Automatic Detection of Wave Boundaries in Multilead ECG Signals: Validation with the CSE Database¹

PABLO LAGUNA,* RAIMON JANÉ,† AND PERE CAMINAL†

*Departamento de Ingeniería Eléctrica e Informática, Centro Politécnico Superior, Universidad de Zaragoza, Spain; and †Institut de Cibernètica, Universitat Politècnica de Catalunya-CSIC,

Barcelona, Spain

Received July 28, 1993

This paper presents an algorithm for automatically locating the waveform boundaries (the onsets and ends of P, QRS, and T waves) in multilead ECG signals (the 12 standard leads and the orthogonal XYZ leads). Given these locations, features of clinical importance (such as the RR interval, the PQ interval, the QRS duration, the ST segment, and the QT interval) may be measured readily. First, a multilead QRS detector locates each beat, using a differentiated and low-pass filtered ECG signal as input. Next, the waveform boundaries are located in each lead. The leads in which the detected electrical activity is of longest duration are used for the final determination of the waveform boundaries. The performance of our algorithm has been evaluated using the CSE multilead measurement database. In comparison with other algorithms tested by the CSE, our algorithm achieves better agreement with manual measurements of the T-wave end and of interval values, while its measurements of other waveform boundaries are within the range of the algorithm and manual measurements obtained by the CSE. © 1994 Academic Press. Inc.

1. Introduction

The electrocardiogram (ECG) is characterized by a recurrent wave sequence (P, Q, R, S, T) associated with each beat. Various time intervals defined by the onsets and ends of these waves are important in electrocardiographic diagnosis. The most important of these intervals are the RR interval, the PQ interval, the QRS duration, the ST segment, and the QT interval. Direct measurement of these intervals requires knowledge of the locations of the boundaries (the onsets and ends) of the P, QRS, and T waves.

Since beat-by-beat manual measurement of these intervals from standard 12-lead ECGs is impractical in routine clinical practice, algorithms for automated measurement have been proposed to locate QRS onsets and ends (1), QT interval limits (2), and onset of P and QRS waves and ends of P, QRS, and T

¹ This work was supported by CICYT (Spain) Grant TIC91-1037.

waves (3, 4). Although these algorithms may work acceptably given noise-free signals, their performance degrades in the presence of noise (5).

The Common Standards for Quantitative Electrocardiography (CSE) project, sponsored by the European Community (4), has studied the performance of many algorithms designed to locate waveform boundaries in the ECG. An important finding of the CSE study is that the algorithms tend to locate the end of the T wave significantly earlier than human experts do (3). Unfortunately, no technical details are given for the algorithms used in (3, 4), limiting their use outside their domains. All these reasons led us to develop a new method for locating waveform boundaries, which is presented in this paper. We evaluated our method using the same methodology and test signals used by the CSE, and show that its agreement with manual measurements of waveform boundaries is excellent, even for measurements of the end of the T wave.

Our method is based on the multilead generalization of a previously described procedure for single-lead measurement of the QT interval (2), and subsequently used for single and multilead waveform boundary determination (6, 7). The method has been applied to ECG records of the MIT-BIH database and validated with the CSE multilead measurement database (8), where other programs have already been validated.

2. Methods

First, a multilead QRS detector (designed for 15 leads) is applied to the ECG record. Next, the algorithm estimates the waveform boundaries independently in each lead of the multilead ECG record. This procedure makes use of the differentiated ECG signal and information about wave shape. The algorithm implements criteria to establish wave presence or absence in each lead according to the relative differentiated signal magnitude in the different waves. Given the information about wave presence and the differentiated signal, the algorithm characterizes the patterns of the P wave (regular or inverted), the QRS complex (in terms of various Q, R, S, R' sequences), and the T wave (regular, inverted, or biphasic), in accordance with the classification used by the CSE working party (9). Using the wave boundaries obtained in each lead, the final wave boundaries are selected from those leads where the detected electrical activity is longest, reducing the influence of possible noisy measurements.

Figure 1 shows the main steps of the procedure for waveform boundary detection. The multilead QRS detector includes 15 single-lead QRS detectors and generates the $QRS_j(i)$ positions of the *i*th QRS in the *j*th lead from each lead, $ECG_j(k)$. Next, a multilead QRS decision rule gives the final $QRS_j(i)$ detections of the *i*th beat in each lead. We analyze each lead, $ECG_j(k)$, using the following single-lead steps: fibrillation process rejection, waveform location $(\mathbf{W}_j(i))$, and waveform boundary determination, yielding single-lead waveform boundary estimates $(\mathbf{WB}_j(i))$ for lead j and beat i. From the $\mathbf{WB}_j(i)$ estimates, a multilead waveform boundary location rule gives the final lead-independent waveform boundaries for each beat $(\mathbf{WB}(i))$. Finally, given these $\mathbf{WB}(i)$ posi-

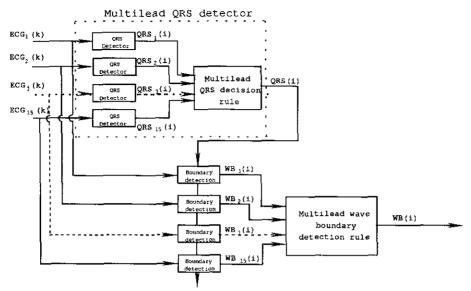


Fig. 1. Diagram of the wave boundary detection procedure.

tions, we compute the clinically relevant intervals (PR, QT, \ldots) . Below, we describe these steps in greater detail.

2.1. Preprocessing

The first step consists of a single-lead filtering process for noise reduction and a nonlinear transformation to improve QRS detection (10). The linear filtering uses a second-order bandpass Lynn filter (0.8-18 Hz, -3 dB) (11) to attenuate baseline drift and high-frequency contamination. Once the bandpass-filtered signal (ECGPB) is reached, a low-pass differentiator (10) is applied to get the information about changes in the signal slope. This differentiated signal is called ECGDER. The nonlinear transformation we use is the moving-window integration of the squared signal described in (10) with an integration width of 95 msec.

2.2. ORS Detection

- 2.2.1. Single-Lead QRS Detection. The single-lead QRS detector used in this work is an adaptation of that described by Pan and Tompkins (10), using the signal slope in the decision rule: any possible detection should have a maximum slope within ± 30 % of that of the previous QRS complexes.
- 2.2.2. Multilead QRS Detection. From the estimates, $QRS_j(i)$, of the position of beat i in lead j obtained by the single-lead detectors (Fig. 1), we apply a multilead QRS detection rule to consider as QRS complexes in each lead only those whose positions do not differ more than 90 msec from one lead to another (12). The decision rule includes the following steps:

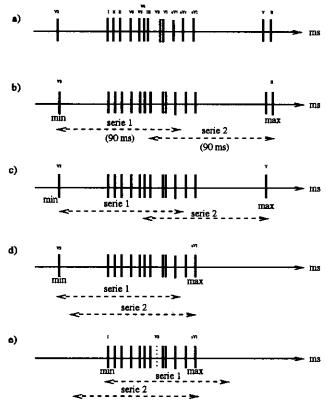


Fig. 2. Multilead QRS decision rule.

- (a) The input values to this processing stage are the detected positions $QRS_j(i)$ (j = 1, ..., 15) of the *i*th beat, that come from the single-lead QRS detectors. Figure 2a shows an example of these detections.
- (b) The first (min) and last (max) $QRS_j(i)$ (j = 1, ..., 15) temporal positions are searched (Fig. 2b). From these time positions we define two series of $QRS_j(i)$ positions: series 1, those $QRS_j(i)$ that are within 90 msec of min, and series 2, those $QRS_j(i)$ that are within 90 msec of max. In Fig. 2b, series 1 has 11 positions and series 2 has 8 positions.
- (c) The two series are compared. If both contain all 15 $QRS_j(i)$ (j = 1, ..., 15) positions, it is assumed that the *i*th beat has been detected correctly in all the leads. If the series contain different numbers of positions, the extreme value (min or max) of the series that contains the smaller number of positions is rejected.

If the rejected position is max, it may result from a missed detection, and max could belong to the next beat. Thus, if max belongs to lead j, we assign $QRS_j(l) = QRS_j(l-1)$ ($l \ge i+1$). In (Figs. 2b and 2c) the max position, belonging to lead II, is rejected as a probable false detection, and the algorithm

assumes that the true QRS in lead II was missed by the single-lead detector. If the rejected position is min, it may result from a false positive detection at this lead. In this case, if min belongs to lead j, $QRS_j(i+1)$ may be the true detection for which we are looking. Thus, we may assign $QRS_j(l) = QRS_j(l+1)$ ($l \ge i$). In (Figs. 2d and 2e) the min position, belonging to lead V_3 , is rejected as a probable false detection, and the algorithm reassigns $QRS_{V_i}(i+1)$ (dashed line) as the position of the ith beat at V_3 .

(d) The process continues recursively until both series are identical. The remaining positions are considered the true detection for the *i*th beat in each lead. Leads where the *i*th beat was not detected, or where a detection was rejected in the previous step, are not used for waveform boundary determination for beat *i*.

In Fig. 3 we have the single-lead detection marks in seven leads of record MO1_109 from the CSE database. The multilead decision rule rejects the 12th detected beat in lead II (it was the P-wave position, rather than the QRS complex position) since it is not in accordance with the other leads and recognizes two missing beats in lead V_3 (7th and 11th). Table 1 summarizes the detections in this record.

2.3. Fibrillation Rejection

During fibrillation, it is meaningless to measure P, QRS, and T boundaries. Fibrillation is detected using the single-lead procedure presented in (13), applied before the wave location procedure.

2.4. Wave Location

The QRS positions $(QRS_j(i))$ given by the detector may be Q, R, or S-wave peaks. The algorithm searches for the nearest peak positions before (p_b) and after (p_a) the $QRS_j(i)$ position in the ECGDER (zero-crossing in this signal). According to the polarity and relative value of these peaks, we decide if $QRS_j(i)$ belongs to the Q, the R, or the S wave (2). The adjacent wave positions are detected as the nearest zero-crossing points to $QRS_j(i)$ in ECGDER. To admit these adjacent detected points as wave positions $(\mathbf{W}_j(i))$, the time distance between waves must be in the range of physiologically plausible intervals, and the maximum slope associated with these waves must be bigger than a threshold of the maximum slope associated with the QRS complex (dermax). The threshold value is experimentally adjusted and is different for Q, R, S, or R' waves, ranging from 3 to 10% of the maximum QRS slope value (dermax). This procedure thus attempts to locate as many of the Q, R, S, and R' peaks as are present.

Next, we search for the P and T-wave peaks. These waves have lower frequency components than the QRS complex. We again apply a low-pass filter (-3 db cutoff frequency of 12 Hz) to ECGDER to reduce remaining noise. In this filtered signal (DERFI) we define a window of 155 msec starting 225 msec

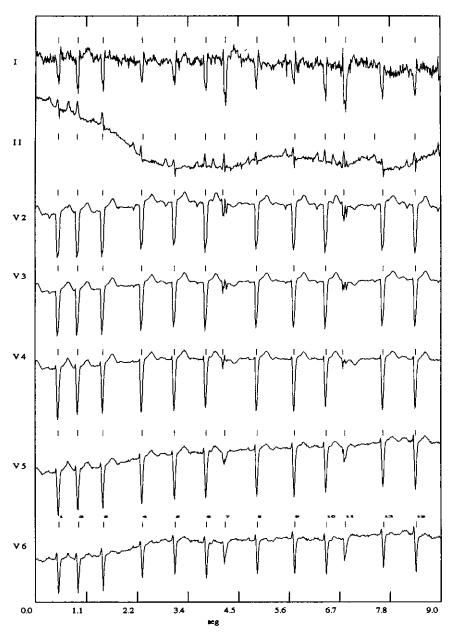


Fig. 3. Example of multilead QRS detection in record MO1_109 of the CSE database.

TABLE 1
QRS DETECTIONS ACCEPTED IN EACH LEAD OF RECORD MO1_109 OF THE CSE DATABASE (Fig. 3)

Beat	Leads														
	I	II	111	aV _R	aV _L	aV _F	V_1	V ₂	V ₃	V ₄	V ₅	V ₆	X	Y	Z
1	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
2	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
3	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
4	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
5	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
6	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
7	+	+	+	+	+	+	+	+	*	+	+	+	+	+	+
8	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
9	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
10	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
11	+	+	+	+	+	+	+	+	*	+	+	+	+	+	+
12	+	*	+	+	+	+	+	+	+	+	+	+	+	+	+
13	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+

Note. The symbol (+) represents accepted detections; the symbol (*) represents beats either rejected or not detected in the corresponding lead.

before the R position. This window is shortened when the previous T or the next Q wave is in it. In this window we search for the maximum and minimum value. If these values are bigger than 2% of the maximum slope of the QRS complex, the algorithm assumes that it has located a P wave; otherwise, the algorithm assumes that the P wave cannot be located in the given lead. The P-wave peak is assumed to occur at the zero-crossing between the maximum and the minimum values in the window.

To detect the T wave, we define a search window in DERFI that is a function of the heart rate (2). The algorithm determines the type of T wave (regular, inverted, biphasic +-, or biphasic -+) according to the relative positions and values of the maximum and minimum values within the search window, using the CSE working party classification (9). The T-wave peak is assumed to occur at the zero-crossing adjacent to the maximum or minimum value.

2.5. Waveform Boundary Location

2.5.1. Single-lead Waveform Boundary Location. Once we have the wave locations (zero-crossing point (zero) in the differentiated signal ECGDER or DERFI), we proceed to locate the onset and end (boundaries) of each waveform. The differentiated threshold method used in this work was presented in (2) for QT interval determination, and in this work we have generalized it to determine

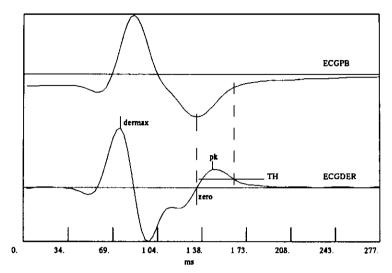


Fig. 4. Determination of the end of the QRS by the threshold method.

any wave limit in multilead ECG records. Figure 4 shows this procedure for QRS end determination. From the zero point (S-wave position) we search for the adjacent peak (pk) on the right (for the end) or on the left (for the onset). This point is the point of maximum slope in the wave. With the value of ECGDER at time instant pk, (ECGDER(pk)), we define a threshold (TH) as TH = ECGDER(pk)/k. Thus, we determine the end (onset) point of the wave as the forward (backward) threshold crossing point from pk in the ECGDER signal (end of S wave in Fig. 4). The value of k is a constant that is experimentally adjusted and reaches its best performance with the values expressed in Table 2.

When two waveforms overlap, the threshold criteria can fail and may give boundary locations far from the physiologically expected points, Thus, the algorithm uses a minimum differentiated criterion as described in Fig. 5. From the pk position we find the smallest absolute peak in the same direction (pk') as for the previous criterion. This peak position, associated with an ECG inflection, is taken as the waveform boundary (Fig. 5).

Figure 6 shows this procedure applied to a single-lead ECG record from the MIT-BIH database. The short horizontal lines at each QRS complex represent the isoelectric level calculated at each beat for wave amplitude measurement purposes. The isoelectric level is estimated as the average ECG signal between the P end (P_e) and the QRS onset (QRS_b) , excluding the first and last 15 msec in this interval.

In the presence of high-amplitude baseline wander, this procedure has been shown to be more robust when applied to the ECG records after removal of baseline interference, given that this interference can overlap the spectrum of the *P* and *T* waves. The use of a threshold criterion in the presence of low-

		Wave boundary (WB)							
		P wave		Q wave	Rw	ave	S wave	T wave	
K Values		$P_{\mathfrak{b}}$	Pe	Q_{b}	$R_{\rm b}$	$R_{\rm e}$	S_{e}	T_{b}	Te
	≤0.13								4.0
	0.13-0.20				5.0		3.0	Ì	5.0
	0.20-0.41		<u> </u> 						6.0
ECGDER $(pk) \times 10$	0.41-2.00	1.35	2.0	1.8		5.0		2.0	
dermax	2.00-4.00				8.0				
	4.00-4.75								
							8.0		
	4.75-6.20				28		9.0		7.0
	≥6.20	ļ					12.0		ļ

P begin (onset), (P_b) , P end (P_c) , etc., as a function of the maximum wave slope (ECGDER(pk)) relative to the maximum QRS slope dermax.

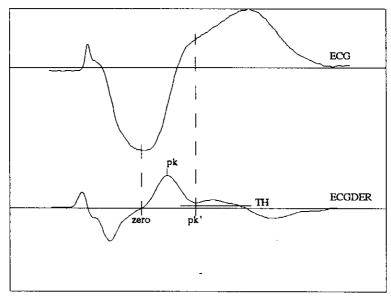


Fig. 5. Minimum differentiated criterion.

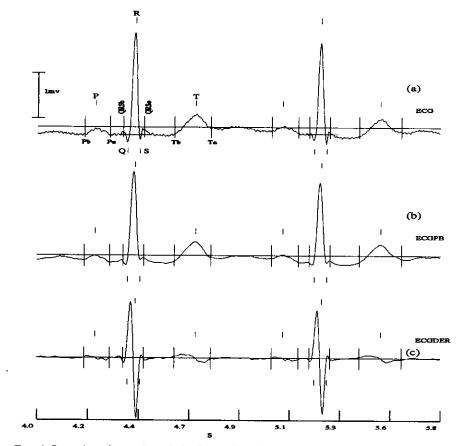


FIG. 6. Detection of wave boundaries in two beats belonging to record 103 (lead MLII) of the MIT-BIH ECG database. Short lines denote the wave positions (P, Q, R, S, and T) and long lines the wave limits: $P \text{ onset } (P_b)$, $P \text{ end } (P_e)$, etc. (a) Original ECG, (b) ECGPB signal, and (c) ECGDER signal.

frequency artifact in the differentiated signal could lead to estimation errors if no a priori baseline cancellation is done.

2.5.2. Multilead Wave Onset and End Determination. From the previous procedure we obtain, for each waveform boundary \mathbf{WB} $(P_b, P_e, QRS_b, \ldots)$, a set of waveform boundary positions $\mathbf{WB}_j(i)$ belonging to beat i of lead j (j can take values from 1 to 15, except for values corresponding to the leads where no detection was made, or where the multilead QRS detection rule rejected the detection). The next step is the selection, from these $\mathbf{WB}_j(i)$ positions, of the one $\mathbf{WB}(i)$ that will be considered as the real onset or end of the waveform at the ith beat. Electrophysiologically, if all $\mathbf{WB}_j(i)$ were correctly detected, we should select the earliest $\mathbf{WB}_j(i)$ $(j = 1, \ldots, 15)$ for the waveform onset and the latest for the waveform end, in order to recover the boundary from that lead where the electrical activity of the heart has the longest temporal

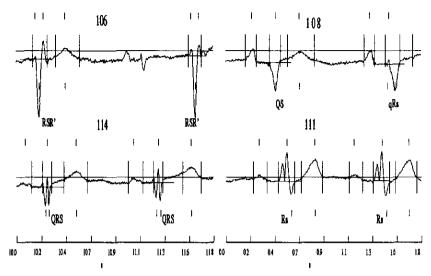


Fig. 7. Results on different ECG patterns.

projection. However, due to noise or errors, misestimations could have occurred in the determination of some $\mathbf{WB}_j(i)$ that may lead to an erroneous final $\mathbf{WB}(i)$ position. To reduce the risk of this occurrence, we apply the following multilead wave boundary detection rule (Fig. 1) for each *i*th beat: we search the minimum (min) time position (for onsets) or maximum (max) time position (for ends) of $\mathbf{WB}_j(i)$ ($j=1,\ldots,15$). If no more than two other leads have their $\mathbf{WB}_j(i)$ mark in the interval $(min, min + \delta)$ or $(max - \delta, max)$, the min or max $\mathbf{WB}_j(i)$ point is rejected as a possible noisy detection. The value of δ is selected according to the usual variability in manual estimations (9) and the empirical practice. Values for δ are δ , δ , δ , δ , δ , δ , δ , and δ 0 max on the minimum δ 1. After that we take the wave onsets (ends) at the minimum (maximum) of the remaining δ 1 most positions, obtaining the final δ 3.

3. RESULTS

The single-lead procedure has been applied to several records of the MIT-BIH database. Figure 7 shows some of the results obtained on four different records with no standard morphologies; record 106 presents a RSR' pattern, record 108 presents a QS pattern, record 114 presents a W pattern, and record 111 presents a R wave with two peaks. In all cases the wave limits are well determined, including wave shape determination.

The multilead procedure has been applied to records of the CSE multilead measurements database. Figure 8 shows the multilead advantage of the results obtained on record MO1_063 of this database. Note how the multilead boundary location procedure improves the location of the *T* end point, which differs significantly between leads V₂ and V₃, and others such as I or III.

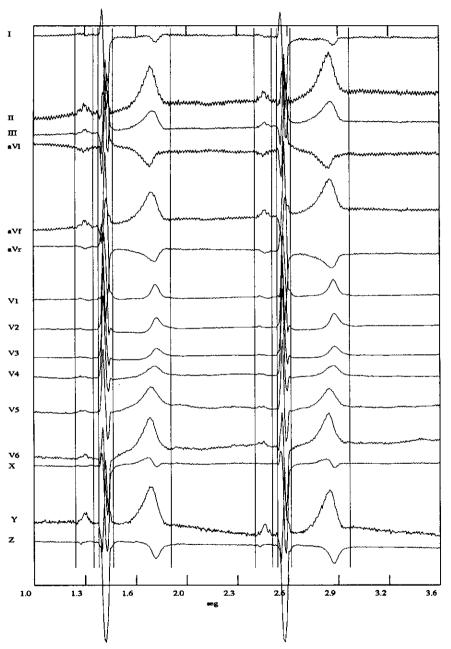


Fig. 8. Multilead waveform boundary determination in record MO1_063 of the CSE database.

TABLE 3 $\label{eq:comparing} \mbox{Evaluation Results, Comparing the Waveform Boundary Detection Method Estimates (ME) with the Mean Referee Estimates (RE_{CSE}) and with the Mean Program Estimates (PE_{CSE})$

	Pon	P_{off}	QRS_{on}	QRS _{off}	$T_{\rm off}$
		ME-P	E _{CSE}		
n	111	111	121	121	121
μ (msec)	-0.072	0.505	-3.587	0.083	9.700
$\sigma({\sf msec})$	5.695	8.310	4.193	7.705	16.467
		ME-R	E _{CSE}		
n	30	29	30	25	26
μ (msec)	1.000	-1.034	-2.067	-0.160	1.846
σ (msec)	7.926	5.144	7.437	7.893	10.552
	Accepted to	olerances for	referee dev	iations (9)	
$\sigma_{ m ref}$	10.2	12.7	6.5	11.6	30.6

4. VALIDATION WITH THE CSE DATABASE

Our algorithm for locating waveform boundaries (onset and end) has been evaluated with the CSE multilead measurement database (14). The evaluation has been carried out in terms of the mean (μ) and standard deviation (σ) of the differences between the estimates obtained using our algorithm (ME) and: a) the mean referee estimates of the CSE database (RE_{CSE}), or b) the mean program estimates of the CSE database (PE_{CSE}), in each measured beat set. We have compared the performance of our algorithm against the mean performance of the algorithms tested by the CSE, because the CSE has not reported independent results from each program tested. In Table 3 we present these results together with the accepted tolerance for referee deviations (σ_{ref}) reported in (9). The value n refers to the number of measured beats available in the CSE database for comparisons (one beat from each CSE multilead ECG records). These numbers (around 120 beats for comparison with other programs and around 30 beats for comparison with human referee measurements) are too small to permit statistical inferences about our algorithm, but are the only accessible comparative measurements provided by the CSE database. Despite the small number of available reference measurements, we have cited these results since no other method would permit a fair comparison of our algorithms with others, or with human experts.

From Table 3 we see that the our algorithm yields unbiased measurements ($\mu \le \text{sampling period} = 2 \text{ msec}$) with standard deviations comparable to those of measurements made by human experts; hence, for the evaluation sample, our algorithm provides valid measurements. With respect to measurements of the end of the T wave, our algorithm (ME) shows much better agreement with

TABLE 4 Evaluation Results, Comparing the ECG Interval Values Measured from the Waveform Boundary Method Estimates (ME) with Those Measures from the Mean Referee Estimates (RE_{CSE}) and with the Mean Program Estimates (PE_{CSE})

	$P_{ m DUR}$	QRS _{DUR}	PR_{INT}	QT_{INT}
		ME-PE _{CSE}		
n	111	121	111	121
μ (msec)	0.577	3.802	-3.423	13.133
σ (msec)	-10.690	9.050	6.803	16.831
]	ME-RE _{CSE}		
n	25	23	25	23
μ (msec)	-0.400	3.217	-2.400	4.261
σ(msec)	7.095	9.812	8.679	10.274
	Error limit tole	rances for prog	grams (15)	
$\mu_{\text{tol}}(\text{msec})$	10.0	3.5	4.5	7.0
$\sigma_{\rm tol}({\sf msec})$	12.0	8.0	8.0	13.5

the RE_{CSE} (1.8 msec mean difference) than for the PE_{CSE} (9.7 msec mean difference). These results suggest that our algorithm is more accurate for determination of T-wave end locations than the mean program estimates.

We have also evaluated our algorithm in terms of the significant interval values: P duration ($P_{\rm DUR}$), PR interval ($PR_{\rm INT}$), QRS duration ($QRS_{\rm DUR}$), and QT interval ($QT_{\rm INT}$). The evaluation has been done in terms of the mean and standard deviation of the differences between intervals estimated by our algorithm (ME) and: a) the intervals measured from the mean referee estimates of the CSE database ($RE_{\rm CSE}$), or b) the intervals measured from the mean program estimates of the CSE database ($PE_{\rm CSE}$). In Table 4 we present these results together with the interval measure tolerances, mean ($\mu_{\rm tol}$), and standard deviation ($\sigma_{\rm tol}$) reported in (15). The value n refers to the number of measured beats available in the CSE database for comparisons.

From this table we see that the interval measures obtained with the proposed method have mean differences and standard deviations within the expert tolerance limits.

5. Conclusions

Our algorithm for locating waveform boundaries in the ECG has been shown to be robust when noise is present. The multilead QRS detector retains the single-lead QRS information, rejecting those detections that can be identified as erroneous when compared with other leads, which are not possible to reject using only one lead. The availability of single-lead QRS detection marks permits

the use of a single-lead procedure for boundary detection; this procedure in turn permits recovery of the temporal projections of cardiac electrical activity. The final decision is taken on the basis that the larger temporal duration of a wave in one lead should not differ significantly from at least a subset of the other leads, allowing the algorithm to reject erroneous measurements due to noise and to detect the larger temporal projection of the wave that is the final objective of the method.

The difficulty of establishing an analytical rule that unambiguously locates the wave boundaries is solved in this work through a threshold that is adjusted by a constant (k) to be in the highest possible agreement with manual expert measurement. Using additional training data might lead to minor adjustments in the value of k, but we would not expect significant changes (since the ECG records of the CSE database already contain a large variety of ECG morphologies). We have shown that the measurements of clinically important intervals obtained using our algorithm are comparable in accuracy with those obtained by human experts. In particular, our algorithm agrees better with human expert measurements of the end of the T wave than the algorithms studied by the CSE. It is important to note, however, that these findings were obtained using only the limited number of ECG records included in the CSE database.

The information about waveform shape obtained with this method is very useful for ECG classification and cardiac diagnosis. The detection of the T-wave onset allows further measures of the ST segment (12). The interval values, wave amplitudes, patterns of P, QRS, and T waves, and wave presence or absence could be used to help cardiac diagnosis, presenting statistical and trend displays to the medical expert. This information can also serve as the input to a system that allows automatic cardiac diagnosis from ECG analysis. At present the algorithm works on either a VMS station or a UNIX machine using the digitized ECG records as inputs.

ACKNOWLEDGMENTS

The authors acknowledge Eudald Bogatell and David Vigo for their contributions to the implementation and validation of the method. They also thank George B. Moody from the Massachusetts Institute of Technology for his review and English editing of the paper which greatly improved it.

REFERENCES

- NYGÄRDS, M. E., AND SÖRNMO, L. Delineation of the QRS complex using the envelope of the e.c.g. Med. Biol. Eng. Comput. 21, 538 (1983).
- LAGUNA, P., THAKOR, N. V., CAMINAL, P., JANÉ, R., AND HYUNG-RO, Y. New algorithm for QT interval analysis in 24 hour Holter ECG: Performance and applications. *Med. Biol. Eng. Comput.* 28, 67 (1990).
- 3. WILLEMS, J. L., et al. Assessment of the performance of electrocardiographic computer programs with the use of a reference database, Circulation 71, 523 (1985).
- 4. WILLEMS, J. L., et al. Common standards for quantitative electrocardiography: Goals and main results. Methods Inf. Med. 29, 263 (1990).
- 5. WILLEMS, J. L., ZYWIETZ, C., ARNAUD, P., VAN BEMMEL, J. H., DEGANI, R., AND MACFARLANE, W. Influence of noise on wave boundary recognition by ECG measurement programs. *Comput. Biomed. Res.* 20, 543 (1987).

- LAGUNA, P., BOGATELL, E., JANÉ, R., AND CAMINAL, P. Automatic detection of characteristic points in the ECG. "Proceedings, Fourth International Symposium on Biomedical Engineering," Peñiscola, Spain, 1991, pp. 338-339.
- LAGUNA, P., VIGO, D., JANÉ, R., AND CAMINAL, P. "Automatic wave onset and offset determination in ECG signals: Validation with the CSE database. In "Computers in Cardiology," pp. 167-170. IEEE Society Press, Los Alamitos, CA, 1992.
- WILLEMS, J. L., ARNAUD, P., VAN BEMMEL, J. H., BOURDILLON, P. J., DEGANI, R., DENIS, B., GRAHAM, I., HARMS, F. M. A., MACFARLANE, W., MAZZOCCA, G., MEYER, J., AND ZYWIETZ, C. A reference data base for multilead electrocardiographic computer measurement programs. J. Am. Coll. Cardiol. 10(6), 1313 (1987).
- The CSE working party. Recommendations for measurement standards in quantitative electrocardiography. Eur. Heart J. 6, 815 (1985).
- PAN, J., AND TOMPKINS, W. J. A real-time QRS detection algorithm. IEEE Trans. Biomed. Eng. 32(3), 230 (1985).
- LYNN, P. A. Online digital filters for biological signals: Some fast designs for a small computer. Med. Biol. Eng. Comput. 15, 534 (1977).
- Webster, J. G. "Encyclopedia of Medical Devices and Instrumentation." Wiley, New York, 1988.
- 13. THAKOR, N. V., ZHU, Y., AND PAN, K. Ventricular tachycardia and fibrillation detection by a sequential hypothesis testing algorithm. *IEEE Trans. Biomed. Eng.* 37(9), 837 (1990).
- WILLEMS, J. L. Common standards for quantitative electrocardiography. CSE multilead atlas. Leuven. ACCO Publ. 1-341 (1988).
- ZYWIETZ, C., AND CELIKAG, D. Testing results and derivation of minimum performance criteria for computerized ECG-analysis. In Computers in Cardiology," pp. 97-100. IEEE Computer Society Press, Venecia, CA, 1992.