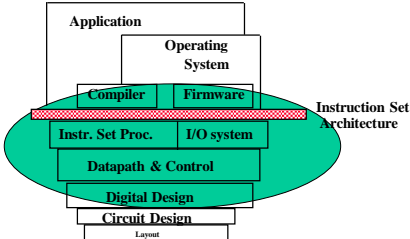
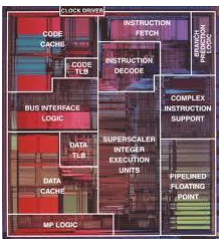




CS/SE 3340

Computer Architecture



Data Representation & Base Conversion

Adapted from "Computer Organization and Design, 4th Ed." by D. Patterson and J. Hennessy



0	HH	37	D5	80	9B	51	46	30	C1	34	D8	75
1	9B	29	99	44	60	A3	18	06	43	48	8B	53
2	0	47	62	E0	E5	F3	B1	74	C0	23	9E	09
3	4	27	7F	62	B9	BA	FC	67	8C	66	7B	95
4	1	29	46	49	4C	EE	D3	58	D3	28	6C	5F
5	0	99	20	67	43	A6	0C	50	24	99	24	27
6	E	7	30	A5	D1	9B	EB	43	68	DE	D0	7F
7	2	6E	A0	97	20	D2	E2	9B	4C	86	81	9B
8	E	DA	57	C5	D4	8B	42	1A	76	A2	3E	A5
9	1	44	87	AA	70	B6	EE	68	06	42	DA	BE
10	5	50	61	56	D7	14	5A	6C	FD	77	A4	20
11	1	87	3D	9F	B9	BC	E7	1E	C8	99	DE	97
12	2	30	38	C7	D2	00	00	F3	DC	97	2B	9B
13	2	99	22	67	66	4F	90	3C	27	99	26	67
14	7	19	C6	F3	54	9B	E2	BA	97	1A	B8	5F
15	6	67	B0	8D	E2	B9	E2	8B	AC	D9	9B	91
16	1	AB	20	68	ED	82	F8	02	7A	A3	58	5F
17	8	E3	11	AB	50	4D	99	03	1B	4B	14	03
18	4	6F	A1	E0	DE	D4	9F	AD	7E	8B	2D	AA
19	0	9C	90	98	D0	F8	4B	98	94	26	48	88
20	5	D6	A9	64	61	C2	29	32	94	D7	83	80

Base Converter

32-bit Unsigned

Clear

UTF-8

Reset All Fields

Char <-> Code

Number Type

Decimal

66

Hex

42

Octal

102

Binary

00000000

00000000

00000000

01000010

BCD

0000

0000

0000

0000

0000

0000

0000

0000

0110

0110

Character to Code

42

0042

42

Code to Character

42

8

ASCII

Unicode

UTF-8

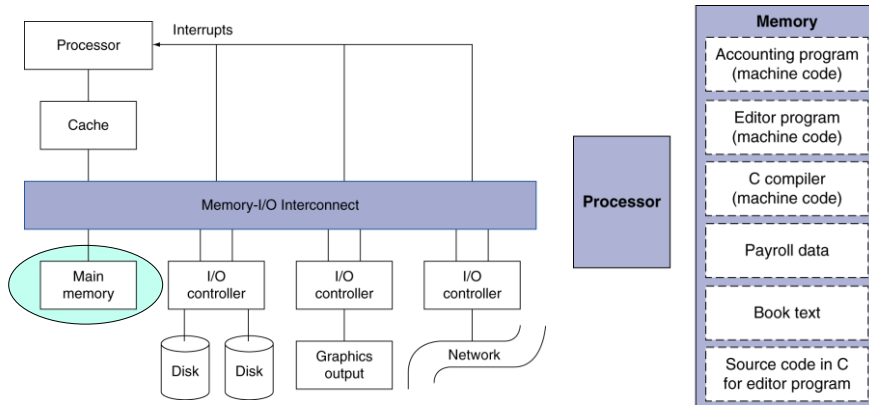
ASCII

The quick brown fox jumps over the lazy dog

54 68 65 20 71 75 69 63 68 20 62 72 6F 77 6E 20 66 6F 78 20 6A 75 6D 70 73 20 6F 76 65 72 20 74 68 65 20 6C 61 7A 79 20 64 6F 67

Valid Characters are any single UTF-8 character

Stored Program Computer



*Both **programs** (instructions) and **data** are stored in main memory*

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Memory Organization

- Main memory can be viewed as a large one-dimension array of bytes (or octets)
- A memory address is an *index* into the memory array
- *Byte addressing* means that the index points to a byte of memory

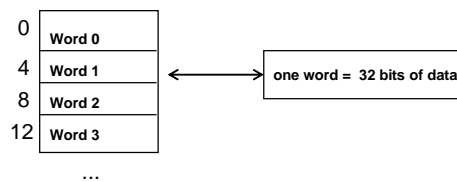
0	8 bits of data
1	8 bits of data
2	8 bits of data
3	8 bits of data
4	8 bits of data
5	8 bits of data
6	8 bits of data

...

But what do we do if our data is larger than a byte?

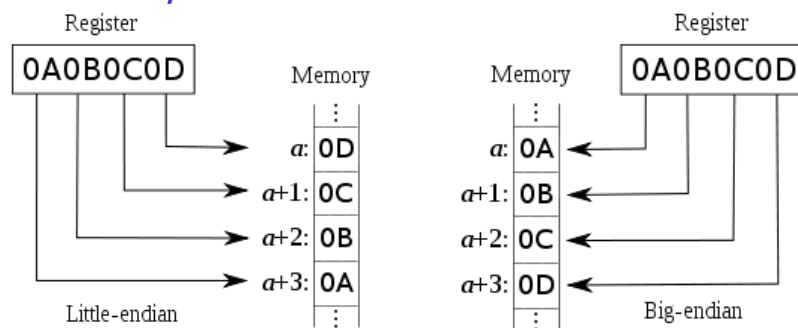
Memory Organization – cont'd

- Bytes are smallest addressable unit, but most data items use larger space: words
- In MIPS architecture a word is 32 bits or 4 bytes
 - 2^{32} bytes with byte addresses from 0 to $2^{32}-1$
 - 2^{30} words with byte addresses 0, 4, 8, ... $2^{32}-4$
- *Can a word start at any arbitrary byte address?*
- *What order the bytes in a word are stored?*



Endianness

- When a data entity is bigger than one byte (e.g. a 32-bit integer), how it is stored in memory?



How Information is Represented in Memory?

- Remember a (digital) computer can only understand binary information (0 and 1)
- How instruction and data are represented in memory?
 - Numbers?
 - Characters?
 - Strings?
 - Multimedia (audio, video)?
 - *Instructions (of a program)?*

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Number Definitions

- Bits: *Binary digit*
 - Two states (0 or 1)
- Nibble = 4 bits (not used much anymore)
- Byte or Octet = 8 bits
- Word
 - processor dependent: 4, 8, 16, 32, 64
 - The “natural” word length for a processor is the size of its register

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Numbers in High-Level Languages

- char = 8 bits,
short = 16 bits,
int = basic size of processor register: 8, 16, 32, 64 bits
long = 32 bits
double = 64 bits
- Largest *number of items* represented in binary word with “n” bits is “2^n”
 - 2^8 = 256
 - 2^16 = 65,536
 - 2^32= 4,294,967,296

NOTE: number of items, NOT largest number (Why?)

Number Base

Common bases for representing a numeric values in computers

Name	Base	Digits	For
Binary	2	0, 1	machine
Octal	8	0, 1, 2, 3, 4, 5, 6, 7	human
Decimal	10	0, 1, 2, 3, 4, 5, 6, 7, 8, 9	human
Hexadecimal	16	0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F	human

Numeric values can be represented in any base!

Number Representation

- Positional Representation

$$n = \sum (d_i \times \text{base}^i)$$

where d is a single digit less than base and “ i ” runs from 0 to number of digits – 1

- for $i = 3$, the number $d_3d_2d_1d_0 =$

$$(d_3 \times \text{base}^3) + (d_2 \times \text{base}^2) + (d_1 \times \text{base}^1) + (d_0 \times \text{base}^0)$$

- Example: given the base-10 number 563

hundreds	tens	units
(5×10^2)	(6×10^1)	(3×10^0)
(5×100)	(6×10)	(3×1)
500	+ 60	+ 3

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Base 2 (Binary) Numbers

- Positional notation:
 - 1) Numbered 0,1,2,...,n from right to left
 - 2) Rightmost binary position is “ b_0 ” and is the “*least_significant_bit*” (LSb) in the number
 - 3) Leftmost binary position is “ b_{n-1} ” and is the “*most_significant_bit*” (MSb) in the number

- Example:

generic form of a 8-bit binary number: $b_7b_6b_5b_4b_3b_2b_1b_0 = (b_7b_6b_5b_4b_3b_2b_1b_0)$
 $b_7 \times (2^7) + b_6 \times (2^6) + b_5 \times (2^5) + b_4 \times (2^4) + b_3 \times (2^3) + b_2 \times (2^2) + b_1 \times (2^1) + b_0 \times (2^0)$

$b_7 \times 128$	$+ b_6 \times 64$	$+ b_5 \times 32$	$+ b_4 \times 16$	$+ b_3 \times 8$	$+ b_2 \times 4$	$+ b_1 \times 2$	$+ b_0 \times 1$
b_7	b_6	b_5	b_4	b_3	b_2	b_1	b_0
MSb							LSb

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Various Number Representation

Decimal	Binary	Octal	Hexadecimal
0	0000	00	0
1	0001	01	1
2	0010	02	2
3	0011	03	3
4	0100	04	4
5	0101	05	5
6	0110	06	6
7	0111	07	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F
16	10000	20	10

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Base Conversion

Convert binary to decimal:

- 1) Positional formula: base = 2 , the number 1011

=
(1x2^3)+
(0x2^2)+
(1x2^1)+
(1x2^0)
base 2 number

=
(1x8)+
(0x4)
+
(1x2)
+
(1x1)
w/base 10 arithmetic

=
8+
0+
2+
1

=
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- 2) Alternate method: The multiplications can be replaced by a conditional add then sum the positional value at each non zero bit position

bn	bn-1		b16	b15	...	b11	b10	b9	b8	b7	b6	b5	b4	b3	b2	b1	b0	
-----	-----		-----	-----	...	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
2^ <i>n</i>	2^(<i>n</i> -1)	...	2^16	2^15	...	2^11	2^10	2^9	2^8	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0	
-----	-----		-----	-----	...	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
			65536	32768		2048	1024	512	256	128	64	32	16	8	4	2	1	
										0	1	0	0	1	0	0	1	
											0	+64	+0	+0	+8	+0	+0	+1

for 01001001

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Base Conversion – cont'd

Using *Horner's* nested form:

- o Rearrange the form of the basic positional formula (power series)

$$\begin{aligned}
 & d_n \times (B^n) + d_{n-1} \times B^{(n-1)} + \dots + d_2 \times (B^2) + d_1 \times (B^1) + d_0 \times (B^0) \\
 &= (d_n \times (B^n) + d_{n-1} \times B^{(n-1)}) + \dots + d_2 \times (B^2) + d_1 \times (B^1) + d_0 \times (B^0) \\
 &= ((d_n \times B + d_{n-1}) \times B^{(n-1)}) + \dots + d_2 \times (B^2) + d_1 \times (B^1) + d_0 \times (B^0) \\
 &= ((\dots(((d_n \times B + d_{n-1}) \times B + \dots + d_2) \times B + d_1) \times 2 + d_0) \\
 &\quad \text{where } B \text{ is the number base (e.g. 2, 10, 16,...)}
 \end{aligned}$$

- o Method (recursive evaluation)

- 1) This implies repeated division by *base B*, the first *remainder* will be the least significant digit (LSD) of the number
- 2) Then repeat with the *quotient* until the entire number is converted (i.e. the quotient is 0)

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Example: Decimal -> Binary

Number	quotient		remainder	binary position
90	90/2	45	0	1
	45/2	22	1	2
	22/2	11	0	4
	11/2	5	1	8
	5/2	2	1	16
	2/2	1	0	32
	1/2	0	1	64

result = 1011010
(64+0+16+8+0+2+0 = 90)

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Hex <-> Decimal

Hex -> decimal: same as binary to decimal but using 16 instead of 2

Positional formula: base = 16 , the number 138D

$$\begin{aligned}
 &= (1 \times 16^3) + (3 \times 16^2) + (8 \times 16^1) + (13 \times 16^0) \\
 &= (1 \times 4096) + (3 \times 256) + (8 \times 16) + (13 \times 1) \\
 &= 4096 + 768 + 128 + 13 \\
 &= 5005
 \end{aligned}$$

Decimal -> hex:

Number		quotient	remainder
5005	5005/16	312	D (13)
	312/16	19	8
	19/16	1	3
	1/16	0	1

result = 138D

$$(1 \times 4096) + (3 \times 256) + (8 \times 16) + (13 \times 1) = 5005$$

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How about Characters?



	0	1	2	3	4	5	6	7
0	NUL	DLE	space	0	@	P	.	p
1	SOH	DC1 XON	!	1	A	Q	a	q
2	STX	DC2	"	2	B	R	b	r
3	ETX	DC3 XOFF	#	3	C	S	c	s
4	EOT	DC4	\$	4	D	T	d	t
5	ENQ	NAK	%	5	E	U	e	u
6	ACK	SYN	&	6	F	V	f	v
7	BEL	ETB	'	7	G	W	g	w
8	BS	CAN	{	8	H	X	h	x
9	HT	EM	}	9	I	Y	i	y
A	LF	SUB	*	:	J	Z	j	z
B	VT	ESC	+	;	K	[k	{
C	FF	FS	,	<	L	\	l	
D	CR	GS	=	=	M]	m	}
E	SO	RS	>	>	N	^	n	~
F	SI	US	/	?	O	_	o	del

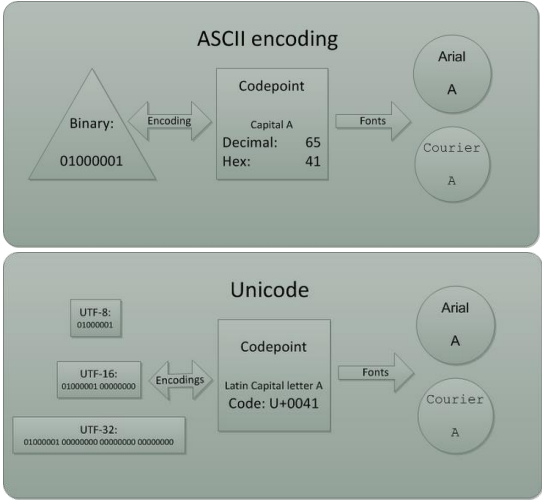
The ASCII character set:

- Initially contained 128 7-bit encoded characters
- Including alphabetic, numeric, graphic and control characters
- Has been extended to include system or country specific characters (Unicode™ standard)
- What character set do IBM computers use?

How to handle Chinese characters?

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Character Encoding: ASCII -> Unicode



UTF?

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<http://www.dotnetnoob.com>

But I want to Store Strings!

- Strings can be represented as one-dimension arrays of characters
- How to signal the end of a string?
 - Length-prefix (e.g. in Pascal) – *what can be a problem?*
 - NULL ('0') terminated (e.g. in C language)
 - An explicit length field in the string object (e.g. C++)

length	F	R	A	N	K	k	e	f	w
5 _{dec}	46 _h	52 _h	41 _h	4E _h	4B _h	6B _h	65 _h	66 _h	77 _h

F	R	A	N	K	NUL	k	e	f	w
46 _h	52 _h	41 _h	4E _h	4B _h	00 _h	6B _h	65 _h	66 _h	77 _h

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...and Multimedia (Audio, Video)

- Multimedia data are encoded into streams of bytes by encoders and stored in memory as sequences of bytes before they can be processed by computers!
- For example
 - MPEG2, MP4 for video
 - MP3 for audio
 - File Format (FF) standards in MPEG



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