#### 大连理工大学 姓名: 学号:\_\_\_\_ 课程名称: 机器学习与模式识别 试 卷: <u>A</u> 院系: 授课院(系):信息与通信工程学院 考试日期:2020年08月19日 试卷共3页 级 \_\_\_班 2 3 1 4 标准分 31 12 22 20 得 分

#### 注意:

- 1. 考试题目为英文, 答题请用中文或者英文(不可混合);
- 2. 请在答题纸上作答, 并标清题号。
- 1. Please use 1-3 sentences to answer each of the following questions.
- (1) (6pts) List three major sources of classification error.
- (2) (5pts) List one drawback for using k-nearest neighbor method for density estimation.

总分

100

5

15

- (3) (5pts) Both principle component analysis and linear discriminant analysis are considered as feature reduction algorithms. What is the fundamental difference between them?
- (4) (5pts) What is the curse of dimensionality?
- (5) (5pts) Use one sentence to describe No Free Lunch Theorem.
- (6) (5pts) Use one sentence to describe Ugly Duckling Theorem.
- In the following algorithms, which can be considered as unsupervised 2. approaches? Which are supervised ones? Please circle your answers. (3 pts each, 12 pts in total)

Adaptive boosting (unsupervised supervised) k-Means clustering (unsupervised supervised) Support vector machine (unsupervised supervised) Principle component analysis (unsupervised supervised)

# 3. k-Means Clustering Algorithm (22 pts).

Supporse you are given 11 samples in a 2D plane:

$$(1,1)$$
  $(1,5)$   $(2,1)$   $(3,1)$   $(5,2)$   $(3,4)$   $(4,4)$   $(2,5)$   $(1,7)$   $(2,8)$   $(4,6)$ 

(1) (16 pts) Use k-Means algorithm to divide the given samples into 2 clusters. Please demonstrate **the first iteration** of the implementation procedure and provide the resulting centroids after the first iteration.

Initial centroids: (1,1) for cluster 1; (1,6) for cluster 2.

(2) (6 pts) List two weaknesses of k-Means algorithm

### 4. Evaluating the Classifiers (20 pts).

- (1) (6pts) What is the major difference between Jackknife algorithm and the simple cross-validation algorithm?
- (2) (6pts) What is the advantage of Bootstrap algorithm comparing to Jackknife algorithm?
- (3) (8pts) Receiver Operating Characteristic (ROC) curve can also be used to evaluate classifiers. In a given pattern recognition application, suppose we have tested two classifiers, and obtained their ROC curves as shown in Fig.1. In this application, which classifier performs better? Why?

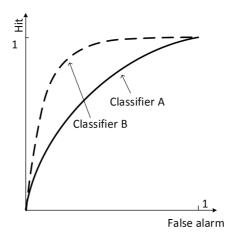


Figure 1: ROC curves of two classifiers.

# 5. Bayesian Decision Theory (15 pts).

Consider a one-dimensional two-category classification problem. The class-conditional densities of these two categories,  $\omega_1$  and  $\omega_2$ , are given by

$$p(x|\omega_1) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x-2)^2}{2}\right\}, x \in (-\infty, +\infty)$$
$$p(x|\omega_2) = \begin{cases} 1/4 & 0 \le x \le 4\\ 0 & \text{otherwise} \end{cases}.$$

- (1) (5pts) Suppose the two categories have equal priors. Show the decision boundaries and decision regions using maximizing-a-posterior decision rule.
- (2) (5pts) Suppose the two categories have equal priors and the loss function is given by

$$\lambda(\omega_1|\omega_2) = 10$$
,  $\lambda(\omega_2|\omega_1) = 20$ ,  $\lambda(\omega_1|\omega_1) = 0$ ,  $\lambda(\omega_2|\omega_2) = 0$ ,

where  $\lambda(\omega_i|\omega_j)$  denotes the loss for deciding  $\omega_i$  when the state of nature is  $\omega_j$ . Show the decision boundaries and decision regions using minimizing-the-risk decision rule.

(3) (5pts) Under the assumption of equal priors in both categories, we still use minimizing-the-risk decision rule, but change the loss function to

$$\lambda(\omega_1|\omega_2) = \alpha$$
,  $\lambda(\omega_2|\omega_1) = \beta$ ,  $\lambda(\omega_1|\omega_1) = 0$ ,  $\lambda(\omega_2|\omega_2) = 0$ ,

where  $\alpha$  and  $\beta$  are two positive constants, and  $\alpha > \beta$ . Will the decision region of category 1 grow bigger or smaller compared to that in (2)? Why?