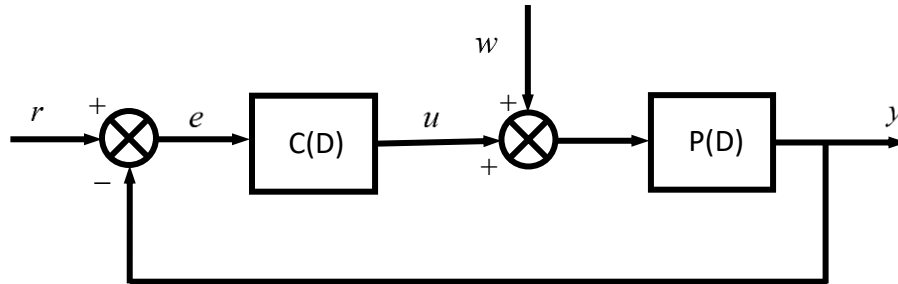


**ENME 585 – Quiz 2 2022**

**Closed book and closed notes. Schulich calculators allowed. Please show your work.**

All questions refer to the following feedback loop.



1. In the above feedback loop, the PI control  $u(t) = k \left( e(t) + 4 \int_{-\infty}^t e(\tau) d\tau \right)$  is applied to the second-order plant  $\ddot{y}(t) + 2\dot{y}(t) + y(t) = u(t)$ .
  - a) Sketch the loci of the closed-loop poles as  $k > 0$  varies. Show any asymptotes and indicate where they intersect the real axis.
  - b) Find the values of any imaginary axis crossings in the root locus and the range of  $k$  for closed-loop stability.
  - c) Design  $k$  to achieve a steady-state error of  $e_{ss} = 1$  when  $r = [t]$  and  $w = 0$ .
  - d) For  $r = [t]$  and  $w = 0$ , why is it not possible to design  $k$  to achieve  $e_{ss} = 0.1$ ? For these values of  $r$  and  $w$ , find the greatest lower bound on the achievable  $e_{ss}$ .
2. In the above feedback loop, proportional control  $C(D) = k$  is applied to the plant  $P(D) = \frac{1}{D(D+2)}$ .
  - a) Sketch the loci of the closed-loop poles as  $k > 0$  varies.
  - b) Design  $k$  for critically-damped closed-loop poles.
  - c) Find the steady-state error  $e_{ss}$  if  $k = 5$ ,  $w = [1]$ , and  $r = 0$ .
  - d) For the conditions of (2c), find the peak magnitude of the error  $|e(t)|$ .