pumiMBBL-GPU with Kokkos

Library Documentation

Vignesh Vittal-Srinivasaragavan RPI-SCOREC

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1 New PUMI Data structure

1.1 Submesh-level – base classes and derived classes

```
class Submesh{
public:
    double xmin;
    double xmax;
    int Nel;
    double t0;
    double r;
    int Nel_cumulative;
    // enum type 0x01-uniform, 0x02-minBL and 0x04-maxBL
    Meshtype meshtype;
    Kokkos::View<double*> BL_coords; // BL coords on device
    double *host_BL_coords; // BL coords on host
    Submesh(....):....{}; //Constructor to submesh class
    // Virtual functions on host
    virtual int locate_cell_host(); // using analtyical expressions
    virtual int update_cell()_host; // using adjacency search
    virtual void calc_weights_host(); // using stored node coordinates
    // Virtual functions not implemented on device
    // device copies of same routines implemented
    // with switch statements
};
```

The submesh class is identical to the struct pumi_submesh we have currently. Only difference is that the BL coordinates array is allocated with Kokkos type. We will have three derived classes for pumi_submesh, one for each type of meshing.

Uniform meshing:

```
class Uniform_Submesh : public Submesh{
public:
    Uniform_Submesh(....):.....{}; // Constructor to uniform submesh cl
    // uniform mesh APIs on host
    int locate_cell_host(); // using analtyical expressions
```

```
int update_cell_host(); // using adjacency search
    void calc_weights_host();
    // uniform mesh APIs on device
    KOKKOS_FUNCTION
    int locate_cell();
    KOKKOS_FUNCTION
    int update_cell();
    KOKKOS_FUNCTION
    void calc_weights();
};
Left/Bottom BL meshing:
class MinBL_Submesh : public Submesh{
public:
    MinBL_Submesh(....):.....{}; // Constructor to minBL submesh class
    // minBL mesh APIs on host
    void locate_cell_host(); // using analtyical expressions
    void update_cell_host(); // using adjacency search
    void calc_weights_host();
    // minBL mesh APIs on device
    KOKKOS_FUNCTION
    int locate_cell();
    KOKKOS_FUNCTION
    int update_cell();
    KOKKOS_FUNCTION
    void calc_weights();
};
Right/Top BL meshing:
class MaxBL_Submesh : public pumi_submesh{
public:
    MaxBL_Submesh(....):.....{}; // Constructor to maxBL submesh class
    // maxBL mesh APIs on host
    void locate_cell_host(); // using analtyical expressions
    void update_cell_host(); // using adjacency search
    void calc_weights_host();
    // maxBL mesh APIs on device
    KOKKOS_FUNCTION
```

```
int locate_cell();
KOKKOS_FUNCTION
int update_cell();
KOKKOS_FUNCTION
void calc_weights();
.
.
.
.
```

This allows us to use the polymorphism feature to define different particle APIs with same name essentially replacing the function pointer data structures we previously implemented.

1.2 Mesh-level classes

```
class MeshOffsets{
// For 2D Mesh with inactive blocks
// Offsets keeps track of nodes/elements in inactive blocks
// Helps speed up computing global element/node ID
public:
    bool is_fullmesh; // Is mesh with no inactive blocks
    // aux data structure to compute nodeoffset - On device
    Kokkos::View<int**> nodeoffset_start;
    Kokkos::View<int**> nodeoffset_skip_bot;
    Kokkos::View<int**> nodeoffset_skip_mid;
    Kokkos::View<int**> nodeoffset_skip_top;
    // aux data structure to compute element offsets - On device
    Kokkos::View<int**> elemoffset_start;
    Kokkos::View<int*> elemoffset_skip;
    // Host copies of aux data structures
    int** host_nodeoffset_start;
    int** host_nodeoffset_skip_bot;
    int ** host_nodeoffset_skip_mid;
    int** host_nodeoffset_skip_top;
    int** host_elemoffset_start;
    int* host_elemoffset_skip;
    int Nel_total; // Total active elements in domain
    int Nnp_total; // Total active nodes in domain
    MeshOffsets(){}; // Class constructor
};
class MeshBdry{
// For 2D Mesh with inactive blocks
// Stores block-level boundary edge/vertex information
public:
    // Block edge boundary info
    Kokkos::View<bool*> is_bdry_edge;
```

```
Kokkos::View<Vector3*> bdry_edge_normal;
    // Block vertex boundary info
    Kokkos::View<bool*> is_bdry_vert;
    Kokkos::View<Vector3*> bdry_vert_normal;
    // Starting boundary face ID on each boundary edge
    Kokkos::View<int*> edge_to_face;
        // Host copies of same info
    bool* host_is_bdry_edge;
    Vector3* host_bdry_edge_normal;
    bool* host_is_bdry_vert;
    Vector3* host_bdry_vert_normal;
    int *host_edge_to_face;
    int Nbdry_faces; // number of boundary element faces
    MeshBdry(){}; // Class constructor
};
class Mesh{
public:
    int ndim; // dimension
    int nsubmesh_x1; // number of x1-blocks
    int nsubmesh_x2; // number of x2-blocks
    Kokkos::View<bool**> isactive; // block activity info on device
    bool **host_isactive; // host copy of block activity
    int Nel_total_x1; // number of x1-elements
    int Nel_total_x2; // number of x2-elements
    int Nel_total; // Total mesh elements
    int Nnp_total; // Total mesh nodes
    MeshOffsets offsets; // object to MeshOffsets class
    MeshBdry bdry; // object to MeshBdry class
    Mesh(....):...{}; // Class constructor
};
```

1.3 Typedefs for submesh objects

Memory for submesh are dynamically allocated based on number of blocks. Hence copies are kept on bith device and host.

```
// Submesh object array allocated in GPU using Kokkos View
// cannot be copied to CPU thru Kokkos::deep_copy()
using SubmeshDeviceViewPtr = Kokkos::View < DevicePointer < Submesh >*>;
// Copy of Submesh object array allocated in CPU
using SubmeshHostViewPtr = Submesh*;
// Convenience class for 3D-vectors of double
class Vector3;
```

1.4 Wrapper struct containing mesh and submesh objects

```
struct MBBL{
    Mesh mesh; // mesh obj
    SubmeshDeviceViewPtr submesh_x1; // x1-submesh obj in GPU
    SubmeshHostViewPtr host_submesh_x1; // x1-submesh obj in CPU
    SubmeshDeviceViewPtr submesh_x2; // x2-submesh obj in GPU
    SubmeshHostViewPtr host_submesh_x2; // x2-submesh obj in CPU
};
```

Object to this structure will be used in hpic2 and passed around in mesh APIs

PUMI Mesh initiation

Mesh initiation is still done through in-memory data structure pumi_inputs. In hPIC the mesh initiation is performed as

```
// Declare mesh inputs object
pumi::Mesh_Inputs *pumi_inputs;
// allocate memory
pumi_inputs = pumi::inputs_allocate(nsubmesh);
// parse inputs (from file or commandline) and populate pumi_inputs dat
// Set options for mesh
pumi::Mesh_Options pumi_options;
pumi_options.BL_storage_option = pumi::store_BL_coords_ON;
// Contruct the final pumi wrapper struct
pumi::MBBL pumi_obj = pumi::initialize_MBBL_mesh(pumi_inputs, pumi_opti
// free pumi inputs memory
pumi::inputs_deallocate(pumi_inputs);
  MBBL pumi_obj variable will ultimately be used in all pumiMBBL mesh APIs as an
```

input as pumi::foo(pumi_obj,...)

Element/Node ID conventions 3

Submesh IDs

A 2D submesh block is indexed by two integers (isub, jsub)

- Original rectangular multi-block domain is padded with one layer of blocks all around. If original set of blocks is $N_{x_1} \times N_{x_2}$, padded domain contains $(N_{x_1} + 2) \times$ $(N_{x_2}+2)$
- Length of padded layer is 1000 times actual domain length along the paddeddirection
- Done for algorithmic convenience, makes the original $N_{x_1} \times N_{x_2}$ blocks all interior blocks, which means homogeneous algorithm implementation with no need for special treatments for blocks in boundary

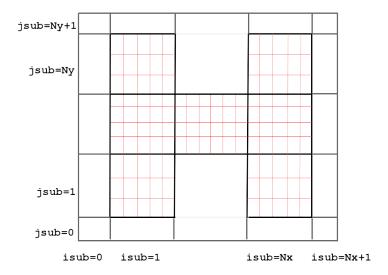


Figure 1: isub – submesh ID in x1-direction jsub – submesh ID in x2-direction

Possible non-padded-ID values:

$$1 \leq \mathtt{isub} \leq N_{x_1}^{submesh} \qquad 1 \leq \mathtt{jsub} \leq N_{x_2}^{submesh}$$

 $N_{x_1}^{submesh}, N_{x_2}^{submesh}$ – Number of submesh blocks in x1, x2 directions respectively. Alternatively, the pairwise indices can also be flattened into one unique index and written as, flattened_sub_ID = (jsub-1) $\times N_{x_1}^{submesh}$ + (isub-1)

Local Cell IDs

A cell inside a submesh block is indexed by two integers (icell, jcell)

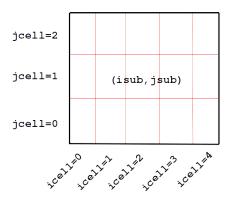


Figure 2: icell - local cell ID in x1-direction jcell - local cell ID in x2-direction

Possible values:

$$0 \leq \mathtt{icell} \leq N_{x_1,\mathtt{isub}}^{el} - 1 \qquad 0 \leq \mathtt{jcell} \leq N_{x_2,\mathtt{jsub}}^{el} - 1$$

 $N_{x_1, \mathtt{isub}}^{el}$ — Number of elements along x1-direction in x1-block with ID isub $N_{x_2, \mathtt{jsub}}^{el}$ — Number of elements along x2-direction in x2-block with ID jsub

Alternatively, the pairwise indices can also be flattened into one unique index and written as,

$$\texttt{flattened_cell_ID} = \texttt{jcell} \times N^{el}_{x_1, \texttt{isub}} + \texttt{icell}$$

Component-wise Global Cell IDs

Same as global row/column index of a cell in rectilinear mesh

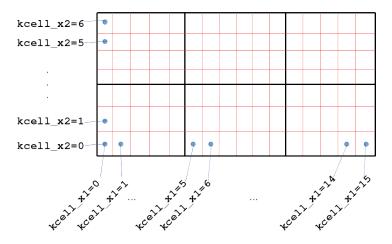


Figure 3: kcell_x1 - component-wise global cell ID in x1-direction kcell_x2 - component-wise global cell ID in x2-direction

Possible values:

$$0 \leq \texttt{kcell_x1} \leq N_{x_1}^{el,tot} - 1 \qquad 0 \leq \texttt{kcell_x2} \leq N_{x_2}^{el,tot} - 1$$

 $N_{x_1}^{el,tot}, N_{x_2}^{el,tot}$ – Number of total elements along x1, x2 directions respectively

Component-wise Global Node IDs

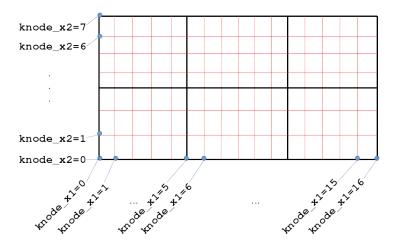


Figure 4: knode_x1 - component-wise global cell ID in x1-direction knode_x2 - component-wise global cell ID in x2-direction

Possible values:

$$0 \leq \texttt{knode_x1} \leq N_{x_1}^{el,tot} \qquad 0 \leq \texttt{knode_x2} \leq N_{x_2}^{el,tot}$$

4 2D Global Element and Node conventions

4.1 Full Mesh (No Inactive Blocks)

2D Element Numbering: For a mesh with no inactive blocks the figure below show how the elements are numbered

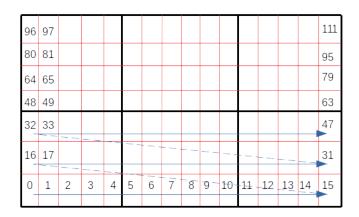
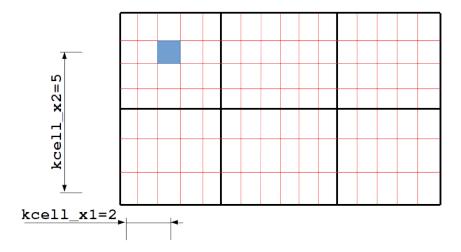


Figure 5: $N_{x_1}^{submesh}=3, N_{x_1}^{el,tot}=16$ $N_{x_2}^{submesh}=2, N_{x_2}^{el,tot}=7$

The global cell ID in 2D space global_2D_cell is computed from component-wise global cell IDs (kcell_x1, kcell_x2) i.e. global row and column IDs as



 $\text{Figure 6: global_2D_cell} = \texttt{kcell_x2} \times N_{x_1}^{el,tot} + \texttt{kcell_x1} = 5(16) + 2 = 82$

Possible values:

$$0 \leq \texttt{global_2D_cell} \leq N_{2D}^{el,tot} - 1$$

 $N_{2D}^{el,tot}$ – Total number of elements in the 2D domain. On a full mesh $N_{2D}^{el,tot}=N_{x_1}^{el,tot}\times N_{x_2}^{el,tot}$

2D Node Numbering: For a mesh with no inactive blocks the figure below show how the nodes are numbered

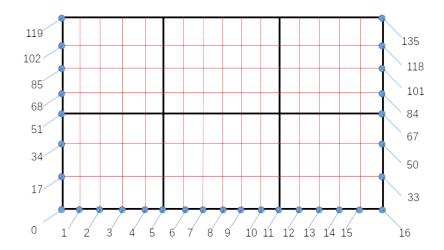


Figure 7: Node numbering is done similar to element numbering

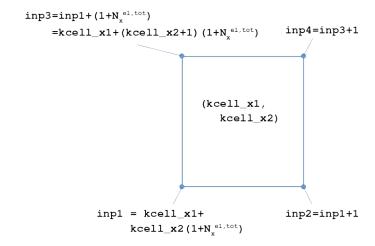


Figure 8: Global Node IDs associated with a given element can be calculated from global column index kcell_x1, global row index kcell_x2 and total elements along x1-direction $N_{x_1}^{el,tot}$

It's only essential to compute the node IDs of left-bottom (inp1) and left-top (inp3) nodes. Their right counterparts (inp2 and inp4) can be obtained by incrementing the values by 1.

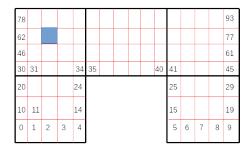
Possible values:

$$0 \leq {\rm inp} \leq N_{2D}^{np,tot} - 1$$

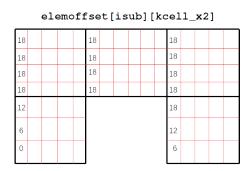
 $N_{2D}^{np,tot}$ – Total number of nodes in the 2D domain. On a full mesh $N_{2D}^{np,tot} = \left(N_{x_1}^{el,tot} + 1\right) \times \left(N_{x_2}^{el,tot} + 1\right)$

4.2 Mesh with Inactive Blocks

2D Element Numbering: For a mesh with inactive blocks the figure below show how the elements are numbered



Elements in the inactive blocks are skipped while numbering. For the sake of analytical computation of node IDs it is necessary to keep track of how many elements are skipped for for each row in each x1-block (see figure below)



Element ID calculation – Example

The global element ID can be computed using the same expression used in full mesh and subtracting an offset (which tracks the number of skipped elements)

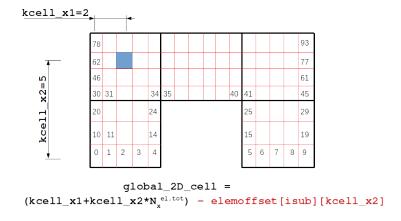
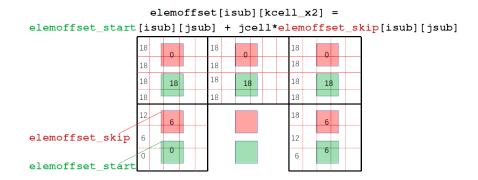
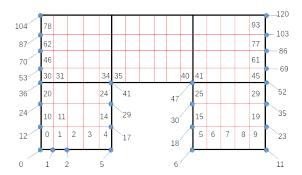


Figure 9: $global_2D_cell = 2+5\times16-18 = 64$

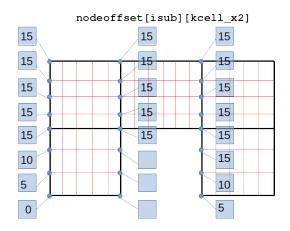
Computation of elemoffset without explicit storage The value of offset for each row in a x1-submesh block can be obtained by storing two additional integers for every submesh block



2D Node Numbering: For a mesh with inactive blocks the figure below show how the nodes are numbered



Same as element numbering, we skip the nodes in the inactive blocks while numbering. However, the offset that keeps track of skipped nodes DO NOT follow the same 'nice' pattern inside a submesh block as the element offsets do.



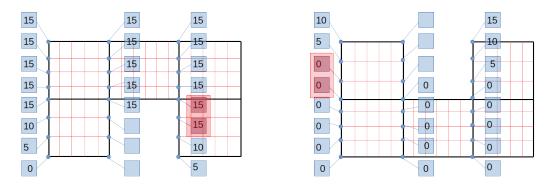
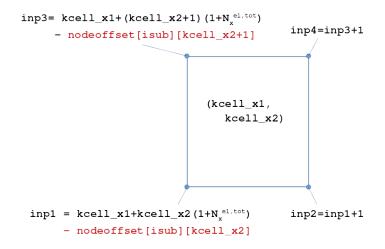


Figure 10: Examples where nodeoffset do not follow the same pattern as the rest of the block



Node ID calculation – Examples

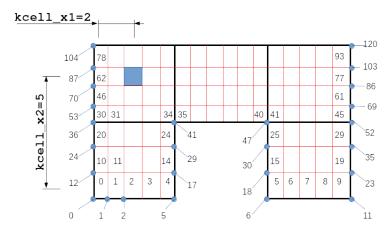


Figure 11: $inp1=2+5\times17-15=72$ $inp3=2+6\times17-15=89$

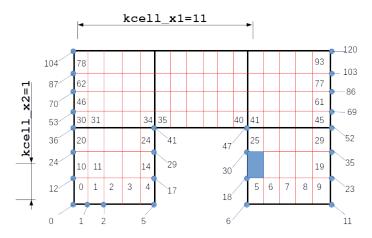
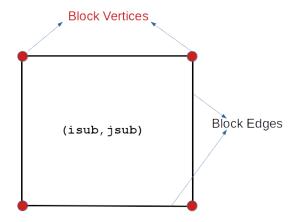


Figure 12: inp1=11+1×17-10=18 inp3=11+2×17-15=30

NOTE: The auxiliary data structures nodeoffset, elemoffset_start, elemoffset_skip are all allocated as kokkos types Kokkos::View<int**> as well as int** so that node/element ID calculations can be performed in GPU and CPU. Class MeshOffsets contains the auxilliary data structures discussed here.

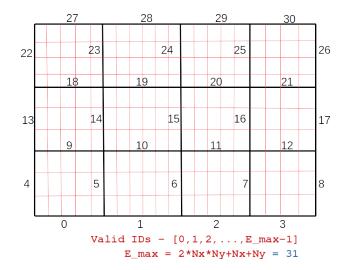
4.3 Block Entity Classification

Every submesh block in a 2D mesh is characterized by 4 edges and 4 vertices



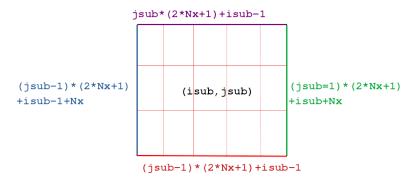
A vertex is a zero-dimensional entity while the edge is an one-dimensional entity. In order to apply different boundary/interface conditions at different locations, we need to ID these entities. In the following sections the convention used for edge and vertex numbering is explained. The convention is standard i.e. regardless of the activity of blocks in the mesh the convention holds.

Standard Block-Edge Numbering

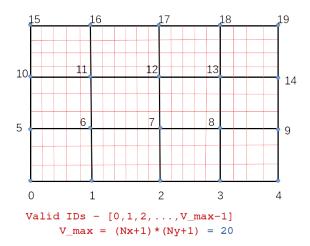


The standardized ID-ing helps us compe up with expressions to obtain the edge IDs of any given block as shown below

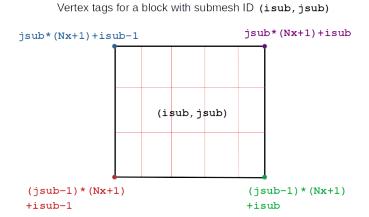
Edge tags for a block with submesh ID (isub, jsub)



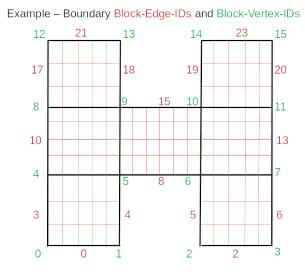
Standard Block-Vertex Numbering



Similarly, for a given block the vertex IDs can be expressed as shown below



For a mesh with inactive blocks, the scheme remains unchanged i.e. the tags corresponding entities in non-active blocks will be invalid



4.4 Boundary Edge/Vertex Information

A boolean value for each edge/vertex stores if the given entity falls on the domain boundary or not. The library provides the API where_is_node() which takes the component-wise node IDs (knode_x1, knode_x2) and returns necessary information on the node such as if node is active, if node is on boundary, if a boundary node is on block-edge or block-vertex. Refer to later sections for API usage. Aside from boundary classification of block edges/vertices, the boundary normal directions are also stored on all boundary entities.

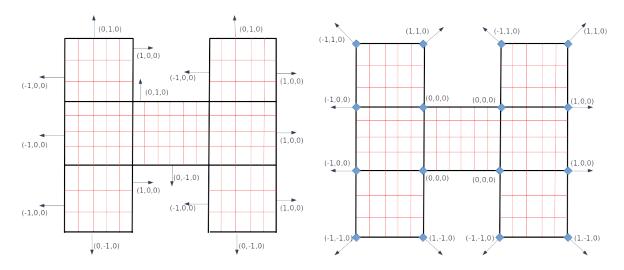
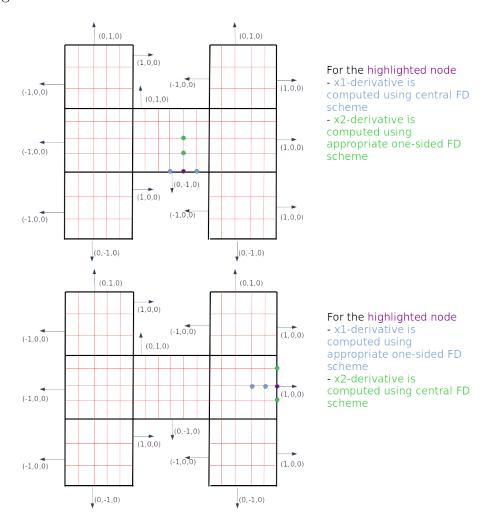


Figure 13: Boundary edge normals (left) and boundary vertex normals (right)

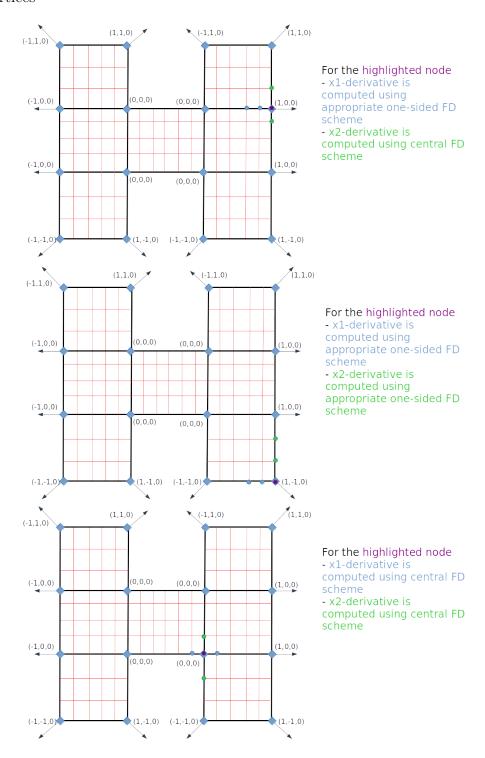
4.5 Gradient computation on boundaries

The normal directions stored on each block-boundary entity defines the rule for gradient computation. The normal direction determines the correct one-sided finite difference (FD) scheme to be implemented. (For second-order accurate gradient, fields from two adjacent nodes are required)

See below, for examples on gradient computation at nodes that falls on boundary block-edge



See below, for examples on gradient computation at nodes that falls on boundary block-vertices



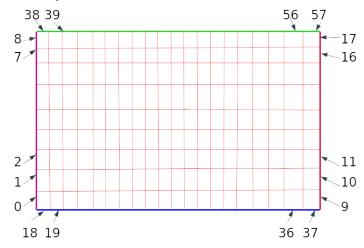
Notice, in the third example, while the node is on boundary it can be treated as a interior node for gradient calculation i.e. central FD scheme can be applied. Hence why the boundary normal for such nodes are set to a zero vector.

4.6 Boundary Element Face IDs

Boundary faces are defined by the part of a mesh element that touches the boundary of a domain. In 1D, a boundary face is a zero-dimensional entity i.e. point. In 2D, it is a one-dimensional entity i.e. line.

In hpic2, there are four possible boundary IDs – east, west, north, south. The boundary element faces are numbered on each boundaries as shown below. First west boundary faces are numbered, then east, then south and finally north faces.

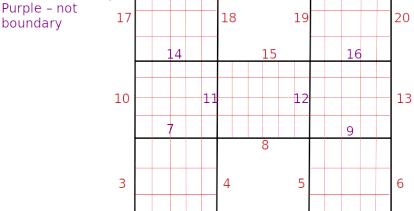
Possible boundary ID in full uniform meshes are east, west, north, south



In pumiMBBL, the possible boundary IDs are set of block-edge tags which are classfied as boundary. See example below,

BDRY-IDs = {0,2,3,4,5,6,10,13,15,17,18,19,20,21,23}
21

Red - is boundary
Purple - not



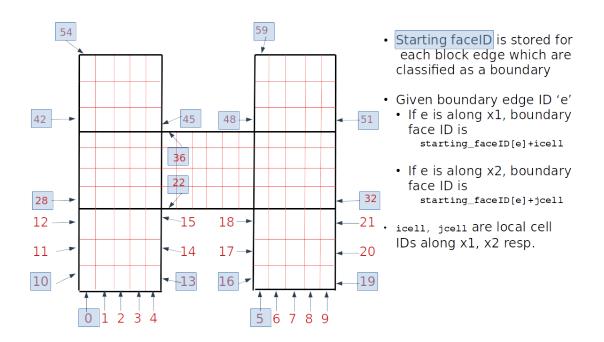
1

23

In pumiMBBL,

- Boundary element faces are numbered on each classified boundary edges
- For the example with $BDRY-IDs=\{0,2,3,4,5,6,10,13,15,17,18,19,20,21,23\}$, first element faces in block-edge #0 are numbered, then block-edge #2, then #3 and so on till block-edge #23
- Numbering order inside an block-edge is done towards the positive direction
 - For block-edges along x1 faces are numbered from left to right
 - For block-edges along x2 faces are numbered from bottom to top

• The starting face ID on each edge is stored, to quickly fetch the face ID of a give a boundary edge ID and an element on that boundary



5 2D weight calculations from 1D linear weights

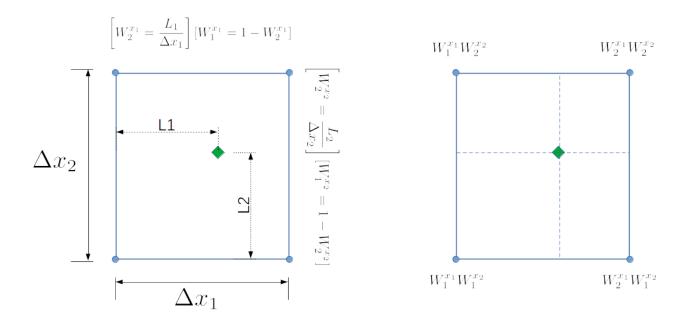


Figure 14: (Left) 1D component-wise weight computation (Right) 1D component-wise weights to 2D weights

6 pumiMBBL-APIs – Get Information (ON HOST)

Mesh-Level Info:

API Name	Args	Return Type	Description
get_global_x1_min	MBBL pumi_obj	double	Domain lower bound x1-coordinate
get_global_x2_min	MBBL pumi_obj	double	Domain lower bound x2-coordinate
get_global_x1_max	MBBL pumi_obj	double	Domain upper bound x1-coordinate
get_global_x2_max	MBBL pumi_obj	double	Domain upper bound x2-coordinate
get_total_mesh_elements	MBBL pumi_obj	int	Total active elements in mesh
get_total_mesh_nodes	MBBL pumi_obj	int	Total active nodes in mesh
get_total_x1_elements	MBBL pumi_obj	int	Total elements along x1
get_total_x2_elements	MBBL pumi_obj	int	Total elements along x2
get_mesh_volume	MBBL pumi_obj	double	Total length in 1D, Active area in 2D of domain

Submesh-Level Info:

API Name	Args	Return Type	Description
get_num_x1_submesh	MBBL pumi_obj	int	Number of blocks along x1
get_num_x2_submesh	MBBL pumi_obj	int	Number of blocks along x2
get_total_submesh_blocks	MBBL pumi_obj	int	Total mesh blocks in domain including inactive blocks
get_num_x1_elems_in_submesh	MBBL pumi_obj, int isub	int	Number of elements along x1 in given block
get_num_x2_elems_in_submesh	MBBL pumi_obj, int jsub	int	Number of elements along x2 in given block
get_num_x1_elems_before_submesh	MBBL pumi_obj, int isub	int	Number of elements along x1 in all preceding blocks
get_num_x2_elems_before_submesh	MBBL pumi_obj, int jsub	int	Number of elements along x2 in all preceding blocks
get_total_elements_in_block	MBBL pumi_obj, int isub, int jsub	int	Total elements in given submesh block
get_total_elements_in_block	MBBL pumi_obj, int flattened_sub_ID	int	Total elements in given submesh block
is_block_active_host	MBBL pumi_obj, int isub, int jsub	bool	Activity status of given submesh block
is_block_active_host	MBBL pumi_obj, int flattened_sub_ID	bool	Activity status of given submesh block

Submesh Vertex related Info:

API Name	Args	Return Type	Description
get_total_mesh_block_verts	MBBL pumi_obj	int	Total number of block-vertices in mesh
is_vert_bdry	MBBL pumi_obj, int vertID	bool	Is given vertex ID part of domain boundary
get_bdry_vert_normal	MBBL pumi_obj, int vertID	Vector3	Boundary normal direction for given vertex ID

Submesh Edge related Info:

API Name	Args	Return Type	Description
get_total_mesh_block_edges	MBBL pumi_obj	int	Total number of block-edges in mesh
is_edge_bdry	MBBL pumi_obj, int edgeID	bool	Is given edge ID part of domain boundary
get_bdry_edge_normal	MBBL pumi_obj, int edgeID	Vector3	Boundary normal direction for given edge ID
get_west_edgeID	<pre>MBBL pumi_obj, int isub, int jsub</pre>	int	edge ID of west edge of given submesh block
get_east_edgeID	<pre>MBBL pumi_obj, int isub, int jsub</pre>	int	edge ID of east edge of given submesh block
get_south_edgeID	<pre>MBBL pumi_obj, int isub, int jsub</pre>	int	edge ID of south edge of given submesh block
get_north_edgeID	MBBL pumi_obj, int isub, int jsub	int	edge ID of north edge of given submesh block
get_num_faces_on_edge	MBBL pumi_obj, int edgeID	int	Number of elements along a given edge ID
get_starting_faceID_on_bdry_edge	MBBL pumi_obj, int edgeID	int	Starting boundary element face ID on give boundary edge

${\bf Mesh~Element/Node~Info}$

API Name	Args	Return Type	Description
get_node_submeshID	MBBL pumi_obj, int knode_x1, int knode_x2	int	Returns the active flattened submesh ID to which a given node belongs to
get_elem_submeshID	MBBL pumi_obj, int kcell_x1, int kcell_x2	int	Returns the active flattened submesh ID to which a given element belongs to
get_global_nodeID_2D	MBBL pumi_obj, int knode_x1, int knode_x2	int	Returns the global node ID (on a 2D mesh) for a given node
get_global_elemID_2D	MBBL pumi_obj, int kcell_x1, int kcell_x2	int	Returns the global element ID (on a 2D mesh) for a given element
where_is_node	<pre>MBBL pumi_obj, int knode_x1, int knode_x2, bool *on_bdry, bool *in_domain, int *bdry_tag, int *bdry_dim</pre>	void	For given node, tells if - if node is on domain boundary - if node is in active domain - boundary tag (if node is on boundary) - boundary dimension (0=block-vertex, 1=block-edge - if node is on boundary)

Directional and flattened IDs

API Name	Args	Return Type	Description
flatten_submeshID_ and_cellID_host	<pre>MBBL pumi_obj, int isub, int icell, int jsub, int jcell, int *flattened_subID, int *flattened_cellID</pre>	void	Converts the directional submesh and cell IDs to flattened submesh and cell IDs on a 2D mesh
<pre>get_directional_submeshID_ and_cellID_host</pre>	<pre>MBBL pumi_obj, int flattened_subID, int flattened_cellID, int *isub, int *icell, int *jsub, int *jcell,</pre>	void	Converts the flattened submesh and cell IDs to directional submesh and cell IDs on a 2D mesh

7 pumiMBBL-APIs – Particle Operations (ON HOST)

API Name	Args	Return Type	Description
get_rand_point_in_mesh_host	MBBL pumi_obj	Vector3	Generates a random point coordinate in active region of the domain
is_point_in_mesh_host	MBBL pumi_obj, Vector3 coords	bool	Tells if a give point coordinates is in active domain
locate_submesh_and_cell_x1_host	MBBL pumi_obj, double x1_coord int *isub, int *icell	void	Computes a give x1-coordinate's submesh ID and cell ID (along x1-direction) Performs global search
locate_submesh_and_cell_x2_host	MBBL pumi_obj, double x2_coord int *jsub, int *jcell	void	Computes a give x2-coordinate's submesh ID and cell ID (along x2-direction) Performs global search
calc_weights_x1_host	MBBL pumi_obj, double x1_coord int isub, int icell, int *kcell_x1, double *Wgh2_x1	void	Computes linear weight (along x1 direction) for the max-side node as well as component-wise global cell ID (along x1), given x1-coords, submesh ID and cell ID
calc_weights_x2_host	MBBL pumi_obj, double x2_coord int jsub, int jcell, int *kcell_x2, double *Wgh2_x2	void	Computes linear weight (along x2 direction) for the max-side node as well as component-wise global cell ID (along x2), given x2-coords, submesh ID and cell ID
calc_global_cellID_and_nodeID_host	<pre>MBBL pumi_obj, int isub, int jsub, int kcell_x1, int kcell_x2, int *global_cellID, int *inp1, int *inp3</pre>	void	Computes global cell and node IDs for a given element (NEEDS the component-wise submesh and cell IDs of the element). Node IDs of bottom-left and top-left nodes of the element are computed. ONLY for 2D mesh

${\bf 8}\quad {\bf pumiMBBL}\ {\bf APIs-ON}\ {\bf DEVICE}$

Submesh-Level Info

API Name	Args	Return Type	Description
	MBBL pumi_obj,		
get_x1_cellID	int isub,	int	Global cell ID along x1
	int icell		
	MBBL pumi_obj,		
get_x2_cellID	int jsub,	int	Global cell ID along x2
	int jcell		
	MBBL pumi_obj,		
get_x1_elem_size_in_submesh	int isub,	double	Element size along x1
	int icell		
	MBBL pumi_obj,		
get_x2_elem_size_in_submesh	int jsub,	double	Elemnet size along x2
	int jcell		

Directional and flattened IDs

API Name	Args	Return Type	Description
flatten_submeshID_ and_cellID	<pre>MBBL pumi_obj, int isub, int icell, int jsub, int jcell, int *flattened_subID, int *flattened_cellID</pre>	void	Converts the directional submesh and cell IDs to flattened submesh and cell IDs on a 2D mesh
<pre>get_directional_submeshID_ and_cellID</pre>	<pre>MBBL pumi_obj, int flattened_subID, int flattened_cellID, int *isub, int *icell, int *jsub, int *jcell,</pre>	void	Converts the flattened submesh and cell IDs to directional submesh and cell IDs on a 2D mesh

Particle Operations

API Name	Args	Return Type	Description
locate_submesh_and_cell_x1	MBBL pumi_obj, double x1_coord int *isub, int *icell	void	Computes a give x1-coordinate's submesh ID and cell ID (along x1-direction) Performs global search
locate_submesh_and_cell_x2	MBBL pumi_obj, double x2_coord int *jsub, int *jcell	void	Computes a give x2-coordinate's submesh ID and cell ID (along x2-direction) Performs global search
update_submesh_and_cell_x1	<pre>MBBL pumi_obj, double x1_coord int isub_old, int icell_old, int *isub, int *icell</pre>	void	Computes a give x1-coordinate's submesh ID and cell ID (along x1-direction) Performs adjacency search with old IDs
update_submesh_and_cell_x2	<pre>MBBL pumi_obj, double x2_coord int jsub_old, int jcell_old, int *jsub, int *jcell</pre>	void	Computes a give x2-coordinate's submesh ID and cell ID (along x2-direction) Performs adjacency search with old IDs
calc_weights_x1	MBBL pumi_obj, double x1_coord int isub, int icell, int *kcell_x1, double *Wgh2_x1	void	Computes linear weight (along x1 direction) for the max-side node as well as component-wise global cell ID (along x1), given x1-coords, submesh ID and cell ID
calc_weights_x2	MBBL pumi_obj, double x2_coord int jsub, int jcell, int *kcell_x2, double *Wgh2_x2	void	Computes linear weight (along x2 direction) for the max-side node as well as component-wise global cell ID (along x2), given x2-coords, submesh ID and cell ID
calc_global_cellID_and_nodeID	<pre>MBBL pumi_obj, int isub, int jsub, int kcell_x1, int kcell_x2, int *global_cellID, int *inp1, int *inp3</pre>	void	Computes global cell and node IDs for a given element (NEEDS the component-wise submesh and cell IDs of the element). Node IDs of bottom- left and top-left nodes of the element are computed. ONLY for 2D mesh
push_particle	MBBL pumi_obj, Vector3 q, Vector3 dq, int *isub, int *jsub, int *icell, int *jcell, bool *crossed_bdry, int *bdry_edge_hit, double *fraction_done, int *bdry_faceID_crossed	Vector3	Particle push performed with convex tracking. Input particle coordinate vector, displacement vector and IDs. Output info includes - updated submesh/cell IDs with adjacency search - did particle cross boundary - boundary ID crossed by particle - fraction of push completed - boundary face ID crossed

9 pumiMBBL APIs – Input Arguments Explained

Variable Name	Description	Valid Inputs
	Object to MBBL structure used	Valid object has
MBBL pumi_obj	to access all pumi mesh informations,	to be initiated from API
	and functions	initialize_MBBL_mesh
int isub	Submesh ID along x1-direction	int b/w $[1, N_{x_1}]$
int jsub	Submesh ID along x2-direction	int b/w $[1, N_{x_2}]$
int	Componentwise IDs converted i.e.	int b/w $[0, N_{x_1}N_{x_2} - 1]$
flattened_subID	flattened to single ID	
int icell	Local x1 cell ID inside a block isub	int b/w $[0, N_{x_1, isub}^{el} - 1]$ int b/w $[0, N_{x_2, jsub}^{el} - 1]$
int jcell	Local x2 cell ID inside a block jsub	int b/w $[0, N_{x_2, jsub}^{el} - 1]$
int	Componentwise IDs converted i.e.	int b/w $[0, N_{x_1, isub}^{el} N_{x_2, jsub}^{el} - 1]$
flattened_cellID	flattened to single ID	
int vertID	Block-Vertex ID	int b/w $[0, (N_{x_1}+1)(N_{x_2}+1)-1]$
int edgeID	Block-Edge ID	int b/w $[0, 2N_{x_1}N_{x_2} + N_{x_1} + N_{x_2} - 1]$
int kcell_x1	x1-component global cell ID	int b/w $[0, N_{x_1}^{el,tot} - 1]$ int b/w $[0, N_{x_2}^{el,tot} - 1]$
int kcell_x2	x2-component global cell ID	int b/w $[0, N_{x_2}^{el,tot} - 1]$
int knode_x1	x1-component global node ID	$\int \int $
int knode_x2	x1-component global node ID	int b/w $[0, N_{x_2}^{el,tot}]$
int	Global cell ID in 1D, 2D	int b/w $0, N^{el,tot}$]
global_cell_ID	(excluding cells in inactive blocks)	int b/w 0, N
bool on_bdry	Tells status of node in 2D mesh	0-true or 1-false
bool on_bary	if it falls on domain boundary or not	0-title of 1-taise
bool in_domain	Tells status of node/coord,	0-true or 1-false
boot in domain	if it falls inside domain or not	o true or r raise
int bdry_tag	Edge-ID or Vertex-ID	Limits based on edge/vertex ID
int bdry_dim	Classification for edge/vertex	0-vertex and 1-edge
double Wgh2_x1	1D linear-weight along x1	double b/w [0.0, 1.0]
double wgiiz_xi	corresponding to max-side	double b/ w [0.0, 1.0]
double Wgh2_x2	1D linear-weight along x2	double b/w $[0.0, 1.0]$
_	corresponding to max-side	, , , ,
double x1_coord	x1-coordinate of particle/point	double b/w $[x_1^{min}, x_1^{max}]$
double x2_coord	x2-coordinate of particle/point	double b/w $[x_2^{min}, x_2^{max}]$
int	IDs of left-bottom,right-	int b/w $[0, N_{np,tot}]$
inp1,inp2,inp3,inp4	bottom,left-top,right-top node in cell	, [, nep,cot
bool crossed_bdry	Tells status if particle has crossed a boundary	0-true or 1-false
int hdry odgo hit	Same as Block-Edge ID where	block-edge ID
int bdry_edge_hit	particle crosses boundary	classified as boundary
double	Fraction of particle push completed	double b/w [0.0, 1.0]
fraction_done		Goudie D/ W [0.0, 1.0]
int	Boundary Face ID where particle	int b/w $[0, N^{bdry-face} - 1]$
bdry_faceID_crossed	crosses a boundary edge	, [~,

NOTE: If pointer versions of variable is passed to function argument, it means the API will compute/update the relevant variable ant store in the argument.

10 PUMI-API Usage

10.1 Particle-related APIs

To locate a particle (and compute its partial nodal weight contributions to the 4 nodes) whose coordinates are (q_1, q_2) in 2D,

- Step-1 Locate the submesh ID and local cell ID (in each direction)
- Step-2 Get the partial component-wise weights corresponding to the max-size node and component-wise global cell IDs (in each direction)
- Step-3 Get the global cell and node IDs in 2D

Step-4 Compute remaining weights and distribute to the corresponding nodes

```
int isub, jsub, icell, jcell, kcell_x1, kcell_x2;
int global_2D_cell, left_bottom_node, left_top_node;
double Wgh2_x1, Wgh2_x2, Wgh1_x1, Wgh1_x2;
// Step-1
pumi::locate_submesh_and_cell_x1(pumi_obj, q1, &isub, &icell);
pumi::locate_submesh_and_cell_x2(pumi_obj, q2, &jsub, &jcell);
// After thist step variables isub, jsub will contain component-wise submesh IDs
// and icell, jcell will contain local cell IDs
//Step-2
pumi::calc_weights_x1(pumi_obj, q1, isub, icell, &kcell_x1, &Wgh2_x1);
pumi::calc_weights_x2(pumi_obj, q2, jsub, jcell, &kcell_x2, &Wgh2_x2);
// After thist step variables kcell_x1, kcell_x2 will contain component-wise global
cell IDs and Wgh2_x1, Wgh2_x2 will contain component-wise weights
//Step-3
pumi::calc_global_cellID_and_nodeID(pumi_obj, kcell_x1, kcell_x2,
&global_2D_cell, &left_bottom_node, &left_top_node);
// After thist step variables global_2D_cell will contain the global element ID and
left_bottom_node, left_top_node will contain the relevant global node IDs
//Step-4
Wgh1_x1 = 1.0 - Wgh2_x1;
Wgh1_x2 = 1.0 - Wgh2_x2;
int right_bottom_node = left_bottom_node + 1;
int right_top_node = left_top_node + 1;
//distribute to relevant nodes
density[left_bottom_node] += Wgh1_x1*Wgh1_x2;
density[left_top_node]
                         += Wgh1_x1*Wgh2_x2;
density[right_bottom_node] += Wgh2_x1*Wgh1_x2;
density[right_top_node]
                          += Wgh2_x1*Wgh2_x2;
```

For a pushed particle whose previous submesh and cell IDs are known use the update routines (implements adjacency search with stored BL node coordinates)

```
int isub, jsub, icell, jcell, kcell_x1, kcell_x2;
int global_2D_cell, left_bottom_node, left_top_node;
double Wgh2_x1, Wgh2_x2;
// Step-1
pumi::update_submesh_and_cell_x1(pumi_obj, q1, isub, icell, &isub, &icell);
pumi::update_submesh_and_cell_x2(pumi_obj, q2, jsub, jcell, &jsub, &jcell);
// After thist step variables isub, jsub will contain component-wise submesh IDs
// and icell, jcell will contain local cell IDs
```

//Step-2 to Step-4 remains unchanged

Particle Push (with inactive blocks)

In case of a domain with inactive blocks particle's coordinate update, previously performed as,

```
q1 += dq1;
q2 += dq2;
pumi::update_submesh_and_cell_x1(pumi_obj, q1, isub, icell, &isub, &icell);
pumi::update_submesh_and_cell_x2(pumi_obj, q2, jsub, jcell, &jsub, &jcell);
needs to be replaced with
pumi::push_particle(pumi_obj, q1, q2, dq1, dq2, &isub, &jsub, &icell, &jcell,
                    &in_domain, &bdry_hit);
```

In addition to updating the submesh and cell IDs, we also update the boolean in_domain to false when a particle goes out of a boundary and the integer bdry_hit to tag of the edge which the particle crosses to go out of the boundary. For particles inside the domain, in_domain is set to true and bdry_hit is set to -1.

NOTE: All the above functions can be called in GPU (i.e. inside Kokkos::parallel_for). Check pumiMBBL_test.cpp for an example.

10.3 Field-related APIs

• The grading ratio (along a given direction) about an node (from its component-wise global node ID i.e. i1, i2) can be obtained as

```
// In x1-direction
double r1 = pumi::return_gradingratio(pumi_obj, pumi::x1_dir, i1);
// In x2-direction
double r2 = pumi::return_gradingratio(pumi_obj, pumi::x2_dir, i2);
```

• The element-length (along a given direction) for an element (from its componentwise global element/node ID i.e. i1, i2) can be obtained as

```
// In x1-direction
double e1 = pumi::return_elemsize(pumi_obj, pumi::x1_dir, kcell_x1,
pumi::elem_input_offset);
```

```
// In x2-direction
double e2 = pumi::return_elemsize(pumi_obj, pumi::x2_dir, kcell_x2,
pumi::elem_input_offset);
```

In the above example kcell_x1, kcell_x2 are element IDs hence the fourth argument is an offset corresponding to element index inputs. If node IDs are to provided as inputs i.e. knode_x1, knode_x2, then provide pumi::elem_on_min_side_offset for element on min-size of node and pumi::elem_on_max_side_offset for max-side element as last argument

• The nodal co-volume about a node (from its component-wise global node IDs i.e. knode_x1, knode_x2) can be obtained as

```
// In 1D mesh
double cv = pumi::return_covolume(pumi_obj, knode_x1);
// In 2D mesh
double cv = pumi::return_covolume(pumi_obj, knode_x1, knode_x2);
```

• Information such as active node, boundary node and entity tag/dimension of a boundary node can be obtained by the following function

After the API call

- If the input node is inside the domain (i.e. not in an inactive block), then in_domain will be set to true. Otherwise it will be false
- If the input node is a boundary node, then on_bdry will be set to true. Otherwise it will be false
- If the input node is a boundary node, then bdry_tag will be set to the tag of the entity to which the node belongs to. For inactive nodes, the tag will be set to −999 and for non-boundary active nodes it will be −1
- If the input node is a boundary node, then bdry_dim will be set to 0 if it falls on block-vertex and 1 if it falls on block-edge. For non-boundary and inactive nodes it will be −1

NOTE: The above APIs can be called only from host. Check pumiMBBL_test.cpp for an example