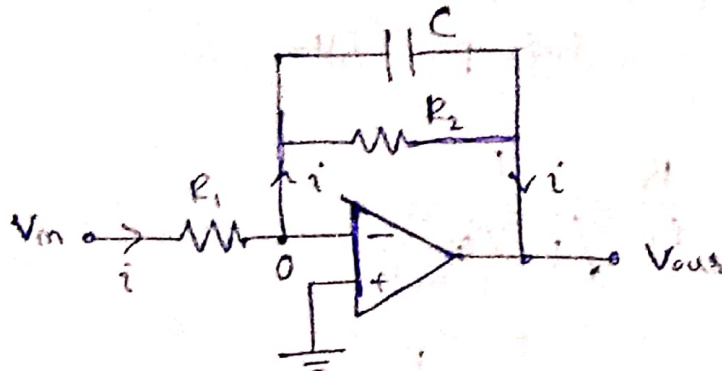


Question 1

- a) *
- Load resistance changes the filter's transfer function.
 - Cannot supply a high current to the output

b)



i)

$$V_m(s) = i R_1 \quad \text{--- (1)}$$

$$-V_{out}(s) = i \left(\frac{R_2 / Cs}{R_2 + 1/Cs} \right) \quad \text{--- (2)}$$

$$\textcircled{2} / \textcircled{1} \Rightarrow \frac{-V_{out}(s)}{V_m(s)} = \frac{R_2}{R_1(1 + R_2Cs)}$$

$$H(s) = -\frac{R_2}{R_1} \left(\frac{1}{1 + R_2Cs} \right)$$

ii) The current going into the inverting input of the opamp is negligible.

iii) Active filter

iv)

$$H(j\omega) = -\frac{R_2}{R_1} \left(\frac{1}{1 + j\omega R_2C} \right)$$

$$|H(j\omega)| = \frac{R_2}{R_1} \cdot \frac{1}{\sqrt{1 + \omega^2 R_2^2 C^2}}$$

$$\omega \rightarrow 0, \quad |H(j\omega)| \rightarrow \frac{R_2}{R_1}$$

$$\omega \rightarrow \infty, \quad |H(j\omega)| \rightarrow 0$$

\therefore This is a high pass filter.

$$\therefore |H(j\omega)| = \frac{R_2}{R_1} \cdot \frac{1}{\sqrt{1 + \left(\frac{\omega}{\omega_c}\right)^2}}$$

$$\text{Passband gain} = \frac{R_2}{R_1}$$

$$\omega_c = \frac{1}{R_2 C} \Rightarrow f_c = \frac{1}{2\pi R_2 C}$$

Question 2

a) When the input to a logic gate is changed, the time taken to produce the corresponding output by the logic gate is called its propagation delay.

b) + Changing the output logic values ~~at~~ from 0-to-1 and 1-to-0 corresponds to switching off a CMOS transistor and switching ON a CMOS transistor.

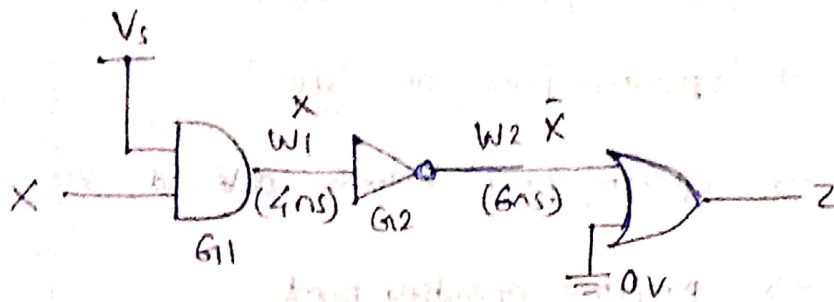
* To switch ON a CMOS (NMOS), we need to place positive charges on the gate which is equivalent to charging a capacitor.

* To turn it off we must remove that charge which is equivalent to discharging a capacitor.

* These two processes take different amounts of time

* Thus t_{PHL} and t_{PLH} differs

c)



2) Input = X, Output = Z

X	Z
0	1
1	0

$$Z = \bar{X}$$

III) Consider the transition of 0-to-1 (Low-to-high)

Gate	Previous output	Current output	Delay (ns)
G3	0	1	13
G2	0	1	10
G1	1	0	15

$$\therefore t_{PLH} = 13 + 10 + 15 + 6 + 4 = 48 \text{ ns}$$

Now consider 1-to-0 transition

Gate	Previous output	Current output	Delay (ns)
G3	1	0	14
G2	1	0	9
G1	0	1	12

$$\therefore t_{PHL} = 14 + 9 + 12 + 6 + 4 = 45 \text{ ns}$$

Question 3

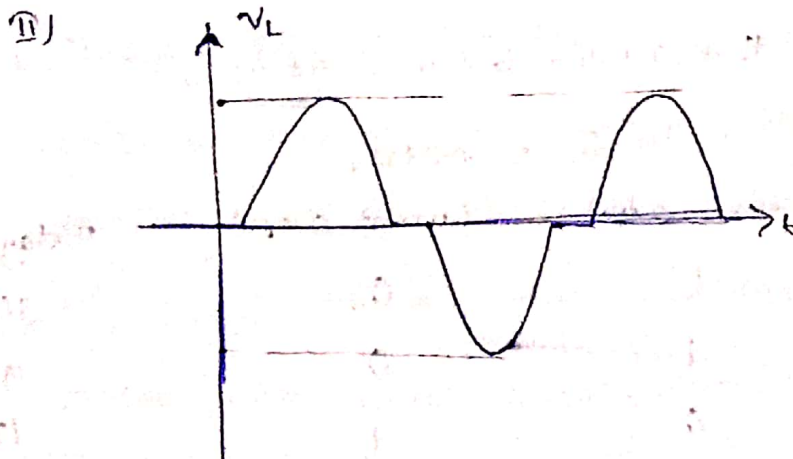
- a)
- * Class A \rightarrow Operating point at $V_{CC}/2$
 - * Class B \rightarrow Operating point at 0V
 - * Class AB \rightarrow Operating point between 0V and $V_{CC}/2$
 - * Class C \rightarrow Negative operating point

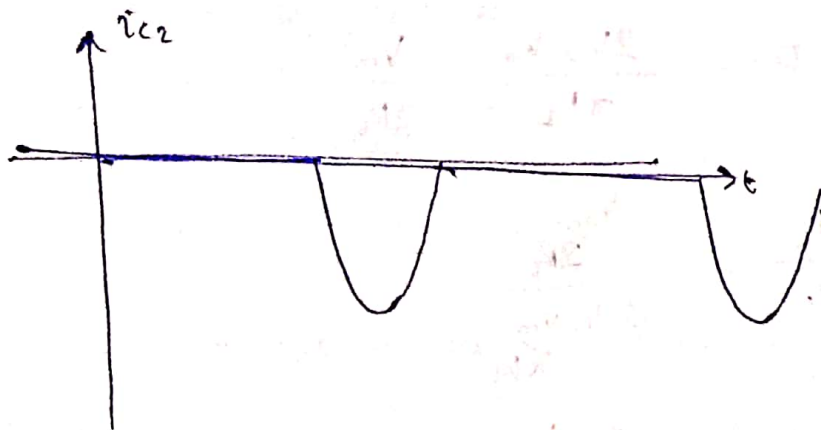
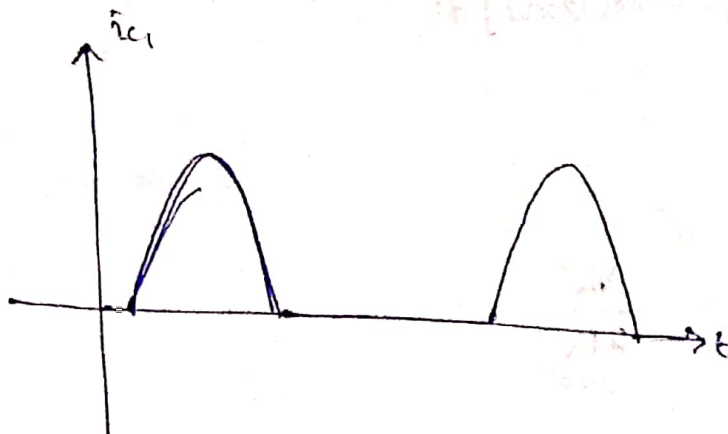
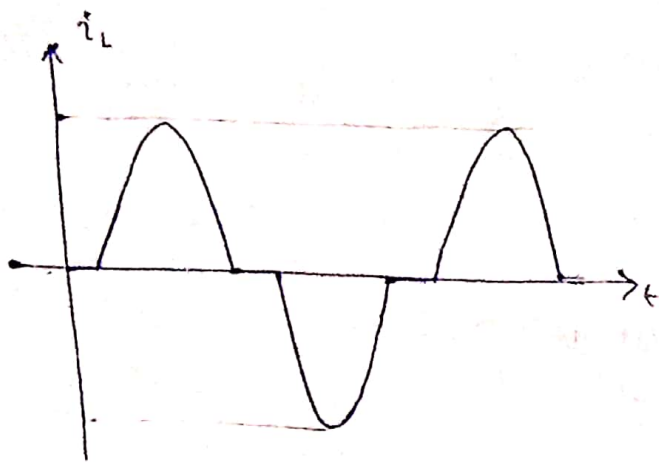
* Conduction angle is the time & during which the transistor conducts when a sinusoidal signal is applied

Class	conduction angle
A	360° (Conducts during the whole cycle)
B	180° (half a cycle)
AB	Slightly higher than 180°
C	Slightly lower than 180°

b) I) * Higher efficiency

* Possible ripples in the power supply is balanced out.





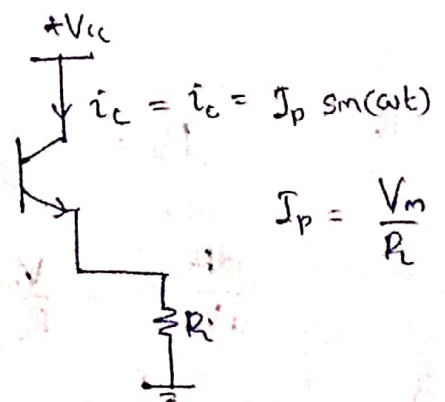
(iii) Considering the positive cycle,

$$P_m = \frac{2}{T} \int_0^{T/2} i_c V_{cc} dt$$

$$= \frac{2V_{cc}}{T} \int_0^{T/2} \frac{V_m}{R_L} \sin(\omega t) dt$$

$$= \frac{2V_{cc}V_m}{TR_L} \left[\frac{-\cos(\omega t)}{\omega} \right]_0^{T/2}$$

$$P_m = \frac{4V_{cc}V_m}{\omega TR_L} = \frac{2V_{cc}V_m}{\pi R_L}$$



$$I_p = \frac{V_m}{R_L}$$

$$\begin{aligned}
 P_L &= \frac{2}{T} \int_0^{T/2} i_c^2 R_L dt \\
 &= \frac{2R_L}{T} \int_0^{T/2} I_p^2 \sin^2 \omega t dt \\
 &= \frac{I_p^2 R_L}{T} \int_0^{T/2} [1 - \cos(2\omega t)] dt \\
 &= \frac{I_p^2 R_L}{T} \cdot \frac{T}{2} \\
 P_L &= \frac{(V_m/R_L)^2 R_L}{2} = \frac{V_m^2}{2R_L}
 \end{aligned}$$

$$P_D = P_m - P_L = \frac{2V_{CC} V_m}{\pi R_L} - \frac{V_m^2}{2R_L}$$

$$\eta = \frac{P_L}{P_m} = \frac{\frac{V_m^2}{2R_L}}{\frac{2V_{CC} V_m}{\pi R_L}}$$

$$\therefore \eta = \frac{\pi}{4} \cdot \frac{V_m}{V_{CC}}$$

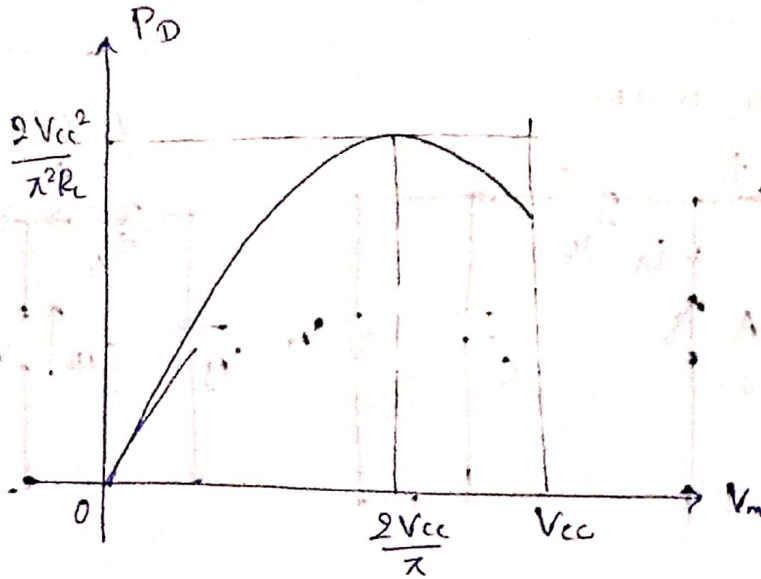
$$(iv) \quad P_D = -\frac{V_m^2}{2R_L} + \frac{2V_{CC} V_m}{\pi R_L}$$

$$\frac{dP_D}{dV_m} = -\frac{V_m}{R_L} + \frac{2V_{CC}}{\pi R_L}$$

$$\text{When } P_D \text{ is maximum, } \frac{dP_D}{dV_m} = 0$$

$$\Rightarrow -\frac{V_m}{R_L} + \frac{2V_{CC}}{\pi R_L} = 0 \Rightarrow V_m = \frac{2V_{CC}}{\pi}$$

$$\therefore (P_D)_{\max} = -\frac{1}{2R_L} \frac{V_{CC}^2}{\pi^2} + \frac{2V_{CC}}{\pi R_L} \cdot \frac{2V_{CC}}{\pi} = \frac{2V_{CC}^2}{\pi^2 R_L}$$



vi)

$$P_L = 20 \text{ W}$$

$$20 = \frac{V_m^2}{2 \times 8}$$

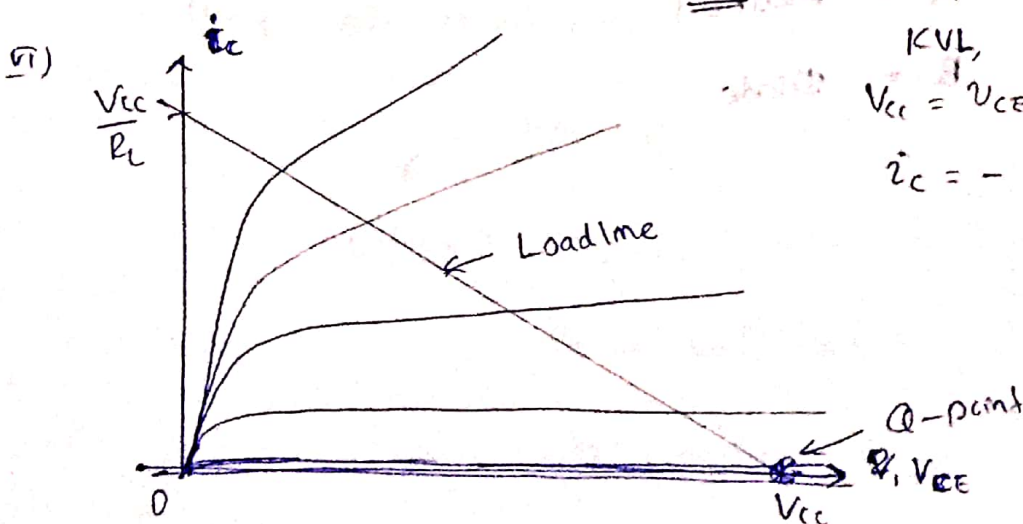
$$V_m = 17.889 \text{ V}$$

To get the maximum efficiency, $V_m = V_{CC}$

$$\Rightarrow V_{CC} = \underline{\underline{17.89 \text{ V}}}$$

$$I_p = \frac{V_m}{R_L} = \frac{17.89}{8}$$

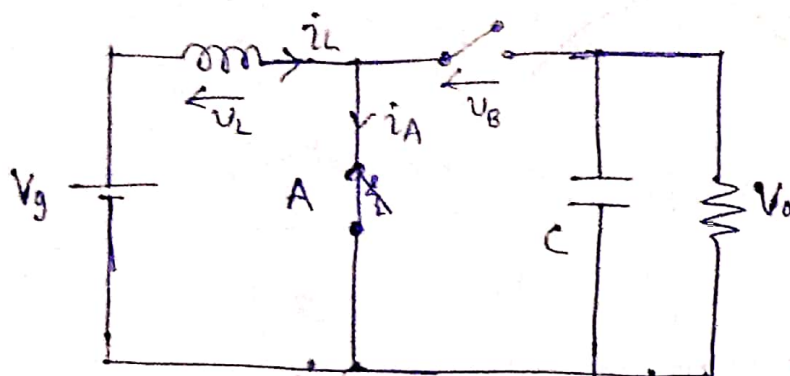
$$I_p = \underline{\underline{2.236 \text{ A}}}$$



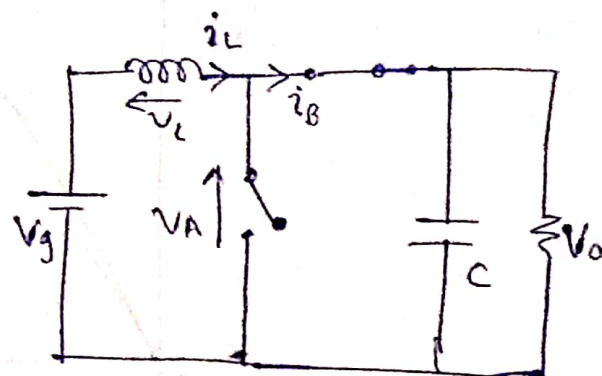
$$\begin{aligned} \text{KVL,} \\ V_{CC} &= V_{CE} + i_C R_L \\ i_C &= -\frac{V_{CE}}{R_L} + \frac{V_{CC}}{R_L} \end{aligned}$$

Question 4

c) I) A ON, B OFF



A OFF, B ON



A : ON $\rightarrow i_A = i_L > 0$ — positive

OFF $\rightarrow v_A = V_o > 0$ (Assuming V_o is positive)

\therefore A conducts positive currents and blocks positive voltages

B : ON $\rightarrow i_B = i_L > 0$

OFF $\rightarrow v_B = V_g - V_o < 0$ ($\because V_o > V_g$ because this is a boost converter)

\therefore B conducts positive currents and blocks negative voltages

II)

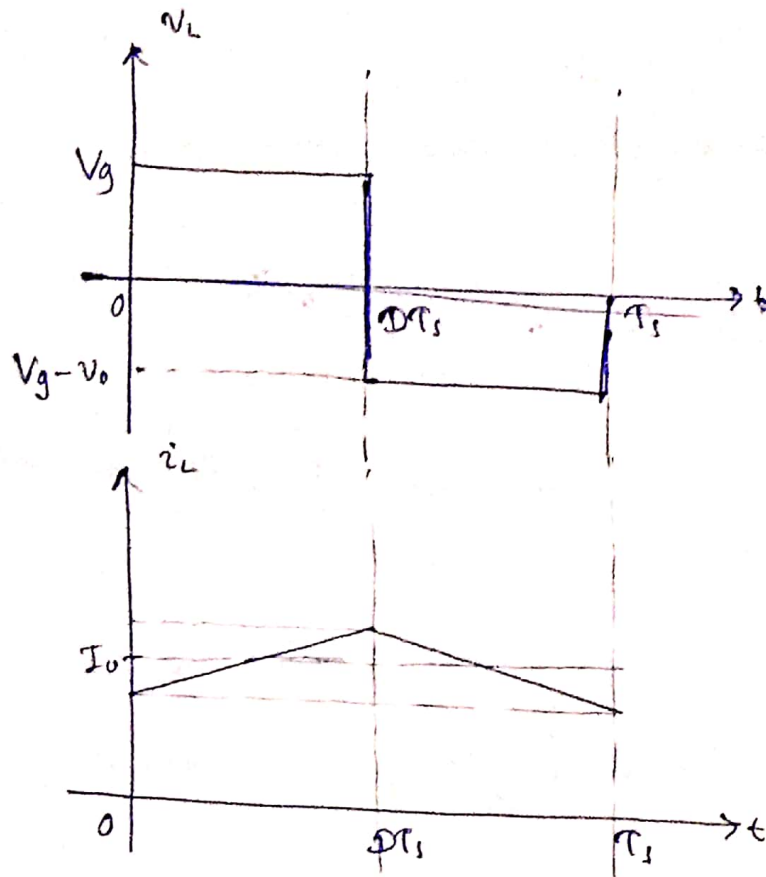
A = MOSFET

B = Diode

III) Assuming steady state operation.

III) $0 \leq t \leq DT_s; \quad v_L = V_g > 0$

$DT_s \leq t \leq T_s; \quad v_L = V_g - V_o < 0$



IV) Using small ripple approximation,

$$v_o \approx V_o$$

$$\therefore v_L \text{ for } 0 \leq t \leq DT_s \approx V_g$$

$$v_L \text{ for } DT_s \leq t \leq T_s \approx V_g - V_o$$

Using volt-second balance,

$$\int_0^{T_s} v_L(t) dt = 0$$

$$\therefore V_g \cdot (DT_s) + (V_g - V_o)(1-D)T_s = 0$$

$$V_g = V_o(1-D)$$

$$V_o = \frac{V_g}{1-D}$$