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Physics I E

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Good Work!

6 (2/2) Lecture questions:

0.5 1) For an ideal coil  $\underline{3} = jL\omega$

0.5 For an ideal capacitor  $\underline{3} = \frac{1}{Cj\omega}$

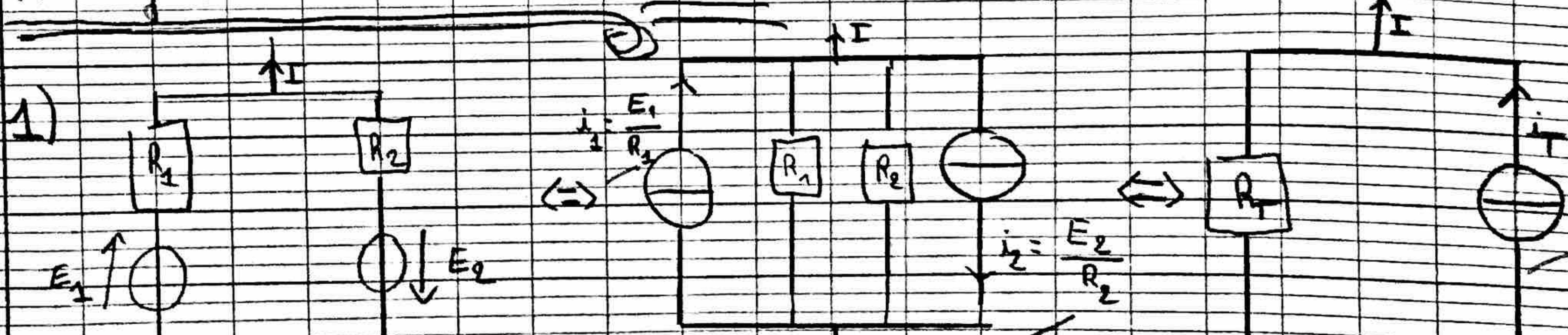
2)  $I = S_1(E) = 4V\sqrt{2} \cos(100\pi t + \frac{\pi}{4})$

0.5 Hence  $U_{m\text{m}} = 6V\sqrt{2}$  we know that  $U_{\text{pp}} = 20\text{m} = 8V\sqrt{2}$  (diminution)

0.5 here  $\omega = 100\pi \text{ rad.s}^{-1}$  since  $f = \frac{\omega}{2\pi}$ ,  $f = 50\text{Hz}$ .  
( $\Phi = \frac{\pi}{4}$  rad,  $T = 0.02\text{s}$ ).

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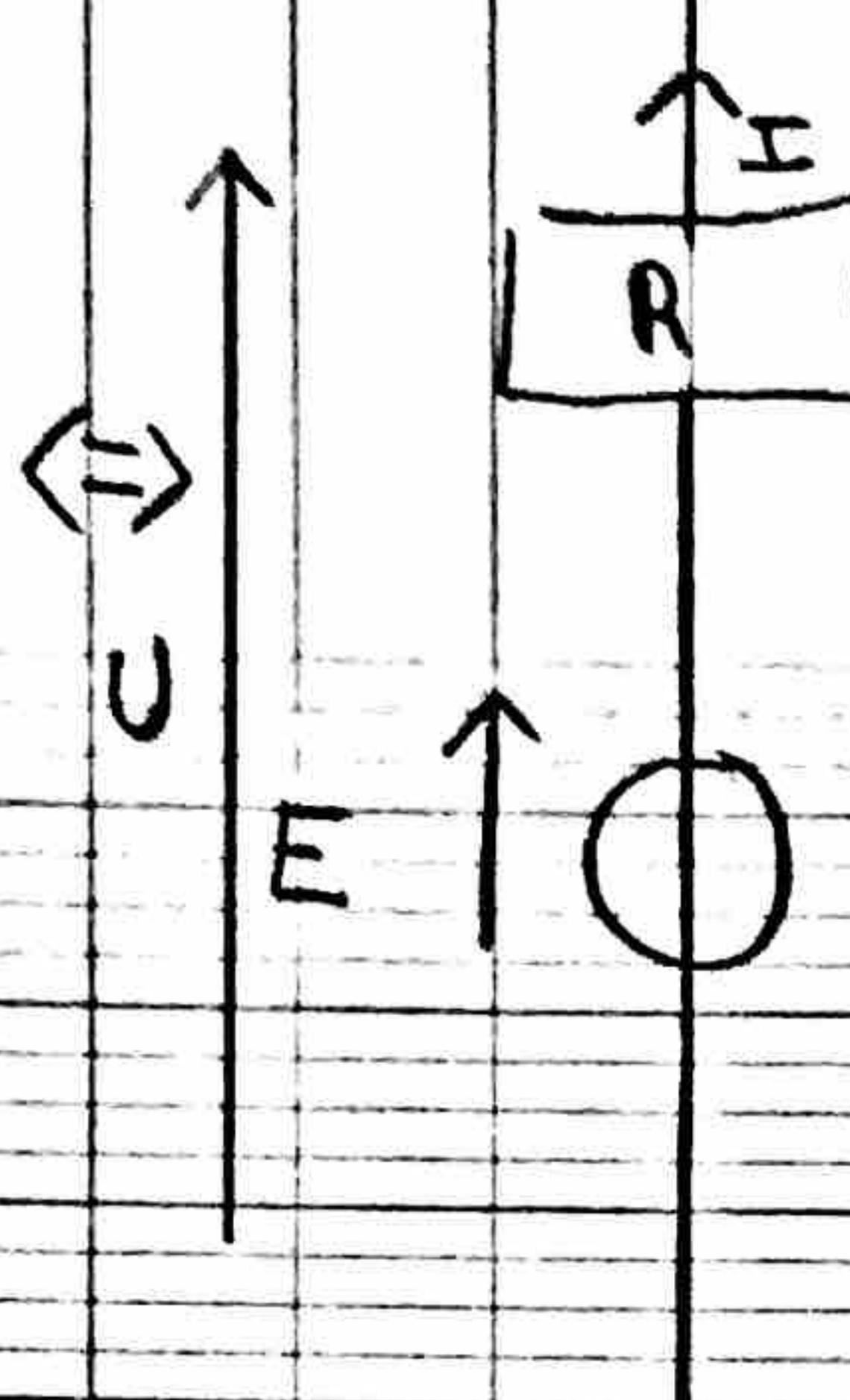
Assignment 1: "Zener diode"



$$\text{with } R_T = \frac{R_1 R_2}{R_1 + R_2}$$

$$I_T = \frac{E_1}{R_1} - \frac{E_2}{R_2}$$

(1)



$$\text{with } R_{\text{eq}} = \frac{R_1 \times R_2}{R_1 + R_2}$$

$$\text{and } E = E_T = i_T \times R_T$$

$$= \left( \frac{E_1}{R_1} - \frac{E_2}{R_2} \right) \times \frac{R_1 R_2}{R_1 + R_2}$$

$$E = \frac{E_1 R_2 - E_2 R_1}{R_1 + R_2}$$

2) In Passive sign convention (PSC)

$$U = E - RI \quad (\text{see figure above for conventions.}) \quad \text{Yes, thank!}$$

0.5  
Hence  $I = \frac{E - U}{R}$  since  $E = 1.5V$  and  $R = 50\Omega$

$$I = 0.03 - \frac{U}{50} \quad \text{Hence the I-V curve of the generator and the resistor is a straight line.}$$

When  $U = 0V$   $I = 0.03 A = 30mA$

$U = 1V$   $I = 0.01 A = 10mA$

0.5  
(Cf graph appendix).

We find  $U = 0V$  and  $I = 0.03A$  as operating point.

Yes, you're right

ders true since the  
the operating points are  
so we calculate. → The graphical method implies a lot of uncertainties especially  
since here the I-V curve of the diode is thick?

Thick?

3) If now the terminal of the diode are switched  
we still have the same I-V curve for the generator and  
the resistor but the diode one is not the same anymore.

We know now that if  $i < 0$   $u = 0$  Excellent!

and if  $i > 0$   $u = 1$

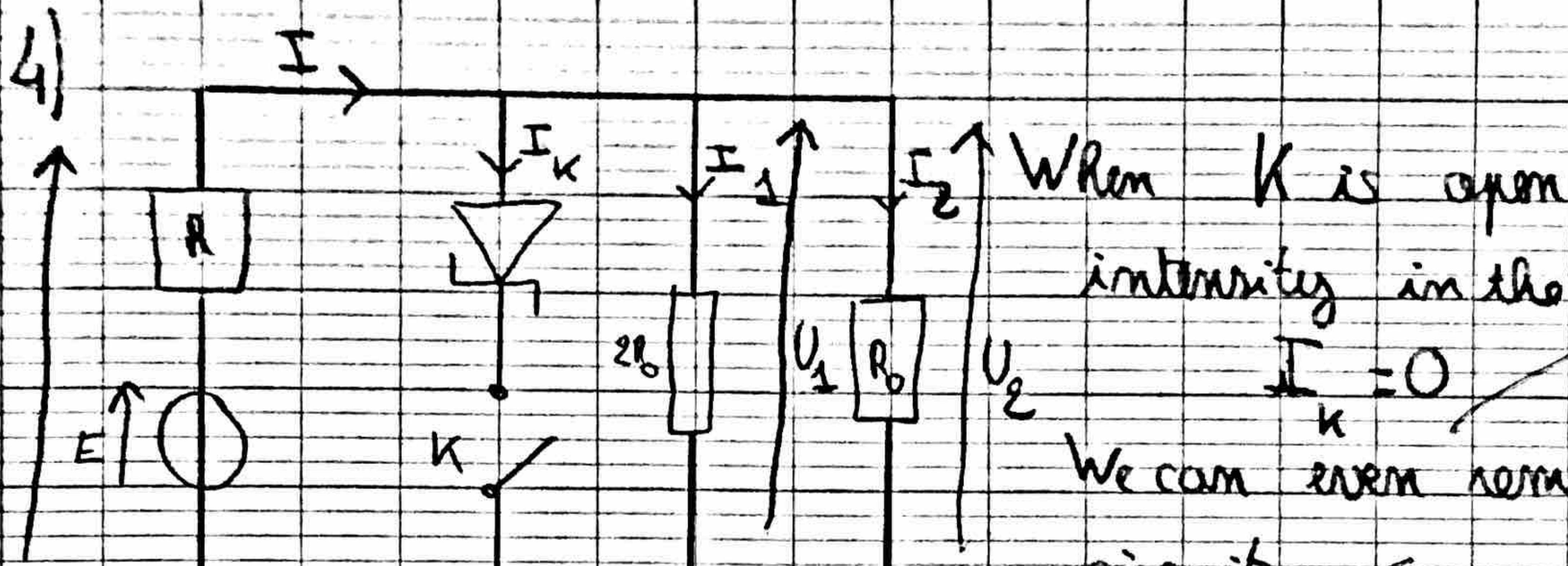
(Cf graph appendix 2).

0.75

The new operating points are  $I = 10mA$  and  $U = 1V$

(Once again, in this method the uncertainties are higher  
than with a direct calculus). Yes indeed.

BONUS: +0.25 Very good comments and specifications plus all equations etc



When K is open there is no intensity in the branch as  $I_K = 0$

We can even remove it from the circuit.

Then thanks to Kirchhoff's current law (KCL)

$$\text{we know that } I = I_1 + I_2 \quad (1)$$

Moreover in PSC we know that  $I = 0,03 - \frac{U}{50}$  (2) numerical values with literal expression. Keep the latter one!

From Kirchhoff's voltage law (KVL) we have  $U = U_1 = U_2$  (3)

$$\text{and in PSC } U_1 = 2R_0 I_1 \quad (4) \quad \text{and } U_2 = R_0 I_2 \quad (5)$$

Since  $U_1 = U_2$  (3) we have  $2R_0 I_1 = R_0 I_2 \quad (4) \wedge (5)$

$$\text{hence } \frac{I_1}{I_2} = \frac{R_0}{2R_0} = \frac{1}{2}$$

~~Non homogeneous expression!!~~

$$\text{From (1) we have } I = \frac{I_1 + I_2}{R_0} = \frac{\frac{1}{2}I_2 + I_2}{R_0} = \frac{3}{2}I_2 \quad \cancel{...}$$

I did not manage to finish these 2 questions because of time but the method is the same for both (except that for the 5<sup>th</sup> question we need to take it into account). Yes so the method won't be the same at the end.

I first need to draw a scheme and define all the conventions.

Then thanks to KCL I can write the intensity in terms of other (I need 2 equat° for 4. and 3 for 5<sup>th</sup> question) Not exactly.

Then with KVL I obtain other equation and I can then solve a system to find all the intensity.

Yes, this is indeed the method you should have used for this question 4.

Method question

4 and 5

specified.

(2)

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Assignment 2

1) For  $t > 0$

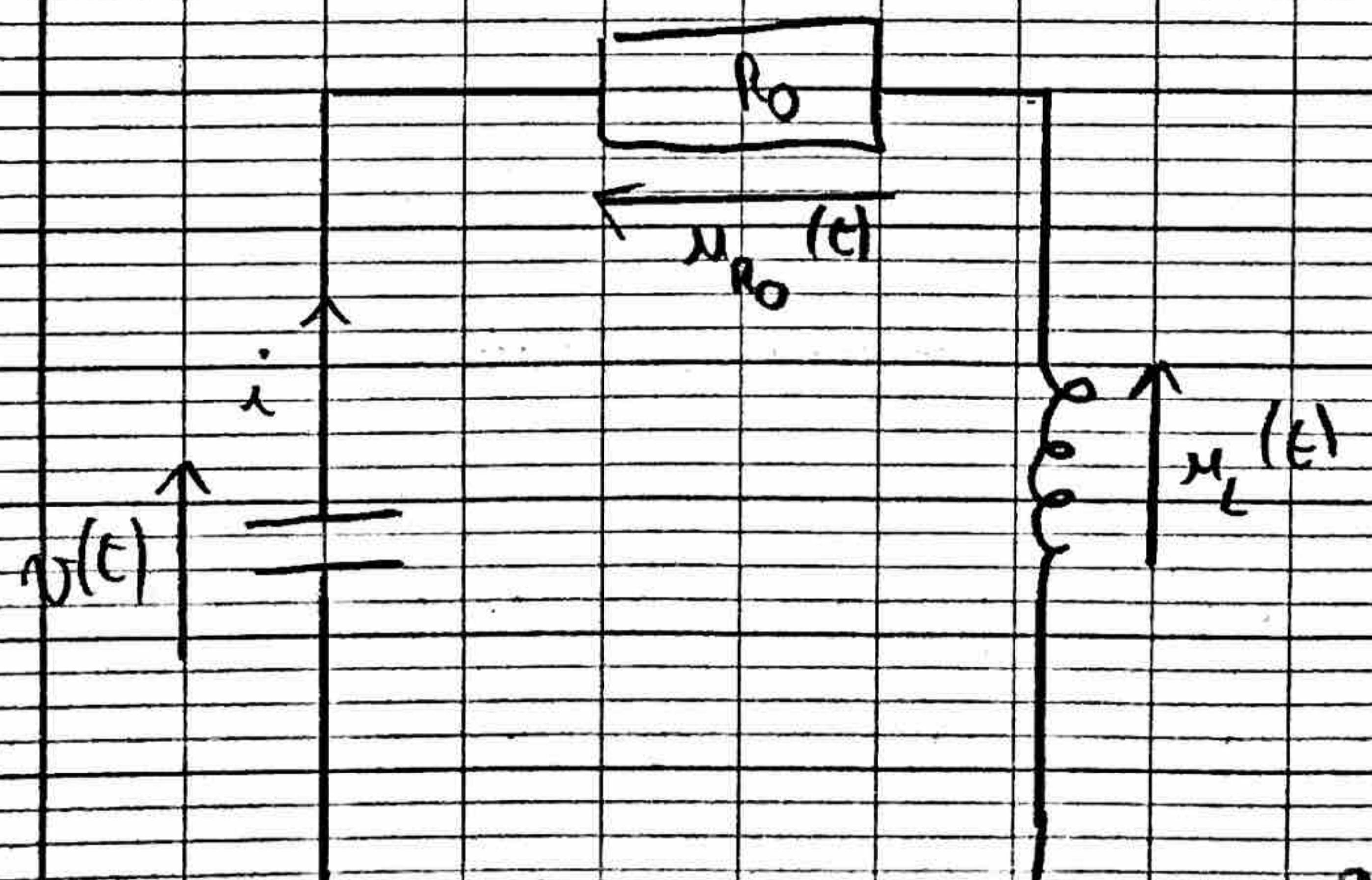
we have this circuit (with the capacitor charged).

0.5

0.5

0.25

0.25



From KVL we have

$$v(t) = u_{R_0}(t) + u_L(t) \quad (1)$$

with  $i(t) = -C \frac{dv}{dt}$   $\frac{di}{dt}$  No here  
this is  
ASC! PSC

and  $u_L(t) = L \frac{di}{dt} \quad (3)$

and  $u_{R_0} = i(t) \times R_0 \quad (4)$

Ques 2) From question 1 we have: from (1), (3), (4).

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$$v(t) = i(t) \cdot R_0 + L \frac{di}{dt} \Leftrightarrow i(t) \cdot R_0 + L \frac{di}{dt} - v(t) = 0$$

0.5

then from (2).  $-LC \frac{d^2v}{dt^2} - CR_0 \frac{dv}{dt} - v(t) = 0$

$$\Leftrightarrow LC \frac{d^2v}{dt^2} + CR_0 \frac{dv}{dt} + v(t) = 0 *$$

0.5

$$\Leftrightarrow \frac{d^2v}{dt^2} + \frac{R_0}{L} \frac{dv}{dt} + \frac{1}{LC} v(t) = 0$$

$$\Leftrightarrow \frac{d^2v}{dt^2} + 2\zeta \frac{dv}{dt} + \omega_0^2 v(t) = 0$$

0.5

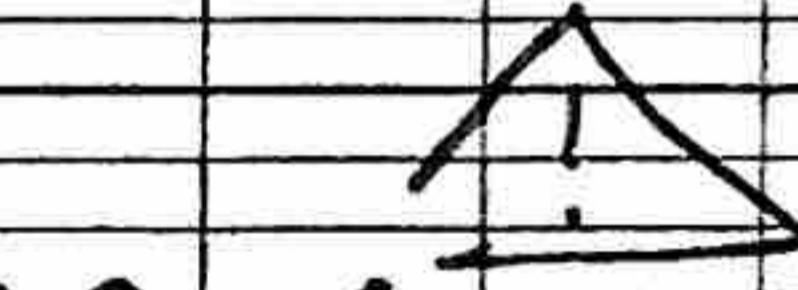
with  $\zeta = \frac{R_0}{2L}$  and  $\omega_0 = \frac{1}{\sqrt{LC}}$

dimension equation + equation

\* This equation is Homogeneous because:

$$\cancel{T^2 \times [v]} + T \times \cancel{[v]} + [v] = 0$$

BONUS: +0.25



the rest is only

change of writing. yes

But the constant to find feels weird.

which constant?

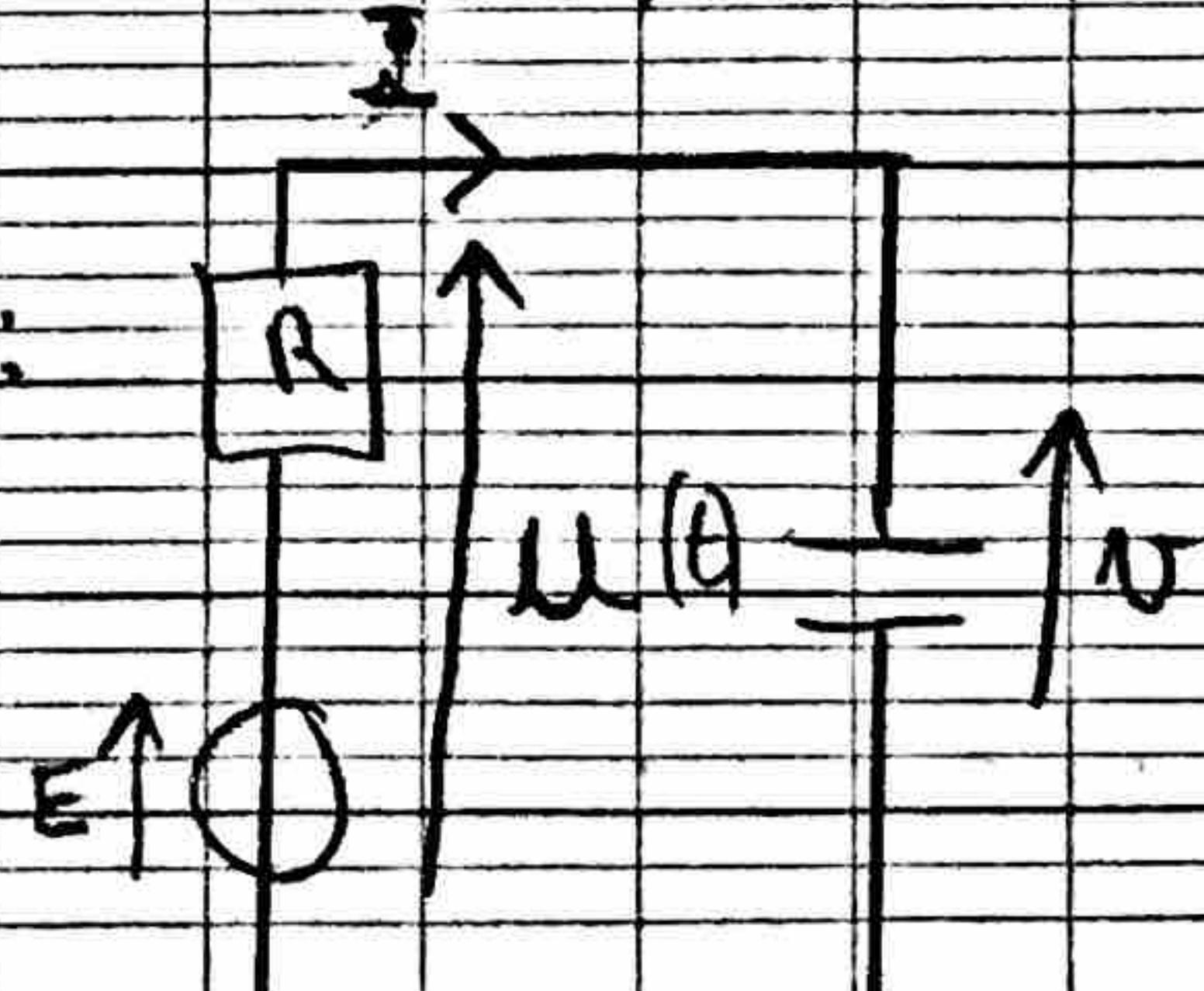
$$3) v(t=0) = v(t=0) \stackrel{!}{=} u(t) = E - R \cdot i(t) \quad \text{Yes}$$

$\rightarrow$  voltage across a capacitor is constant as a function of

0.25

time.

at time  $t < 0$ :



$$0.25 \quad i(t=0^+) = i(t=0^-) = 0 \quad \text{since } u(t) = i(t) R$$

$\hookrightarrow$  continuous function of time

$$\text{we have} \quad u(t=0^+) = u(t=0^-) = 0 \quad \times$$

$\hookrightarrow$  continuous function of time

$$u_L(t=0^+) = u_L(t=0^-) = 0 \quad \times \quad \text{since at } t < 0 \text{ switch was open.}$$

$\hookrightarrow$  voltage across a coil is a continuous function of time. Noooo! For a coil, this is the intensity, which is continuous function of time.

4) We know that a pseudo period corresponds to  $T$  as shown below:



0.5 Graphically we obtained  $T = 70 \mu\text{s}$

But we have different sources of uncertainties (random and systematic).:

$\rightarrow$  uncertainties on the position of  $U_{\frac{1}{2}}$  more (estimated at  $2 \mu\text{s} \times 2$ )

$\rightarrow$  uncertainty on the ruler (estimated at  $1 \mu\text{s} \times 2$ )

$$\text{Hence } \Delta T = 6 \mu\text{s}$$

0.5

Hence  $\bar{T} = (70) \pm 6 \mu\text{s}$  (High uncertainty due to graphical method).

5) Graphically

$$A = ?$$

$$\Phi = ?$$

$$6) T \approx \frac{2\pi}{\omega_0} \Leftrightarrow \omega_0 = \frac{2\pi}{T} = 89759 \text{ Unit?}$$

Never give a numerical result without its uncertainty.

We know from question 2) (if it is correct) that:

$$0.25 \quad \omega_0 = \frac{1}{VLC} \Leftrightarrow L = \frac{1}{\omega_0^2 \times C}$$

$$0.25 \quad L_{\max} = \frac{1}{\omega_{\min}^2 \times C_{\min}} = \frac{1}{\omega^2 \times (C + \Delta C)} = 0,0137 \text{ H} \times$$

(method) This can also be minor max.

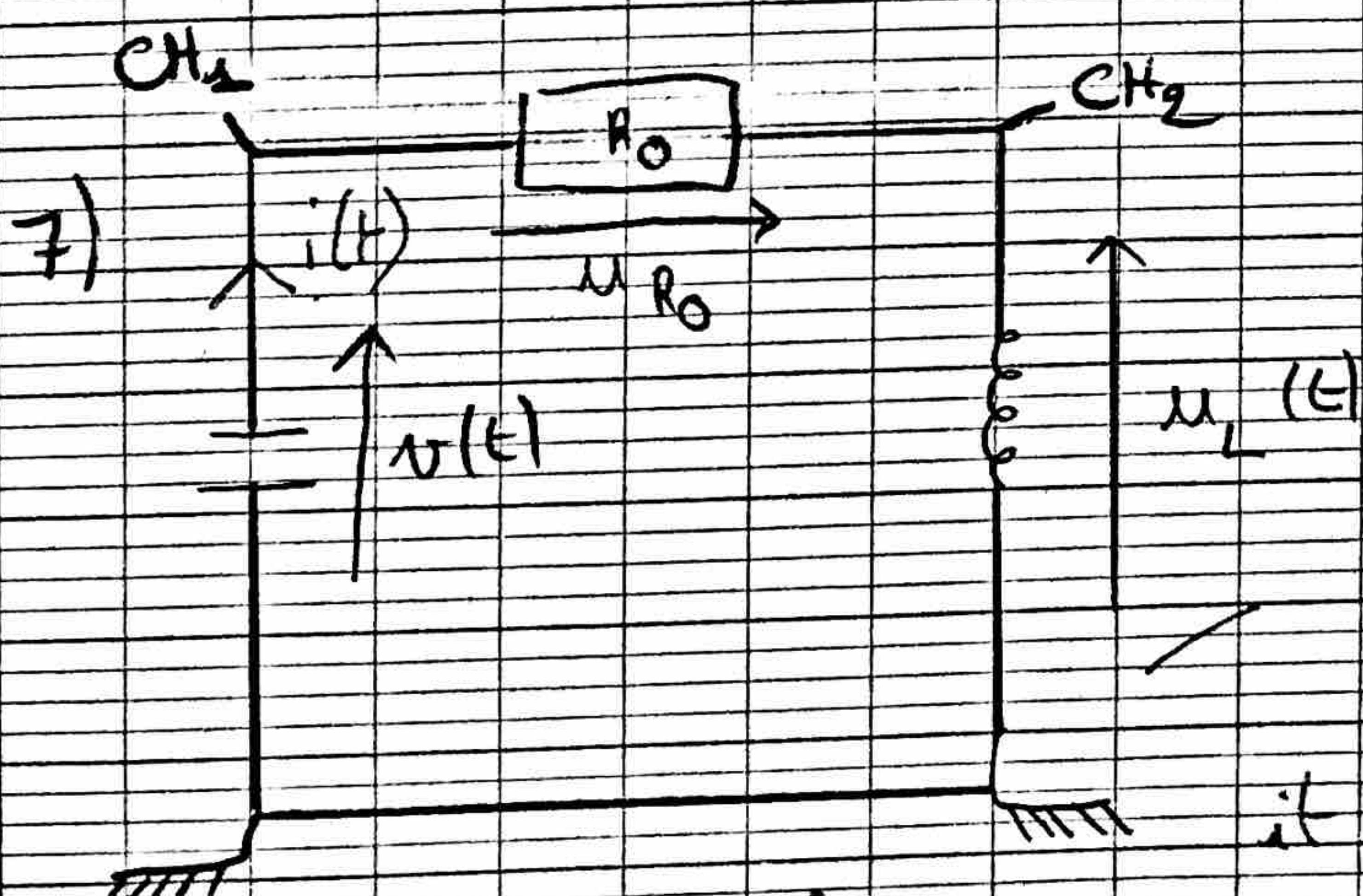
$$0.25/0.5 \quad L_{\min} = \frac{1}{\omega_{\max}^2 \times C_{\max}} = \frac{1}{\omega^2 \times (C - \Delta C)} = 0,0113 \text{ H} \times$$

$$L = \frac{L_{\max} + L_{\min}}{2} = 0,0125 \text{ Unit?}$$

$$\Delta L = \left| \frac{L_{\max} - L_{\min}}{2} \right| = 1,2 \cdot 10^{-3}$$

(Uncertainty is a bit higher because the equation used at the beginning is not a perfect one).

$$0.25 \quad L = (11,3 \pm 1,2) \text{ mH}$$



We can visualize  $v(t)$  directly in Channel 1.

As for  $i(t)$  we can visualize it through the ratio function (careful at the scale used) by doing  $\text{CH}_2 - \text{CH}_1$

we would obtain the signal corresponding to

$$u = i(t) R_0 \cdot \times$$

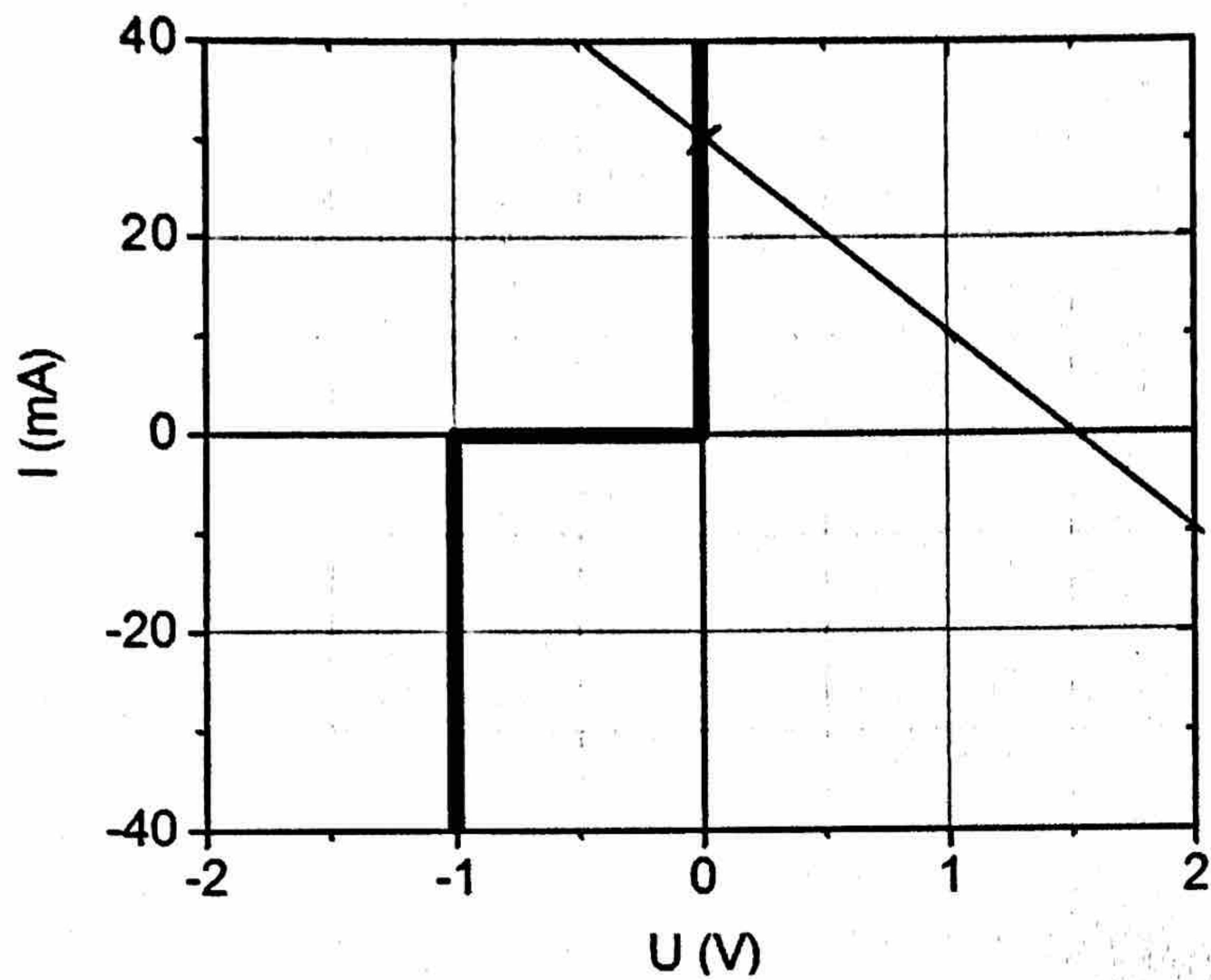
You have to do  $\text{CH}_1 - \text{CH}_2$  to get  $+i R_0$ !

(4)

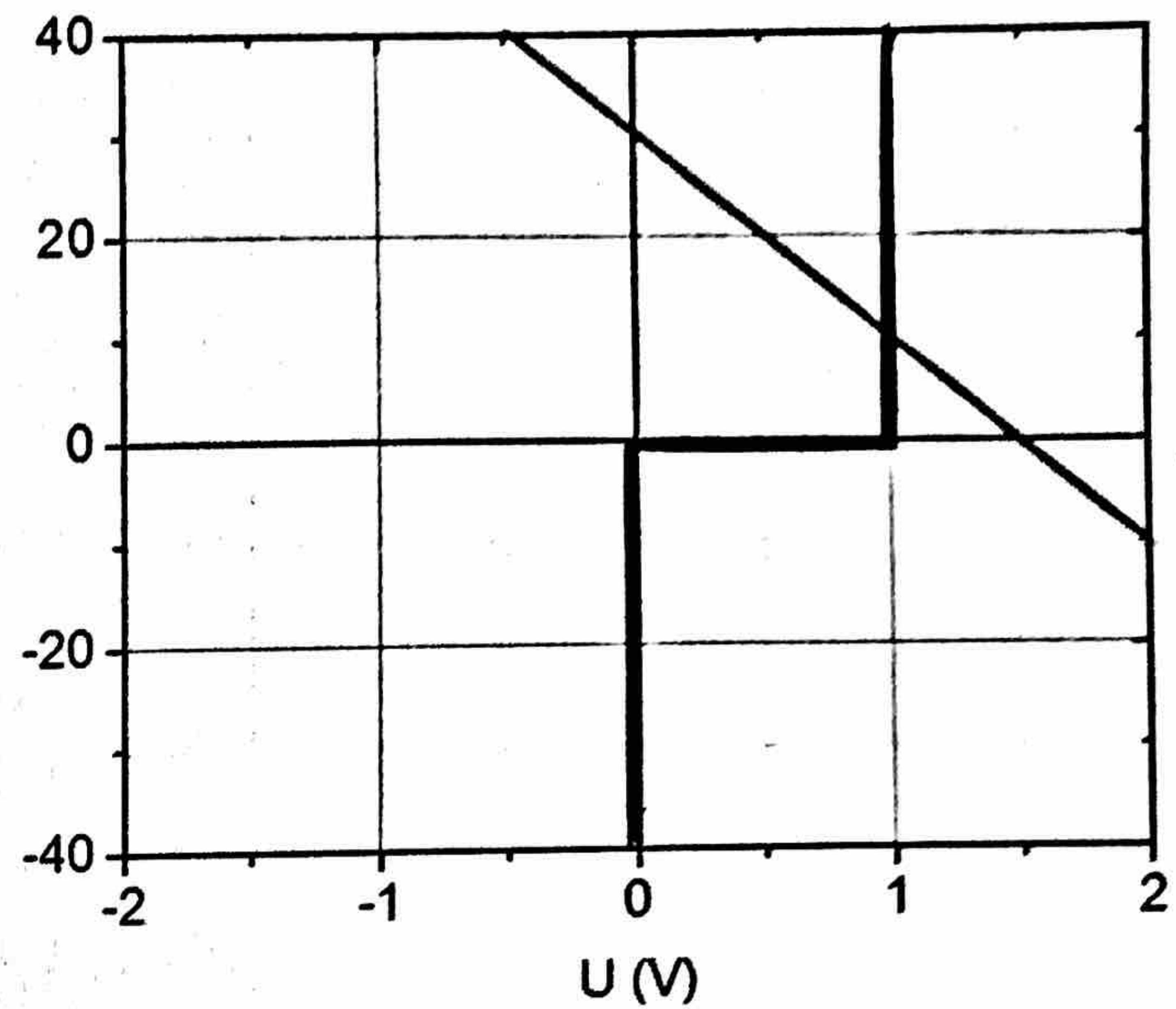
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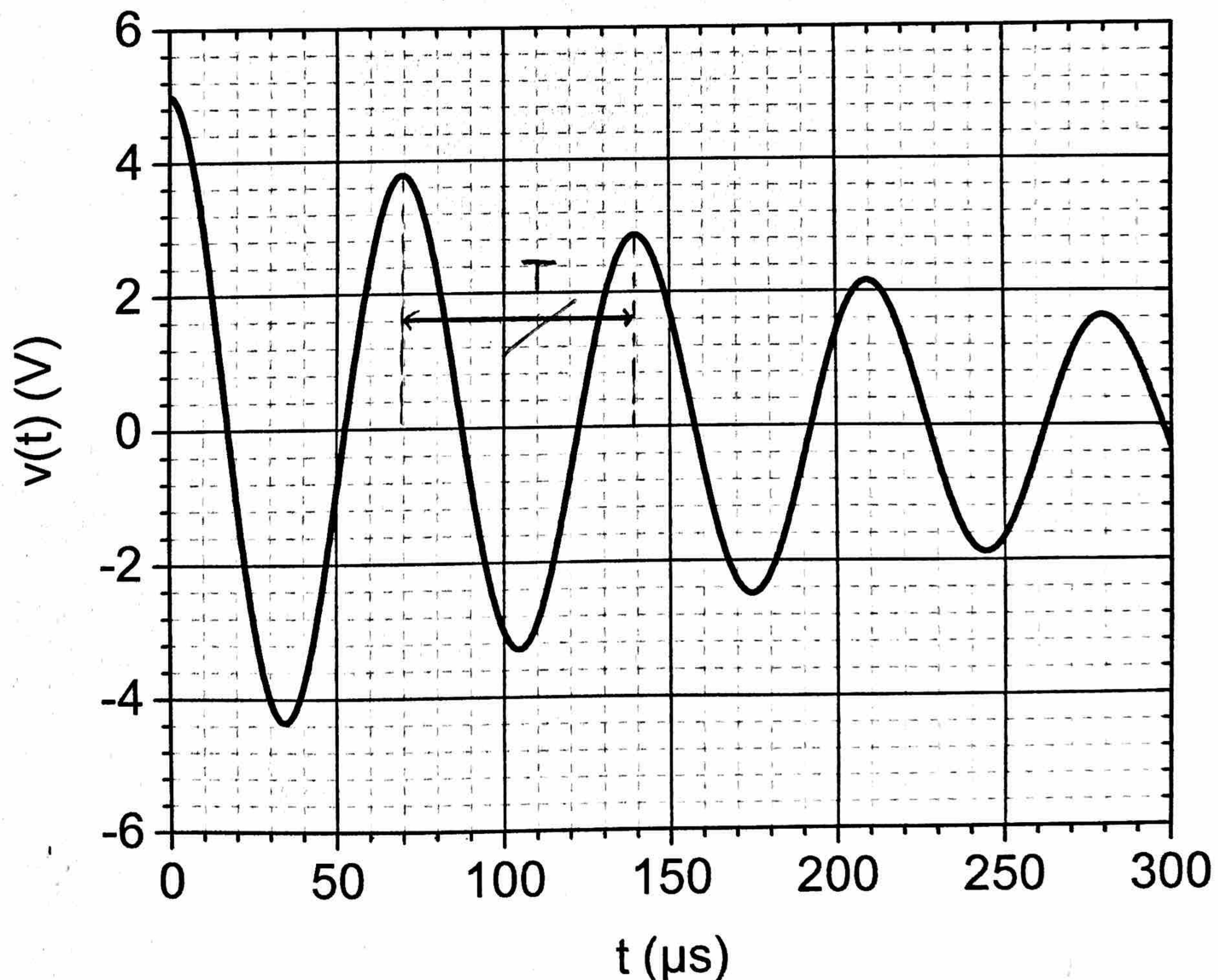
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Appendix 1:  $I$ - $V$  curve of a Zener diode in passive sign convention



Appendix 2



Appendix 3