

Exercise 8

Task 1 a) first, we draw the correspondence graph of each attribute and target:

Professional Status				Contract Duration		
civil servant	Employee	self-employed	non-employed	Low	medium	high
yes	yes	yes	no	yes	no	no yes
no	no	no	no	yes	no	no
					no	no

Second, we compute the information gain for each attribute:

$$\text{Professional Status: } \frac{2}{9} \cdot \text{entropy}([1,1]) + \frac{3}{9} \cdot \text{entropy}([1,2]) + \frac{4}{9} \cdot \text{entropy}([1,1]) + 0 \\ = \frac{4}{9} + 0.3061 = 0.7505 \text{ bits}$$

$$\text{Contract Duration: } \frac{2}{9} \cdot 0 + \frac{4}{9} \cdot 0 + \frac{1}{3} \cdot (0.5283 + 0.39) = 0.3061 \text{ bits}$$

$$\text{Information gain}_p = \text{entropy}([3,6]) - 0.7505 = 0.9183 - 0.7505 = 0.1678 \text{ bits}$$

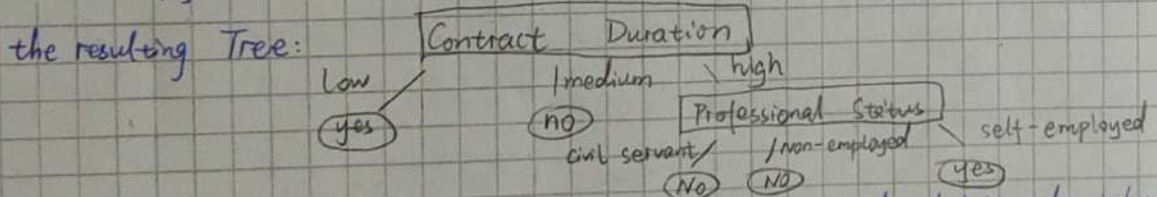
$$\text{Information gain}_c = 0.9183 - 0.3061 = 0.6122 \text{ bits}$$

Therefore, we choose the variable "Contract Duration" as the root:

Since we have only "yes" for "low", "no" for "medium" of variable "Contract Duration", we complete to split for them. Now we only need to compute the information gain for "high":

$$\text{Entropy}(\text{Contract Duration} = \text{high}) = \text{Entropy}([1,2]) = 0.9183$$

$$\text{Entropy}(\text{Contract Duration} = \text{high} | \text{Professional Status}) = 0$$



The order of the attributes of the resulting tree is decided by the information gain. We pick the attribute with max information gain for each split.

The leaf nodes is yes/no.

b) We classify Number 11 & 12 by the tree from (a):

No. 11 with "low" of "Contract Duration", it is classified to "yes" of termination

No. 12 with "medium" of "Contract Duration", it is classified to "no".

Hence Customer with number 11 is at risk of termination.

c) Customer with low contract duration tend to terminate; with medium duration tend to not terminate. For customer with high duration, the ones ~~with~~ who are

self-employed at risk of termination. Unexpectedly, customer with high duration but with non-employed tend to not terminate.

d) Assume dataset X and attribute V with n possible different values (V_1, V_2, \dots, V_n)

The information gain of splitting X with V is:

$$\text{Gain}(X, v) = \text{Entropy}(X) - \sum_{i=1}^n \frac{|X_i|}{|X|} \text{Entropy}(X|V_1, V_2, \dots, V_n)$$

The information gain ratio is:

$$\text{Gainratio}(X, v) = \frac{\text{Gain}(X, v)}{\sum_{i=1}^n \frac{|X_i|}{|X|} \log_2 \frac{|X_i|}{|X|}} - \text{split information}$$

From the definition of $\text{Gain}(X, v)$, the attribute with more possible values (higher possibility with pure classification) might has larger information gain and so be chosen.

Therefore we introduce Gainratio to reduce the bias caused by higher branching attribute (larger n means larger split information)

The definition of Gini index:

$$\text{Gini}(X, v) = \sum_{i=1}^n \frac{|X_i|}{|X|} \text{Gini}(X_i)$$

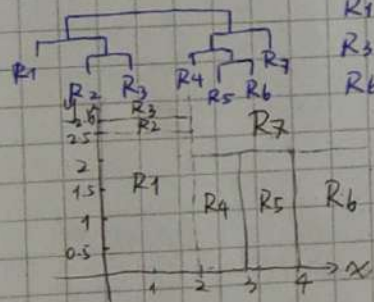
$$= 1 - P^2 - (1-P)^2 = 2P(1-P)$$

* A, B
assume there are 2 possible outcomes
P is the possibility of event A.

e) $\text{Gini}(\text{Contract Duration}) = \frac{3}{11} \cdot 0 + \frac{4}{9} \cdot 0 + \frac{3}{9} \cdot 2 \cdot \frac{1}{3} \cdot \frac{2}{3} = \frac{1}{3}$

Task 2.

a)



$$\begin{aligned} R_1: x \leq 2, y \leq 2.5; & \quad R_2: x \leq 2, 2.5 < y \leq 2.6; \\ R_3: x \leq 2, y > 2.6; & \quad R_4: 2 < x \leq 3, y \leq 2; \\ R_6: x > 4, y \leq 2; & \quad R_7: x > 2, y > 2. \end{aligned}$$

b) Partition R_2 and R_5 can be described as overfitted. The subtrees of R_2 and R_5 should be removed.

c) The generalization capability of a classifier mean the classification not only works well on the training data, but also on the testing data. (new data).