simple errors are common.”

What Went Wrong?

A blasé approach to high-dimensional data analysis:

What Went Wrong?

A blasé approach to high-dimensional data analysis:

- ▶ Need to have a proper independent test set, that you simply cannot peek at under any circumstances!

What Went Wrong?

A blasé approach to high-dimensional data analysis:

- ▶ Need to have a proper independent test set, that you simply cannot peek at under any circumstances!
- ▶ Need to have clearly documented code that contains all steps of the analysis, from start to finish. You must be able to share this code with independent researchers, and you must be confident that your code is correct. If not, then your work isn't ready for prime time.

The Stakes are High!

At Duke:

- ▶ Dozens of papers retracted;
- ▶ Careers and reputations ruined;
- ▶ Patients endangered through unethical clinical trials.

Plus, a 60 Minutes special feature and an Institute of Medicine Committee!!!

Discussion Questions

Suppose someone came to a statistical consulting service you were running and said...

I want to try and classify patients as having breast cancer, or not based on gene expression in serum.

I'm pretty excited because I just found two awesome datasets:

The first, from the Farnsworth Lab, has serum expression measured using RNA-seq in 5000 patients with breast cancer;

The second, from the Wernstrom Lab, has serum expression measured using microarrays on 5000 healthy patients.

I wanted to combine them to build my classifier

What concerns, if any, come to mind?

Discussion Questions

Suppose we want to classify patients as having cancer/not having cancer using methylation on cf-dna fragments

In particular, say we initially consider 10000 cpg sites, and try to build a classification model that uses proportion of methylated fragments at each of those sites as features.

Would it make sense to run an SVM with a non-linear kernel here?

If we used cross-validation to select between both that SVM, and a LASSO-logistic regression, what might happen?