Exercise set #5

Release:

Thursday, 7 November 2024

Discussion: Wednesday, 13 November 2024

You do not have to hand in your solutions to the exercises and they will **not** be graded. However, there will be four short tests during the semester. You need to reach $\geq 50\%$ of the total points in order to be admitted to the final exam (Klausur). The tests are held at the start of a lecture (room 2522.U1.74) at the following dates:

Test 1: Thursday, 31 October 2024, 10:30-10:45 Test 2: Thursday, 21 November 2024, 10:30-10:45 Test 3: Thursday, 5 December 2024, 10:30-10:45 Test 4: Thursday, 9 January 2025, 10:30-10:45

Please ask questions in the RocketChat

The exercises are discussed every Wednesday, 14:30-16:00 in room 2512.02.33.

1. TD and MC prediction

In the lecture we have seen *batch* versions of TD and MC prediction (lecture 6, slide 17). Assume an MDP with a single action a_0 that has no effect (also known as Markov reward process or MRP). Given the following batch of episodes (i.e., sequences $s_0, r_1, s_1, r_2, \ldots$, the action is a_0 in every step)

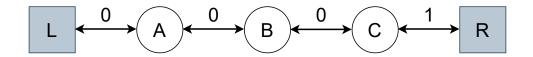
(1) A, 0, B, 6, C	(6) $B, 2, C$
(2) $A, 3, C$	(7) B, 6, C
(3) A, 2, B, 0, A, 3, C	(8) $B, 2, C$
(4) B, 0, A, 2, B, 2, C	(9) $B, 6, C$
(5) B, 0, A, 3, C	

and assuming no discounting (i.e., $\gamma = 1$), your tasks are the following:

- (a) Apply batch TD to the episodes (1), (2), (3), i.e., apply Algorithm 2 from lecture 6, where the tuples are sampled from the batch in chronological order. Initialize all values with zero and use the learning rate $\alpha = 0.1$.
- (b) Derive the MDP that best fits the data, i.e., calculate the most likely transition probabilities $\mathcal{P}(s'|s,a)$ and reward function $\mathcal{R}(s,a)$, and draw the graphical model.
- (c) Calculate the values for states A and B using the MDP derived in part (b). Since there is only one action, the policy does not matter. From the lecture we know that batch TD converges to this solution.
- (d) Calculate the values for states A and B by applying batch first-visit and every-visit MC to the given episodes.

2. TD and MC prediction

The following graph depicts an example of a Markov reward process (MRP). In this MRP, every episode starts in the center state B, then proceed either left or right by one state on each step, with equal probability. Episodes terminate either on the extreme left or right in states L or R. When an episode terminates in R, a reward of 1 occurs; all other rewards are 0.



- (a) Your friend guesses that the state-values for the MRP are given as v(L) = 0, v(A) = 1/4, v(B) = 1/2, v(C) = 3/4, v(R) = 0. Proof that these are the true values.
- (b) Name two algorithms that would also lead to the true state-value function.
- (c) Implement Monte-Carlo prediction and TD-prediction in order to produce estimates for v(A), v(B), v(C) of the Markov reward process. Follow the instructions in the Jupyter notebook mc-td-prediction.ipynb.