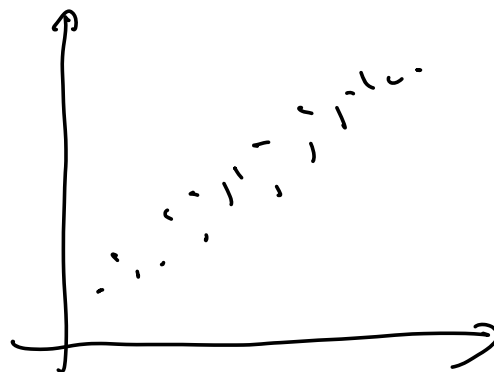


# Polynomial Regression

$\Rightarrow$  Multi-col  $\Rightarrow$  VIF  $\rightarrow$   $\uparrow \searrow \rightarrow$  bad col  
 $\downarrow \rightarrow$  good col

$\Rightarrow$  SGD / mini-Batch GD



$x$			$y$
$c_0$	$c_1$	$c_2$	
1	-	-	
1	-	-	
1	-	-	

$\rightarrow$  predict( $X$ , weight)  
 $\text{np.dot}(x, \text{weights}) \rightarrow w^T \cdot x$

$\rightarrow$  gradient( $x, y, \text{weight}$ )  
 $y - \text{pred}$   
 $\text{grad}$

$x(y - y_{\text{pred}})$

$\downarrow$   
 $\text{np.dot}(x, y - y_{\text{pred}})$   
 $\downarrow$   
 $x \cdot \text{transposed}$

$w^T x$

$x^T w$

$\text{np.dot}(w, x)$

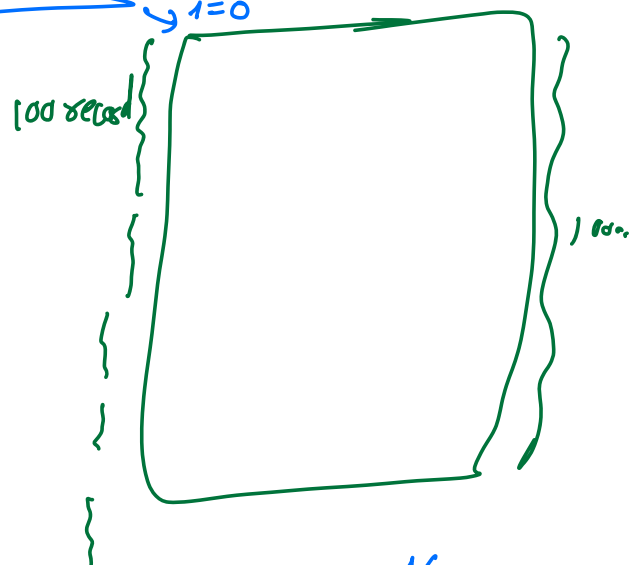
$\text{np.dot}(x, w)$

```
def cost(x, y, weight):
    y_pred =
    e =
```

```
def create_mini_batches(x, y, batch_size):
    data = hstack(x, y)
    np.random.shuffle(data)
    count = —————→ i=0
```

for → 10 times

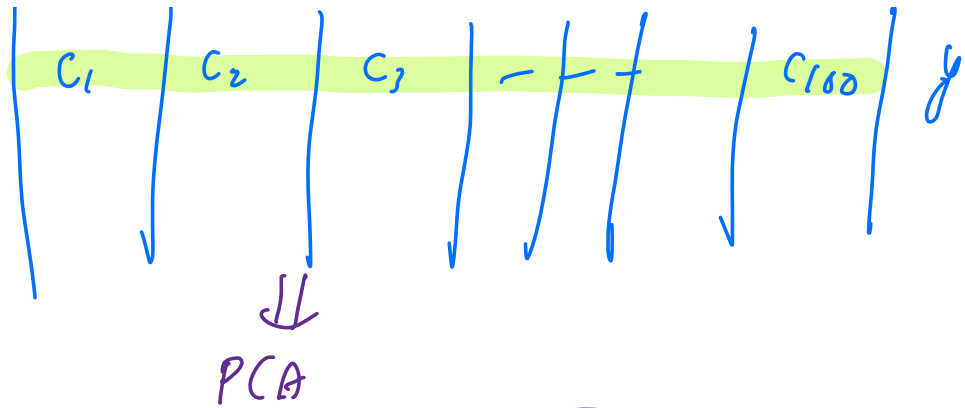
i \* batch : (i+1) \* batch  
 0 \* 100 : (1) \* batch  
 0 : 100



1100 // 100  
 ⇒

100 - 199

RFE



RFE  $\Rightarrow$

$\Downarrow$

10 columns

$\Downarrow$

p-value  
mult

100 columns  $\Rightarrow$  LR

$\Downarrow$   
 $R^2$  Adj  $R^2$

$\Downarrow$   
15 col

Adj  $R^2 = 0.8$

$\Downarrow$   
10 col

Adj  $R^2 = 0.9$

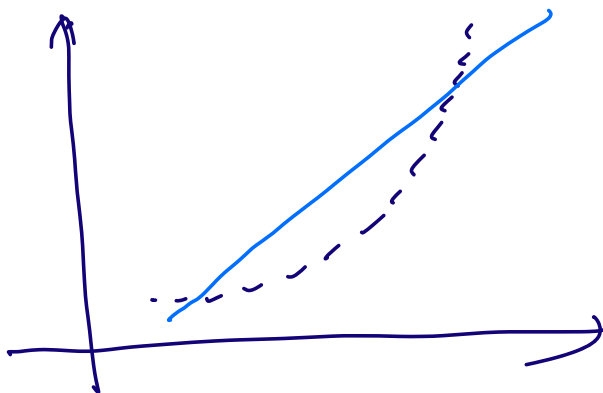
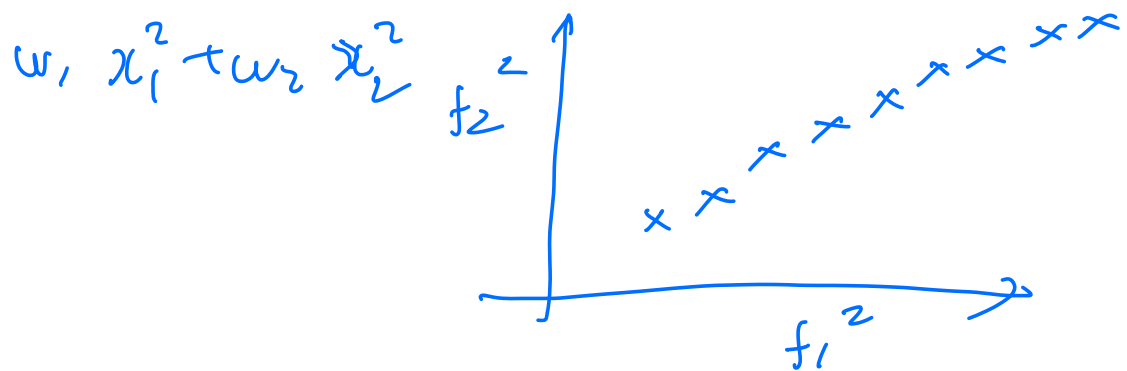
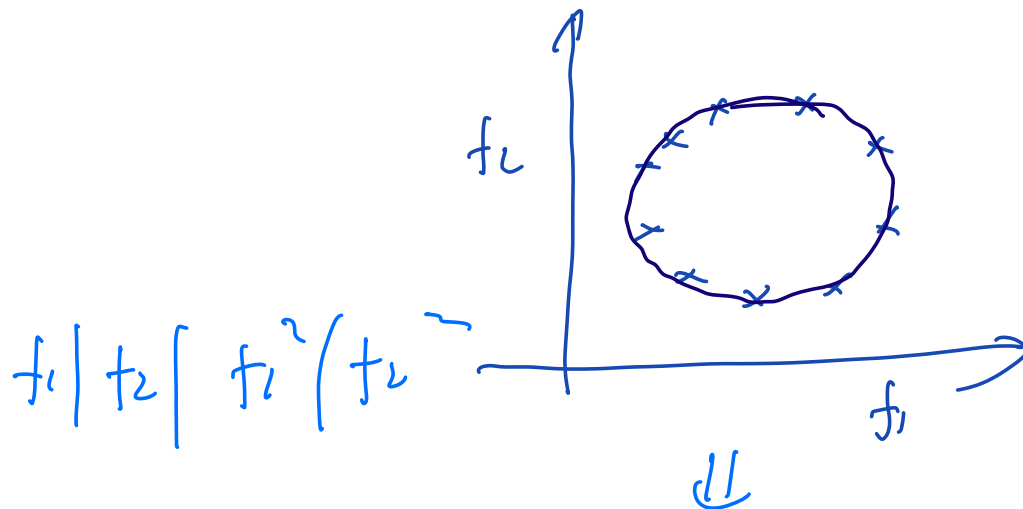
$\Downarrow$

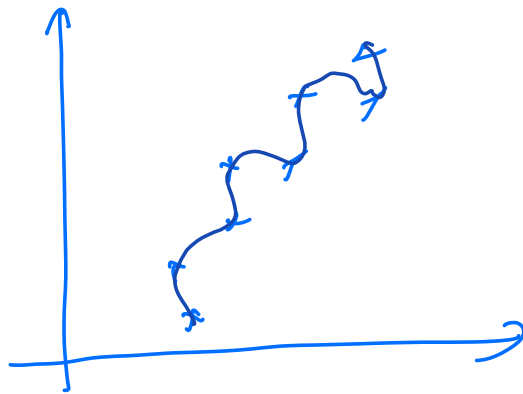
8 col

Adj  $R^2 = 0.86$

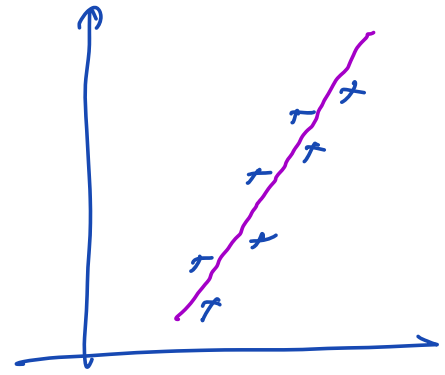
break: 12 : 0.5

# Polynomial Regression





$f_1, f_1^2, f_1^3$



$f_1$

$R^2 \rightarrow 90\%$

## ① Generalization

test  $\rightarrow R^2$

## ② Occum razor

Linear:  $f_1$

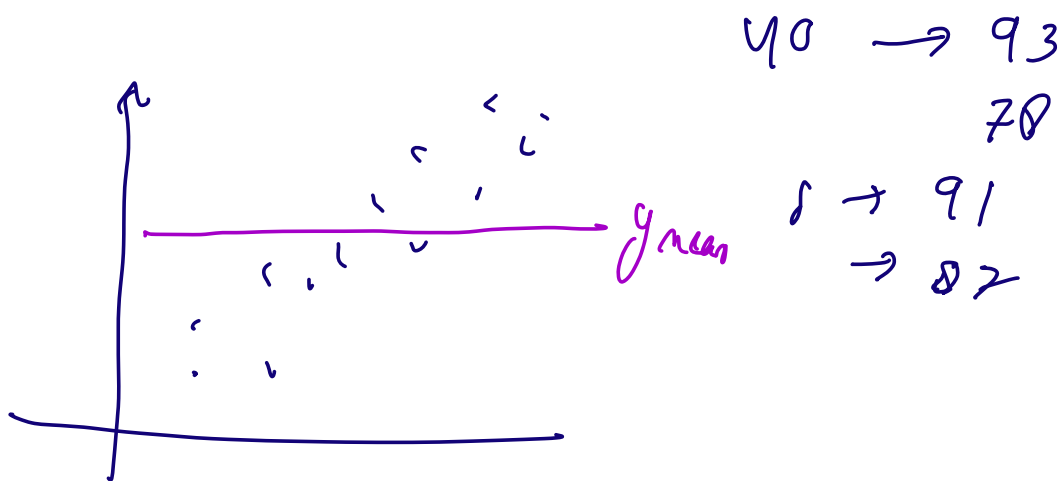
Quard:  $f_1, f_1^2$

Cubic:  $f_1, f_1^2, f_1^3$

Occ	L	Q	C
Test err	H	L	L

Train  $\uparrow$   $\Rightarrow$  over fitting  
 Test  $\downarrow$

Train  $\downarrow$   $\Rightarrow$  under fit  
 Test  $\downarrow$



underfit	$\rightarrow$	$D_{Tr}$ 100	$D_{T_s}$ 120
$\checkmark$	$\Rightarrow$	20	30
overfit	$\rightarrow$	0.1	50

$$y_i = w_0 + w_1 x_1 + w_2 x_2 + w_3 x_3 + w_4 x_4$$

$w_1 \neq w_2 \neq w_3 \neq w_4 \neq 0$   
 overfit

$w_2$