

# Shapley Analysis

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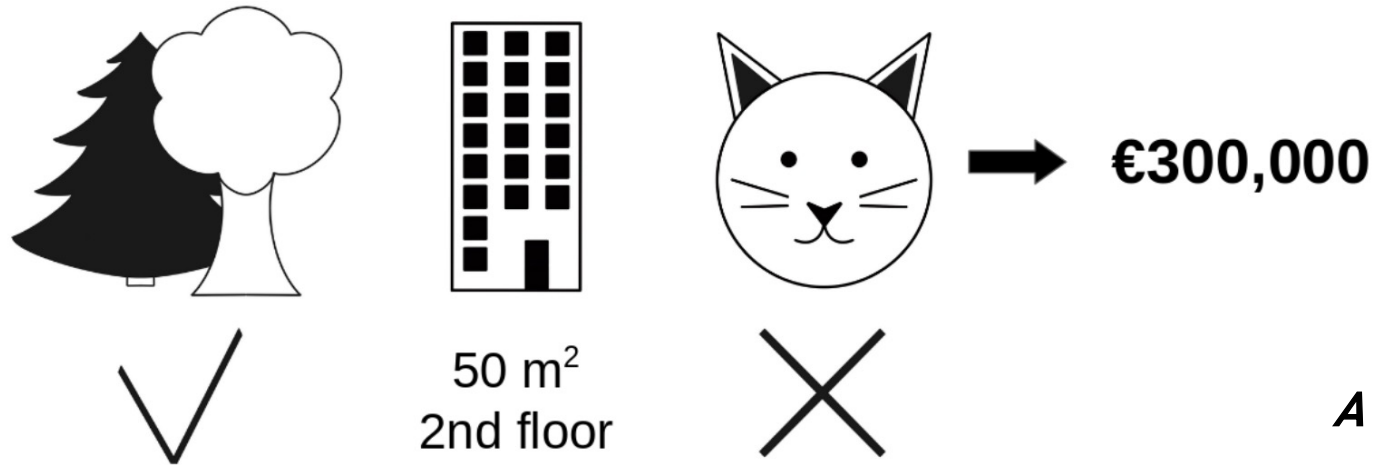
# Shapley Values

**Goal:** Explain feature importances and individual feature values

**Origin:** Shapley values are a method from coalitional game theory.

“A prediction can be explained by assuming that each feature value of the instance is a “player” where the prediction is the payout.”

**Example:** Predict Apartment Prices | Average Prediction for all instances: **€310,000**

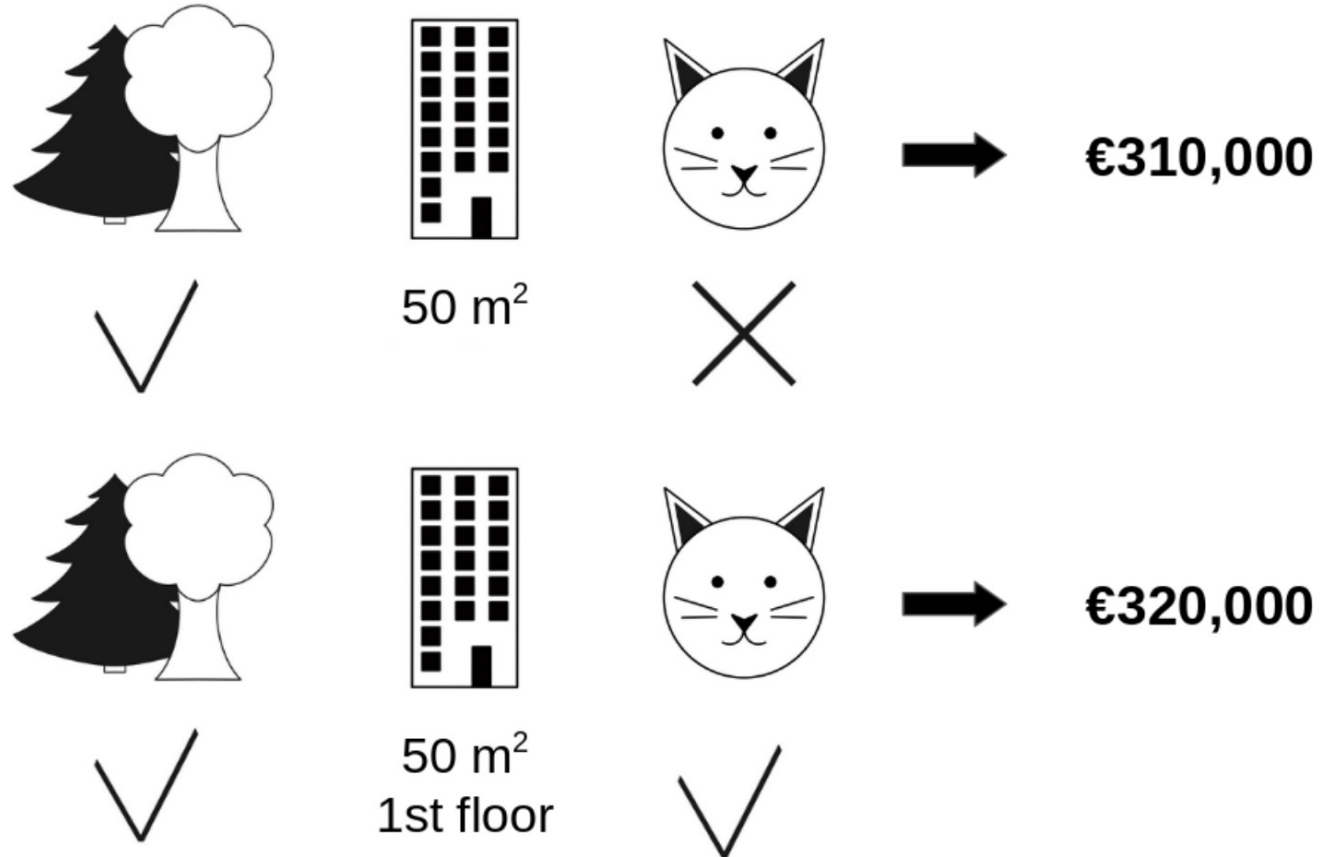


**Interpretable Machine Learning**  
*A Guide for Making Black Box Models Explainable*

The Shapley value is the average marginal contribution of a feature value across all possible coalitions.

**Evaluate: Cat-banned feature**

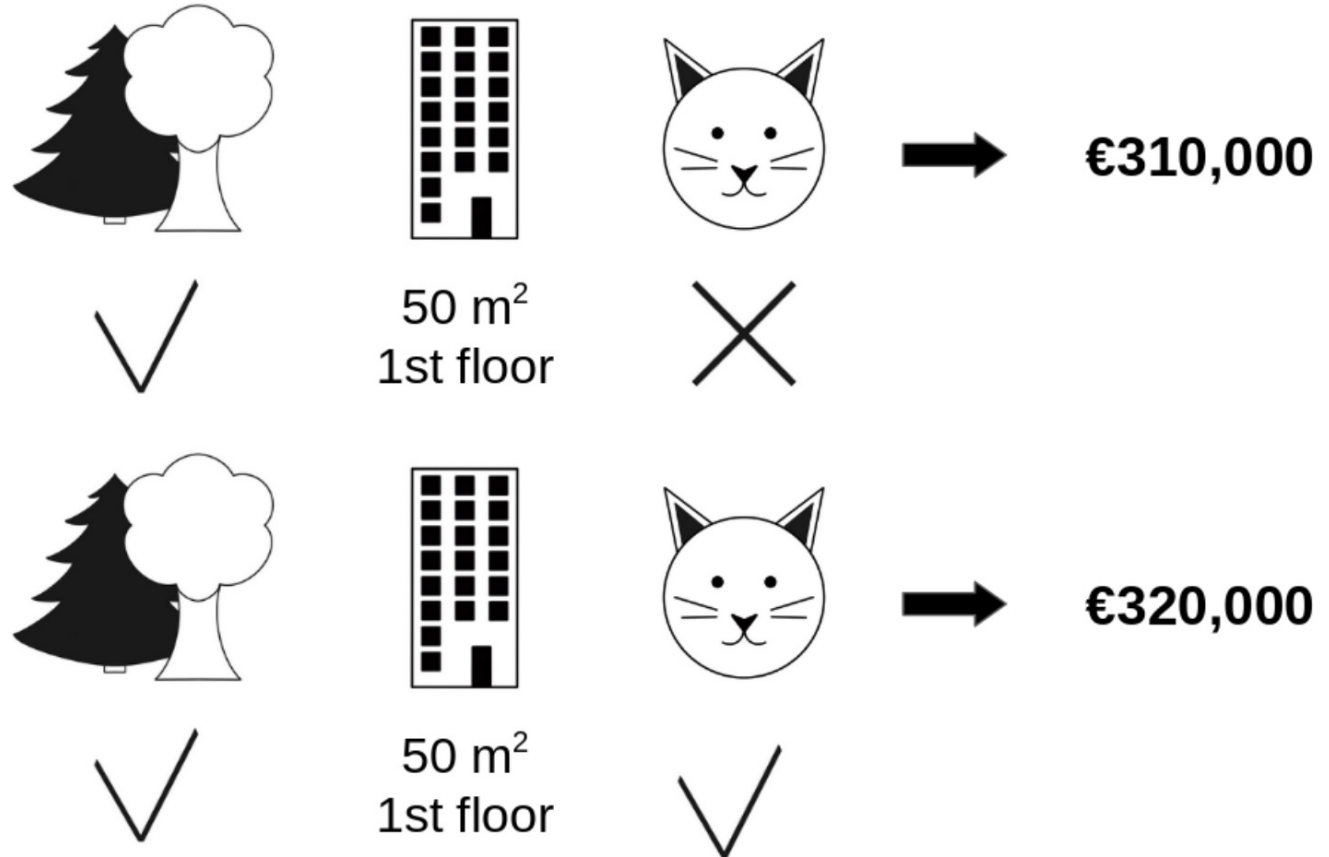
**If feature not in coalition:**  
randomly draw sample from data  
(1<sup>st</sup> floor)



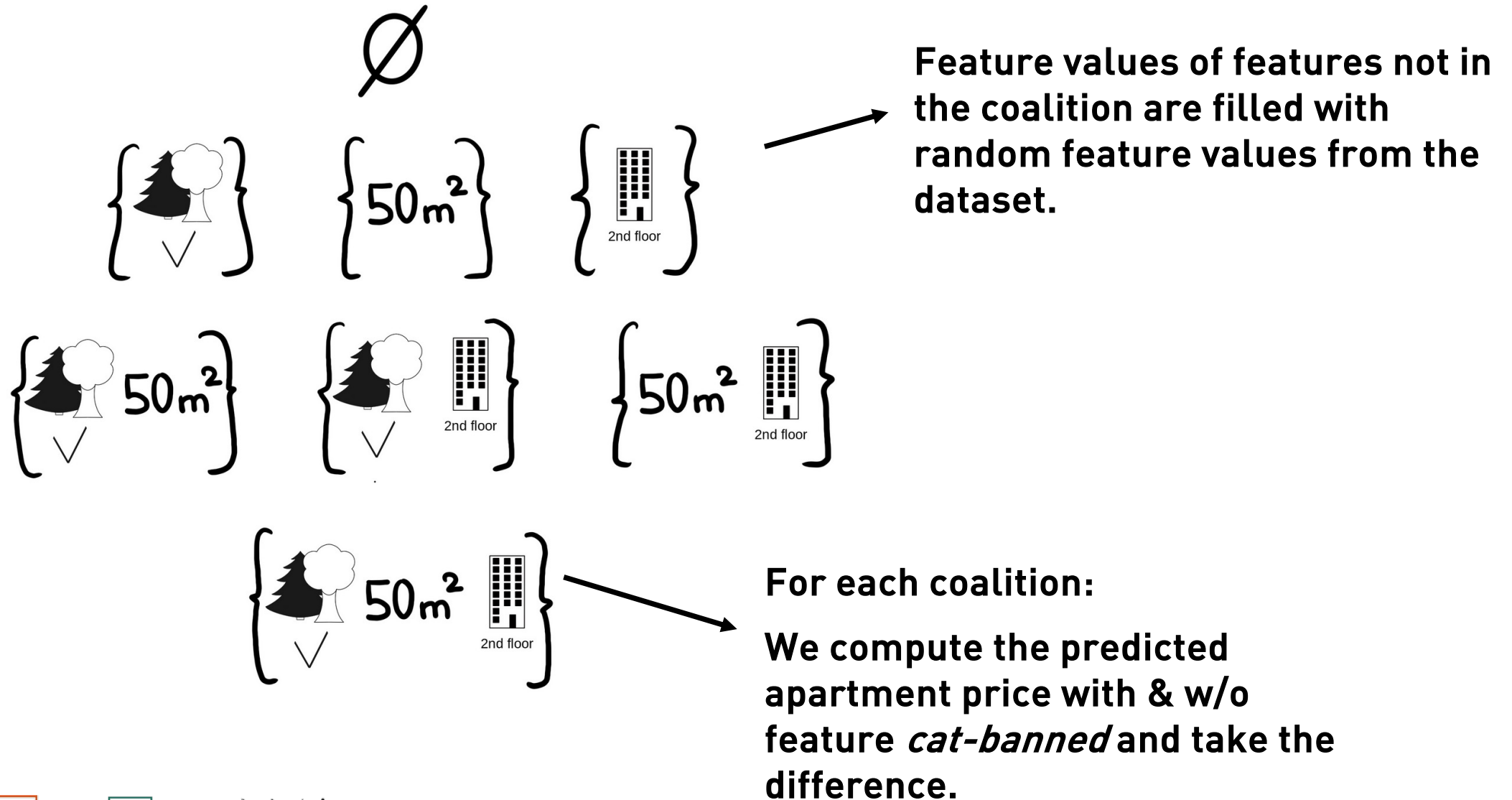
# The Shapley value is the average marginal contribution of a feature value across all possible coalitions.

**Evaluate: Cat-banned feature**

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We repeat this computation for all possible coalitions.



# Example: Bike rental dataset (Random Forest model)

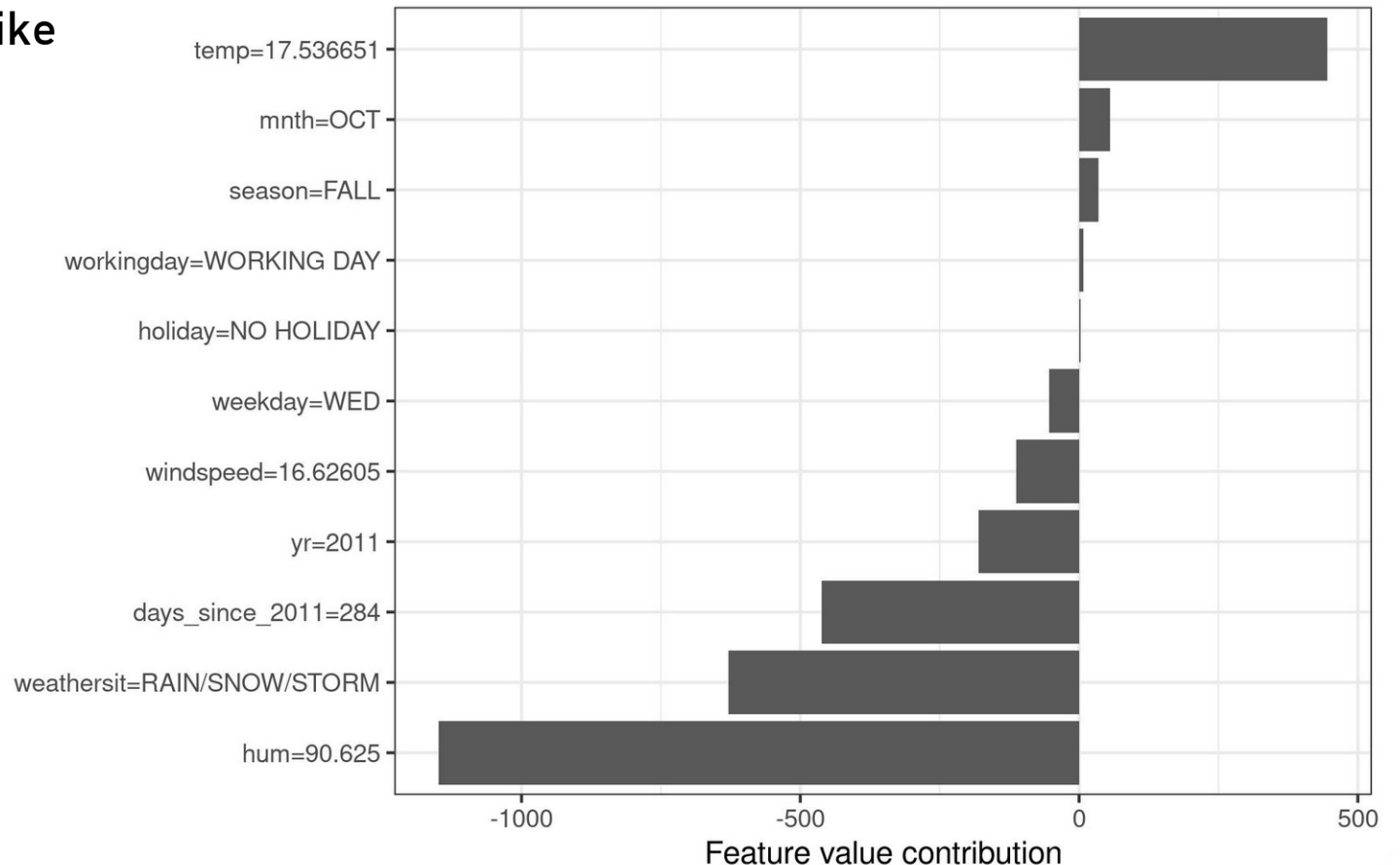
Prediction for one day: Day 285

Weather & humidity lead to a decrease in bike rentals

$$\phi_j(val) = \sum_{S \subseteq \{1, \dots, p\} \setminus \{j\}} \frac{|S|! (p - |S| - 1)!}{p!} (val(S \cup \{j\}) - val(S))$$

$$val_x(S) = \int \hat{f}(x_1, \dots, x_p) d\mathbb{P}_{x \notin S} - E_X(\hat{f}(X))$$

Actual prediction: 2409  
Average prediction: 4518  
Difference: -2108



# TUTORIAL





Thank you!