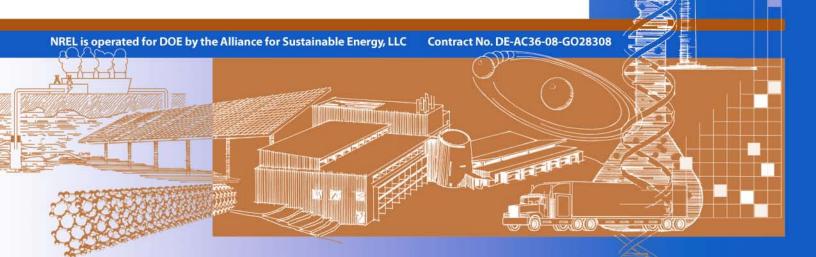


**Innovation for Our Energy Future** 

# Definition of a 5-MW Reference Wind Turbine for Offshore System Development

J. Jonkman, S. Butterfield, W. Musial, and G. Scott

Technical Report NREL/TP-500-38060 February 2009

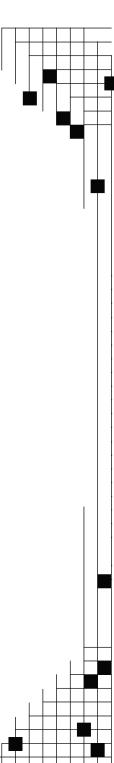


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Prepared under Task No. WER5.3301

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# **Acronyms and Abbreviations**

ADAMS<sup>®</sup> = Automatic Dynamic Analysis of Mechanical Systems

A2AD = ADAMS-to-AeroDyn

BEM = blade-element / momentum

CM = center of mass

DLL = dynamic link library

DOE = U.S. Department of Energy

DOF = degree of freedom

DOWEC = Dutch Offshore Wind Energy Converter project

DU = Delft University

ECN = Energy Research Center of the Netherlands

equiripple = equalized-ripple

FAST = Fatigue, Aerodynamics, Structures, and Turbulence

GE = General Electric

IEA = International Energy Agency

MSL = mean sea level

NACA = National Advisory Committee for Aeronautics

NREL = National Renewable Energy Laboratory

NWTC = National Wind Technology Center

OCS = offshore continental shelf

OC3 = Offshore Code Comparison Collaborative

PI = proportional-integral

PID = proportional-integral-derivative

RECOFF = Recommendations for Design of Offshore Wind Turbines project

WindPACT = Wind Partnerships for Advanced Component Technology project

w.r.t. = with respect to

#### **Nomenclature**

 $A_d$  = discrete-time state matrix

 $B_d$  = discrete-time input matrix

 $C_d$  = discrete-time output state matrix

 $C_{\varphi}$  = effective damping in the equation of motion for the rotor-speed error

 $D_d$  = discrete-time input transmission matrix

 $f_c$  = corner frequency

GK = gain-correction factor

 $I_{Drivetrain}$  = drivetrain inertia cast to the low-speed shaft

 $I_{Gen}$  = generator inertia relative to the high-speed shaft

 $I_{Rotor}$  = rotor inertia

 $K_D$  = blade-pitch controller derivative gain

 $K_I$  = blade-pitch controller integral gain

 $K_P$  = blade-pitch controller proportional gain

 $K_{\varphi}$  = effective stiffness in the equation of motion for the rotor-speed error

 $M_{\varphi}$  = effective inertia (mass) in the equation of motion for the rotor-speed error

*n* = discrete-time-step counter

 $N_{Gear}$  = high-speed to low-speed gearbox ratio

P = mechanical power

 $P_0$  = rated mechanical power

 $\partial P/\partial \theta$  = sensitivity of the aerodynamic power to the rotor-collective blade-pitch angle

t = simulation time

 $T_{Aero}$  = aerodynamic torque in the low-speed shaft

 $T_{Gen}$  = generator torque in the high-speed shaft

 $T_s$  = discrete-time step

*u* = unfiltered generator speed

x = for the control-measurement filter, the filter state

x,y,z = set of orthogonal axes making up a reference-frame coordinate system

y = for the control-measurement filter, the filtered generator speed

 $\alpha$  = low-pass filter coefficient

 $\Delta\theta$  = small perturbation of the blade-pitch angles about their operating point

 $\Delta\Omega$  = small perturbation of the low-speed shaft rotational speed about the rated speed

 $\Delta \dot{\Omega}$  = low-speed shaft rotational acceleration

 $\zeta_{\varphi}$  = damping ratio of the response associated with the equation of motion for the rotor-speed error

 $\theta$  = full-span rotor-collective blade-pitch angle

 $\theta_K$  = rotor-collective blade-pitch angle at which the pitch sensitivity has doubled from

its value at the rated operating point

 $\pi$  = the ratio of a circle's circumference to its diameter

 $\varphi$  = the integral of  $\dot{\varphi}$  with respect to time

 $\dot{\phi}$  = small perturbation of the low-speed shaft rotational speed about the rated speed

 $\ddot{\varphi}$  = low-speed shaft rotational acceleration

 $\Omega$  = low-speed shaft rotational speed

 $Q_0$  = rated low-speed shaft rotational speed

 $\omega_{\varphi n}$  = natural frequency of the response associated with the equation of motion for the

rotor-speed error

# **Executive Summary**

To support concept studies aimed at assessing offshore wind technology, we developed the specifications of a representative utility-scale multimegawatt turbine now known as the "NREL offshore 5-MW baseline wind turbine." This wind turbine is a conventional three-bladed upwind variable-speed variable blade-pitch-to-feather-controlled turbine. To create the model, we obtained some broad design information from the published documents of turbine manufacturers, with a heavy emphasis on the REpower 5M machine. Because detailed data was unavailable, however, we also used the publicly available properties from the conceptual models in the WindPACT, RECOFF, and DOWEC projects. We then created a composite from these data, extracting the best available and most representative specifications. This report documents the specifications of the NREL offshore 5-MW baseline wind turbine—including the aerodynamic, structural, and control-system properties—and the rationale behind its development. The model has been, and will likely continue to be, used as a reference by research teams throughout the world to standardize baseline offshore wind turbine specifications and to quantify the benefits of advanced land- and sea-based wind energy technologies.

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#### 1 Introduction

The U.S. Department of Energy's (DOE's) National Renewable Energy Laboratory (NREL), through the National Wind Technology Center (NWTC), has sponsored conceptual studies aimed at assessing offshore wind technology suitable in the shallow and deep waters off the U.S. offshore continental shelf (OCS) and other offshore sites worldwide. To obtain useful information from such studies, use of realistic and standardized input data is required. This report documents the turbine specifications of what is now called the "NREL offshore 5-MW baseline wind turbine" and the rationale behind its development. Our objective was to establish the detailed specifications of a large wind turbine that is representative of typical utility-scale land- and sea-based multimegawatt turbines, and suitable for deployment in deep waters.

Before establishing the detailed specifications, however, we had to choose the basic size and power rating of the machine. Because of the large portion of system costs in the support structure of an offshore wind system, we understood from the outset that if a deepwater wind system is to be cost-effective, each individual wind turbine must be rated at 5 MW or higher [23]. Ratings considered for the baseline ranged from 5 MW to 20 MW. We decided that the baseline should be 5 MW because it has precedence:

- Feasible floater configurations for offshore wind turbines scoped out by Musial, Butterfield, and Boone [23] were based on the assumption of a 5-MW unit.
- Unpublished DOE offshore cost studies were based on a rotor diameter of 128 m, which is a size representative of a 5- to 6-MW wind turbine.
- The land-based Wind Partnerships for Advanced Component Technology (WindPACT) series of studies, considered wind turbine systems rated up to 5 MW [19,24,29].
- The Recommendations for Design of Offshore Wind Turbines project (known as RECOFF) based its conceptual design calculations on a wind turbine with a 5-MW rating [32].
- The Dutch Offshore Wind Energy Converter (DOWEC) project based its conceptual design calculations on a wind turbine with a 6-MW rating [8,14,17].
- At the time of this writing, the largest wind turbine prototypes in the world—the Multibrid M5000 [5,21,22] and the REpower 5M [18,26,27]—each had a 5-MW rating.

We gathered the publicly available information on the Multibrid M5000 and REpower 5M prototype wind turbines. And because detailed information on these machines was unavailable, we also used the publicly available properties from the conceptual models used in the WindPACT, RECOFF, and DOWEC projects. These models contained much greater detail than was available about the prototypes. We then created a composite from these models, extracting the best available and most representative specifications.

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<sup>&</sup>lt;sup>1</sup> A single 5-MW wind turbine can supply enough energy annually to power 1,250 average American homes.

The Multibrid M5000 machine has a significantly higher tip speed than typical onshore wind turbines and a lower tower-top mass than would be expected from scaling laws previously developed in one of the WindPACT studies [29]. In contrast, the REpower 5M machine has properties that are more "expected" and "conventional." For this reason, we decided to use the specifications of the REpower 5M machine as the target specifications<sup>2</sup> for our baseline model.

The wind turbine used in the DOWEC project had a slightly higher rating than the rating of the REpower 5M machine, but many of the other basic properties of the DOWEC turbine matched the REpower 5M machine very well. In fact, the DOWEC turbine matched many of the properties of the REpower 5M machine better than the turbine properties derived for the WindPACT and RECOFF studies.<sup>3</sup> As a result of these similarities, we made the heaviest use of data from the DOWEC study in our development of the NREL offshore 5-MW baseline wind turbine.

The REpower 5M machine has a rotor radius of about 63 m. Wanting the same radius and the lowest reasonable hub height possible to minimize the overturning moment acting on an offshore substructure, we decided that the hub height for the baseline wind turbine should be 90 m. This would give a 15-m air gap between the blade tips at their lowest point when the wind turbine is undeflected and an estimated extreme 50-year individual wave height of 30 m (i.e., 15-m amplitude). The additional gross properties we chose for the NREL 5-MW baseline wind turbine, most of which are identical to those of the REpower 5M, are given in Table 1-1. The (x,y,z) coordinates of the overall center of mass (CM) location of the wind turbine are indicated in a tower-base coordinate system, which originates along the tower centerline at ground or mean

Table 1-1. Gross Properties Chosen for the NREL 5-MW Baseline Wind Turbine

| Rating                            | 5 MW                               |
|-----------------------------------|------------------------------------|
| Rotor Orientation, Configuration  | Upwind, 3 Blades                   |
| Control                           | Variable Speed, Collective Pitch   |
| Drivetrain                        | High Speed, Multiple-Stage Gearbox |
| Rotor, Hub Diameter               | 126 m, 3 m                         |
| Hub Height                        | 90 m                               |
| Cut-In, Rated, Cut-Out Wind Speed | 3 m/s, 11.4 m/s, 25 m/s            |
| Cut-In, Rated Rotor Speed         | 6.9 rpm, 12.1 rpm                  |
| Rated Tip Speed                   | 80 m/s                             |
| Overhang, Shaft Tilt, Precone     | 5 m, 5°, 2.5°                      |
| Rotor Mass                        | 110,000 kg                         |
| Nacelle Mass                      | 240,000 kg                         |
| Tower Mass                        | 347,460 kg                         |
| Coordinate Location of Overall CM | (-0.2 m, 0.0 m, 64.0 m)            |

<sup>&</sup>lt;sup>2</sup> Note that we established the target specifications using information about the REpower 5M machine that was published in January 2005 [26,27]. Some of the information presented in Refs. [26] and [27] disagrees with more recently published information. For example, the published nacelle and rotor masses of the REpower 5M are higher in the more recent publications.

2

<sup>&</sup>lt;sup>3</sup> This was probably because the REpower 5M prototype utilized blades provided by LM Glasfiber [18], a company that helped establish the structural properties of the blades used in the DOWEC study.

sea level (MSL). The x-axis of this coordinate system is directed nominally downwind, the y-axis is directed transverse to the nominal wind direction, and the z-axis is directed vertically from the tower base to the yaw bearing.

The actual REpower 5M wind turbine uses blades with built-in prebend as a means of increasing tower clearance without a large rotor overhang. Because many of the available simulation tools and design codes cannot support blades with built-in prebend, we chose a 2.5°-upwind precone in the baseline wind turbine to represent the smaller amount of precone and larger amount of prebend that are built into the actual REpower 5M machine.

The rotor diameter indicated in Table 1-1 ignores the effect of blade precone, which reduces the actual diameter and swept area. The exact rotor diameter in the turbine specifications (assuming that the blades are undeflected) is actually (126 m)  $\times cos(2.5^{\circ}) = 125.88$  m and the actual swept area is  $(\pi/4) \times (125.88 \text{ m})^2 = 12,445.3 \text{ m}^2$ .

We present other information about this model as follows:

- The blade structural properties in Section 2
- The blade aerodynamic properties in Section 3
- The hub and nacelle properties in Section 4
- The drivetrain properties in Section 5
- The tower properties in Section 6
- The baseline control system properties in Section 7
- The aero-servo-elastic FAST (Fatigue, Aerodynamics, Structures, and Turbulence) [11] with AeroDyn [16,20] and MSC.ADAMS® (Automatic Dynamic Analysis of Mechanical Systems) with A2AD (ADAMS-to-AeroDyn)<sup>4</sup> [6,15] and AeroDyn models of the wind turbine in Section 8
- The basic responses of the land-based version of the wind turbine, including its full-system natural frequencies and steady-state behavior in Section 9.

Although we summarize much of this information<sup>5</sup> for conciseness and clarity, Section 7 contains a high level of detail about the development of the wind turbine's baseline control system. These details are provided because they are fundamental to the development of more advanced control systems.

The NREL offshore 5-MW baseline wind turbine has been used to establish the reference specifications for a number of research projects supported by the U.S. DOE's Wind & Hydropower Technologies Program [1,2,7,12,28,33,34]. In addition, the integrated European

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<sup>&</sup>lt;sup>4</sup> Note that we use the term "ADAMS" to mean "MSC.ADAMS with A2AD" in this work.

<sup>&</sup>lt;sup>5</sup> Note that some of the turbine properties are presented with a large number (>4) of significant figures. Most of these were carried over from the turbine properties documented in the DOWEC study [8,14,17]—We did not truncate their precision to maintain consistency with the original data source.

Union UpWind research program<sup>6</sup> and the International Energy Agency (IEA) Wind Annex XXIII Subtask 2<sup>7</sup> Offshore Code Comparison Collaboration (OC3) [13,25] have adopted the NREL offshore 5-MW baseline wind turbine as their reference model. The model has been, and will likely continue to be, used as a reference by research teams throughout the world to standardize baseline offshore wind turbine specifications and to quantify the benefits of advanced land- and sea-based wind energy technologies.

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<sup>&</sup>lt;sup>6</sup> Web site: <a href="http://www.upwind.eu/default.aspx">http://www.upwind.eu/default.aspx</a>

<sup>&</sup>lt;sup>7</sup> Web site: <u>http://www.ieawind.org/Annex%20XXIII/Subtask2.html</u>

# 2 Blade Structural Properties

The NREL offshore 5-MW baseline wind turbine has three blades. We based the distributed blade structural properties of each blade on the structural properties of the 62.6-m-long LM Glasfiber blade used in the DOWEC study (using the data given in Appendix A of Ref. [17]). Because the blades in the DOWEC study were 1.1 m longer than the 61.5-m-long LM Glasfiber blades [18] used on the actual REpower 5M machine, we truncated the 62.6-m blades at 61.5-m span to obtain the structural properties of the NREL 5-MW baseline blades (we found the structural properties at the blade tip by interpolating between the 61.2-m and 61.7-m stations given in Appendix A of Ref. [17]). Table 2-1 lists the resulting properties.

The entries in the first column of Table 2-1, labeled "Radius," are the spanwise locations along the blade-pitch axis relative to the rotor center (apex). "BlFract" is the fractional distance along the blade-pitch axis from the roto (0.0) to the tip (1.0). We located the blade root 1.5 m along the pitch axis from the rotor center, equivalent to half the hub diameter listed in Table 1-1.

"AeroCent" is the name of a FAST input parameter. The FAST code assumes that the blade-pitch axis passes through each airfoil section at 25% chord. By definition, then, the quantity (AeroCent – 0.25) is the fractional distance to the aerodynamic center from the blade-pitch axis along the chordline, positive toward the trailing edge. Thus, at the root (i.e., BlFract = 0.0), AeroCent = 0.25 means that the aerodynamic center lies on the blade-pitch axis [because (0.25 – 0.25) = 0.0], and at the tip (i.e., BlFract = 1.0), AeroCent = 0.125 means that the aerodynamic center lies 0.125 chordlengths toward the leading edge from the blade-pitch axis [because (0.125)].

**Table 2-1. Distributed Blade Structural Properties** 

| Radius | BIFract | AeroCent | StrcTwst | BMassDen | FlpStff             | EdgStff             | GJStff              | EAStff      | Alpha | FlpIner | Edglner | PrecryRet | PreswpRef | FlpcgOf | EdgcgOf  | FlpEAOf | f EdgEAOf |
|--------|---------|----------|----------|----------|---------------------|---------------------|---------------------|-------------|-------|---------|---------|-----------|-----------|---------|----------|---------|-----------|
| (m)    | (-)     | (-)      | (°)      | (kg/m)   | (N•m <sup>2</sup> ) | (N•m <sup>2</sup> ) | (N•m <sup>2</sup> ) | (N)         | (-)   | (kg•m)  | (kg•m)  | (m)       | (m)       | (m)     | (m)      | (m)     | (m)       |
|        | 0.00000 | 0.25000  | 13.308   | 678.935  | 18110.00E+6         | 18113.60E+6         | 5564.40E+6          | 9729.48E+6  | 0.0   | 972.86  | 973.04  | 0.0       | 0.0       | 0.0     | 0.00017  | 0.0     |           |
| 1.70   | 0.00325 | 0.25000  | 13.308   | 678.935  | 18110.00E+6         | 18113.60E+6         | 5564.40E+6          | 9729.48E+6  | 0.0   | 972.86  | 973.04  | 0.0       | 0.0       | 0.0     | 0.00017  | 0.0     |           |
| 2.70   | 0.01951 | 0.24951  | 13.308   | 773.363  | 19424.90E+6         | 19558.60E+6         | 5431.59E+6          | 10789.50E+6 | 0.0   | 1091.52 | 1066.38 | 0.0       | 0.0       | 0.0     | -0.02309 | 0.0     | 0.0       |
| 3.70   | 0.03577 | 0.24510  | 13.308   | 740.550  | 17455.90E+6         | 19497.80E+6         | 4993.98E+6          | 10067.23E+6 | 0.0   | 966.09  | 1047.36 | 0.0       | 0.0       | 0.0     | 0.00344  | 0.0     | 0.0       |
| 4.70   | 0.05203 | 0.23284  | 13.308   | 740.042  | 15287.40E+6         | 19788.80E+6         | 4666.59E+6          | 9867.78E+6  | 0.0   | 873.81  | 1099.75 | 0.0       | 0.0       | 0.0     | 0.04345  | 0.0     |           |
| 5.70   | 0.06829 | 0.22059  | 13.308   | 592.496  | 10782.40E+6         | 14858.50E+6         | 3474.71E+6          | 7607.86E+6  | 0.0   | 648.55  | 873.02  | 0.0       | 0.0       | 0.0     | 0.05893  | 0.0     |           |
| 6.70   | 0.08455 | 0.20833  | 13.308   | 450.275  | 7229.72E+6          | 10220.60E+6         | 2323.54E+6          | 5491.26E+6  | 0.0   | 456.76  | 641.49  | 0.0       | 0.0       | 0.0     | 0.06494  | 0.0     | 0.0       |
| 7.70   | 0.10081 | 0.19608  | 13.308   | 424.054  | 6309.54E+6          | 9144.70E+6          | 1907.87E+6          | 4971.30E+6  | 0.0   | 400.53  | 593.73  | 0.0       | 0.0       | 0.0     | 0.07718  | 0.0     | 0.0       |
| 8.70   | 0.11707 | 0.18382  | 13.308   | 400.638  | 5528.36E+6          | 8063.16E+6          | 1570.36E+6          | 4493.95E+6  | 0.0   | 351.61  | 547.18  | 0.0       | 0.0       | 0.0     | 0.08394  | 0.0     | 0.0       |
| 9.70   | 0.13335 | 0.17156  | 13.308   | 382.062  | 4980.06E+6          | 6884.44E+6          | 1158.26E+6          | 4034.80E+6  | 0.0   | 316.12  | 490.84  | 0.0       | 0.0       | 0.0     | 0.10174  | 0.0     |           |
| 10.70  | 0.14959 | 0.15931  | 13.308   | 399.655  | 4936.84E+6          | 7009.18E+6          | 1002.12E+6          | 4037.29E+6  | 0.0   | 303.60  | 503.86  | 0.0       | 0.0       | 0.0     | 0.10758  | 0.0     | 0.0       |
| 11.70  | 0.16585 | 0.14706  | 13.308   | 426.321  | 4691.66E+6          | 7167.68E+6          | 855.90E+6           | 4169.72E+6  | 0.0   | 289.24  | 544.70  | 0.0       | 0.0       | 0.0     | 0.15829  | 0.0     | 0.0       |
| 12.70  | 0.18211 | 0.13481  | 13.181   | 416.820  | 3949.46E+6          | 7271.66E+6          | 672.27E+6           | 4082.35E+6  | 0.0   | 246.57  | 569.90  | 0.0       | 0.0       | 0.0     | 0.22235  | 0.0     | 0.0       |
| 13.70  | 0.19837 | 0.12500  | 12.848   | 406.186  | 3386.52E+6          | 7081.70E+6          | 547.49E+6           | 4085.97E+6  | 0.0   | 215.91  | 601.28  | 0.0       | 0.0       | 0.0     | 0.30756  | 0.0     | 0.0       |
| 14.70  | 0.21465 | 0.12500  | 12.192   | 381.420  | 2933.74E+6          | 6244.53E+6          | 448.84E+6           | 3668.34E+6  | 0.0   | 187.11  | 546.56  | 0.0       | 0.0       | 0.0     | 0.30386  | 0.0     | 0.0       |
| 15.70  | 0.23089 | 0.12500  | 11.561   | 352.822  | 2568.96E+6          | 5048.96E+6          | 335.92E+6           | 3147.76E+6  | 0.0   | 160.84  | 468.71  | 0.0       | 0.0       | 0.0     | 0.26519  | 0.0     | 0.0       |
| 16.70  | 0.24715 | 0.12500  | 11.072   | 349.477  | 2388.65E+6          | 4948.49E+6          | 311.35E+6           | 3011.58E+6  | 0.0   | 148.56  | 453.76  | 0.0       | 0.0       | 0.0     | 0.25941  | 0.0     | 0.0       |
| 17.70  | 0.26341 | 0.12500  | 10.792   | 346.538  | 2271.99E+6          | 4808.02E+6          | 291.94E+6           | 2882.62E+6  | 0.0   | 140.30  | 436.22  | 0.0       | 0.0       | 0.0     | 0.25007  | 0.0     | 0.0       |
| 19.70  | 0.29595 | 0.12500  | 10.232   | 339.333  | 2050.05E+6          | 4501.40E+6          | 261.00E+6           | 2613.97E+6  | 0.0   | 124.61  | 398.18  | 0.0       | 0.0       | 0.0     | 0.23155  | 0.0     | 0.0       |
| 21.70  | 0.32846 | 0.12500  | 9.672    | 330.004  | 1828.25E+6          | 4244.07E+6          | 228.82E+6           | 2357.48E+6  | 0.0   | 109.42  | 362.08  | 0.0       | 0.0       | 0.0     | 0.20382  | 0.0     | 0.0       |
| 23.70  | 0.36098 | 0.12500  | 9.110    | 321.990  | 1588.71E+6          | 3995.28E+6          | 200.75E+6           | 2146.86E+6  | 0.0   | 94.36   | 335.01  | 0.0       | 0.0       | 0.0     | 0.19934  | 0.0     | 0.0       |
| 25.70  | 0.39350 | 0.12500  | 8.534    | 313.820  | 1361.93E+6          | 3750.76E+6          | 174.38E+6           | 1944.09E+6  | 0.0   | 80.24   | 308.57  | 0.0       | 0.0       | 0.0     | 0.19323  | 0.0     | 0.0       |
| 27.70  | 0.42602 | 0.12500  | 7.932    | 294.734  | 1102.38E+6          | 3447.14E+6          | 144.47E+6           | 1632.70E+6  | 0.0   | 62.67   | 263.87  | 0.0       | 0.0       | 0.0     | 0.14994  | 0.0     | 0.0       |
| 29.70  | 0.45855 | 0.12500  | 7.321    | 287.120  | 875.80E+6           | 3139.07E+6          | 119.98E+6           | 1432.40E+6  | 0.0   | 49.42   | 237.06  | 0.0       | 0.0       | 0.0     | 0.15421  | 0.0     | 0.0       |
| 31.70  | 0.49106 | 0.12500  | 6.711    | 263.343  | 681.30E+6           | 2734.24E+6          | 81.19E+6            | 1168.76E+6  | 0.0   | 37.34   | 196.41  | 0.0       | 0.0       | 0.0     | 0.13252  | 0.0     | 0.0       |
| 33.70  | 0.52358 | 0.12500  | 6.122    | 253.207  | 534.72E+6           | 2554.87E+6          | 69.09E+6            | 1047.43E+6  | 0.0   | 29.14   | 180.34  | 0.0       | 0.0       | 0.0     | 0.13313  | 0.0     | 0.0       |
| 35.70  | 0.55610 | 0.12500  | 5.546    | 241.666  | 408.90E+6           | 2334.03E+6          | 57.45E+6            | 922.95E+6   | 0.0   | 22.16   | 162.43  | 0.0       | 0.0       | 0.0     | 0.14035  | 0.0     | 0.0       |
| 37.70  | 0.58862 | 0.12500  | 4.971    | 220.638  | 314.54E+6           | 1828.73E+6          | 45.92E+6            | 760.82E+6   | 0.0   | 17.33   | 134.83  | 0.0       | 0.0       | 0.0     | 0.13950  | 0.0     | 0.0       |
| 39.70  | 0.62115 | 0.12500  | 4.401    | 200.293  | 238.63E+6           | 1584.10E+6          | 35.98E+6            | 648.03E+6   | 0.0   | 13.30   | 116.30  | 0.0       | 0.0       | 0.0     | 0.15134  | 0.0     | 0.0       |
| 41.70  | 0.65366 | 0.12500  | 3.834    | 179.404  | 175.88E+6           | 1323.36E+6          | 27.44E+6            | 539.70E+6   | 0.0   | 9.96    | 97.98   | 0.0       | 0.0       | 0.0     | 0.17418  | 0.0     | 0.0       |
| 43.70  | 0.68618 | 0.12500  | 3.332    | 165.094  | 126.01E+6           | 1183.68E+6          | 20.90E+6            | 531.15E+6   | 0.0   | 7.30    | 98.93   | 0.0       | 0.0       | 0.0     | 0.24922  | 0.0     | 0.0       |
| 45.70  | 0.71870 | 0.12500  | 2.890    | 154.411  | 107.26E+6           | 1020.16E+6          | 18.54E+6            | 460.01E+6   | 0.0   | 6.22    | 85.78   | 0.0       | 0.0       | 0.0     | 0.26022  | 0.0     |           |
| 47.70  | 0.75122 | 0.12500  | 2.503    | 138.935  | 90.88E+6            | 797.81E+6           | 16.28E+6            | 375.75E+6   | 0.0   | 5.19    | 69.96   | 0.0       | 0.0       | 0.0     | 0.22554  | 0.0     |           |
| 49.70  | 0.78376 | 0.12500  | 2.116    | 129.555  | 76.31E+6            | 709.61E+6           | 14.53E+6            | 328.89E+6   | 0.0   | 4.36    | 61.41   | 0.0       | 0.0       | 0.0     | 0.22795  | 0.0     | 0.0       |
| 51.70  | 0.81626 | 0.12500  | 1.730    | 107.264  | 61.05E+6            | 518.19E+6           | 9.07E+6             | 244.04E+6   | 0.0   | 3.36    | 45.44   | 0.0       | 0.0       | 0.0     | 0.20600  | 0.0     | 0.0       |
| 53.70  | 0.84878 | 0.12500  | 1.342    | 98.776   | 49.48E+6            | 454.87E+6           | 8.06E+6             | 211.60E+6   | 0.0   | 2.75    | 39.57   | 0.0       | 0.0       | 0.0     | 0.21662  | 0.0     |           |
| 55.70  | 0.88130 | 0.12500  | 0.954    | 90.248   | 39.36E+6            | 395.12E+6           | 7.08E+6             | 181.52E+6   | 0.0   | 2.21    | 34.09   | 0.0       | 0.0       | 0.0     | 0.22784  | 0.0     | 0.0       |
| 56.70  | 0.89756 | 0.12500  | 0.760    | 83.001   | 34.67E+6            | 353.72E+6           | 6.09E+6             | 160.25E+6   | 0.0   | 1.93    | 30.12   | 0.0       | 0.0       | 0.0     | 0.23124  | 0.0     |           |
| 57.70  | 0.91382 | 0.12500  | 0.574    | 72.906   | 30.41E+6            | 304.73E+6           | 5.75E+6             | 109.23E+6   | 0.0   | 1.69    | 20.15   | 0.0       | 0.0       | 0.0     | 0.14826  | 0.0     |           |
| 58.70  | 0.93008 | 0.12500  | 0.404    | 68.772   | 26.52E+6            | 281.42E+6           | 5.33E+6             | 100.08E+6   | 0.0   | 1.49    | 18.53   | 0.0       | 0.0       | 0.0     | 0.15346  | 0.0     |           |
| 59.20  | 0.93821 | 0.12500  | 0.319    | 66.264   | 23.84E+6            | 261.71E+6           | 4.94E+6             | 92.24E+6    | 0.0   | 1.34    | 17.11   | 0.0       | 0.0       | 0.0     | 0.15382  | 0.0     | 0.0       |
| 59.70  | 0.94636 | 0.12500  | 0.253    | 59.340   | 19.63E+6            | 158.81E+6           | 4.24E+6             | 63.23E+6    | 0.0   | 1.10    | 11.55   | 0.0       | 0.0       | 0.0     | 0.09470  | 0.0     | 0.0       |
| 60.20  | 0.95447 | 0.12500  | 0.216    | 55.914   | 16.00E+6            | 137.88E+6           | 3.66E+6             | 53.32E+6    | 0.0   | 0.89    | 9.77    | 0.0       | 0.0       | 0.0     | 0.09018  | 0.0     |           |
| 60.70  | 0.96260 | 0.12500  | 0.178    | 52.484   | 12.83E+6            | 118.79E+6           | 3.13E+6             | 44.53E+6    | 0.0   | 0.71    | 8.19    | 0.0       | 0.0       | 0.0     | 0.08561  | 0.0     | 0.0       |
| 61.20  | 0.97073 | 0.12500  | 0.140    | 49.114   | 10.08E+6            | 101.63E+6           | 2.64E+6             | 36.90E+6    | 0.0   | 0.56    | 6.82    | 0.0       | 0.0       | 0.0     | 0.08035  | 0.0     | 0.0       |
| 61.70  | 0.97886 | 0.12500  | 0.101    | 45.818   | 7.55E+6             | 85.07E+6            | 2.17E+6             | 29.92E+6    | 0.0   | 0.42    | 5.57    | 0.0       | 0.0       | 0.0     | 0.07096  | 0.0     | 0.0       |
| 62.20  | 0.98699 | 0.12500  | 0.062    | 41.669   | 4.60E+6             | 64.26E+6            | 1.58E+6             | 21.31E+6    | 0.0   | 0.25    | 4.01    | 0.0       | 0.0       | 0.0     | 0.05424  | 0.0     |           |
| 62.70  | 0.99512 | 0.12500  | 0.023    | 11.453   | 0.25E+6             | 6.61E+6             | 0.25E+6             | 4.85E+6     | 0.0   | 0.04    | 0.94    | 0.0       | 0.0       | 0.0     | 0.05387  | 0.0     | 0.0       |
| 63.00  | 1.00000 | 0.12500  | 0.000    | 10.319   | 0.17E+6             | 5.01E+6             | 0.19E+6             | 3.53E+6     | 0.0   | 0.02    | 0.68    | 0.0       | 0.0       | 0.0     | 0.05181  | 0.0     | 0.0       |

$$-0.25$$
) =  $-0.125$ ].

The flapwise and edgewise section stiffness and inertia values, "FlpStff," "EdgStff," "FlpIner," and "EdgIner" in Table 2-1, are given about the principal structural axes of each cross section as oriented by the structural-twist angle, "StrcTwst." The values of the structural twist were assumed to be identical to the aerodynamic twist discussed in Section 3.

"GJStff" represents the values of the blade torsion stiffness. Because the DOWEC blade data did not contain extensional stiffness information, we estimated the blade extensional stiffness values—"EAStff" in Table 2-1—to be  $10^7$  times the average mass moment of inertia at each blade station. This came from a rule of thumb derived from the data available in the WindPACT rotor design study [19], but the exact values are not important because of the low rotational speed of the rotor.

The edgewise CM offset values, "EdgcgOf," are the distances in meters along the chordline from the blade-pitch axis to the CM of the blade section, positive toward the trailing edge. We neglected the insignificant values of the flapwise CM offsets, "FlpcgOf," and flapwise and edgewise elastic offsets, "FlpEAOf" and "EdgEAOf," given in Appendix A of Ref. [17]. Instead, we assumed that they were zero as shown in Table 2-1.

The distributed blade section mass per unit length values, "BMassDen," given in Table 2-1 are the values documented in Appendix A of Ref. [17]. We increased these by 4.536% in the model to scale the overall (integrated) blade mass to 17,740 kg, which was the nominal mass of the blades in the REpower 5M prototype. In our baseline specifications, the nominal second mass moment of inertia, nominal first mass moment of inertia, and the nominal radial CM location of each blade are 11,776,047 kg·m², 363,231 kg·m, and 20.475 m with respect to (w.r.t.) the blade root, respectively.

We specified a structural-damping ratio of 0.477465% critical in all modes of the isolated blade, which corresponds to the 3% logarithmic decrement used in the DOWEC study from page 20 of Ref. [14].

Table 2-2 summarizes the undistributed blade structural properties discussed in this section.

Table 2-2. Undistributed Blade Structural Properties

| rabio 2 2. Orialotribatoa Blado Otraotaran roportico |                  |  |  |  |  |  |  |  |
|--|------------------|--|--|--|--|--|--|--|
| Length (w.r.t. Root Along Preconed Axis)             | 61.5 m           |  |  |  |  |  |  |  |
| Mass Scaling Factor                                  | 4.536 %          |  |  |  |  |  |  |  |
| Overall (Integrated) Mass                            | 17,740 kg        |  |  |  |  |  |  |  |
| Second Mass Moment of Inertia (w.r.t. Root)          | 11,776,047 kg•m² |  |  |  |  |  |  |  |
| First Mass Moment of Inertia (w.r.t. Root)           | 363,231 kg•m     |  |  |  |  |  |  |  |
| CM Location (w.r.t. Root along Preconed Axis)        | 20.475 m         |  |  |  |  |  |  |  |
| Structural-Damping Ratio (All Modes)                 | 0.477465 %       |  |  |  |  |  |  |  |

# 3 Blade Aerodynamic Properties

Similar to the blade structural properties, we based the blade aerodynamic properties of the NREL 5-MW baseline wind turbine on the DOWEC blades (using the data described in Table 1 on page 13 of Ref. [14] and in Appendix A of Ref. [17]). We set the FAST with AeroDyn and ADAMS with AeroDyn models to use 17 blade elements for integration of the aerodynamic and structural forces. To better capture the large structural gradients at the blade root and the large aerodynamic gradients at the blade tip, the 3 inboard and 3 outboard elements are two-thirds the size of the 11 equally spaced midspan elements. Table 3-1 gives the aerodynamic properties at the blade nodes, which are located at the center of the blade elements.

The blade node locations, labeled as "RNodes" in Table 3-1, are directed along the blade-pitch axis from the rotor center (apex) to the blade cross sections. The element lengths, "DRNodes," sum to the total blade length of 61.5 m indicated in Table 2-2. The aerodynamic twist, "AeroTwst," as given in Table 3-1, are offset by  $-0.09182^{\circ}$  from the values provided in Appendix A of Ref. [17] to ensure that the zero-twist reference location is at the blade tip. Integrating the chord distribution along the blade span reveals that the rotor solidity is roughly 5.16%.

As indicated in Table 3-1, we incorporated eight unique airfoil-data tables for the NREL offshore 5-MW baseline wind turbine. The two innermost airfoil tables represent cylinders with drag coefficients of 0.50 (Cylinder1.dat) and 0.35 (Cylinder2.dat) and no lift. We created the remaining six airfoil tables by making corrections for three-dimensional behavior to the two-dimensional airfoil-data coefficients of the six airfoils used in the DOWEC study (as detailed in

Table 3-1. Distributed Blade Aerodynamic Properties

|      | <u> </u> |          |         | - J   |                |
|------|----------|----------|---------|-------|----------------|
| Node | RNodes   | AeroTwst | DRNodes | Chord | Airfoil Table  |
| (-)  | (m)      | (°)      | (m)     | (m)   | (-)            |
| 1    | 2.8667   | 13.308   | 2.7333  | 3.542 | Cylinder1.dat  |
| 2    | 5.6000   | 13.308   | 2.7333  | 3.854 | Cylinder1.dat  |
| 3    | 8.3333   | 13.308   | 2.7333  | 4.167 | Cylinder2.dat  |
| 4    | 11.7500  | 13.308   | 4.1000  | 4.557 | DU40_A17.dat   |
| 5    | 15.8500  | 11.480   | 4.1000  | 4.652 | DU35_A17.dat   |
| 6    | 19.9500  | 10.162   | 4.1000  | 4.458 | DU35_A17.dat   |
| 7    | 24.0500  | 9.011    | 4.1000  | 4.249 | DU30_A17.dat   |
| 8    | 28.1500  | 7.795    | 4.1000  | 4.007 | DU25_A17.dat   |
| 9    | 32.2500  | 6.544    | 4.1000  | 3.748 | DU25_A17.dat   |
| 10   | 36.3500  | 5.361    | 4.1000  | 3.502 | DU21_A17.dat   |
| 11   | 40.4500  | 4.188    | 4.1000  | 3.256 | DU21_A17.dat   |
| 12   | 44.5500  | 3.125    | 4.1000  | 3.010 | NACA64_A17.dat |
| 13   | 48.6500  | 2.319    | 4.1000  | 2.764 | NACA64_A17.dat |
| 14   | 52.7500  | 1.526    | 4.1000  | 2.518 | NACA64_A17.dat |
| 15   | 56.1667  | 0.863    | 2.7333  | 2.313 | NACA64_A17.dat |
| 16   | 58.9000  | 0.370    | 2.7333  | 2.086 | NACA64_A17.dat |
| 17   | 61.6333  | 0.106    | 2.7333  | 1.419 | NACA64_A17.dat |
|      |          |          |         |       |                |

Appendix A of Ref. [14]).<sup>8</sup> In these airfoil tables, "DU" refers to Delft University and "NACA" refers to the National Advisory Committee for Aeronautics. We used AirfoilPrep v2.0 [9] to "tailor" these airfoil data. We first corrected the lift and drag coefficients for rotational stall delay using the Selig and Eggars method for 0° to 90° angles of attack. We then corrected the drag coefficients using the Viterna method for 0° to 90° angles of attack assuming an aspect ratio of 17. Finally, we estimated the Beddoes-Leishman dynamic-stall hysteresis parameters. We made no corrections to the DOWEC-supplied pitching-moment coefficients. The resulting three-dimensionally corrected airfoil-data coefficients are illustrated graphically in Figure 3-1 through Figure 3-6. The numerical values are documented in the AeroDyn airfoil-data input files that make up Appendix B.

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<sup>&</sup>lt;sup>8</sup> C. Lindenburg of the Energy Research Center of the Netherlands (ECN) provided numerical values for these coefficients.

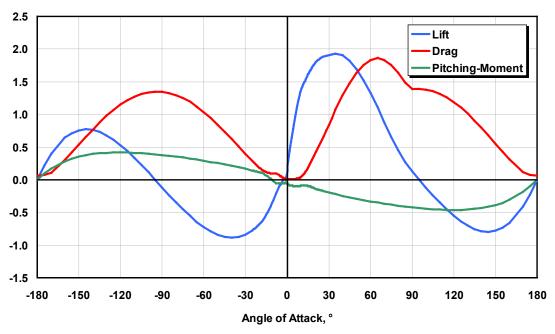


Figure 3-1. Corrected coefficients of the DU40 airfoil

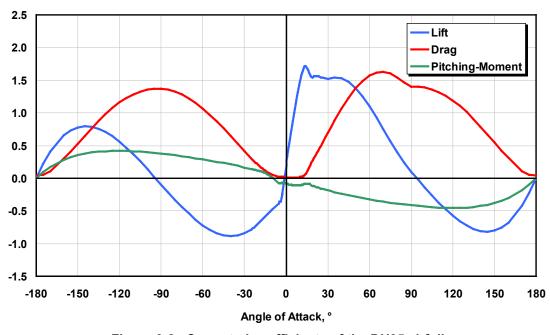


Figure 3-2. Corrected coefficients of the DU35 airfoil

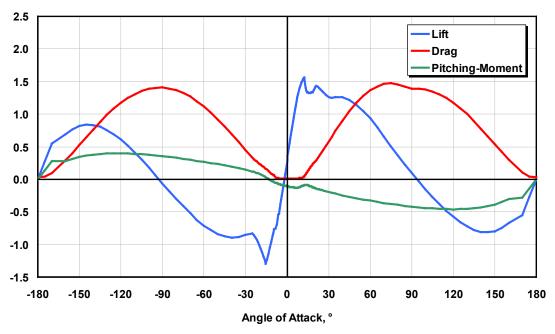


Figure 3-3. Corrected coefficients of the DU30 airfoil

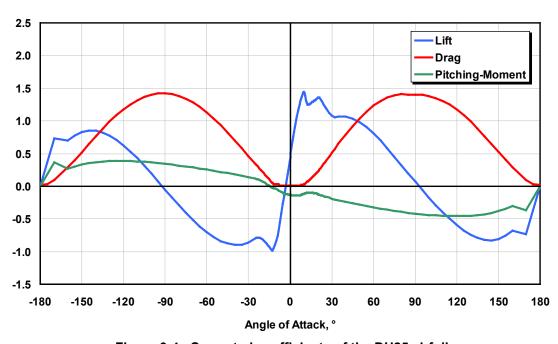


Figure 3-4. Corrected coefficients of the DU25 airfoil

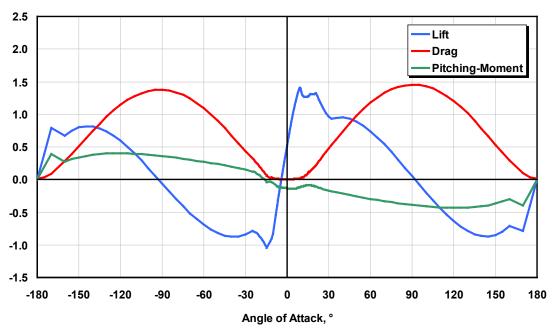


Figure 3-5. Corrected coefficients of the DU21 airfoil

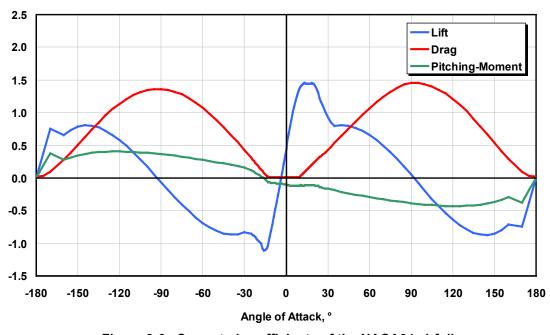


Figure 3-6. Corrected coefficients of the NACA64 airfoil

# 4 Hub and Nacelle Properties

As indicated in Table 1-1, we located the hub of the NREL 5-MW baseline wind turbine 5 m upwind of the tower centerline at an elevation of 90 m above the ground when the system is undeflected. We also specified the same vertical distance from the tower top to the hub height used by the DOWEC study—that is, 2.4 m (as specified in Table 6 on page 26 of Ref. [14]). Consequently, the elevation of the yaw bearing above ground or MSL is 87.6 m. With a shaft tilt of 5°, this made the distance directed along the shaft from the hub center to the yaw axis 5.01910 m and the vertical distance along the yaw axis from the tower top to the shaft 1.96256 m. The distance directed along the shaft from the hub center to the main bearing was taken to be 1.912 m (from Table 6 on page 26 of Ref. [14]).

We specified the hub mass to be 56,780 kg like in the REpower 5M, and we located its CM at the hub center. The hub inertia about the shaft, taken to be 115,926 kg·m², was found by assuming that the hub casting is a thin spherical shell with a radius of 1.75 m (this is 0.25 m longer than the actual hub radius because the nacelle height of the DOWEC turbine was 3.5 m, based on the data in Table 6 on page 26 of Ref. [14]).

We specified the nacelle mass to be 240,000 kg like in the REpower 5M and we located its CM 1.9 m downwind of the yaw axis like in the DOWEC turbine (from Table 7 on page 27 of Ref. [14]) and 1.75 m above the yaw bearing, which was half the height of the DOWEC turbine's nacelle (from Table 6 on page 26 of Ref. [14]). The nacelle inertia about the yaw axis was taken to be 2,607,890 kg·m². We chose this to be equivalent to the DOWEC turbine's nacelle inertia about its nacelle CM, but translated to the yaw axis using the parallel-axis theorem with the nacelle mass and downwind distance to the nacelle CM.

We took the nacelle-yaw actuator to have a natural frequency of 3 Hz, which is roughly equivalent to the highest full-system natural frequency in the FAST model (see Section 9), and a damping ratio of 2% critical. This resulted in an equivalent nacelle-yaw-actuator linear-spring constant of 9,028,320,000 N•m/rad and an equivalent nacelle-yaw-actuator linear-damping constant of 19,160,000 N•m/(rad/s). The nominal nacelle-yaw rate was chosen to be the same as that for the DOWEC 6-MW turbine, or 0.3°/s (from page 27 of Ref. [14]).

Table 4-1 summarizes the nacelle and hub properties discussed in this section.

Table 4-1. Nacelle and Hub Properties

| Elevation of Yaw Bearing above Ground                      | 87.6 m                 |
|--|------------------------|
| Vertical Distance along Yaw Axis from Yaw Bearing to Shaft | 1.96256 m              |
| Distance along Shaft from Hub Center to Yaw Axis           | 5.01910 m              |
| Distance along Shaft from Hub Center to Main Bearing       | 1.912 m                |
| Hub Mass   | 56,780 kg              |
| Hub Inertia about Low-Speed Shaft                          | 115,926 kg•m²          |
| Nacelle Mass   | 240,000 kg             |
| Nacelle Inertia about Yaw Axis                             | 2,607,890 kg•m²        |
| Nacelle CM Location Downwind of Yaw Axis                   | 1.9 m                  |
| Nacelle CM Location above Yaw Bearing                      | 1.75 m                 |
| Equivalent Nacelle-Yaw-Actuator Linear-Spring Constant     | 9,028,320,000 N•m/rad  |
| Equivalent Nacelle-Yaw-Actuator Linear-Damping Constant    | 19,160,000 N•m/(rad/s) |
| Nominal Nacelle-Yaw Rate                                   | 0.3 °/s                |

# 5 Drivetrain Properties

We specified the NREL 5-MW baseline wind turbine to have the same rated rotor speed (12.1 rpm), rated generator speed (1173.7 rpm), and gearbox ratio (97:1) as the REpower 5M machine. The gearbox was assumed be a typical multiple-stage gearbox but with no frictional losses—a requirement of the preprocessor functionality in FAST for creating ADAMS models [11]. The electrical efficiency of the generator was taken to be 94.4%. This was chosen to be roughly the same as the total mechanical-to-electrical conversion loss used by the DOWEC turbine at rated power—that is, the DOWEC turbine had about 0.35 MW of power loss at about 6.25 MW of aerodynamic power (from Figure 15, page 24 of Ref. [14]). The generator inertia about the high-speed shaft was taken to be 534.116 kg·m², which is the same equivalent low-speed shaft generator inertia used in the DOWEC study (i.e., 5,025,500 kg·m² from page 36 of Ref. [14]).

The driveshaft was taken to have the same natural frequency as the RECOFF turbine model and a structural-damping ratio—associated with the free-free mode of a drivetrain composed of a rigid generator and rigid rotor—of 5% critical. This resulted in an equivalent driveshaft linear-spring constant of 867,637,000 N•m/rad and a linear-damping constant of 6,215,000 N•m/(rad/s).

The high-speed shaft brake was assumed to have the same ratio of maximum brake torque to maximum generator torque and the same time lag as used in the DOWEC study (from page 29 of Ref. [14]). This resulted in a fully deployed high-speed shaft brake torque of 28,116.2 N•m and a time lag of 0.6 s. This time lag is the amount of time it takes for the brake to fully engage once deployed. The FAST and ADAMS models employ a simple linear ramp from nothing to full braking over the 0.6-s period.

Table 5-1 summarizes the drivetrain properties discussed in this section.

Table 5-1. Drivetrain Properties

| 145.00 5  |                       |
|---|-----------------------|
| Rated Rotor Speed                                 | 12.1 rpm              |
| Rated Generator Speed                             | 1173.7 rpm            |
| Gearbox Ratio                                     | 97 :1                 |
| Electrical Generator Efficiency                   | 94.4 %                |
| Generator Inertia about High-Speed Shaft          | 534.116 kg•m²         |
| Equivalent Drive-Shaft Torsional-Spring Constant  | 867,637,000 N•m/rad   |
| Equivalent Drive-Shaft Torsional-Damping Constant | 6,215,000 N•m/(rad/s) |
| Fully-Deployed High-Speed Shaft Brake Torque      | 28,116.2 N•m          |
| High-Speed Shaft Brake Time Constant              | 0.6 s                 |

# **6 Tower Properties**

The properties of the tower for the NREL offshore 5-MW baseline wind turbine will depend on the type support structure used to carry the rotor-nacelle assembly. The type of support structure will, in turn, depend on the installation site, whose properties vary significantly through differences in water depth, soil type, and wind and wave severity. Offshore support-structure types include fixed-bottom monopiles, gravity bases, and space-frames—such as tripods, quadpods, and lattice frames (e.g., "jackets")—and floating structures. This section documents the tower properties for the equivalent land-based version of the NREL 5-MW baseline wind turbine. These properties provide a basis with which to design towers for site-specific offshore support structures. For example, different types of offshore support structures for the NREL 5-MW baseline wind turbine have been designed for—and investigated in—separate phases of the OC3 project [13,25].

We based the distributed properties of the land-based tower for the NREL 5-MW baseline wind turbine on the base diameter (6 m) and thickness (0.027 m), top diameter (3.87 m) and thickness (0.019 m), and effective mechanical steel properties of the tower used in the DOWEC study (as given in Table 9 on page 31 of Ref. [14]). The Young's modulus was taken to be 210 GPa, the shear modulus was taken to be 80.8 GPa, and the effective density of the steel was taken to be 8,500 kg/m³. The density of 8,500 kg/m³ was meant to be an increase above steel's typical value of 7,850 kg/m³ to account for paint, bolts, welds, and flanges that are not accounted for in the tower thickness data. The radius and thickness of the tower were assumed to be linearly tapered from the tower base to tower top. Because the REpower 5M machine had a larger tower-top mass than the DOWEC wind turbine, we scaled up the thickness of the tower relative to the values given earlier in this paragraph to strengthen the tower. We chose an increase of 30% to ensure that the first fore-aft and side-to-side tower frequencies were placed between the one- and three-per-rev frequencies throughout the operational range of the wind turbine in a Campbell diagram. Table 6-1 gives the resulting distributed tower properties.

The entries in the first column, "Elevation," are the vertical locations along the tower centerline relative to the tower base. "HtFract" is the fractional height along the tower centerline from the tower base (0.0) to the tower top (1.0). The rest of columns are similar to those described for the distributed blade properties presented in Table 2-1.

The resulting overall (integrated) tower mass is 347,460 kg and is centered at 38.234 m along the

**Table 6-1. Distributed Tower Properties** 

|           | rabio o il Biotribatoa romoi i roportico |          |           |           |           |           |          |          |          |          |
|-----------|--|----------|-----------|-----------|-----------|-----------|----------|----------|----------|----------|
| Elevation | HtFract                                  | TMassDen | TwFAStif  | TwSSStif  | TwGJStif  | TwEAStif  | TwFAlner | TwSSIner | TwFAcgOf | TwSScgOf |
| (m)       | (-)                                      | (kg/m)   | (N•m²)    | (N•m²)    | (N•m²)    | (N)       | (kg•m)   | (kg•m)   | (m)      | (m)      |
| 0.00      | 0.0                                      | 5590.87  | 614.34E+9 | 614.34E+9 | 472.75E+9 | 138.13E+9 | 24866.3  | 24866.3  | 0.0      | 0.0      |
| 8.76      | 0.1                                      | 5232.43  | 534.82E+9 | 534.82E+9 | 411.56E+9 | 129.27E+9 | 21647.5  | 21647.5  | 0.0      | 0.0      |
| 17.52     | 0.2                                      | 4885.76  | 463.27E+9 | 463.27E+9 | 356.50E+9 | 120.71E+9 | 18751.3  | 18751.3  | 0.0      | 0.0      |
| 26.28     | 0.3                                      | 4550.87  | 399.13E+9 | 399.13E+9 | 307.14E+9 | 112.43E+9 | 16155.3  | 16155.3  | 0.0      | 0.0      |
| 35.04     | 0.4                                      | 4227.75  | 341.88E+9 | 341.88E+9 | 263.09E+9 | 104.45E+9 | 13838.1  | 13838.1  | 0.0      | 0.0      |
| 43.80     | 0.5                                      | 3916.41  | 291.01E+9 | 291.01E+9 | 223.94E+9 | 96.76E+9  | 11779.0  | 11779.0  | 0.0      | 0.0      |
| 52.56     | 0.6                                      | 3616.83  | 246.03E+9 | 246.03E+9 | 189.32E+9 | 89.36E+9  | 9958.2   | 9958.2   | 0.0      | 0.0      |
| 61.32     | 0.7                                      | 3329.03  | 206.46E+9 | 206.46E+9 | 158.87E+9 | 82.25E+9  | 8356.6   | 8356.6   | 0.0      | 0.0      |
| 70.08     | 0.8                                      | 3053.01  | 171.85E+9 | 171.85E+9 | 132.24E+9 | 75.43E+9  | 6955.9   | 6955.9   | 0.0      | 0.0      |
| 78.84     | 0.9                                      | 2788.75  | 141.78E+9 | 141.78E+9 | 109.10E+9 | 68.90E+9  | 5738.6   | 5738.6   | 0.0      | 0.0      |
| 87.60     | 1.0                                      | 2536.27  | 115.82E+9 | 115.82E+9 | 89.13E+9  | 62.66E+9  | 4688.0   | 4688.0   | 0.0      | 0.0      |

tower centerline above the ground. This result follows directly from the overall tower height of 87.6 m.

We specified a structural-damping ratio of 1% critical in all modes of the isolated tower (without the rotor-nacelle assembly mass present), which corresponds to the values used in the DOWEC study (from page 21 of Ref. [14]).

Table 6-2 summarizes the undistributed tower properties discussed in this section.

**Table 6-2. Undistributed Tower Properties** 

| Height above Ground                                | 87.6 m     |
|--|------------|
| Overall (Integrated) Mass                          | 347,460 kg |
| CM Location (w.r.t. Ground along Tower Centerline) | 38.234 m   |
| Structural-Damping Ratio (All Modes)               | 1 %        |

# 7 Baseline Control System Properties

For the NREL 5-MW baseline wind turbine, we chose a conventional variable-speed, variable blade-pitch-to-feather configuration. In such wind turbines, the conventional approach for controlling power-production operation relies on the design of two basic control systems: a generator-torque controller and a full-span rotor-collective blade-pitch controller. The two control systems are designed to work independently, for the most part, in the below-rated and above-rated wind-speed range, respectively. The goal of the generator-torque controller is to maximize power capture below the rated operation point. The goal of the blade-pitch controller is to regulate generator speed above the rated operation point.

We based the baseline control system for the NREL 5-MW wind turbine on this conventional design approach. We did not establish additional control actions for nonpower-production operations, such as control actions for normal start-up sequences, normal shutdown sequences, and safety and protection functions. Nor did we develop control actions to regulate the nacelle-yaw angle. (The nacelle-yaw control system is generally neglected within aero-servo-elastic simulation because its response is slow enough that it does not generally contribute to large extreme loads or fatigue damage.)

We describe the development of our baseline control system next, including the control-measurement filter (Section 7.1), the generator-torque controller (Section 7.2), the blade-pitch controller (Section 7.3), and the blade-pitch actuator (Section 7.4). Section 7.5 shows how these systems are put together in the overall integrated control system.

#### 7.1 Baseline Control-Measurement Filter

As is typical in utility-scale multimegawatt wind turbines, both the generator-torque and bladepitch controllers use the generator speed measurement as the sole feedback input. To mitigate high-frequency excitation of the control systems, we filtered the generator speed measurement for both the torque and pitch controllers using a recursive, single-pole low-pass filter with exponential smoothing [30]. The discrete-time recursion (difference) equation for this filter is

$$y[n] = (I - \alpha)u[n] + \alpha y[n - I], \tag{7-1}$$

with

$$\alpha = e^{-2\pi T_s f_c}, \tag{7-2}$$

where y is the filtered generator speed (output measurement), u is the unfiltered generator speed (input),  $\alpha$  is the low-pass filter coefficient, n is the discrete-time-step counter,  $T_s$  is the discrete time step, and  $f_c$  is the corner frequency.

By defining the filter state,

$$x[n] = y[n-1], \tag{7-3a}$$

or

$$x[n+1] = y[n], \tag{7-3b}$$

one can derive a discrete-time state-space representation of this filter:

$$x[n+I] = A_d x[n] + B_d u[n]$$

$$y[n] = C_d x[n] + D_d u[n]$$
(7-4)

where  $A_d = \alpha$  is the discrete-time state matrix,  $B_d = I - \alpha$  is the discrete-time input matrix,  $C_d = \alpha$  is the discrete-time output state matrix, and  $D_d = I - \alpha$  is the discrete-time input transmission matrix.

The state-space representation of Eq. (7-4) is useful for converting the filter into other forms, such as transfer-function form or frequency-response form [31].

We set the corner frequency (the -3 dB point in Figure 7-1) of the low-pass filter to be roughly one-quarter of the blade's first edgewise natural frequency (see Section 9) or 0.25 Hz. For a discrete time step of 0.0125 s, the frequency response of the resulting filter is shown in the Bode plot of Figure 7-1.

We chose the recursive, single-pole filter for its simplicity in implementation and effectiveness

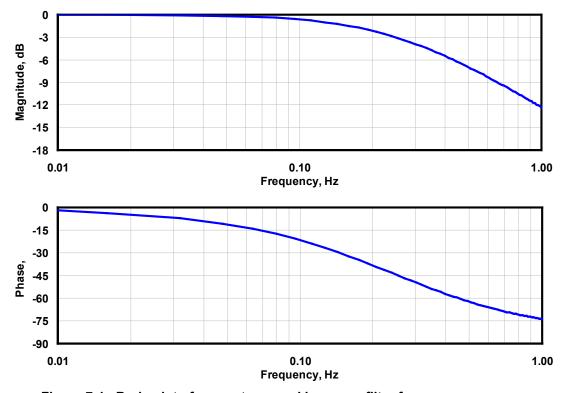


Figure 7-1. Bode plot of generator speed low-pass filter frequency response

in the time domain. The drawbacks to this filter are its gentle roll-off in the stop band (-6 dB/octave) and the magnitude and nonlinearity of its phase lag in the pass band [30]. We considered other linear low-pass filters, such as Butterworth, Chebyshev, Elliptic, and Bessel filters because of their inherent advantages relative to the chosen filter. Like the chosen filter, a Butterworth filter has a frequency response that is flat in the pass band, but the Butterworth filter offers steeper roll-off in the stop band. Chebyshev filters offer even steeper roll-off in the stop band at the expense of equalized-ripple (equiripple) in the pass band (Type 1) or stop band (Type 2), respectively. Elliptic filters offer the steepest roll-off of any linear filter, but have equiripple in both the pass and stop bands. Bessel filters offer the flattest group delay (linear phase lag) in the pass band. We designed and tested examples of each of these other low-pass filter types, considering state-space representations of up to fourth order (four states). None were found to give superior performance in the overall system response, however, so they did not warrant the added complexity of implementation.

#### 7.2 Baseline Generator-Torque Controller

The generator torque is computed as a tabulated function of the filtered generator speed, incorporating five control regions: 1, 1½, 2, 2½, and 3. Region 1 is a control region before cut-in wind speed, where the generator torque is zero and no power is extracted from the wind; instead, the wind is used to accelerate the rotor for start-up. Region 2 is a control region for optimizing power capture. Here, the generator torque is proportional to the square of the filtered generator speed to maintain a constant (optimal) tip-speed ratio. In Region 3, the generator power is held constant so that the generator torque is inversely proportional to the filtered generator speed. Region 1½, a start-up region, is a linear transition between Regions 1 and 2. This region is used to place a lower limit on the generator speed to limit the wind turbine's operational speed range. Region 2½ is a linear transition between Regions 2 and 3 with a torque slope corresponding to the slope of an induction machine. Region 2½ is typically needed (as is the case for my 5-MW turbine) to limit tip speed (and hence noise emissions) at rated power.

We found the peak of the power coefficient as a function of the tip-speed ratio and blade-pitch surface by running FAST with AeroDyn simulations at a number of given rotor speeds and a number of given rotor-collective blade-pitch angles at a fixed wind speed of 8 m/s. From these simulations, we found that the peak power coefficient of 0.482 occurred at a tip-speed ratio of 7.55 and a rotor-collective blade-pitch angle of 0.0°. With the 97:1 gearbox ratio, this resulted in an optimal constant of proportionality of 0.0255764 N•m/rpm² in the Region 2 control law. With the rated generator speed of 1173.7 rpm, rated electric power of 5 MW, and a generator efficiency of 94.4%, the rated mechanical power is 5.296610 MW and the rated generator torque is 43,093.55 N•m. We defined Region 1½ to span the range of generator speeds between 670 rpm and 30% above this value (or 871 rpm). The minimum generator speed of 670 rpm corresponds to the minimum rotor speed of 6.9 rpm used by the actual REpower 5M machine [26]. We took the transitional generator speed between Regions 2½ and 3 to be 99% of the rated generator speed, or 1,161.963 rpm. The generator-slip percentage in Region 2½ was taken to be 10%, in accordance with the value used in the DOWEC study (see page 24 of Ref. [14]). Figure 7-2 shows the resulting generator-torque versus generator speed response curve.

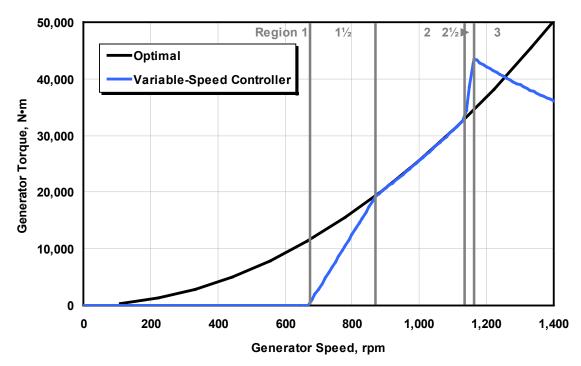


Figure 7-2. Torque-versus-speed response of the variable-speed controller

Because of the high intrinsic structural damping of the drivetrain, we did not need to incorporate a control loop for damping drivetrain torsional vibration in our baseline generator-torque controller.

We did, however, place a conditional statement on the generator-torque controller so that the torque would be computed as if it were in Region 3—regardless of the generator speed—whenever the previous blade-pitch-angle command was 1° or greater. This results in improved output power quality (fewer dips below rated) at the expense of short-term overloading of the generator and the gearbox. To avoid this excessive overloading, we saturated the torque to a maximum of 10% above rated, or 47,402.91 N•m. We also imposed a torque rate limit of 15,000 N•m/s. In Region 3, the blade-pitch control system takes over.

#### 7.3 Baseline Blade-Pitch Controller

In Region 3, the full-span rotor-collective blade-pitch-angle commands are computed using gain-scheduled proportional-integral (PI) control on the speed error between the filtered generator speed and the rated generator speed (1173.7 rpm).

We designed the blade-pitch control system using a simple single-degree-of-freedom (single-DOF) model of the wind turbine. Because the goal of the blade-pitch control system is to regulate the generator speed, this DOF is the angular rotation of the shaft. To compute the required control gains, it is beneficial to examine the equation of motion of this single-DOF system. From a simple free-body diagram of the drivetrain, the equation of motion is

$$T_{Aero} - N_{Gear} T_{Gen} = \left( I_{Rotor} + N_{Gear}^2 I_{Gen} \right) \frac{d}{dt} \left( \Omega_0 + \Delta \Omega \right) = I_{Drivetrain} \Delta \dot{\Omega} , \qquad (7-5)$$

where  $T_{Aero}$  is the low-speed shaft aerodynamic torque,  $T_{Gen}$  is the high-speed shaft generator torque,  $N_{Gear}$  is the high-speed to low-speed gearbox ratio,  $I_{Drivetrain}$  is the drivetrain inertia cast to the low-speed shaft,  $I_{Rotor}$  is the rotor inertia,  $I_{Gen}$  is the generator inertia relative to the high-speed shaft,  $\Omega_0$  is the rated low-speed shaft rotational speed,  $\Delta\Omega$  is the small perturbation of low-speed shaft rotational speed about the rated speed,  $\Delta\dot{\Omega}$  is the low-speed shaft rotational acceleration, and t is the simulation time.

Because the generator-torque controller maintains constant generator power in Region 3, the generator torque in Region 3 is inversely proportional to the generator speed (see Figure 7-2), or

$$T_{Gen}(N_{Gear}\Omega) = \frac{P_0}{N_{Gear}\Omega},$$
(7-6)

where  $P_{\theta}$  is the rated mechanical power and  $\Omega$  is the low-speed shaft rotational speed.

Similarly, assuming negligible variation of aerodynamic torque with rotor speed, the aerodynamic torque in Region 3 is

$$T_{Aero}(\theta) = \frac{P(\theta, \Omega_0)}{\Omega_0}, \tag{7-7}$$

where P is the mechanical power and  $\theta$  is the full-span rotor-collective blade-pitch angle.

Using a first-order Taylor series expansion of Eqs. (7-6) and (7-7), one can see that

$$T_{Gen} \approx \frac{P_0}{N_{Geor} \Omega_0} - \frac{P_0}{N_{Geor} \Omega_0^2} \Delta \Omega \tag{7-8}$$

and

$$T_{Aero} \approx \frac{P_0}{\Omega_0} + \frac{1}{\Omega_0} \left(\frac{\partial P}{\partial \theta}\right) \Delta \theta ,$$
 (7-9)

where  $\Delta\theta$  is a small perturbation of the blade-pitch angles about their operating point. With proportional-integral-derivative (PID) control, this is related to the rotor-speed perturbations by

$$\Delta \theta = K_P N_{Gear} \Delta \Omega + K_I \int_0^t N_{Gear} \Delta \Omega dt + K_D N_{Gear} \Delta \dot{\Omega}, \qquad (7-10)$$

where  $K_P$ ,  $K_I$ , and  $K_D$  are the blade-pitch controller proportional, integral, and derivative gains, respectively.

By setting  $\dot{\phi} = \Delta\Omega$ , combining the above expressions, and simplifying, the equation of motion for the rotor-speed error becomes

$$\underbrace{\left[I_{Drivetrain} + \frac{1}{\Omega_{0}} \left(-\frac{\partial P}{\partial \theta}\right) N_{Gear} K_{D}\right]}_{M_{s}} \dot{\varphi} + \underbrace{\left[\frac{1}{\Omega_{0}} \left(-\frac{\partial P}{\partial \theta}\right) N_{Gear} K_{P} - \frac{P_{0}}{\Omega_{0}^{2}}\right]}_{K_{s}} \dot{\varphi} + \underbrace{\left[\frac{1}{\Omega_{0}} \left(-\frac{\partial P}{\partial \theta}\right) N_{Gear} K_{I}\right]}_{K_{s}} \varphi = 0$$
(7-11)

One can see that the idealized PID-controlled rotor-speed error will respond as a second-order system with the natural frequency,  $\omega_{\varphi n}$ , and damping ratio,  $\zeta_{\varphi}$ , equal to

$$\omega_{\varphi n} = \sqrt{\frac{K_{\varphi}}{M_{\varphi}}} \tag{7-12}$$

and

$$\zeta_{\varphi} = \frac{C_{\varphi}}{2\sqrt{K_{\varphi}M_{\varphi}}} = \frac{C_{\varphi}}{2M_{\varphi}\omega_{\varphi n}}.$$
 (7-13)

In an active pitch-to-feather wind turbine, the sensitivity of aerodynamic power to the rotor-collective blade-pitch angle,  $\partial P/\partial\theta$ , is negative in Region 3. With positive control gains, then, the derivative term acts to increase the effective inertia of the drivetrain, the proportional term adds damping, and the integral term adds restoring. Also, because the generator torque drops with increasing speed error (to maintain constant power) in Region 3, one can see that the generator-torque controller introduces a negative damping in the speed error response [indicated by the  $-P_0/\Omega_0^2$  term in Eq. (7-11)]. This negative damping must be compensated by the proportional term in the blade-pitch controller.

In the design of the blade-pitch controller, Ref. [10] recommends neglecting the derivative gain, ignoring the negative damping from the generator-torque controller, and aiming for the response characteristics given by  $\omega_{\varphi n} = 0.6$  rad/s and  $\zeta_{\varphi} = 0.6$  to 0.7. This specification leads to direct expressions for choosing appropriate PI gains once the sensitivity of aerodynamic power to rotor-collective blade pitch,  $\partial P/\partial \theta$ , is known:

$$K_{P} = \frac{2I_{Drivetrain}\Omega_{0}\zeta_{\varphi}\omega_{\varphi n}}{N_{Gear}\left(-\frac{\partial P}{\partial \theta}\right)}$$
(7-14)

and

$$K_{I} = \frac{I_{Drivetrain} \Omega_{0} \omega_{\varphi n}^{2}}{N_{Gear} \left( -\frac{\partial P}{\partial \theta} \right)}.$$
 (7-15)

The blade-pitch sensitivity,  $\partial P/\partial \theta$ , is an aerodynamic property of the rotor that depends on the wind speed, rotor speed, and blade-pitch angle. We calculated it for the NREL offshore 5-MW baseline wind turbine by performing a linearization analysis in FAST with AeroDyn at a number

of given, steady, and uniform wind speeds; at the rated rotor speed ( $\Omega_0 = 12.1$  rpm); and at the corresponding blade-pitch angles that produce the rated mechanical power ( $P_0 = 5.296610$  MW). The linearization analysis involves perturbing the rotor-collective blade-pitch angle at each operating point and measuring the resulting variation in aerodynamic power. Within FAST, the partial derivative is computed using the central-difference-perturbation numerical technique. We created a slightly customized copy of FAST with AeroDyn so that the linearization procedure would invoke the frozen-wake assumption, in which the induced wake velocities are held constant while the blade-pitch angle is perturbed. This gives a more accurate linearization for heavily loaded rotors (i.e., for operating points in Region 3 closest to rated). Table 7-1 presents the results.

Table 7-1. Sensitivity of Aerodynamic Power to Blade
Pitch in Region 3

| Pitch in Region 3 |             |             |                        |
|-------------------|-------------|-------------|------------------------|
| Wind Speed        | Rotor Speed | Pitch Angle | ∂ <i>P1</i> ∂ <b>0</b> |
| (m/s)             | (rpm)       | (°)         | (watt/rad)             |
| 11.4 - Rated      | 12.1        | 0.00        | -28.24E+6              |
| 12.0              | 12.1        | 3.83        | -43.73E+6              |
| 13.0              | 12.1        | 6.60        | -51.66E+6              |
| 14.0              | 12.1        | 8.70        | -58.44E+6              |
| 15.0              | 12.1        | 10.45       | -64.44E+6              |
| 16.0              | 12.1        | 12.06       | -70.46E+6              |
| 17.0              | 12.1        | 13.54       | -76.53E+6              |
| 18.0              | 12.1        | 14.92       | -83.94E+6              |
| 19.0              | 12.1        | 16.23       | -90.67E+6              |
| 20.0              | 12.1        | 17.47       | -94.71E+6              |
| 21.0              | 12.1        | 18.70       | -99.04E+6              |
| 22.0              | 12.1        | 19.94       | -105.90E+6             |
| 23.0              | 12.1        | 21.18       | -114.30E+6             |
| 24.0              | 12.1        | 22.35       | -120.20E+6             |
| 25.0              | 12.1        | 23.47       | -125.30E+6             |

As Table 7-1 shows, the sensitivity of aerodynamic power to rotor-collective blade pitch varies considerably over Region 3, so constant PI gains are not adequate for effective speed control. The pitch sensitivity, though, varies nearly linearly with blade-pitch angle:

$$\frac{\partial P}{\partial \theta} = \left[ \frac{\partial P}{\partial \theta} (\theta = 0) \over \theta_K} \right] \theta + \left[ \frac{\partial P}{\partial \theta} (\theta = 0) \right]$$
 (7-16a)

or

$$\frac{I}{\frac{\partial P}{\partial \theta}} = \frac{I}{\frac{\partial P}{\partial \theta} (\theta = \theta) \left( I + \frac{\theta}{\theta_{V}} \right)},\tag{7-16b}$$

where  $\frac{\partial P}{\partial \theta}(\theta = 0)$  is the pitch sensitivity at rated and  $\theta_K$  is the blade-pitch angle at which the pitch sensitivity has doubled from its value at the rated operating point; that is,

$$\frac{\partial P}{\partial \theta} (\theta = \theta_K) = 2 \frac{\partial P}{\partial \theta} (\theta = 0). \tag{7-17}$$

On the right-hand side of Eq. (7-16a), the first and second terms in square brackets represent the slope and intercept of the best-fit line, respectively. We computed this regression for the NREL 5-MW baseline wind turbine and present the results in Figure 7-3.

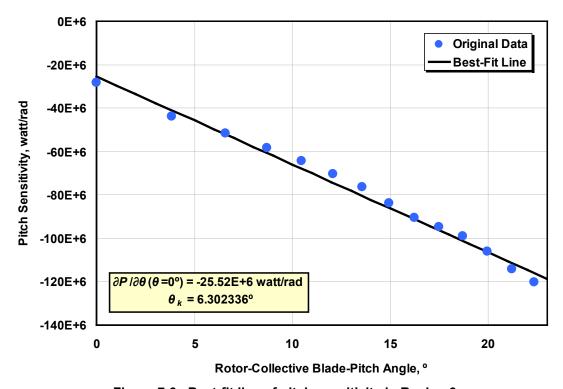


Figure 7-3. Best-fit line of pitch sensitivity in Region 3

The linear relation between pitch sensitivity and blade-pitch angle presents a simple technique for implementing gain scheduling based on blade-pitch angle; that is,

$$K_{P}(\theta) = \frac{2I_{Drivetrain} \Omega_{0} \zeta_{\varphi} \omega_{\varphi n}}{N_{Gear} \left[ -\frac{\partial P}{\partial \theta} (\theta = 0) \right]} GK(\theta)$$
(7-18)

and

$$K_{I}(\theta) = \frac{I_{Drivetrain} \Omega_{0} \omega_{\varphi n}^{2}}{N_{Gear} \left[ -\frac{\partial P}{\partial \theta} (\theta = 0) \right]} GK(\theta), \tag{7-19}$$

where  $GK(\theta)$  is the dimensionless gain-correction factor (from Ref. [10]), which is dependent on the blade-pitch angle:

$$GK(\theta) = \frac{1}{1 + \frac{\theta}{\theta_K}}. (7-20)$$

In our implementation of the gain-scheduled PI blade-pitch controller, we used the blade-pitch angle from the previous controller time step to calculate the gain-correction factor at the next time step.

Using the properties for the baseline wind turbine and the recommended response characteristics from Ref. [10], the resulting gains are  $K_P(\theta = 0^\circ) = 0.01882681$  s,  $K_I(\theta = 0^\circ) = 0.008068634$ , and  $K_D = 0.0$  s<sup>2</sup>. Figure 7-4 presents the gains at other blade-pitch angles, along with the gain-correction factor. We used the upper limit of the recommended damping ratio range,  $\zeta_{\varphi} = 0.7$ , to compensate for neglecting negative damping from the generator-torque controller in the determination of  $K_P$ .

Unfortunately, the simple gain-scheduling law derived in this section for the proportional and integral gains cannot retain consistent response characteristics (i.e., constant values of  $\omega_{on}$  and

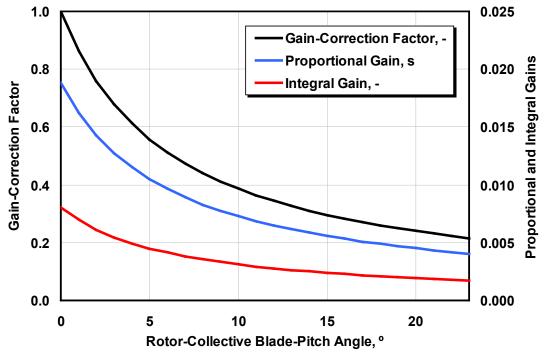


Figure 7-4. Baseline blade-pitch control system gain-scheduling law

 $\zeta_{\varphi}$ ) across all of Region 3 when applied to the derivative gain. We, nevertheless, considered adding a derivative term by selecting and testing a range of gains, but none were found to give better performance in the overall system response. Instead, the baseline control system uses the gains derived previously in this section (without the derivative term).

We set the blade-pitch rate limit to 8°/s in absolute value. This is speculated to be the blade-pitch rate limit of conventional 5-MW machines based on General Electric (GE) Wind's long-blade test program. We also set the minimum and maximum blade-pitch settings to 0° and 90°, respectively. The lower limit is the set blade pitch for maximizing power in Region 2, as described in Section 7.2. The upper limit is very close to the fully feathered blade pitch for neutral torque. We saturated the integral term in the PI controller between these limits to ensure a fast response in the transitions between Regions 2 and 3.

#### 7.4 Baseline Blade-Pitch Actuator

Because of limitations in the FAST code, the FAST model does not include any blade-pitch actuator dynamic effects. Blade-pitch actuator dynamics are, however, needed in ADAMS. To enable successful comparisons between the FAST and ADAMS response predictions, then, we found it beneficial to reduce the effect of the blade-pitch actuator response in ADAMS. Consequently, we designed the blade-pitch actuator in the ADAMS model with a very high natural frequency of 30 Hz, which is higher than the highest full-system natural frequency in the FAST model (see Section 9), and a damping ratio of 2% critical. This resulted in an equivalent blade-pitch actuator linear-spring constant of 971,350,000 N•m/rad and an equivalent blade-pitch actuator linear-damping constant of 206,000 N•m/(rad/s).

## 7.5 Summary of Baseline Control System Properties

We implemented the NREL offshore 5-MW wind turbine's baseline control system as an external dynamic link library (DLL) in the style of Garrad Hassan's *BLADED* wind turbine software package [3]. Appendix C contains the source code for this DLL, and Figure 7-5 presents a flowchart of the overall integrated control system calculations. Table 7-2 summarizes the baseline generator-torque and blade-pitch control properties we discussed earlier in this section.

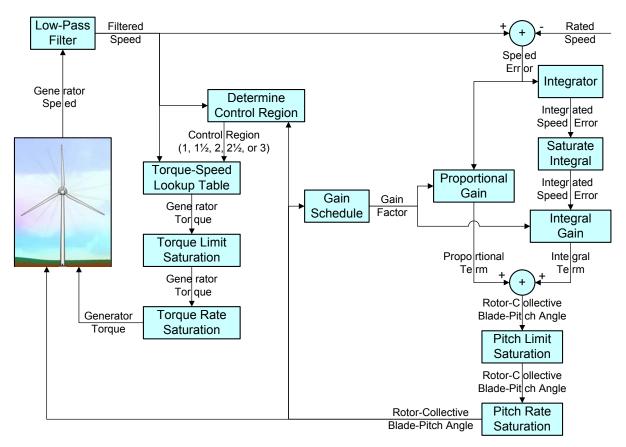


Figure 7-5. Flowchart of the baseline control system

Table 7-2. Baseline Control System Properties

| Corner Frequency of Generator-Speed Low-Pass Filter          | 0.25 Hz                        |
|--|--------------------------------|
| Peak Power Coefficient                                       | 0.482                          |
| Tip-Speed Ratio at Peak Power Coefficient                    | 7.55                           |
| Rotor-Collective Blade-Pitch Angle at Peak Power Coefficient | 0.0 °                          |
| Generator-Torque Constant in Region 2                        | 0.0255764 N•m/rpm <sup>2</sup> |
| Rated Mechanical Power                                       | 5.296610 MW                    |
| Rated Generator Torque                                       | 43,093.55 N•m                  |
| Transitional Generator Speed between Regions 1 and 11/2      | 670 rpm                        |
| Transitional Generator Speed between Regions 1½ and 2        | 871 rpm                        |
| Transitional Generator Speed between Regions 2½ and 3        | 1,161.963 rpm                  |
| Generator Slip Percentage in Region 2½                       | 10 %                           |
| Minimum Blade Pitch for Ensuring Region 3 Torque             | 1 °                            |
| Maximum Generator Torque                                     | 47,402.91 N•m                  |
| Maximum Generator Torque Rate                                | 15,000 N•m/s                   |
| Proportional Gain at Minimum Blade-Pitch Setting             | 0.01882681 s                   |
| Integral Gain at Minimum Blade-Pitch Setting                 | 0.008068634                    |
| Blade-Pitch Angle at which the Rotor Power Has Doubled       | 6.302336°                      |
| Minimum Blade-Pitch Setting                                  | 0 °                            |
| Maximum Blade-Pitch Setting                                  | 90 °                           |
| Maximum Absolute Blade Pitch Rate                            | 8 °/s                          |
| Equivalent Blade-Pitch-Actuator Linear-Spring Constant       | 971,350,000 N•m/rad            |
| Equivalent Blade-Pitch-Actuator Linear-Damping Constant      | 206,000 N•m/rad/s              |

# 8 FAST with AeroDyn and ADAMS with AeroDyn Models

Using the turbine properties described previously in this report, we put together models of the NREL offshore 5-MW baseline wind turbine within FAST [11] with AeroDyn [16,20]. The input files for these models are given in Appendix A and Appendix B, for version (v) 6.10a-jmj of FAST and v12.58 of AeroDyn, respectively. We then generated the higher fidelity ADAMS with AeroDyn models through the preprocessor functionality built into the FAST code.

The input files in Appendix A are for the FAST model of the equivalent land-based version of the NREL 5-MW baseline wind turbine. The input files for other versions of the model, such as those for different support structures, require only a few minor changes. These include changes to input parameters "PtfmModel" and "PtfmFile," which identify the type and properties of the support platform, and modifications to the prescribed mode shapes in the tower input file, "TwrFile."

Although most of the input-parameter specifications in Appendix A and Appendix B are self-explanatory, the specifications of the prescribed mode shapes needed by FAST to characterize the flexibility of the blades and tower deserve a special explanation. The required mode shapes depend on the member's boundary conditions. For the blade modes, we used v2.22 of the Modes program [4] to derive the equivalent polynomial representations of the blade mode shapes needed by FAST. The Modes program calculates the mode shapes of rotating blades, assuming that a blade mode shape is unaffected by its coupling with other system modes of motion. This is a common assumption in wind turbine analysis. For the tower modes, however, there is a great deal of coupling with the rotor motions, and in offshore floating systems, there is coupling with the platform motions as well. To take the former factor into account, we used the linearization functionality of the full-system ADAMS model to obtain the tower modes for the land-based version of the NREL 5-MW baseline wind turbine. In other words, we built an ADAMS model of the wind turbine, enabled all system DOFs, and linearized the model. Then we passed a best-fit polynomial through the resulting tower mode shapes to get the equivalent polynomial representations of the tower mode shapes needed by FAST.

Not including platform motions, the FAST model of the land-based version of the NREL 5-MW baseline wind turbine incorporates 16 DOFs as follows:

- Two flapwise and one edgewise bending-mode DOFs for each of the three blades
- One variable-generator speed DOF and one driveshaft torsional DOF
- One nacelle-yaw-actuator DOF
- Two fore-aft and two side-to-side bending-mode DOFs in the tower.

Not including platform motion, the higher fidelity ADAMS model of the land-based version of the wind turbine incorporates 438 DOFs as follows:

- One hundred and two DOFs in each of the three blades, including flapwise and edgewise shear and bending, torsion, and extension DOFs
- One blade-pitch actuator DOF in each of the three blades

- One variable-generator speed DOF and one driveshaft torsional DOF
- One nacelle-yaw actuator DOF
- One hundred and twenty-six DOFs in the tower, including fore-aft and side-to-side shear and bending, torsion, and extension DOFs.

The support platform motions in, for example, the floating-platform versions of the NREL 5-MW baseline wind turbine add six DOFs per model.

We use a constant time step of 0.0125 s in FAST's fixed-step-size time-integration scheme and a maximum step size of 0.0125 s in ADAMS' variable-step-size time integrator. We have AeroDyn perform aerodynamic calculations every other structural time step (i.e., 0.025 s) to ensure that there are at least 200-azimuth-step computations per revolution at 12 rpm. Data are output at 20 Hz or every fourth structural time step. We made these time steps as large as possible to ensure numerical stability and suitable output resolution across a range of operating conditions

# 9 Full-System Natural Frequencies and Steady-State Behavior

To provide a cursory overview of the overall system behavior of the equivalent land-based version of the NREL 5-MW baseline wind turbine, we calculated the full-system natural frequencies and the steady-state response of the system as a function of wind speed.

We obtained the full-system natural frequencies with both the FAST model and the ADAMS model. In FAST, we calculated the natural frequencies by performing an eigenanalysis on the first-order state matrix created from a linearization analysis. In ADAMS, we obtained the frequencies by invoking a "LINEAR/EIGENSOL" command, which linearizes the complete ADAMS model and computes eigendata. To avoid the rigid-body drivetrain mode, the analyses considered the wind turbine in a stationary condition with the high-speed shaft brake engaged. The blades were pitched to their minimum set point (0°), but aerodynamic damping was ignored. Table 9-1 lists results for the first 13 full-system natural frequencies.

Table 9-1. Full-System Natural Frequencies in Hertz

| Mode | Description                         | FAST   | ADAMS  |
|------|-------------------------------------|--------|--------|
| 1    | 1st Tower Fore-Aft                  | 0.3240 | 0.3195 |
| 2    | 1st Tower Side-to-Side              | 0.3120 | 0.3164 |
| 3    | 1st Drivetrain Torsion              | 0.6205 | 0.6094 |
| 4    | 1st Blade Asymmetric Flapwise Yaw   | 0.6664 | 0.6296 |
| 5    | 1st Blade Asymmetric Flapwise Pitch | 0.6675 | 0.6686 |
| 6    | 1st Blade Collective Flap           | 0.6993 | 0.7019 |
| 7    | 1st Blade Asymmetric Edgewise Pitch | 1.0793 | 1.0740 |
| 8    | 1st Blade Asymmetric Edgewise Yaw   | 1.0898 | 1.0877 |
| 9    | 2nd Blade Asymmetric Flapwise Yaw   | 1.9337 | 1.6507 |
| 10   | 2nd Blade Asymmetric Flapwise Pitch | 1.9223 | 1.8558 |
| 11   | 2nd Blade Collective Flap           | 2.0205 | 1.9601 |
| 12   | 2nd Tower Fore-Aft                  | 2.9003 | 2.8590 |
| 13   | 2nd Tower Side-to-Side              | 2.9361 | 2.9408 |

The agreement between FAST and ADAMS is quite good. The biggest differences exist in the predictions of the blades' second asymmetric flapwise yaw and pitch modes. By "yaw" and "pitch" we mean that these blade asymmetric modes couple with the nacelle-yaw and nacelle-pitching motions, respectively. Because of the offsets of the blade section CM from the pitch axis, higher-order modes, and tower-torsion DOFs—which are available in ADAMS, but not in FAST—ADAMS predicts lower natural frequencies in these modes than FAST does.

Bir and Jonkman have published [2] a much more exhaustive eigenanalysis for the NREL 5-MW baseline wind turbine. The referenced publication documents the natural frequencies and damping ratios of the land- and floating-platform versions of the 5-MW turbine across a range of operating conditions.

We obtained the steady-state response of the land-based 5-MW baseline wind turbine by running a series of FAST with AeroDyn simulations at a number of given, steady, and uniform wind speeds. The simulations lengths were long enough to ensure that all transient behavior had died out; we then recorded the steady-state output values. We ran the simulations using the blade-

element / momentum (BEM) wake option of AeroDyn and with all available and relevant land-based DOFs enabled. Figure 9-1 shows the results for several output parameters, which are defined as follows:

- "GenSpeed" represents the rotational speed of the generator (high-speed shaft).
- "RotPwr" and "GenPwr" represent the mechanical power within the rotor and the electrical output of the generator, respectively.
- "RotThrust" represents the rotor thrust.
- "RotTorq" represents the mechanical torque in the low-speed shaft.
- "RotSpeed" represents the rotational speed of the rotor (low-speed shaft).
- "BlPitch1" represents the pitch angle of Blade 1.
- "GenTq" represents the electrical torque of the generator.
- "TSR" represents the tip-speed ratio.
- "OoPDefl1" and "IPDefl1" represent the out-of-plane and in-plane tip deflections of Blade 1 relative to the undeflected blade-pitch axis.
- "TTDspFA" and "TTDspSS" represent the fore-aft and side-to-side deflection of the tower top relative to the centerline of the undeflected tower.

As planned, the generator and rotor speeds increase linearly with wind speed in Region 2 to maintain constant tip-speed ratio and optimal wind-power conversion efficiency. Similarly, the generator and rotor powers and generator and rotor torques increase dramatically with wind speed in Region 2, increasing cubically and quadratically, respectively. Above rated, the generator and rotor powers are held constant by regulating to a fixed speed with active blade-pitch control. The out-of-plane tip deflection of the reference blade (Blade 1) reaches a maximum at the rated operating point before dropping again. This response characteristic is the result of the peak in rotor thrust at rated. This peak is typical of variable generator speed variable blade-pitch-to-feather wind turbines because of the transition that occurs in the control system at rated between the active generator-torque and the active blade-pitch control regions. This peak in response is also visible, though less pronounced, in the in-plane tip deflection of the reference blade and the tower-top fore-aft displacement.

Start-up transient behavior is an artifact of computational analysis. To mitigate this behavior, we suggest using the steady-state values of the rotor speed and blade-pitch angles found in Figure 9-1 as initial conditions in simulations.

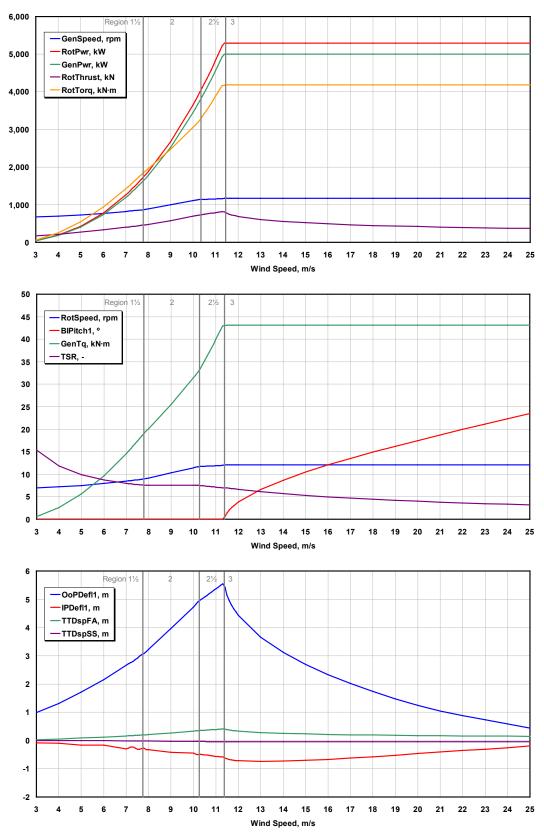


Figure 9-1. Steady-state responses as a function of wind speed

#### 10 Conclusions

To support concept studies aimed at assessing offshore wind technology, we developed the specifications of a representative utility-scale multimegawatt turbine now known as the "NREL offshore 5-MW baseline wind turbine." This wind turbine is a conventional three-bladed upwind variable-speed variable blade-pitch-to-feather-controlled turbine. To create the model, we obtained some broad design information from the published documents of turbine manufacturers, with a heavy emphasis on the REpower 5M machine. Because detailed data was unavailable, however, we also used the publicly available properties from the conceptual models in the WindPACT, RECOFF, and DOWEC projects. We then created a composite from these data, extracting the best available and most representative specifications. This report documented the specifications of the NREL offshore 5-MW baseline wind turbine—including the aerodynamic, structural, and control-system properties—and the rationale behind its development. The model has been, and will likely continue to be, used as a reference by research teams throughout the world to standardize baseline offshore wind turbine specifications and to quantify the benefits of advanced land- and sea-based wind energy technologies.

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# Appendix A FAST Input Files

#### A.1 Primary Input File

```
---- FAST INPUT FILE ------
NREL 5.0 MW Baseline Wind Turbine for Use in Offshore Analysis.
Properties from Dutch Offshore Wind Energy Converter (DOWEC) 6MW Pre-Design (10046_009.pdf) and REpower 5M 5MW (5m_uk.pdf); C
    ----- SIMULATION CONTROL
                        - Echo input data to "echo.out" (flag)
            ADAMSPrep
                         - ADAMS preprocessor mode {1: Run FAST, 2: use FAST as a preprocessor to create an ADAMS model, 3: do
            AnalMode
                         - Analysis mode {1: Run a time-marching simulation, 2: create a periodic linearized model} (switch)
            NumB1
                         - Number of blades (-)
630.0
            TMax
                         - Total run time (s)
                          - Integration time step (s)
  0.0125
            DT
            ----- TURBINE CONTROL
            YCMode
                         - Yaw control mode {0: none, 1: user-defined from routine UserYawCont, 2: user-defined from Simulink}
9999.9
                         - Time to enable active yaw control (s) [unused when YCMode=0]
                         - Pitch control mode {0: none, 1: user-defined from routine PitchCntrl, 2: user-defined from Simulink
            PCMode
  0.0
                           Time to enable active pitch control (s) [unused when PCMode=0]
            VSContr1
                          - Variable-speed control mode {0: none, 1: simple VS, 2: user-defined from routine UserVSCont, 3: use
9999.9
            VS_RtGnSp
                           Rated generator speed for simple variable-speed generator control (HSS side) (rpm) [used only when
            VS_RtTq
VS_Rgn2K
                         - Rated generator torque/constant generator torque in Region 3 for simple variable-speed generator co - Generator torque constant in Region 2 for simple variable-speed generator control (HSS side) (N-m/r
9999.9
9999.9
9999.9
                           Rated generator slip percentage in Region 2 1/2 for simple variable-speed generator control (%) [us
            VS SIPc
                           Generator model {1: simple, 2: Thevenin, 3: user-defined from routine UserGen} (switch) [used only
            GenModel
True
            GenTiStr
                           Method to start the generator {T: timed using TimGenOn, F: generator speed using SpdGenOn} (flag)
                           Method to stop the generator \{T: timed using TimGenOf, F: when generator power = 0\} (flag)
            GenTiStp
9999.9
                           Generator speed to turn on the generator for a startup (HSS speed) (rpm) [used only when GenTiStr=F
            SpdGen0n
  0.0
            TimGenOn
                         - Time to turn on the generator for a startup (s) [used only when GenTiStr=True]
9999.9
            TimGenOf
                         - Time to turn off the generator (s) [used only when GenTiStp=True]
            HSSBrMode
                         - HSS brake model {1: simple, 2: user-defined from routine UserHSSBr} (switch) - Time to initiate deployment of the HSS brake (s) \,
9999.9
            THSSBrDn
9999.9
            TiDynBrk
                          - Time to initiate deployment of the dynamic generator brake [CURRENTLY IGNORED] (s)
                         - Time to initiate deployment of tip brake 1 (s)
9999.9
            TTpBrDp(1)
                           Time to initiate deployment of tip brake 2 (s)
9999.9
             TTpBrDp(2)
9999.9
                         - Time to initiate deployment of tip brake 3 (s) [unused for 2 blades]
            TTpBrDp(3)
9999.9
            TBDepISp(1) - Deployment-initiation speed for the tip brake on blade 1 (rpm)
9999.9
            TBDepISp(2) - Deployment-initiation speed for the tip brake on blade 2 (rpm)
9999.9
            TBDepISp(3) - Deployment-initiation speed for the tip brake on blade 3 (rpm) [unused for 2 blades]
            TYawManS - Time to start override yaw maneuver and end standard yaw control (s)
YawManRat - Yaw rate (in absolute value) at which override yaw maneuver heads toward final yaw angle (deg/s)
9999.9
  0.3
            NacYawF - Final yaw angle for override yaw maneuvers (degrees)

TPitManS(1) - Time to start override pitch maneuver for blade 1 and end standard pitch control (s)
  0.0
9999.9
9999.9
             TPitManS(2) - Time to start override pitch maneuver for blade 2 and end standard pitch control (s)
9999.9
            TPitManS(3) - Time to start override pitch maneuver for blade 3 and end standard pitch control (s) [unused for 2
            PitManRat(1)- Pitch rate (in absolute value) at which override pitch maneuver for blade 1 heads toward final pitc PitManRat(2)- Pitch rate (in absolute value) at which override pitch maneuver for blade 2 heads toward final pitc
  8.0
  8.0
  8.0
            PitManRat(3)- Pitch rate (in absolute value) at which override pitch maneuver for blade 3 heads toward final pitc
            BlPitch(1) - Blade 1 initial pitch (degrees)
BlPitch(2) - Blade 2 initial pitch (degrees)
   0.0
   0.0
   0.0
                           Blade 3 initial pitch (degrees) [unused for 2 blades]
   0.0
            BlPitchF(1) - Blade 1 final pitch for override pitch maneuvers (degrees)
            BlPitchF(2) - Blade 2 final pitch for override pitch maneuvers (degrees)
   0.0
            BlPitchF(3) - Blade 3 final pitch for override pitch maneuvers (degrees) [unused for 2 blades]
  0.0
            ----- ENVIRONMENTAL CONDITIONS ------
  9.80665 Gravity
                         - Gravitational acceleration (m/s^2)
                        FEATURE FLAGS -----
                        - First flapwise blade mode DOF (flag)
True
            FlapDOF1
                         - Second flapwise blade mode DOF (flag)
            FlapDOF2
True
            EdgeD0F
                           First edgewise blade mode DOF (flag)
True
                           Rotor-teeter DOF (flag) [unused for 3 blades]
False
             TeetD0F
            DrTrD0F
                         - Drivetrain rotational-flexibility DOF (flag)
True
            GenD0F
                         - Generator DOF (flag)
True
True
            YawDOF
                         - Yaw DOF (flag)
                         - First fore-aft tower bending-mode DOF (flag)
- Second fore-aft tower bending-mode DOF (flag)
            TwFADOF1
True
            TwFADOF2
True
            TwSSD0F1
                           First side-to-side tower bending-mode DOF (flag)
True
            TwSSD0F2
                           Second side-to-side tower bending-mode DOF (flag)
True
                           Compute aerodynamic forces (flag)
            CompAero
True
                           Compute aerodynamic noise (flag)
False
            CompNoise
                        INITIAL CONDITIONS ----
   0.0
            OoPDef1
                         - Initial out-of-plane blade-tip displacement (meters)
  0.0
            IPDef1
                         - Initial in-plane blade-tip deflection (meters)
   0.0
            TeetDef1
                         - Initial or fixed teeter angle (degrees) [unused for 3 blades]
  0.0
            Azimuth
                          - Initial azimuth angle for blade 1 (degrees)
                           Initial or fixed rotor speed (rpm)
  12.1
            RotSpeed
            NacYaw
                           Initial or fixed nacelle-yaw angle (degrees)
            TTDspFA
                         - Initial fore-aft tower-top displacement (meters)
                         - Initial side-to-side tower-top displacement (meters)
```

```
----- TURBINE CONFIGURATION -----
 63.0
            TipRad
                         - The distance from the rotor apex to the blade tip (meters)
                         - The distance from the rotor apex to the blade root (meters)
  1.5
            HubRad
            PSpnE1N
                           Number of the innermost blade element which is still part of the pitchable portion of the blade for
  0.0
            UndSling
                           Undersling length [distance from teeter pin to the rotor apex] (meters) [unused for 3 blades]
  0.0
            HubCM
                           Distance from rotor apex to hub mass [positive downwind] (meters)
  -5.01910
            OverHang
                           Distance from yaw axis to rotor apex [3 blades] or teeter pin [2 blades] (meters)
  1.9
            NacCMxn

    Downwind distance from the tower-top to the nacelle CM (meters)

            NacCMvn
                         - Lateral distance from the tower-top to the nacelle CM (meters)
  0.0
                         - Vertical distance from the tower-top to the nacelle CM (meters)
  1.75
            NacCMzn
 87.6
            TowerHt
                           Height of tower above ground level [onshore] or MSL [offshore] (meters)
  1.96256
            Twr2Shft
                           Vertical distance from the tower-top to the rotor shaft (meters)
  0.0
            TwrRBHt
                         - Tower rigid base height (meters)
            ShftTilt
  -5.0
                           Rotor shaft tilt angle (degrees)
  0.0
            Delta3
                           Delta-3 angle for teetering rotors (degrees) [unused for 3 blades]
                           Blade 1 cone angle (degrees)
  -2.5
            PreCone(1)
                         - Blade 2 cone angle (degrees)
 -2.5
            PreCone(2)
                           Blade 3 cone angle (degrees) [unused for 2 blades]
            PreCone(3)
  -2.5
                           Azimuth value to use for I/O when blade 1 points up (degrees)
            AzimB1Up
  0.0
                        MASS AND INERTIA -----
            YawBrMass
  0.0
                        - Yaw bearing mass (kg)
240.00E3
            NacMass
                         - Nacelle mass (kg)
 56.78E3
            HubMass
                         - Hub mass (kg)
  0.0
            TipMass(1)
                        - Tip-brake mass, blade 1 (kg)
            TipMass(2)
                        - Tip-brake mass, blade 2 (kg) - Tip-brake mass, blade 3 (kg) [unused for 2 blades]
  0.0
            TipMass(3)
  0.0
2607.89E3
            NacYIner
                           Nacelle inertia about yaw axis (kg m^2)
534.116
            GenIner
                           Generator inertia about HSS (kg m^2)
                           Hub inertia about rotor axis [3 blades] or teeter axis [2 blades] (kg m^2)
115.926E3
            HubIner
                        DRTVFTRATN ---
                         - Gearbox efficiency (%)
100.0
            GBoxEff
 94.4
            GenEff
                           Generator efficiency [ignored by the Thevenin and user-defined generator models] (%)
 97.0
            GBRatio
                         - Gearbox ratio (-)
False
            GBRevers
                           Gearbox reversal {T: if rotor and generator rotate in opposite directions} (flag)
 28.1162E3
            HSSBrTqF
                           Fully deployed HSS-brake torque (N-m)
  0.6
                           Time for HSS-brake to reach full deployment once initiated (sec) [used only when HSSBrMode=1]
            HSSBrDT
            DynBrkFi
                           File containing a mech-gen-torque vs HSS-speed curve for a dynamic brake [CURRENTLY IGNORED] (quote
867.637E6
            DTTorSpr
                           Drivetrain torsional spring (N-m/rad)
  6.215E6 DTTorDmp
                         - Drivetrain torsional damper (N-m/(rad/s))
                        SIMPLE INDUCTION GENERATOR -----
                         - Rated generator slip percentage (%) [used only when VSContrl=0 and GenModel=1]
9999.9
            STG SIPC
9999.9
                           Synchronous (zero-torque) generator speed (rpm) [used only when VSContrl=0 and GenModel=1] Rated torque (N-m) [used only when VSContrl=0 and GenModel=1]
            SIG SvSp
9999.9
            SIG RtTa
                           Pull-out ratio (Tpullout/Trated) (-) [used only when VSContrl=0 and GenModel=1]
9999.9
            SIG PORt
                        THEVENIN-EQUIVALENT INDUCTION GENERATOR ------
9999.9
                        - Line frequency [50 or 60] (Hz) [used only when VSContrl=0 and GenModel=2]
            TEC Freq
9998
            TEC_NPol
                           Number of poles [even integer > 0] (-) [used only when VSContrl=0 and GenModel=2]
9999.9
            TEC_SRes
                           Stator resistance (ohms) [used only when VSContrl=0 and GenModel=2]
9999.9
            TEC RRes
                           Rotor resistance (ohms) [used only when VSContrl=0 and GenModel=2]
                         - Line-to-line RMS voltage (volts) [used only when VSContrl=0 and GenModel=2]
9999.9
            TEC_VLL
                         - Stator leakage reactance (ohms) [used only when VSContrl=0 and GenModel=2]
9999.9
            TEC SLR
                         - Rotor leakage reactance (ohms) [used only when VSContrl=0 and GenModel=2]
            TEC RLR
9999.9
                         - Magnetizing reactance (ohms) [used only when VSContrl=0 and GenModel=2]
9999.9
            TEC_MR
            PtfmModel
                      - Platform model {0: none, 1: onshore, 2: fixed bottom offshore, 3: floating offshore} (switch)
 0
            PtfmFile
                         - Name of file containing platform properties (quoted string) [unused when PtfmModel=0]
            -----
                        TOWER -----
                        - Number of tower nodes used for analysis (-)
            TwrNodes
"NRELOffshrBsline5MW_Tower_Onshore.dat"
                                                                - Name of file containing tower properties (quoted string)
                                                  TwrFile
 ------ NACELLE-YAW ------
9028.32E6
                           Nacelle-yaw spring constant (N-m/rad)
            YawSpr
 19.16E6
            YawDamp
                           Nacelle-yaw damping constant (N-m/(rad/s))
            YawNeut
                           Neutral yaw position--yaw spring force is zero at this yaw (degrees)
                        FURLING --
            Furling
False
                         - Read in additional model properties for furling turbine (flag)
            FurlFile
                           Name of file containing furling properties (quoted string) [unused when Furling=False]
                        ROTOR-TEETER ---
                        - Rotor-teeter spring/damper model {0: none, 1: standard, 2: user-defined from routine UserTeet} (swi - Rotor-teeter damper position (degrees) [used only for 2 blades and when TeetMod=1]
  a
            TeetMod
  0.0
            TeetDmpP
  0.0
            TeetDmp
                           Rotor-teeter damping constant (N-m/(rad/s)) [used only for 2 blades and when TeetMod=1]
                           Rotor-teeter rate-independent Coulomb-damping moment (N-m) [used only for 2 blades and when TeetMod
            TeetCDmp
                           Rotor-teeter soft-stop position (degrees) [used only for 2 blades and when TeetMod-1] Rotor-teeter hard-stop position (degrees) [used only for 2 blades and when TeetMod-1]
  0.0
            TeetSStP
  0.0
            TeetHStP
  0.0
            TeetSSSp
                           Rotor-teeter soft-stop linear-spring constant (N-m/rad) [used only for 2 blades and when TeetMod=1]
            TeetHSSp
                           Rotor-teeter hard-stop linear-spring constant (N-m/rad) [used only for 2 blades and when TeetMod=1]
  0.0
                        TTP-BRAKE ----
            TBDrConN
  0.0
                        - Tip-brake drag constant during normal operation, Cd*Area (m^2)
                         - Tip-brake drag constant during fully-deployed operation, Cd*Area (m^2) - Time for tip-brake to reach full deployment once released (sec)
            TBDrConD
  0.0
            TpBrDT
  0.0
               ----- BLADE ---
'NRELOffshrBsline5MW Blade.dat"
                                                   BldFile(1) - Name of file containing properties for blade 1 (quoted string)
                                                               - Name of file containing properties for blade 2 (quoted string)
- Name of file containing properties for blade 3 (quoted string)
'NRELOffshrBsline5MW_Blade.dat"
                                                   BldFile(2)
'NRELOffshrBsline5MW_Blade.dat"
                                                   BldFile(3)
       ----- AFRODYN ------
```

```
'NRELOffshrBsline5MW AeroDyn.ipt"
                                                                                  ADFile
                                                                                                       - Name of file containing AeroDyn input parameters (quoted strin
                                  -- NOISE --
                    NoiseFile - Name of file containing aerodynamic noise input parameters (quoted string) [used only when CompNois
               ----- ADAMS -----
"NRELOffshrBsline5MW_ADAMSSpecific.dat"
                                                                                 ADAMSFile - Name of file containing ADAMS-specific input parameters (quote
                ----- LINEARIZATION CONTROL
"NRELOffshrBsline5MW Linear.dat"
                                                                                LinFile - Name of file containing FAST linearization parameters (quoted
 SumPrint
                                       - Print summary data to "<RootName>.fsm" (flag)
True
                                        - Generate a tab-delimited tabular output file. (flag)
                    TabDelim
True
 'ES10.3E2"
                   OutFmt
                                        - Format used for tabular output except time. Resulting field should be 10 characters. (quoted strin
  30.0
                                        - Time to begin tabular output (s)
                    DecFact
                                        - Decimation factor for tabular output {1: output every time step} (-)
    1.0
                    SttsTime
                                        - Amount of time between screen status messages (sec)
  -3.09528
                   NcIMUxn
                                        - Downwind distance from the tower-top to the nacelle IMU (meters)
   0.0
                   NcTMUvn
                                        - Lateral distance from the tower-top to the nacelle IMU (meters)
    2.23336
                   NcIMUzn
                                        - Vertical distance from the tower-top to the nacelle IMU (meters)
                                        - Distance from rotor apex [3 blades] or teeter pin [2 blades] to shaft strain gages [positive for up
    1.912
                    ShftGagL
                                        - Number of tower nodes that have strain gages for output [0 to 9] (-)
                    NTwGages
                                            List of tower nodes that have strain gages [1 to TwrNodes] (-) [unused if NTwGages=0]
  10
                    TwrGagNd
                                        - Number of blade nodes that have strain gages for output [0 to 9] (-)
                    NB1Gages
    9
                                           List of blade nodes that have strain gages [1 to BldNodes] (-) [unused if NBlGages=0]
                    BldGagNd
                                        - The next line(s) contains a list of output parameters. See Outlist.txt for a listing of available
                    OutList
_..uvxi ,
"WaveElev"
"Wass
                   WindVyi , WindVzi"
                                                                                                        - Longitudinal, lateral, and vertical wind speeds
                                                                                                         - Wave elevation at the platform reference point
"Wave1Vxi , Wave1Vyi , Wave1Vzi"
                                                                                                        - Longitudinal, lateral, and vertical wave particle velocities a
"Wave1Axi ,
                   Wave1Ayi , Wave1Azi"
                                                                                                        - Longitudinal, lateral, and vertical wave particle acceleration
...veiA
"GenTq"
"HSSBrTq"
                                                                                                           Electrical generator power and torque
                                                                                                        - High-speed shaft brake torque
"BldPitch1, BldPitch2, BldPitch3"
                                                                                                        - Pitch angles for blades 1, 2, and 3
"Azimuth"
                                                                                                        - Blade 1 azimuth angle
"RotSpeed , GenSpeed"
                                                                                                        - Low-speed shaft and high-speed shaft speeds
"NacYaw , NacYawErr"
"OoPDefl1 , IPDefl1 , TwstDefl1"
                                                                                                        - Nacelle yaw angle and nacelle yaw error estimate
                                                                                                        - Blade 1 out-of-plane and in-plane deflections and tip twist
                                 , TwstDef12"
"OoPDef12 , IPDef12
                                                                                                        - Blade 2 out-of-plane and in-plane deflections and tip twist
                                  , TwstDef13"
 'OoPDef13 , IPDef13
                                                                                                         - Blade 3 out-of-plane and in-plane deflections and tip twist
"TwrClrnc1, TwrClrnc2, TwrClrnc3"
                                                                                                        - Tip-to-tower clearance estimate for blades 1, 2, and 3
"NcIMUTAxs, NcIMUTAys, NcIMUTAzs"
                                                                                                         - Nacelle IMU translational accelerations (absolute) in the nonr
"TTDspFA , TTDspSS , TTDspTwst"
                                                                                                        - Tower fore-aft and side-to-side displacements and top twist
"PtfmSurge, PtfmSway , PtfmHeave"
                                                                                                        - Platform translational surge, sway, and heave displacements
"PtfmRoll , PtfmPitch, PtfmYaw"
                                                                                                        - Platform rotational roll, pitch and yaw displacements
"PtfmTAxt , PtfmTAyt , PtfmTAzt"
                                                                                                        - Platform translation accelerations (absolute) in the tower-bas % \left( \frac{1}{2}\right) =\left( \frac{1}{2}\right) \left( \frac{1}{2}\right) 
"RootFxc1 , RootFyc1 , RootFzc1"
"RootMxc1 , RootMyc1 , RootMzc1"
                                                                                                        - Out-of-plane shear, in-plane shear, and axial forces at the ro - In-plane bending, out-of-plane bending, and pitching moments a
 'RootFxc2 , RootFyc2 ,
                                      RootFzc2"
                                                                                                         - Out-of-plane shear, in-plane shear, and axial forces at the ro
 'RootMxc2 , RootMyc2 , RootMzc2"
                                                                                                         - In-plane bending, out-of-plane bending, and pitching moments a
"RootFxc3 , RootFyc3 ,
                                       RootFzc3"
                                                                                                        - Out-of-plane shear, in-plane shear, and axial forces at the ro
"RootMxc3 , RootMyc3 , RootMzc3"
                                                                                                        - In-plane bending, out-of-plane bending, and pitching moments a
 'Spn1MLxb1, Spn1MLyb1, Spn1MLzb1"
                                                                                                        - Blade 1 local edgewise bending, flapwise bending, and pitching
"Spn1MLxb2, Spn1MLyb2, Spn1MLzb2"
                                                                                                        - Blade 2 local edgewise bending, flapwise bending, and pitching
"Spn1MLxb3, Spn1MLyb3, Spn1MLzb3"
                                                                                                        - Blade 3 local edgewise bending, flapwise bending, and pitching
                                                                                                        - Rotor thrust and low-speed shaft 0- and 90-rotating shear forc
"RotThrust, LSSGagFya, LSSGagFza"
"RotTorq , LSSGagMya, LSSGagMza"
"YawBrFxp , YawBrFyp , YawBrFzp"
                                                                                                        - Rotor torque and low-speed shaft 0- and 90-rotating bending mo
                                                                                                         - Fore-aft shear, side-to-side shear, and vertical forces at the
"YawBrMxp , YawBrMyp , YawBrMzp"
"TwrBsFxt , TwrBsFyt , TwrBsFzt"
                                                                                                        - Side-to-side bending, fore-aft bending, and yaw moments at the
                                                                                                        - Fore-aft shear, side-to-side shear, and vertical forces at the
"TwrBsMxt , TwrBsMyt , TwrBsMzt"
                                                                                                        - Side-to-side bending, fore-aft bending, and yaw moments at the
"TwHt1MLxt, TwHt1MLyt, TwHt1MLzt"
                                                                                                        - Local side-to-side bending, fore-aft bending, and yaw moments

    Line 1 fairlead and anchor effective tensions and vertical ang
    Line 2 fairlead and anchor effective tensions and vertical ang

"Fair1Ten , Fair1Ang , Anch1Ten , Anch1Ang"
"Fair2Ten , Fair2Ang , Anch2Ten , Anch2Ang"
"Fair3Ten , Fair3Ang , Anch3Ten , Anch3Ang"
                                                                                                       - Line 3 fairlead and anchor effective tensions and vertical ang
"Fair4Ten , Fair4Ang , Anch4Ten , Anch4Ang"
                                                                                                        - Line 4 fairlead and anchor effective tensions and vertical ang
"Fair5Ten , Fair5Ang , Anch5Ten , Anch5Ang"
                                                                                                        - Line 5 fairlead and anchor effective tensions and vertical ang
"Fair6Ten , Fair6Ang , Anch6Ten , Anch6Ang"
                                                                                                        - Line 6 fairlead and anchor effective tensions and vertical ang
"Fair7Ten , Fair7Ang , Anch7Ten , Anch7Ang"
                                                                                                        - Line 7 fairlead and anchor effective tensions and vertical ang
"Fair8Ten , Fair8Ang , Anch8Ten , Anch8Ang"
                                                                                                        - Line 8 fairlead and anchor effective tensions and vertical ang
"TipSpdRat, RotCp
                                    , RotCt
                                                        RotCq"
                                                                                                        - Rotor tip speed ratio and power, thrust, and torque coefficien
END of FAST input file (the word "END" must appear in the first 3 columns of this last line).
```

### A.2 Blade Input File - NRELOffshrBsline5MW\_Blade.dat

```
FlStTunr(1) - Blade flapwise modal stiffness tuner, 1st mode (-)
   1.0
            FlStTunr(2) - Blade flapwise modal stiffness tuner, 2nd mode (-)
   1.04536
           AdiBlMs
                       - Factor to adjust blade mass density (-)
            AdjF1St
                        - Factor to adjust blade flap stiffness (-)
   1.0
            AdjEdSt
                        - Factor to adjust blade edge stiffness (-)
           ----- DISTRIBUTED BLADE PROPERTIES ------
                                                   EdgStff
                                                               GTS+ff
BlFract AeroCent StrcTwst BMassDen FlpStff
                                                                         EAStff
                                                                                     Alpha FlpIner EdgIner PrecrvRef Pre
         (-)
                   (deg)
                             (kg/m)
                                       (Nm^2)
                                                   (Nm^2)
                                                               (Nm^2)
                                                                          (N)
                                                                                      (-)
                                                                                             (kg m)
                                                                                                      (kg m)
                                                                                                               (m)
                                                                                                                          (m)
(-)
0.00000 0.25000
                             678.935
                                                                           9729.48E6 0.0
                   13.308
                                       18110.00E6 18113.60E6 5564.40E6
                                                                                              972.86
                                                                                                       973.04
                                                                                                              0.0
                                                                                                                         0.0
0.00325 0.25000
                             678.935
                                       18110.00E6
                                                  18113.60E6 5564.40E6
                   13.308
                                                                           9729.48E6 0.0
                                                                                              972.86
                                                                                                       973.04
                                                                                                              0.0
                                                                                                                         0.0
0.01951
         0.24951
                   13.308
                             773.363
                                       19424.90E6
                                                   19558.60E6
                                                               5431.59E6
                                                                          10789.50E6
                                                                                             1091.52
                                                                                                      1066.38
                                                                                     0.0
                                                                                                              0.0
                                                                                                                          0.0
                             740.550
         0.24510
                   13.308
                                       17455.90E6
                                                   19497.80E6
                                                               4993.98E6
                                                                          10067.23E6
0.05203
         0.23284
                   13.308
                             740.042
                                       15287.40E6
                                                   19788.80E6
                                                               4666.59E6
                                                                           9867.78E6
                                                                                     0.0
                                                                                              873.81
                                                                                                      1099.75
                                                                                                              0.0
                                                                                                                          0.0
0.06829
        0.22059
                   13.308
                             592,496
                                       10782.40E6
                                                   14858.50E6
                                                               3474.71E6
                                                                           7607.86E6
                                                                                     0.0
                                                                                              648.55
                                                                                                       873.02 0.0
                                                                                                                          0.0
0.08455
         0.20833
                   13.308
                             450.275
                                       7229.72E6
                                                  10220.60E6
                                                              2323.54F6
                                                                           5491.26E6 0.0
                                                                                              456.76
                                                                                                       641.49
                                                                                                             0.0
                                                                                                                         9.9
0.10081 0.19608
                   13.308
                             424.054
                                        6309.54F6
                                                   9144.70F6 1907.87F6
                                                                           4971.30F6 0.0
                                                                                              400.53
                                                                                                       593.73 0.0
                                                                                                                          9.9
                             400.638
                                        5528.36E6
                                                                           4493.95E6 0.0
0.11707
         0.18382
                   13,308
                                                   8063,16E6
                                                              1570.36E6
                                                                                              351.61
                                                                                                       547.18 0.0
                                                                                                                         0.0
                                                                           4034.80E6
0.13335
         0.17156
                   13.308
                             382,062
                                        4980.06E6
                                                   6884.44E6
                                                              1158,26E6
                                                                                     0.0
                                                                                                       490.84 0.0
                                                                                              316.12
                                                                                                                         0.0
                                                              1002.12E6
0.14959
         0.15931
                   13.308
                             399.655
                                        4936.84E6
                                                   7009.18E6
                                                                           4037,29E6
                                                                                     0.0
                                                                                                       503.86
                                                                                              303.60
                                                                                                               0.0
                                                                                                                         0.0
0.16585
         0.14706
                   13.308
                             426.321
                                        4691.66E6
                                                    7167.68E6
                                                                855.90E6
                                                                           4169.72E6
                                                                                     0.0
                                                                                                       544.70
                                                                                                              0.0
                                        3949.46E6
0.18211
         0.13481
                   13.181
                             416.820
                                                    7271.66E6
                                                                672.27E6
                                                                           4082.35E6
                                                                                     0.0
                                                                                              246.57
                                                                                                       569.90 0.0
0.19837
                                                                547.49E6
         0.12500
                             406.186
                                        3386.52E6
                                                    7081.70E6
                                                                           4085.97E6
                                                                                              215.91
                                                                                                       601.28 0.0
                   12.848
                                                                                     0.0
                                                                                                                          0.0
0.21465
        0.12500
                   12.192
                             381.420
                                        2933.74E6
                                                   6244.53E6
                                                                448.84E6
                                                                           3668.34E6 0.0
                                                                                              187.11
                                                                                                       546.56 0.0
                                                                                                                         0.0
0.23089
         0.12500
                   11,561
                             352.822
                                        2568.96E6
                                                   5048,96E6
                                                                335.92E6
                                                                           3147.76E6 0.0
                                                                                              160.84
                                                                                                       468.71 0.0
                                                                                                                         0.0
                                                   4948,49E6
0.24715
         0.12500
                   11.072
                             349,477
                                        2388.65E6
                                                                311.35E6
                                                                           3011.58E6 0.0
                                                                                              148.56
                                                                                                       453.76 0.0
                                                                                                                          0.0
0.26341
         0.12500
                   10.792
                             346.538
                                        2271.99E6
                                                   4808.02E6
                                                                291.94E6
                                                                           2882.62E6
                                                                                     0.0
                                                                                              140.30
                                                                                                       436.22 0.0
                                                                                                                         0.0
                                        2050.05E6
                                                   4501.40E6
                                                                261.00E6
                                                                           2613.97E6
                                                                                                       398.18 0.0
0.29595
         0.12500
                   10.232
                             339.333
                                                                                              124.61
                                                                                     0.0
                                                                                                                         0.0
0.32846
         0.12500
                             330.004
                                        1828.25E6
                                                   4244.07E6
                                                                228.82E6
                                                                           2357.48E6
                                                                                     0.0
                                                                                              109.42
                                                                                                       362.08
                   9.672
                                                                                                             0.0
                                                                                                                          0.0
0.36098
         0.12500
                    9.110
                             321.990
                                        1588.71E6
                                                    3995.28E6
                                                                200.75E6
                                                                           2146.86E6
                                                                                                       335.01
0.39350
         0.12500
                    8.534
                             313.820
                                        1361.93E6
                                                   3750.76E6
                                                                174.38E6
                                                                           1944.09E6
                                                                                               80.24
                                                                                                       308.57 0.0
                                                                                     0.0
                                                                                                                          0.0
                                                                                     0.0
0.42602
         0.12500
                    7.932
                             294.734
                                        1102.38E6
                                                    3447.14E6
                                                                144.47E6
                                                                           1632.70E6
                                                                                               62.67
                                                                                                       263.87 0.0
                                                                                                                          0.0
0.45855
         0.12500
                    7.321
                             287.120
                                        875.80E6
                                                   3139.07E6
                                                                119.98E6
                                                                           1432,40E6 0.0
                                                                                               49.42
                                                                                                       237.06 0.0
                                                                                                                          0.0
0.49106
         0.12500
                    6.711
                             263.343
                                         681.30E6
                                                   2734,24E6
                                                                81.19E6
                                                                           1168.76E6 0.0
                                                                                               37.34
                                                                                                       196.41 0.0
                                                                                                                         0.0
0.52358
         0.12500
                    6.122
                             253.207
                                         534.72F6
                                                   2554.87F6
                                                                 69.09F6
                                                                           1047.43F6 0.0
                                                                                               29.14
                                                                                                       180.34 0.0
                                                                                                                         9.9
                                                                           922.95E6 0.0
0.55610
         0.12500
                    5.546
                             241.666
                                         408.90E6
                                                    2334.03E6
                                                                 57.45E6
                                                                                               22.16
                                                                                                       162.43
                                                                                                             0.0
                                                                                                                         0.0
0.58862
         0.12500
                    4.971
                             220.638
                                         314.54E6
                                                    1828.73E6
                                                                 45.92E6
                                                                            760.82E6 0.0
                                                                                               17.33
                                                                                                       134.83 0.0
                                                                                                                          0.0
0.62115
         0.12500
                    4.401
                             200.293
                                         238.63E6
                                                   1584.10E6
                                                                 35.98E6
                                                                            648.03E6 0.0
                                                                                               13.30
                                                                                                       116.30
                                                                                                              0.0
                                                                                                                         0.0
0.65366
         0.12500
                    3.834
                                         175.88E6
                                                    1323.36E6
                                                                 27.44E6
                                                                            539.70E6
0.68618
         0.12500
                    3.332
                             165.094
                                         126.01E6
                                                    1183.68E6
                                                                 20.90E6
                                                                            531.15E6 0.0
                                                                                                7.30
                                                                                                        98.93 0.0
                                                                                                                          0.0
0.71870
         0.12500
                    2.890
                             154,411
                                         107.26E6
                                                    1020.16E6
                                                                18.54E6
                                                                            460.01E6 0.0
                                                                                                6.22
                                                                                                        85.78 0.0
                                                                                                                          0.0
0.75122
         0.12500
                   2.503
                             138.935
                                          90.88E6
                                                     797.81E6
                                                                16.28E6
                                                                            375.75E6 0.0
                                                                                                5.19
                                                                                                        69.96 0.0
                                                                                                                         9.9
0.78376
         0.12500
                    2.116
                             129.555
                                          76.31F6
                                                     709.61F6
                                                                 14.53F6
                                                                            328.89F6 0.0
                                                                                                4.36
                                                                                                        61.41 0.0
                                                                                                                         9.9
         0.12500
                             107.264
                                                     518.19E6
                                                                  9.07E6
                                                                            244.04E6 0.0
0.81626
                    1.730
                                          61.05E6
                                                                                                        45.44 0.0
                                                                                                3.36
                                                                                                                         0.0
0.84878
         0.12500
                    1.342
                             98.776
                                          49.48E6
                                                     454.87E6
                                                                            211.60E6
                                                                                     0.0
                                                                                                2.75
                                                                                                        39.57
                                                                  8.06E6
                                                                                                               0.0
                                                                                                                          0.0
0.88130
         0.12500
                    0.954
                              90.248
                                          39.36E6
                                                     395.12E6
                                                                  7.08E6
                                                                            181.52E6 0.0
                                                                                                2.21
                                                                                                        34.09
                                                                                                             0.0
                                                                                                                         0.0
         0.12500
                    0.760
                                          34.67E6
                                                     353.72E6
                                                                  6.09E6
                                                                            160.25E6
                                                                                                        30.12
0.91382
         0.12500
                    0.574
                              72.906
                                          30.41E6
                                                     304.73E6
                                                                  5.75E6
                                                                            109.23E6 0.0
                                                                                                1.69
                                                                                                        20.15 0.0
                                                                                                                          0.0
                                                                                               1.49
0.93008
         0.12500
                    0.404
                              68.772
                                          26.52E6
                                                     281.42E6
                                                                  5.33E6
                                                                            100.08E6 0.0
                                                                                                        18.53 0.0
                                                                                                                          0.0
0.93821
         0.12500
                    0.319
                              66.264
                                          23.84E6
                                                     261.71F6
                                                                  4.94F6
                                                                            92.24E6 0.0
                                                                                                1.34
                                                                                                        17.11 0.0
                                                                                                                         9.9
0.94636
         0.12500
                    0.253
                              59.340
                                          19.63F6
                                                     158.81F6
                                                                  4.24F6
                                                                            63.23F6 0.0
                                                                                                1.10
                                                                                                        11.55 0.0
                                                                                                                         9.9
0.95447
         0.12500
                    0.216
                              55.914
                                          16.00E6
                                                     137.88E6
                                                                  3.66E6
                                                                            53.32E6 0.0
                                                                                                0.89
                                                                                                        9.77 0.0
                                                                                                                         0.0
                                                     118.79E6
0.96260
         0.12500
                    0.178
                              52,484
                                          12.83E6
                                                                  3.13E6
                                                                            44.53E6 0.0
                                                                                                0.71
                                                                                                        8.19 0.0
                                                                                                                         0.0
                    0.140
                              49.114
                                          10.08E6
                                                     101.63E6
                                                                            36.90E6 0.0
                                                                                                0.56
0.97073
         0.12500
                                                                  2.64E6
                                                                                                        6.82 0.0
                                                                                                                         0.0
                                                                                                              0.0
0.97886
         0.12500
                    0.101
                              45.818
                                           7.55E6
                                                      85.07E6
                                                                  2.17E6
                                                                             29.92E6 0.0
                                                                                                0.42
                                                                                                        5.57
                                                                                                                         0.0
                                                                                                0.25
0.98699
         0.12500
                    0.062
                              41.669
                                           4.60E6
                                                      64.26E6
                                                                  1.58E6
                                                                            21.31E6 0.0
                                                                                                         4.01 0.0
                              11.453
                                                       6.61E6
0.99512
         0.12500
                    0.023
                                           0.25E6
                                                                  0.25E6
                                                                             4.85E6 0.0
                                                                                                0.04
                                                                                                         0.94 0.0
                                                                                                                          0.0
1.00000 0.12500
                   0.000
                              10.319
                                           0.17E6
                                                       5.01E6
                                                                  0.19F6
                                                                             3.53E6 0.0
                                                                                                0.02
                                                                                                        0.68 0.0
                                                                                                                         0.0
  ----- BLADE MODE SHAPES ------
           BldFl1Sh(2) - Flap mode 1, coeff of x^2
BldFl1Sh(3) - , coeff of x^3
   0.0622
                            , coeff of x^3
  1.7254
                                     , coeff of x^4
            BldFl1Sh(4) -
  -3.2452
                                   , coeff of x^5
   4.7131
            BldFl1Sh(5) -
            BldFl1Sh(6) -
                                     , coeff of x^6
  -0.5809
           BldFl2Sh(2) - Flap mode 2, coeff of x^2
  1.2067
            BldFl2Sh(3) - , coeff of x^3
                                    , coeff of x^4
            BldFl2Sh(4) -
 -15.5349
                                    , coeff of x^5
 29.7347
           BldFl2Sh(5) -
            BldF12Sh(6) -
                                     , coeff of x^6
 -13.8255
   0.3627
            BldEdgSh(2) - Edge mode 1, coeff of x^2
                            , coeff of x^3
            BldEdgSh(3) -
   2.5337
            BldEdgSh(4) -
   2.3760
            BldEdgSh(5) -
                                    , coeff of x^5
            BldEdgSh(6) -
```

## A.3 Tower Input File - NRELOffshrBsline5MW\_Tower\_Onshore.dat

```
TwrFADmp(1) - Tower 1st fore-aft mode structural damping ratio (%)
            TwrFADmp(2) - Tower 2nd fore-aft mode structural damping ratio (%)
   1.0
            TwrSSDmp(1) - Tower 1st side-to-side mode structural damping ratio (%)
           TwrSSDmp(2) - Tower 2nd side-to-side mode structural damping ratio (%)
           ----- TOWER ADJUSTMUNT FACTORS ------
  1.0
           FAStTunr(1) - Tower fore-aft modal stiffness tuner, 1st mode (-)
           FAStTunr(2) - Tower fore-aft modal stiffness tuner, 2nd mode (-)
  1.0
           SSStTunr(1) - Tower side-to-side stiffness tuner, 1st mode (-)
  1.0
           SSStTunr(2) - Tower side-to-side stiffness tuner, 2nd mode (-)
   1.0
                     - Factor to adjust tower mass density (-)
  1.0
           AdjTwMa
           AdjFASt
                      - Factor to adjust tower fore-aft stiffness (-)
   1.0
                      - Factor to adjust tower side-to-side stiffness (-)
           AdjSSSt
 ----- DISTRIBUTED TOWER PROPERTIES -----
HtFract TMassDen TwFAStif TwSSStif TwGJStif TwEAStif TwFAIner TwSSIner TwFAcgOf TwSScgOf
         (kg/m)
                  (Nm^2)
                             (Nm^2)
                                       (Nm^2)
                                                  (N)
                                                            (kg m)
                                                                      (kg m)
        5590.87
                  614.343E9 614.343E9 472.751E9 138.127E9 24866.3
9.9
                                                                      24866.3
                                                                               0.0
                                                                                         9.9
                  534.821E9 534.821E9 411.558E9 129.272E9 21647.5
        5232.43
                                                                      21647.5
0.1
                                                                                0.0
                                                                                         0.0
                  463.267E9 463.267E9
                                       356.495E9 120.707E9 18751.3
        4885.76
                                                                      18751.3
0.2
                                                                                0.0
                                                                                         0.0
                                                                      16155.3
        4550.87
                  399.131E9 399.131E9
                                       307.141E9 112.433E9 16155.3
                                                                                0.0
                                                                                         0.0
0.3
        4227.75
                  341.883E9 341.883E9 263.087E9 104.450E9
                                                            13838.1
                                                                      13838.1
                  291.011E9 291.011E9 223.940E9 96.758E9 11779.0
        3916.41
                                                                      11779.0
        3616.83
                  246.027E9 246.027E9 189.323E9
                                                   89.357E9
                                                             9958.2
                                                                       9958.2
                  206.457E9 206.457E9 158.874E9
                                                                                         0.0
0.7
        3329.03
                                                   82.247E9
                                                             8356.6
                                                                       8356.6
                                                                               0.0
0.8
        3053.01
                  171.851E9 171.851E9 132.244E9
                                                   75.427E9
                                                             6955.9
                                                                       6955.9
                                                                                0.0
                                                                                         0.0
        2788.75 141.776E9 141.776E9 109.100E9
2536.27 115.820E9 115.820E9 89.126E9
0.9
                                                   68.899E9
                                                             5738.6
                                                                       5738.6
                                                                                0.0
                                                                                         0.0
                                       89.126E9 62.661E9
                                                             4688.0
                                                                       4688.0
1.0
                                                                               0.0
                                                                                         0.0
 ----- TOWER FORE-AFT MODE SHAPES -----
           TwFAM1Sh(2) - Mode 1, coefficient of x^2 term
                           , coefficient of x^3 term
           TwFAM1Sh(3) -
   2.1963
                              , coefficient of x^4 term
  -5.6202
           TwFAM1Sh(4) -
                           , coefficient of x^5 term
   6.2275
           TwFAM1Sh(5) -
           TWFAM1Sh(6) - , coefficient of x^6 term
TWFAM2Sh(2) - Mode 2, coefficient of x^2 term
  -2.5040
 -70.5319
           TwFAM2Sh(3) - , coefficient of x^3 term
 -63.7623
                              , coefficient of x^4 term
           TwFAM2Sh(4) -
 289.7369
                            , coefficient of x^5 term
           TwFAM2Sh(5) -
 176.5134
 22.0706
           TwFAM2Sh(6) -
                               , coefficient of x^6 term
      ----- TOWER SIDE-TO-SIDE MODE SHAPES -----
 1.3850
           TwSSM1Sh(2) - Mode 1, coefficient of x^2 term
                           , coefficient of x^3 term
  -1.7684
           TwSSM1Sh(3) -
                              , coefficient of x^4 term
           TwSSM1Sh(4) -
  3.0871
                            , coefficient of x^5 term
           TwSSM1Sh(5) -
  -2.2395
           TwSSM1Sh(6) - , coefficient of x^6 term TwSSM2Sh(2) - Mode 2, coefficient of x^2 term
  0.5357
 121.2097
 184,4151
           TwSSM2Sh(3) - , coefficient of x^3 term
           TwSSM2Sh(4) -
                              , coefficient of x^4 term
 298.5360
           TwSSM2Sh(5) -
                            , coefficient of x^5 term
           TwSSM2Sh(6) -
                              , coefficient of x^6 term
```

## A.4 ADAMS Input File – NRELOffshrBsline5MW\_ADAMSSpecific.dat

```
NREL 5.0 MW offshore baseline ADAMS-specific input properties.
 ----- FEATURE FLAGS
           SaveGrphcs - Save GRAPHICS output (flag)
MakeLINacf - Make an ADAMS/LINEAR control / command file (flag)
True
False
------ DAMPING PARAMETERS
           CRatioTGJ - Ratio of damping to stiffness for the tower torsion deflection (-)
CRatioTEA - Ratio of damping to stiffness for the tower extensional deflection (-)
  0.01
  0.01
                      - Ratio of damping to stiffness for the blade torsion
  0.01
           CRatioBGJ
                      - Ratio of damping to stiffness for the blade extensional deflections (-)
  0.01
           CRatioBEA
            ----- BLADE PITCH ACTUATOR PARAMETERS -----
971.350E6 BPActrSpr - Blade pitch actuator spring stiffness constant (N-m/rad)
  0.206E6 BPActrDmp - Blade pitch actuator damping constant (N-m/(rad/s))
------ GRAPHICS PARAMETERS ------
                      - Number of sides used in GRAPHICS CYLINDER and FRUSTUM statements (-)
 20
           NSides
  3.000
           TwrBaseRad - Tower base radius used for linearly tapered tower GRAPHICS CYLINDERs (m)
  1.935
           TwrTopRad
                      - Tower top radius used for linearly tapered tower GRAPHICS CYLINDERS (m)
                       - Length of nacelle used for the nacelle GRAPHICS (m)
           NacLength .
                       - Bottom (opposite rotor) radius of nacelle FRUSTUM used for the nacelle GRAPHICS (m)
  1.75
           NacRadBot
           NacRadTop
  1.75
                       - Top (rotor end) radius of nacelle FRUSTUM used for the nacelle GRAPHICS (m)
  1.0
           GBoxLength
                      - Length, width, and height of the gearbox BOX for gearbox GRAPHICS (m)
  2.39
           GenLength
                       - Length of the generator CYLINDER used for generator GRAPHICS (m)
                       - Length of the high-speed shaft CYLINDER used for HSS GRAPHICS (m)
  1.195
           HSSLength
                         Length of the low-speed shaft CYLINDER used for LSS GRAPHICS (m)
  4.78
           LSSLength
                         Radius of the generator CYLINDER used for generator GRAPHICS (m)
  0.75
           GenRad
  0.2
           HSSRad
                         Radius of the high-speed shaft CYLINDER used for HSS GRAPHICS (m)
                         Radius of the low -speed shaft CYLINDER used for LSS GRAPHICS (m)
  0.875
           HubCy1Rad
                         Radius of hub CYLINDER used for hub GRAPHICS (m)
  0.18
           ThkOvrChrd -
                         Ratio of blade thickness to blade chord used for blade element BOX GRAPHICS (-)
  9.9
           BoomRad
                       - Radius of the tail boom CYLINDER used for tail boom GRAPHICS (m)
```

## A.5 Linearization Input File - NRELOffshrBsline5MW\_Linear.dat

```
------ FAST LINEARIZATION CONTROL FILE ------
NREL 5.0 MW offshore baseline linearization input properties.
                 ----- PERIODIC STEADY STATE SOLUTION -----
                             - Calculate periodic steady state condition {False: linearize about initial conditions} (flag)
- Trim case {1: find nacelle yaw, 2: find generator torque, 3: find collective blade pitch} (switch)
- Convergence tolerance for the 2-norm of displacements in the periodic steady state calculation (rad
- Convergence tolerance for the 2-norm of velocities in the periodic steady state calculation (rad
               CalcStdy
True
               TrimCase
   0.0001
              DispTol
   0.0010 VelTol
              ----- MODEL LINEARIZATION -----
               NAzimStep - Number of equally-spaced azimuth steps in periodic linearized model (-)
               Md10rder
                             - Order of output linearized model {1: 1st order A, B, Bd, C, D, Dd; 2: 2nd order M, C, K, F, Fd, Vel
                            INPUTS AND DISTURBANCES -----
   0
              NInputs
                             - Number of control inputs [0 (none) or 1 to 4+NumBl] (-)
              CntrlInpt
                             - List of control inputs [1 to NInputs] {1: nacelle yaw angle, 2: nacelle yaw rate, 3: generator to
                            - Number of wind disturbances [0 (none) or 1 to 7] (-)
- List of input wind disturbances [1 to NDisturbs] {1: horizontal hub-height wind speed, 2: horizon
              NDisturbs
   0
              Disturbnc
```

# Appendix B AeroDyn Input Files

#### B.1 Primary Input File – NRELOffshrBsline5MW\_AeroDyn.ipt

```
NREL 5.0 MW offshore baseline aerodynamic input properties; Compatible with AeroDyn v12.58.
                          - System of units used for input and output [must be SI for FAST] (unquoted string)
- Dynamic stall included [BEDDOES or STEADY] (unquoted string)
             SysUnits
BEDDOES
             StallMod
USE CM
                          - Use aerodynamic pitching moment model? [USE CM or NO CM] (unquoted string)
             UseCm
EQUIL
             InfModel
                            Inflow model [DYNIN or EQUIL] (unquoted string)
                            Induction-factor model [NONE or WAKE or SWIRL] (unquoted string)
WAKE
             IndModel
  0.005
             AToler
                          - Induction-factor tolerance (convergence criteria) (-)
                          - Tip-loss model (EQUIL only) [PRANDtl, GTECH, or NONE] (unquoted string) - Hub-loss model (EQUIL only) [PRANdtl or NONE] (unquoted string)
PRANDt1
             TLModel
PRANDt1
             HLModel
"WindData\90m 12mps"
                                                     WindFile
                                                                  - Name of file containing wind data (quoted string)
  90.0
            нн
                          - Wind reference (hub) height [TowerHt+Twr2Shft+OverHang*SIN(ShftTilt)] (m)
             TwrShad
  0.0
                          - Tower-shadow velocity deficit (-)
9999.9
             ShadHWid
                            Tower-shadow half width (m)
9999.9
             T_Shad_Refpt- Tower-shadow reference point (m)
  1.225
             AirDens

    Air density (kg/m<sup>3</sup>)

   1.464E-5 KinVisc
                            Kinematic air viscosity [CURRENTLY IGNORED] (m^2/sec)
                          - Time interval for aerodynamic calculations (sec)
   0.02479 DTAero
            NumFoil
                            Number of airfoil files (-)
 'AeroData\Cylinder1.dat"
                                                                  - Names of the airfoil files [NumFoil lines] (quoted strings)
"AeroData\Cylinder2.dat"
"AeroData\DU40 A17.dat'
"AeroData\DU35_A17.dat"
 'AeroData\DU30_A17.dat"
"AeroData\DU25_A17.dat"
"AeroData\DU21 A17.dat"
 'AeroData\NACA64_A17.dat"
 17
            BldNodes
                         - Number of blade nodes used for analysis (-)
RNodes
         AeroTwst DRNodes Chord NFoil PrnElm
 2.8667
                                             NOPRINT
         13.308
                    2.7333
                              3.542 1
                                             NOPRINT
 5.6000
         13.308
                    2.7333
                              3.854
         13.308
                    2.7333
                                             NOPRINI
 8.3333
                              4.167
11.7500
         13.308
                    4.1000
                              4.557
                                             NOPRINT
15.8500
         11.480
                    4.1000
                              4.652
                                             NOPRINT
19.9500
         10.162
                    4.1000
                              4.458
                                             NOPRINT
24.0500
          9.011
                    4.1000
                              4.249
                                             NOPRINT
28,1500
          7.795
                    4.1000
                              4.007
                                             NOPRINT
32,2500
          6.544
                    4.1000
                              3.748
                                             NOPRINT
36.3500
          5.361
                    4.1000
                              3.502
                                             NOPRINT
40.4500
                    4.1000
                              3.256
                                             NOPRINT
           4.188
44.5500
           3.125
                    4.1000
                              3.010
48.6500
           2.319
                    4.1000
                              2.764
                                             NOPRINT
52.7500
           1.526
                    4.1000
                              2.518
                                              NOPRINT
56.1667
           0.863
                    2.7333
                              2.313
                                             NOPRINT
58,9000
          0.370
                    2.7333
                              2.086
                                      8
                                             NOPRINI
                                             NOPRINI
61.6333
           0.106
                    2.7333
                              1.419
```

#### B.2 Airfoil-Data Input File - Cylinder1.dat

```
Round root section with a Cd of 0.50
Made by Jason Jonkman
            Number of airfoil tables in this file
  9.9
            Table ID parameter
  0.0
            Stall angle (deg)
            No longer used, enter zero
No longer used, enter zero
  0.0
  0.0
  0.0
            No longer used, enter zero
            Zero Cn angle of attack (deg)
  0.0
            Cn slope for zero lift (dimensionless)
  0.0
            Cn extrapolated to value at positive stall angle of attack
  9.9
            Cn at stall value for negative angle of attack
  0.0
            Angle of attack for minimum CD (deg)
            Minimum CD value
  0.50
180.00
           0.000
                   0.5000
                             0.000
  0.00
           0.000
                   0.5000
                             0.000
                   0.5000
```

#### B.3 Airfoil-Data Input File - Cylinder2.dat

```
Round root section with a Cd of 0.35
Made by Jason Jonkman

1 Number of airfoil tables in this file
```

```
Table ID parameter
  0.0
           Stall angle (deg)
           No longer used, enter zero
           No longer used, enter zero
  0.0
           No longer used, enter zero
  0.0
           Zero Cn angle of attack (deg)
  9.9
           Cn slope for zero lift (dimensionless)
           Cn extrapolated to value at positive stall angle of attack
  9.9
           Cn at stall value for negative angle of attack
  0.0
           Angle of attack for minimum CD (deg)
  0.0
  0.35
           Minimum CD value
                 0.3500
180.00
 0.00
          0.000
                  0.3500
                           0.000
180.00
          0.000
                  0.3500
                           0.000
```

### B.4 Airfoil-Data Input File - DU40\_A17.dat

```
DU40 airfoil with an aspect ratio of 17. Original -180 to 180deg Cl, Cd, and Cm versus AOA data taken from Appendix A of DOW
Cl and Cd values corrected for rotational stall delay and Cd values corrected using the Viterna method for 0 to 90deg AOA by
            Number of airfoil tables in this file
   0.0
            Table ID parameter
   9.00
            Stall angle (deg)
   9.9
            No longer used, enter zero
            No longer used, enter zero
No longer used, enter zero
   0.0
  0.0
            Zero Cn angle of attack (deg)
  -1.3430
  7.4888
            Cn slope for zero lift (dimensionless)
   1.3519
            Cn extrapolated to value at positive stall angle of attack
  -0.3226
            Cn at stall value for negative angle of attack
  0.00
            Angle of attack for minimum CD (deg)
  0.0113
            Minimum CD value
-180.00
                   0.0602
                            0.0000
           0.000
                   0.0699
                            0.0934
-175.00
           0.218
-170.00
           0.397
                   0.1107
                            0.1697
-160.00
           0.642
                   0.3045
                            0.2813
-155.00
           0.715
                   0.4179
                             0.3208
-150.00
           0.757
                   0.5355
                            0.3516
-145.00
           0.772
                   0.6535
                            0.3752
-140.00
           0.762
                   0.7685
                             0.3926
-135.00
           0.731
                   0.8777
                            0.4048
-130.00
           0.680
                   0.9788
                            0.4126
           0.613
                   1.0700
-125.00
                            0.4166
           0.532
-120.00
                   1.1499
                            0.4176
-115.00
           0.439
                   1.2174
-110.00
           0.337
                   1.2716
                             0.4117
-105.00
           0.228
                   1.3118
                            0.4057
-100.00
           0.114
                   1.3378
                            0.3979
-95.00
          -0.002
                   1.3492
                            0.3887
                   1.3460
-90.00
          -0.120
                            0.3781
-85.00
          -0.236
                   1.3283
                            0.3663
          -0.349
                   1.2964
-80.00
                            0.3534
 -75.00
          -0.456
                   1.2507
                             0.3394
                   1.1918
-70.00
          -0.557
                             0.3244
-65.00
          -0.647
                   1.1204
                            0.3084
-60.00
          -0.727
                   1.0376
                            0.2914
-55.00
          -0.792
                   0.9446
                            0.2733
-50.00
          -0.842
                   0.8429
                            0.2543
          -0.874
                   0.7345
-45.00
                            0.2342
-40.00
          -0.886
                   0.6215
                            0.2129
-35.00
          -0.875
                   0.5067
                            0.1906
                   0.3932
-30.00
          -0.839
                             0.1670
-25.00
          -0.777
                   0.2849
                             0.1422
 -24.00
          -0.761
                   0.2642
                            0.1371
-23.00
          -0.744
                   0.2440
                            0.1320
-22.00
          -0.725
                   0.2242
                            0.1268
-21.00
          -0.706
                   0.2049
                            0.1215
-20.00
          -0.685
                   0.1861
                            0.1162
-19.00
          -0.662
                   0.1687
                            0.1097
-18.00
          -0.635
                   0.1533
                            0.1012
-17.00
          -0.605
                   0.1398
                             0.0907
-16.00
          -0.571
                   0.1281
                            0.0784
-15.00
          -0.534
                   0.1183
                            0.0646
-14.00
          -0.494
                   0.1101
                             0.0494
-13.00
          -0.452
                   0.1036
                            0.0330
-12.00
          -0.407
                   0.0986
                            0.0156
                   0.0951
 -11.00
          -0.360
                            -0.0026
 -10.00
          -0.311
                   0.0931
                            -0.0213
 -8.00
          -0.208
                   0.0930
                            -0.0600
  -6.00
          -0.111
                   0.0689
 -5.50
          -0.090
                   0.0614
                            -0.0516
 -5.00
          -0.072
                   0.0547
                            -0.0532
  -4.50
          -0.065
                   0.0480
                            -0.0538
```

```
-4.00
          -0.054
                   0.0411
                           -0.0544
 -3.50
          -0.017
                   0.0349
                           -0.0554
 -3.00
          0.003
                   0.0299
                           -0.0558
                           -0.0555
 -2.50
          0.014
                   0.0255
 -2.00
          0.009
                   0.0198
                           -0.0534
 -1.50
          0.004
                   0.0164
                           -0.0442
 -1.00
          0.036
                   0.0147
                           -0.0469
 -0.50
          0.073
                   0.0137
                           -0.0522
          0.137
                   0.0113
                           -0.0573
  0.00
  0.50
          0.213
                   0.0114
                           -0.0644
  1.00
          0.292
                   0.0118
                           -0.0718
          0.369
                   0.0122
                           -0.0783
  1.50
  2.00
          0.444
                   0.0124
                           -0.0835
  2.50
          0.514
                   0.0124
                           -0.0866
  3.00
          0.580
                   0.0123
                           -0.0887
          0.645
                           -0.0900
  3.50
                   0.0120
          0.710
                   0.0119
                           -0.0914
  4.00
          0.776
  4.50
                   0.0122
                           -0.0933
  5.00
          0.841
                   0.0125
                           -0.0947
          0.904
                   0.0129
                           -0.0957
  5.50
  6.00
          0.967
                   0.0135
                           -0.0967
  6.50
          1.027
                   0.0144
                           -0.0973
  7.00
          1.084
                   0.0158
                           -0.0972
  7.50
          1.140
                   0.0174
                           -0.0972
  8.00
          1.193
                   0.0198
                           -0.0968
  8.50
          1.242
                   0.0231
                           -0.0958
          1.287
                   0.0275
                           -0.0948
  9.00
  9.50
          1.333
                   0.0323
                           -0.0942
 10.00
          1.368
                   0.0393
                           -0.0926
 10.50
          1.400
                   0.0475
                           -0.0908
11.00
          1.425
                   0.0580
                           -0.0890
11.50
          1.449
                   0.0691
                           -0.0877
12.00
          1.473
                   0.0816
                           -0.0870
12.50
          1.494
                   0.0973
                           -0.0870
          1.513
13.00
                   0.1129
                           -0.0876
13.50
          1.538
                   0.1288
                           -0.0886
14.50
          1.587
                   0.1650
                           -0.0917
 15.00
          1.614
                   0.1845
                           -0.0939
 15.50
          1.631
                   0.2052
                           -0.0966
16.00
          1.649
                   0.2250
                           -0.0996
16.50
          1.666
                   0.2467
                           -0.1031
17.00
          1.681
                   0.2684
                           -0.1069
          1.699
                   0.2900
                           -0.1110
17.50
18.00
          1.719
                   0.3121
                           -0.1157
19.00
          1.751
                   0.3554
                           -0.1242
 19.50
          1.767
                   0.3783
                           -0.1291
 20.50
          1.798
                   0.4212
                           -0.1384
 21.00
          1.810
                   0.4415
                           -0.1416
22.00
          1.830
                   0.4830
                           -0.1479
 23.00
          1.847
                   0.5257
                           -0.1542
24.00
          1.861
                   0.5694
                           -0.1603
 25.00
          1.872
                   0.6141
                           -0.1664
 26.00
          1.881
                   0.6593
                           -0.1724
 28.00
          1.894
                   0.7513
                           -0.1841
 30.00
          1.904
                   0.8441
                           -0.1954
 32.00
          1.915
                   0.9364
                           -0.2063
 35.00
          1.929
                   1.0722
                           -0.2220
40.00
          1.903
                   1.2873
                           -0.2468
45.00
          1.820
                   1.4796
                           -0.2701
          1.690
50.00
                   1.6401
                           -0.2921
          1.522
                   1.7609
 55.00
                           -0.3127
 60.00
          1.323
                   1.8360
                           -0.3321
 65.00
          1.106
                   1.8614
                           -0.3502
 70.00
          0.880
                   1.8347
                           -0.3672
 75.00
          0.658
                   1.7567
                           -0.3830
 80.00
          0.449
                   1.6334
                           -0.3977
85.00
          0.267
                   1.4847
                           -0.4112
90.00
          0.124
                   1.3879
                           -0.4234
95.00
          0.002
                   1.3912
                           -0.4343
100.00
         -0.118
                   1.3795
                           -0.4437
105.00
         -0.235
                   1.3528
                           -0.4514
110.00
         -0.348
                   1.3114
                           -0.4573
115.00
         -0.453
                   1.2557
                           -0.4610
120.00
         -0.549
                   1.1864
                           -0.4623
125.00
         -0.633
                   1.1041
                           -0.4606
130.00
         -0.702
                   1.0102
                           -0.4554
         -0.754
                   0.9060
                           -0.4462
135.00
                   0.7935
140.00
         -0.787
                           -0.4323
145.00
         -0.797
                   0.6750
                           -0.4127
150.00
         -0.782
                   0.5532
                           -0.3863
155.00
          -0.739
                   0.4318
                           -0.3521
160.00
         -0.664
                   0.3147
                           -0.3085
170.00
         -0.410
                   0.1144
                           -0.1858
                   0.0702
175.00
         -0.226
                           -0.1022
```

### B.5 Airfoil-Data Input File - DU35\_A17.dat

```
DU35 airfoil with an aspect ratio of 17. Original -180 to 180deg Cl, Cd, and Cm versus AOA data taken from Appendix A of DOW
Cl and Cd values corrected for rotational stall delay and Cd values corrected using the Viterna method for 0 to 90deg AOA by
            Number of airfoil tables in this file
   0.0
            Table ID parameter
            Stall angle (deg)
 11.50
   0.0
            No longer used, enter zero
            No longer used, enter zero
   0.0
            No longer used, enter zero
  -1.8330
            Zero Cn angle of attack (deg)
  7.1838
            Cn slope for zero lift (dimensionless)
  1.6717
            \mbox{\it Cn} extrapolated to value at positive stall angle of attack
            Cn at stall value for negative angle of attack
  -0.3075
  0.00
            Angle of attack for minimum CD (deg)
   0.0094
            Minimum CD value
-180.00
           0.000
                   0.0407
                             0.0000
-175.00
           0.223
                   0.0507
                             0.0937
-170.00
           0.405
                   0.1055
                             0.1702
-160.00
           0.658
                   0.2982
                             0.2819
-155.00
           0.733
                   0.4121
                             0.3213
           0.778
                   0.5308
-150.00
                             0.3520
-145.00
           0.795
                   0.6503
                             0.3754
-140.00
           0.787
                   0.7672
                             0.3926
           0.757
                   0.8785
                             0.4046
-135.00
-130.00
           0.708
                   0.9819
                             0.4121
-125.00
           0.641
                   1.0756
                             0.4160
-120.00
           0.560
                   1.1580
                             0.4167
-115.00
           0.467
                   1.2280
                             0.4146
-110.00
           0.365
                   1.2847
                             0.4104
-105.00
           0.255
                   1.3274
                             0.4041
-100.00
           0.139
                   1.3557
                             0.3961
 -95.00
           0.021
                   1.3692
                             0.3867
 -90.00
          -0.098
                   1.3680
                             0.3759
 -85.00
          -0.216
                   1.3521
                             0.3639
 -80.00
          -0.331
                   1.3218
                             0.3508
 -75.00
          -0.441
                   1.2773
                             0.3367
 -70.00
          -0.544
                   1.2193
                             0.3216
 -65.00
          -0.638
                   1.1486
                             0.3054
                             0.2884
 -60.00
          -0.720
                   1.0660
          -0.788
 -55.00
                   0.9728
                             0.2703
 -50.00
          -0.840
                   0.8705
                             0.2512
 -45.00
          -0.875
                   0.7611
                             0.2311
 -40.00
          -0.889
                   0.6466
                             0.2099
 -35.00
          -0.880
                   0.5299
                             0.1876
 -30.00
          -0.846
                   0.4141
                             0.1641
 -25.00
          -0.784
                   0.3030
                             0.1396
 -24.00
          -0.768
                   0.2817
                             0.1345
                   0.2608
 -23.00
          -0.751
                             0.1294
 -22.00
          -0.733
                   0.2404
                             0.1243
                   0.2205
 -21.00
          -0.714
                             0.1191
 -20.00
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                   0.2011
                             0.1139
 -19.00
          -0.671
                   0.1822
                             0.1086
 -18.00
          -0.648
                   0.1640
                             0.1032
 -17.00
          -0.624
                   0.1465
                             0.0975
          -0.601
                             0.0898
 -16.00
                   0.1300
 -15.00
          -0.579
                   0.1145
                             0.0799
 -14.00
          -0.559
                   0.1000
                             0.0682
 -13.00
          -0.539
                   0.0867
                             0.0547
 -12.00
          -0.519
                   0.0744
                             0.0397
 -11.00
          -0.499
                   0.0633
                             0.0234
 -10.00
          -0.480
                   0.0534
                             0.0060
 -5.54
          -0.385
                   0.0245
                            -0.0800
 -5.04
          -0.359
                   0.0225
                            -0.0800
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          -0.360
                   0.0196
                            -0.0800
          -0.355
  -4.04
                   0.0174
                            -0.0800
  -3.54
          -0.307
                   0.0162
                            -0.0800
          -0.246
                   0.0144
                            -0.0800
  -3.00
          -0.240
                   0.0240
                            -0.0623
  -2.50
          -0.163
                   0.0188
                            -0.0674
  -2.00
          -0.091
                   0.0160
                            -0.0712
  -1.50
          -0.019
                   0.0137
                            -0.0746
  -1.00
           0.052
                   0.0118
                            -0.0778
  -0.50
           0.121
                   0.0104
                            -0.0806
   0.00
           0.196
                   0.0094
                            -0.0831
   0.50
           0.265
                   0.0096
                            -0.0863
   1.00
           0.335
                   0.0098
                            -0.0895
   1.50
           0.404
                   0.0099
                            -0.0924
   2.00
           0.472
                   0.0100
                            -0.0949
   2.50
           9.549
                   0.0102
                            -0.0973
```

```
0.608
                  0.0103
                          -0.0996
  3.50
          0.674
                  0.0104
                           -0.1016
          0.742
                  0.0105
          0.809
                  0.0107
  5.00
          0.875
                  0.0108
                           -0.1076
  5.50
          0.941
                  0.0109
                           -0.1094
  6.00
          1.007
                  0.0110
                          -0.1109
  6.50
          1.071
                  0.0113
                          -0.1118
  7.00
                  0.0115
          1.134
                          -0.1127
  7.50
          1.198
                  0.0117
                          -0.1138
  8.00
          1.260
                  0.0120
                          -0.1144
          1.318
                  0.0126
  8.50
  9.00
          1.368
                  0.0133
                          -0.1112
 9.50
          1.422
                  0.0143
                           -0.1100
 10.00
          1.475
                  0.0156
                          -0.1086
10.50
          1.523
                  0.0174
                          -0.1064
11.00
          1.570
                  0.0194
                          -0.1044
11.50
          1,609
                  0.0227
                          -0.1013
12.00
          1.642
                  0.0269
                           -0.0980
 12.50
          1.675
                  0.0319
                           -0.0953
 13.00
          1.700
                  0.0398
                           -0.0925
 13.50
          1.717
                  0.0488
                           -0.0896
14.00
          1.712
                  0.0614
                          -0.0864
14.50
          1.703
                  0.0786
                          -0.0840
15.50
          1.671
                  0.1173
                          -0.0830
16.00
          1.649
                           -0.0848
                  0.1377
                           -0.0880
16.50
          1.621
                  0.1600
 17.00
          1.598
                  0.1814
                          -0.0926
          1.571
                  0.2042
 18.00
          1.549
                  0.2316
                           -0.1052
 19.00
          1.544
                  0.2719
                           -0.1158
 19.50
          1.549
                  0.2906
                          -0.1213
 20.00
          1.565
                  0.3085
                          -0.1248
 21.00
          1.565
                  0.3447
                           -0.1317
                  0.3820
 22.00
          1.563
                          -0.1385
 23.00
          1.558
                  0.4203
                          -0.1452
 24.00
          1.552
                  0.4593
                          -0.1518
 25.00
          1.546
                  0.4988
                           -0.1583
 26.00
          1.539
                  0.5387
                          -0.1647
 28.00
          1.527
                  0.6187
                           -0.1770
 30.00
          1.522
                  0.6978
                          -0.1886
 32.00
          1.529
                  0.7747
                          -0.1994
          1.544
                  0.8869
 35.00
                          -0.2148
40.00
          1.529
                  1.0671
                          -0.2392
 45.00
          1.471
                  1.2319
                          -0.2622
 50.00
          1.376
                  1.3747
 55.00
          1.249
                  1.4899
                           -0.3043
 60.00
          1.097
                  1.5728
                           -0.3236
 65.00
          0.928
                  1.6202
                          -0.3417
 70.00
          0.750
                  1.6302 -0.3586
 75.00
          0.570
                  1.6031 -0.3745
          0.396
80.00
                  1.5423
                          -0.3892
          0.237
85.00
                  1.4598
                          -0.4028
90.00
          0.101
                  1.4041
                          -0.4151
95.00
         -0.022
                  1.4053
                           -0.4261
100.00
         -0.143
                  1.3914
                           -0.4357
105.00
         -0.261
                  1.3625
                          -0.4437
110.00
         -0.374
                  1.3188
                          -0.4498
115.00
         -0.480
                  1.2608
                          -0.4538
         -0.575
120.00
                  1.1891
                          -0.4553
                  1.1046
125.00
         -0.659
                           -0.4540
130.00
         -0.727
                  1.0086
                          -0.4492
135.00
                  0.9025
                           -0.4405
140.00
         -0.809
                  0.7883
                          -0.4270
145.00
         -0.818
                  0.6684
                           -0.4078
150.00
         -0.800
                  0.5457
                           -0.3821
155.00
         -0.754
                  0.4236
                          -0.3484
160.00
         -0.677
                  0.3066
                          -0.3054
170.00
         -0.417
                  0.1085
                          -0.1842
175.00
         -0.229
                  0.0510
                           -0.1013
                  0.0407
                           0.0000
```

# B.6 Airfoil-Data Input File – DU30\_A17.dat

```
-2.3220
            Zero Cn angle of attack (deg)
  7.3326
            Cn slope for zero lift (dimensionless)
  1.4490
            Cn extrapolated to value at positive stall angle of attack
  -0.6138
            Cn at stall value for negative angle of attack
  0.00
            Angle of attack for minimum CD (deg)
  0.0087
           Minimum CD value
                            9.9999
-180.00
           0.000
                   0.0267
                            0.1379
-175.00
           0.274
                   0.0370
-170.00
           0.547
                   0.0968
                             0.2778
                   0.2876
-160.00
          0.685
                             0.2740
-155.00
           0.766
                   0.4025
                             0.3118
-150.00
           0.816
                   0.5232
                             0.3411
-145.00
           0.836
                   0.6454
                             0.3631
-140.00
           0.832
                   0.7656
                             0.3791
-135.00
           0.804
                   0.8807
                             0.3899
-130.00
           0.756
                   0.9882
                             0.3965
                   1.0861
          0.690
                             0.3994
-125.00
          0.609
                             0.3992
-120.00
                   1,1730
-115.00
           0.515
                   1.2474
                             0.3964
-110.00
           0.411
                   1.3084
                             0.3915
-105.00
           0.300
                   1.3552
                             0.3846
-100.00
           0.182
                   1.3875
                             0.3761
-95.00
          0.061
                   1.4048
                             0.3663
-90.00
          -0.061
                   1.4070
                             0.3551
-85.00
          -0.183
                   1.3941
                             0.3428
-80.00
          -0.302
                   1.3664
                             0.3295
-75.00
          -0.416
                   1.3240
                             0.3153
-70.00
          -0.523
                   1.2676
                             0.3001
-65.00
                   1.1978
                             0.2841
          -0.622
-60.00
          -0.708
                   1.1156
                             0.2672
-55.00
          -0.781
                   1.0220
                             0.2494
-50.00
          -0.838
                   0.9187
                             0.2308
-45.00
          -0.877
                   0.8074
                             0.2113
-40.00
          -0.895
                   0.6904
                             0.1909
          -0.889
-35.00
                   0.5703
                             0.1696
-30.00
          -0.858
                   0.4503
                             0.1475
-25.00
          -0.832
                   0.3357
                             0.1224
-24.00
          -0.852
                   0.3147
                             0.1156
-23.00
          -0.882
                   0.2946
                             0.1081
-22.00
          -0.919
                   0.2752
                             0.1000
-21.00
          -0.963
                   0.2566
                             0.0914
-20.00
          -1.013
                   0.2388
                             0.0823
                             0.0728
-19.00
          -1.067
                   0.2218
-18.00
          -1.125
                   0.2056
                             0.0631
-17.00
          -1.185
                   0.1901
                             0.0531
                   0.1754
                             0.0430
-16.00
          -1.245
-15.25
          -1.290
                   0.1649
                             0.0353
-14.24
          -1.229
                   0.1461
                             0.0240
-13.24
          -1.148
                   0.1263
                             0.0100
-12.22
          -1.052
                   0.1051
                            -0.0090
                            -0.0230
-11.22
         -0.965
                   0.0886
          -0.867
                   0.0740
                            -0.0336
-10.19
 -9.70
          -0.822
                   0.0684
                            -0.0375
 -9.18
          -0.769
                   0.0605
                            -0.0440
          -0.756
                   0.0270
                            -0.0578
 -8.18
 -7.19
          -0.690
                   0.0180
                            -0.0590
 -6.65
          -0.616
                   0.0166
                            -0.0633
 -6.13
          -0.542
                   0.0152
                            -0.0674
 -6.00
          -0.525
                   0.0117
                            -0.0732
                            -0.0766
 -5.50
          -0.451
                   0.0105
                   0.0097
                            -0.0797
 -5.00
          -0.382
 -4.50
          -0.314
                   0.0092
                            -0.0825
 -4.00
          -0.251
                   0.0091
                            -0.0853
 -3.50
          -0.189
                   0.0089
                            -0.0884
 -3.00
          -0.120
                   0.0089
                            -0.0914
 -2.50
          -0.051
                   0.0088
                            -0.0942
 -2.00
          0.017
                   0.0088
                            -0.0969
 -1.50
          0.085
                   0.0088
                            -0.0994
 -1.00
          0.152
                   0.0088
                            -0.1018
 -0.50
          0.219
                   0.0088
                            -0.1041
           0.288
                   0.0087
                            -0.1062
  0.00
  0.50
           0.354
                   0.0087
                            -0.1086
  1.00
           0.421
                   0.0088
                            -0.1107
  1.50
           0.487
                   0.0089
                            -0.1129
  2.00
           0.554
                   0.0090
                            -0.1149
  2.50
          0.619
                   0.0091
                            -0.1168
                   0.0092
  3.00
          0.685
                            -0.1185
  3.50
           0.749
                   0.0093
                            -0.1201
  4.00
           0.815
                   0.0095
                            -0.1218
                   0.0096
  4.50
           0.879
                            -0.1233
  5.00
           0.944
                   0.0097
                            -0.1248
  5.50
           1.008
                   0.0099
                            -0.1260
  6.00
           1.072
                   0.0101
                            -0.1270
  6.50
           1.135
                   0.0103
                            -0.1280
```

```
1.197
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                           -0.1287
  7.50
          1.256
                  0.0112
                           -0.1289
          1.305
                  0.0125
          1.390
                  0.0155
  9.50
          1.424
                  0.0171
                           -0.1158
 10.00
          1.458
                  0.0192
                           -0.1116
 10.50
          1.488
                  0.0219
                           -0.1073
11.00
          1.512
                  0.0255
                           -0.1029
                  0.0307
                           -0.0983
 11.50
          1.533
12.00
          1.549
                  0.0370
                           -0.0949
          1.558
                  0.0452
                           -0.0921
 12.50
          1.470
 13.00
                  0.0630
                           -0.0899
 13.50
          1.398
                  0.0784
                           -0.0885
 14.00
          1.354
                  0.0931
                           -0.0885
14.50
          1.336
                  0.1081
                           -0.0902
15.00
          1.333
                  0.1239
                           -0.0928
15.50
          1.326
                  0.1415
                           -0.0963
 16.00
          1.329
                  0.1592
                           -0.1006
 16.50
          1.326
                  0.1743
                           -0.1042
                  0.1903
 17.00
          1.321
                           -0.1084
 17.50
          1.331
                  0.2044
 18.00
          1.333
                  0.2186
                           -0.1169
 18.50
          1.340
                  0.2324
                           -0.1215
19.00
          1.362
                  0.2455
                           -0.1263
 19.50
          1.382
                  0.2584
                           -0.1313
 20.00
          1.398
                  0.2689
                           -0.1352
                  0.2814
 20.50
          1.426
                           -0.1406
 21.00
          1.437
                  0.2943
                           -0.1462
                  0.3246
 23.00
          1.397
                  0.3557
                           -0.1570
 24.00
          1.376
                  0.3875
                           -0.1623
 25.00
          1.354
                  0.4198
                           -0.1676
 26.00
          1.332
                  0.4524
                           -0.1728
 28.00
          1.293
                  0.5183
                           -0.1832
 30.00
          1.265
                  0.5843
                           -0.1935
 32.00
          1.253
                  0.6492
                           -0.2039
 35.00
          1.264
                  0.7438
                           -0.2193
 40.00
          1.258
                  0.8970
                           -0.2440
 45.00
          1.217
                  1.0402
                           -0.2672
 50.00
          1.146
                  1.1686
                           -0.2891
 55.00
          1.049
                  1.2779
                           -0.3097
 60.00
          0.932
                  1.3647
                           -0.3290
          0.799
                  1.4267
 65.00
                           -0.3471
 70.00
          0.657
                  1.4621
                           -0.3641
 75.00
          0.509
                  1.4708
                           -0.3799
          0.362
                  1.4544
                           -0.3946
 80.00
 85.00
          0.221
                  1.4196
                           -0.4081
90.00
          0.092
                  1.3938
                           -0.4204
95.00
         -0.030
                  1.3943
                           -0.4313
                  1.3798
100.00
         -0.150
                           -0.4408
                           -0.4486
105.00
         -0.267
                  1.3504
110.00
         -0.379
                  1.3063
                           -0.4546
115.00
         -0.483
                  1.2481
                           -0.4584
120.00
         -0.578
                  1.1763
                           -0.4597
125.00
                  1.0919
                           -0.4582
         -0.660
130.00
         -0.727
                  0.9962
                           -0.4532
135.00
         -0.777
                  0.8906
                           -0.4441
140.00
         -0.807
                  0.7771
                           -0.4303
145.00
         -0.815
                  0.6581
                           -0.4109
150.00
         -0.797
                  0.5364
                           -0.3848
                  0.4157
155.00
         -0.750
                           -0.3508
160.00
         -0.673
                  0.3000
                           -0.3074
170.00
                  0.1051
         -0.547
175.00
         -0.274
                  0.0388
                           -0.1380
180.00
          0.000
                  0.0267
                            0.0000
```

# B.7 Airfoil-Data Input File – DU25\_A17.dat

```
DU25 airfoil with an aspect ratio of 17. Original -180 to 180deg Cl, Cd, and Cm versus AOA data taken from Appendix A of DOW
Cl and Cd values corrected for rotational stall delay and Cd values corrected using the Viterna method for 0 to 90deg AOA by
            Number of airfoil tables in this file
  0.0
            Table ID parameter
  8.50
            Stall angle (deg)
  0.0
            No longer used, enter zero
  9.9
            No longer used, enter zero
  0.0
           No longer used, enter zero
Zero Cn angle of attack (deg)
  -4.2422
  6.4462
            Cn slope for zero lift (dimensionless)
  1.4336
            Cn extrapolated to value at positive stall angle of attack
  -0.6873
            Cn at stall value for negative angle of attack
  0.00
            Angle of attack for minimum CD (deg)
  0.0065
           Minimum CD value
```

```
-180.00
           0.000
                   0.0202
                             0.0000
-175.00
           0.368
                   0.0324
                             0.1845
-170.00
           0.735
                   0.0943
                             0.3701
-160.00
           0.695
                   0.2848
                             0.2679
-155.00
           0.777
                   0.4001
                             0.3046
-150.00
          0.828
                   0.5215
                             0.3329
-145.00
          0.850
                   0.6447
                             0.3540
                   9.7669
-140.00
          0.846
                             0.3693
-135.00
          0.818
                   0.8823
                             0.3794
-130.00
          0.771
                   0.9911
                             0.3854
-125.00
          0.705
                   1.0905
                             0.3878
-120.00
           0.624
                   1.1787
                             0.3872
-115.00
          0.530
                   1.2545
                             0.3841
-110.00
          0.426
                   1.3168
                             0.3788
-105.00
          0.314
                   1.3650
                             0.3716
-100.00
          0.195
                   1.3984
                             0.3629
                   1.4169
          0.073
                             0.3529
-95.00
-90.00
          -0.050
                   1,4201
                             0.3416
-85.00
          -0.173
                   1.4081
                             0.3292
-80.00
          -0.294
                   1.3811
                             0.3159
-75.00
          -0.409
                   1.3394
                             0.3017
-70.00
          -0.518
                   1.2833
                             0.2866
-65.00
          -0.617
                   1.2138
                             0.2707
-60.00
          -0.706
                   1.1315
                             0.2539
-55.00
          -0.780
                   1.0378
                             0.2364
-50.00
          -0.839
                   0.9341
                             0.2181
-45.00
                   0.8221
          -0.879
                             0.1991
                   0.7042
-40.00
          -0.898
                             0.1792
-35.00
          -0.893
                   0.5829
                             0.1587
-30.00
          -0.862
                   0.4616
                             0.1374
-25.00
          -0.803
                   0.3441
                             0.1154
-24.00
          -0.792
                   0.3209
                             0.1101
-23.00
          -0.789
                   0.2972
                             0.1031
-22.00
          -0.792
                   0.2730
                             0.0947
          -0.801
                   0.2485
                             0.0849
-21.00
-20.00
          -0.815
                   0.2237
                             0.0739
-19.00
          -0.833
                   0.1990
                             0.0618
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                   0.1743
                             0.0488
-17.00
          -0.879
                   0.1498
                             0.0351
-16.00
          -0.905
                   0.1256
                             0.0208
-15.00
          -0.932
                   0.1020
                            0.0060
                   0.0789
                            -0.0091
-14.00
          -0.959
-13.00
          -0.985
                   0.0567
                            -0.0243
-13.00
          -0.985
                   0.0567
                            -0.0243
-12.01
          -0.953
                   0.0271
                            -0.0349
          -0.900
                   0.0303
                            -0.0361
-11.00
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          -0.827
                   0.0287
                            -0.0464
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          -0.753
                   0.0271
                            -0.0534
 -8.47
          -0.691
                   0.0264
                            -0.0650
                            -0.0782
 -7.45
          -0.555
                   0.0114
                   0.0094
                            -0.0904
 -6.42
         -0.413
          -0.271
                   0.0086
                            -0.1006
 -5.40
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          -0.220
                   0.0073
                            -0.1107
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                   0.0071
                            -0.1135
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                   0.0070
                            -0.1162
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                   0.0069
                            -0.1186
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                   0.0068
                            -0.1209
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                   0.0068
                            -0.1231
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                   0.0068
                            -0.1252
                   0.0067
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          0.247
                            -0.1272
                   0.0067
 -1.00
          0.312
                            -0.1293
          0.377
 -0.50
                   0.0067
                            -0.1311
  0.00
           0.444
                   0.0065
                            -0.1330
  0.50
          0.508
                   0.0065
                            -0.1347
  1.00
          0.573
                   0.0066
                            -0.1364
  1.50
          0.636
                   0.0067
                            -0.1380
  2.00
          0.701
                   0.0068
                            -0.1396
  2.50
          0.765
                   0.0069
                            -0.1411
  3.00
          0.827
                   0.0070
                            -0.1424
  3.50
          0.890
                   0.0071
                            -0.1437
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                   0.0073
                            -0.1448
  4.50
          1.013
                   0.0076
                            -0.1456
  5.00
           1.062
                   0.0079
                            -0.1445
  6.00
          1.161
                   0.0099
                            -0.1419
  6.50
          1.208
                   0.0117
                            -0.1403
  7.00
          1.254
                   0.0132
                            -0.1382
                   0.0143
  7.50
          1.301
                            -0.1362
  8.00
          1.336
                   0.0153
                            -0.1320
  8.50
           1.369
                   0.0165
                            -0.1276
  9.00
           1.400
                   0.0181
                            -0.1234
  9.50
           1.428
                   0.0211
                            -0.1193
 10.00
           1.442
                   0.0262
                            -0.1152
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                            -0.1115
 11.00
           1.374
                   0.0420
                            -0.1081
```

```
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                          -0.1026
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                  0.0693
 13.00
          1.246
                  0.0785
                          -0.0980
 13.50
          1.247
                  0.0888
                          -0.0969
14.00
          1.256
                  0.1000
                          -0.0968
14.50
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                  0.1108
                          -0.0973
15.00
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                  0.1219
                          -0.0981
          1.281
                          -0.0992
 15.50
                  0.1325
16.00
          1.289
                  0.1433
                          -0.1006
 16.50
          1.294
                  0.1541
                          -0.1023
 17.00
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                          -0.1042
 17.50
          1.309
                  0.1754
                          -0.1064
 18.00
          1.315
                  0.1845
                          -0.1082
18.50
          1.320
                  0.1953
                          -0.1110
19.00
         1.330
                  0.2061
                          -0.1143
19.50
          1.343
                  0.2170
                          -0.1179
 20.00
          1.354
                  0.2280
                          -0.1219
 20.50
          1.359
                  0.2390
                          -0.1261
 21.00
          1.360
                  0.2536
                          -0.1303
 22.00
          1.325
                  0.2814
                          -0.1375
 23.00
          1.288
                  0.3098
                          -0.1446
 24.00
          1.251
                  0.3386
                          -0.1515
 25.00
          1.215
                  0.3678
                          -0.1584
 26.00
          1.181
                  0.3972 -0.1651
 28.00
                  0.4563
                          -0.1781
         1.120
                  0.5149
 30.00
          1.076
                          -0.1904
 32.00
          1.056
                  0.5720
                          -0.2017
                  0.6548
          1.066
 40.00
          1.064
                  0.7901
                          -0.2418
 45.00
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                  0.9190
                          -0.2650
 50.00
          0.980
                  1.0378
                          -0.2867
 55.00
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                  1.1434
                          -0.3072
 60.00
          0.810
                  1.2333
                          -0.3265
          0.702
65.00
                  1.3055
                          -0.3446
 70.00
          0.582
                  1.3587
                          -0.3616
 75.00
          0.456
                  1.3922
                          -0.3775
 80.00
          0.326
                  1.4063
 85.00
          0.197
                  1.4042
                          -0.4057
90.00
          0.072
                  1.3985
                          -0.4180
95.00
         -0.050
                  1.3973
                          -0.4289
100.00
         -0.170
                  1.3810
                          -0.4385
105.00
         -0.287
                  1.3498
                          -0.4464
110.00
         -0.399
                  1.3041
                          -0.4524
115.00
         -0.502
                  1.2442
                          -0.4563
         -0.596
                  1.1709
120.00
125.00
         -0.677
                  1.0852
                          -0.4563
130.00
         -0.743
                  0.9883
                          -0.4514
135.00
         -0.792
                  0.8818
                          -0.4425
140.00
         -0.821
                  0.7676 -0.4288
145.00
         -0.826
                  0.6481 -0.4095
                  0.5264
150.00
         -0.806
                          -0.3836
155.00
         -0.758
                  0.4060
                          -0.3497
160.00
         -0.679
                  0.2912
                          -0.3065
170.00
         -0.735
                  0.0995
                          -0.3706
175.00
         -0.368
                  0.0356
                          -0.1846
180.00
         0.000
                  0.0202
                           0.0000
```

### B.8 Airfoil-Data Input File - DU21\_A17.dat

```
DU21 airfoil with an aspect ratio of 17. Original -180 to 180deg Cl, Cd, and Cm versus AOA data taken from Appendix A of DOW
Cl and Cd values corrected for rotational stall delay and Cd values corrected using the Viterna method for 0 to 90deg AOA by
            Number of airfoil tables in this file
   0.0
            Table ID parameter
   8.00
            Stall angle (deg)
  0.0
            No longer used, enter zero
            No longer used, enter zero
No longer used, enter zero
  0.0
  0.0
            Zero Cn angle of attack (deg)
 -5.0609
  6.2047
            Cn slope for zero lift (dimensionless)
  1.4144
            Cn extrapolated to value at positive stall angle of attack
 -0.5324
            Cn at stall value for negative angle of attack
 -1.50
            Angle of attack for minimum CD (deg)
            Minimum CD value
  0.0057
-180.00
           0.000
                   0.0185
                            0.0000
           0.394
                            0.1978
-175.00
                   0.0332
-170.00
           0.788
                   0.0945
                             0.3963
-160.00
           0.670
                   0.2809
                             0.2738
-155.00
           0.749
                   0.3932
                             0.3118
-150.00
           0.797
                   0.5112
                             0.3413
-145.00
           0.818
                   0.6309
                             0.3636
-140.00
           0.813
                   0.7485
                             0.3799
```

```
-135.00
           0.786
                   0.8612
                             0.3911
-130.00
           0.739
                   0.9665
                             0.3980
-125.00
           0.675
                   1.0625
                             0.4012
-120.00
           0.596
                   1.1476
                             0.4014
-115.00
          0.505
                   1.2206
                             0.3990
-110.00
          0.403
                   1.2805
                             0.3943
-105.00
          0.294
                   1.3265
                             0.3878
-100.00
          0.179
                   1.3582
                             0.3796
-95.00
          0.060
                   1.3752
                             0.3700
          -0.060
-90.00
                   1.3774
                             0.3591
-85.00
          -0.179
                   1.3648
                             0.3471
-80.00
          -0.295
                   1.3376
                             0.3340
-75.00
          -0.407
                   1.2962
                             0.3199
-70.00
          -0.512
                   1.2409
                             0.3049
-65.00
          -0.608
                   1.1725
                             0.2890
          -0.693
-60.00
                   1.0919
                             0.2722
                   1.0002
                             0.2545
-55.00
          -0.764
-50.00
          -0.820
                   0.8990
                             0.2359
-45.00
          -0.857
                   0.7900
                             0.2163
-40.00
                   0.6754
          -0.875
                             0.1958
-35.00
          -0.869
                   0.5579
                             0.1744
-30.00
          -0.838
                   0.4405
                             0.1520
-25.00
          -0.791
                   0.3256
                             0.1262
-24.00
          -0.794
                   0.3013
                             0.1170
-23.00
          -0.805
                   0.2762
                             0.1059
-22.00
          -0.821
                   0.2506
                             0.0931
                   0.2246
                             0.0788
-21.00
          -0.843
-20.00
          -0.869
                   0.1983
                             0.0631
-19.00
          -0.899
                   0.1720
                             0.0464
-18.00
          -0.931
                   0.1457
                             0.0286
-17.00
          -0.964
                   0.1197
                             0.0102
-16.00
          -0.999
                   0.0940
                            -0.0088
-15.00
          -1.033
                   0.0689
                            -0.0281
-14.50
          -1.050
                   0.0567
                            -0.0378
-12.01
          -0.953
                            -0.0349
                   0.0271
-11.00
          -0.900
                   0.0303
                            -0.0361
 -9.98
          -0.827
                   0.0287
                            -0.0464
 -8.12
          -0.536
                   0.0124
                            -0.0821
 -7.62
          -0.467
                   0.0109
                            -0.0924
 -7.11
          -0.393
                   0.0092
                            -0.1015
 -6.60
          -0.323
                   0.0083
                            -0.1073
 -6.50
          -0.311
                   0.0089
                            -0.1083
                   0.0082
                            -0.1112
 -6.00
          -0.245
 -5.50
          -0.178
                   0.0074
                            -0.1146
 -5.00
          -0.113
                   0.0069
                            -0.1172
 -4.50
          -0.048
                   0.0065
                            -0.1194
 -4.00
          0.016
                   0.0063
                            -0.1213
 -3.50
          0.080
                   0.0061
                            -0.1232
 -3.00
          0.145
                   0.0058
                            -0.1252
 -2.50
          0.208
                   0.0057
                            -0.1268
                   0.0057
 -2.00
          0.270
                            -0.1282
                   0.0057
 -1.50
          0.333
                            -0.1297
          0.396
                   0.0057
                            -0.1310
 -1.00
 -0.50
          0.458
                   0.0057
                            -0.1324
  0.00
          0.521
                   0.0057
                            -0.1337
  0.50
          0.583
                   0.0057
                            -0.1350
  1.00
          0.645
                   0.0058
                            -0.1363
  1.50
          0.706
                   0.0058
                            -0.1374
  2.00
          0.768
                   0.0059
                            -0.1385
          0.828
                   0.0061
  2.50
                            -0.1395
          0.888
                   0.0063
  3.00
                            -0.1403
  3.50
          0.948
                   0.0066
                            -0.1406
          0.996
                   0.0071
                            -0.1398
  4.50
          1.046
                   0.0079
                            -0.1390
  5.00
          1.095
                   0.0090
                            -0.1378
  5.50
          1.145
                   0.0103
                            -0.1369
  6.00
          1.192
                   0.0113
                            -0.1353
  6.50
          1.239
                   0.0122
                            -0.1338
          1.283
  7.00
                   0.0131
                            -0.1317
  7.50
          1.324
                   0.0139
                            -0.1291
  8.00
          1.358
                   0.0147
                            -0.1249
  8.50
          1.385
                   0.0158
                            -0.1213
  9.00
           1.403
                   0.0181
                            -0.1177
  9.50
          1.401
                   0.0211
                            -0.1142
 10.00
          1.358
                   0.0255
                            -0.1103
 10.50
          1.313
                   0.0301
                            -0.1066
          1.287
                   0.0347
                            -0.1032
 11.00
 11.50
          1,274
                   0.0401
                            -0.1002
 12.00
           1.272
                   0.0468
                            -0.0971
 12.50
           1.273
                   0.0545
                            -0.0940
 13.00
           1.273
                   0.0633
                            -0.0909
 13.50
           1.273
                   0.0722
                            -0.0883
 14.00
           1.272
                   0.0806
                            -0.0865
                   0.0900
 14.50
           1.273
                            -0.0854
```

```
15.00
          1.275
                  0.0987
                           -0.0849
 15.50
          1.281
                  0.1075
                           -0.0847
          1.284
                  0.1170
 16.50
          1.296
                  0.1270
                           -0.0858
 17.00
          1.306
                  0.1368
                           -0.0869
17.50
          1.308
                  0.1464
                           -0.0883
18.00
          1.308
                  0.1562
                           -0.0901
18.50
          1.308
                  0.1664
                           -0.0922
 19.00
          1.308
                  0.1770
                           -0.0949
                           -0.0980
19.50
          1.307
                  0.1878
 20.00
          1.311
                  0.1987
                           -0.1017
                  0.2100
          1.325
 21.00
          1.324
                  0.2214
                           -0.1105
 22.00
          1.277
                  0.2499
                           -0.1172
 23.00
          1.229
                  0.2786
                           -0.1239
                  0.3077
 24.00
          1.182
                           -0.1305
                  0.3371 -0.1370
 25.00
          1.136
                  0.3664
 26.00
          1.093
                           -0.1433
 28.00
          1.017
                  0.4246
                           -0.1556
          0.962
                  0.4813
 30.00
                           -0.1671
 32.00
          0.937
                  0.5356
                           -0.1778
 35.00
          0.947
                  0.6127
                           -0.1923
 40.00
          0.950
                  0.7396
                          -0.2154
 45.00
          0.928
                  0.8623 -0.2374
 50.00
          0.884
                  0.9781 -0.2583
 55.00
          0.821
                  1.0846
                           -0.2782
          0.740
                  1.1796
 60.00
                           -0.2971
 65.00
          0.646
                  1.2617
                           -0.3149
 70.00
          0.540
                  1.3297
 75.00
          0.425
                  1.3827
                           -0.3476
80.00
          0.304
                  1.4202
                           -0.3625
 85.00
          0.179
                  1.4423
                           -0.3763
90.00
          0.053
                  1.4512
                           -0.3890
95.00
         -0.073
                  1.4480
                           -0.4004
         -0.198
                  1.4294
100.00
                           -0.4105
105.00
         -0.319
                  1.3954
                           -0.4191
110.00
         -0.434
                  1.3464
                          -0.4260
                           -0.4308
115.00
         -0.541
                  1.2829
120.00
         -0.637
                  1.2057
                           -0.4333
125.00
         -0.720
                  1.1157
                           -0.4330
130.00
         -0.787
                  1.0144
                          -0.4294
                  0.9033 -0.4219
135.00
         -0.836
140.00
         -0.864
                  0.7845
                           -0.4098
145.00
         -0.869
                  0.6605
                           -0.3922
150.00
         -0.847
                  0.5346
                           -0.3682
         -0.795
                  0.4103
160.00
         -0.711
                  0.2922
                           -0.2954
170.00
         -0.788
                  0.0969
                           -0.3966
175.00
         -0.394
                  0.0334
                           -0.1978
          9.999
180.00
                  0.0185
                           9.9999
```

#### B.9 Airfoil-Data Input File - NACA64 A17.dat

```
NACA64 airfoil with an aspect ratio of 17. Original -180 to 180deg Cl, Cd, and Cm versus AOA data taken from Appendix A of D
Cl and Cd values corrected for rotational stall delay and Cd values corrected using the Viterna method for 0 to 90deg AOA by
            Number of airfoil tables in this file
   9.9
            Table ID parameter
   9.00
            Stall angle (deg)
   0.0
            No longer used, enter zero
No longer used, enter zero
  0.0
            No longer used, enter zero
  -4.4320
            Zero Cn angle of attack (deg)
  6.0031
            Cn slope for zero lift (dimensionless)
  1.4073
            Cn extrapolated to value at positive stall angle of attack
 -0.7945
            Cn at stall value for negative angle of attack
 -1.00
            Angle of attack for minimum CD (deg)
  0.0052
            Minimum CD value
180.00
           0.000
                   0.0198
                            0.0000
-175.00
           0.374
                   0.0341
                            0.1880
-170.00
           0.749
                   0.0955
                             0.3770
-160.00
           0.659
                   0.2807
                             0.2747
-155.00
           0.736
                   0.3919
                             0.3130
-150.00
           0.783
                   0.5086
                             0.3428
-145.00
           0.803
                   0.6267
                             0.3654
-140.00
           0.798
                   0.7427
                             0.3820
           0.771
-135.00
                   0.8537
                             0.3935
-130.00
           0.724
                   0.9574
                             0.4007
-125.00
           0.660
                   1.0519
                             0.4042
                             0.4047
-120.00
           0.581
                   1.1355
-115.00
           0.491
                   1.2070
                             0.4025
-110.00
           0.390
                   1.2656
                             0.3981
-105.00
           0.282
                   1.3104
                             0.3918
```

```
100.00
          0.169
                  1.3410
                            0.3838
-95.00
          0.052
                  1.3572
                            0.3743
-90.00
          -0.067
                  1.3587
                            0.3636
-85.00
         -0.184
                  1.3456
                            0.3517
-80.00
         -0.299
                   1.3181
                            0.3388
-75.00
         -0.409
                  1.2765
                            0.3248
-70.00
         -0.512
                  1.2212
                            0.3099
-65.00
         -0.606
                  1.1532
                            0.2940
-60.00
         -0.689
                  1.0731
                            0.2772
         -0.759
-55.00
                  0.9822
                            0.2595
-50.00
         -0.814
                  0.8820
                            0.2409
-45.00
         -0.850
                   0.7742
                            0.2212
-40.00
         -0.866
                   0.6610
                            0.2006
-35.00
         -0.860
                  0.5451
                            0.1789
-30.00
         -0.829
                  0.4295
                            0.1563
-25.00
         -0.853
                  0.3071
                            0.1156
                            0.1040
-24.00
         -0.870
                  0.2814
-23.00
         -0.890
                  0.2556
                            0.0916
-22.00
         -0.911
                  0.2297
                            0.0785
         -0.934
                   0.2040
                            0.0649
-21.00
-20.00
         -0.958
                  0.1785
                            0.0508
-19.00
         -0.982
                  0.1534
                            0.0364
-18.00
         -1.005
                  0.1288
                            0.0218
-17.00
         -1.082
                  0.1037
                            0.0129
-16.00
         -1.113
                  0.0786
                           -0.0028
-15.00
         -1.105
                  0.0535
                           -0.0251
         -1.078
                  0.0283
-14.00
                           -0.0419
-13.50
         -1.053
                   0.0158
                           -0.0521
-13.00
         -1.015
                   0.0151
                           -0.0610
-12.00
         -0.904
                  0.0134
                           -0.0707
-11.00
         -0.807
                  0.0121
                           -0.0722
-10.00
         -0.711
                  0.0111
                           -0.0734
-9.00
         -0.595
                  0.0099
                           -0.0772
                           -0.0807
-8.00
         -0.478
                  0.0091
         -0.375
                  0.0086
                           -0.0825
 -7.00
 -6.00
         -0.264
                  0.0082
                           -0.0832
 -5.00
         -0.151
                  0.0079
                           -0.0841
 -4.00
         -0.017
                   0.0072
                           -0.0869
 -3.00
          0.088
                  0.0064
                           -0.0912
 -2.00
          0.213
                   0.0054
                           -0.0946
 -1.00
          0.328
                  0.0052
                           -0.0971
  9.99
          9.442
                  0.0052
                           -0.1014
          0.556
                  0.0052
  1.00
                           -0.1076
  2.00
          0.670
                  0.0053
                           -0.1126
  3.00
          0.784
                  0.0053
                           -0.1157
          0.898
                   0.0054
                           -0.1199
  4.00
  5.00
          1.011
                   0.0058
                           -0.1240
  6.00
          1.103
                   0.0091
                           -0.1234
  7.00
          1.181
                  0.0113
                           -0.1184
  8.00
          1.257
                  0.0124
                           -0.1163
  8.50
          1.293
                  0.0130
                           -0.1163
  9.00
          1.326
                  0.0136
                           -0.1160
          1.356
  9.50
                  0.0143
                           -0.1154
 10.00
          1.382
                   0.0150
                           -0.1149
 10.50
          1.400
                   0.0267
                           -0.1145
11.00
          1.415
                   0.0383
                           -0.1143
11.50
          1.425
                  0.0498
                           -0.1147
12.00
          1.434
                  0.0613
                           -0.1158
12.50
          1.443
                  0.0727
                           -0.1165
          1.451
                  0.0841
13.00
                           -0.1153
                  0.0954
13.50
          1.453
                           -0.1131
14.00
          1.448
                  0.1065
                           -0.1112
 14.50
          1.444
                   0.1176
                           -0.1101
15.00
          1.445
                  0.1287
                           -0.1103
15.50
          1.447
                  0.1398
                           -0.1109
16.00
          1.448
                  0.1509
                           -0.1114
16.50
          1.444
                  0.1619
                           -0.1111
17.00
          1.438
                  0.1728
                           -0.1097
17.50
          1.439
                  0.1837
                           -0.1079
18.00
          1.448
                  0.1947
                           -0.1080
 18.50
          1.452
                   0.2057
                           -0.1090
 19.00
          1.448
                  0.2165
                           -0.1086
 19.50
          1.438
                  0.2272
                           -0.1077
20.00
          1.428
                  0.2379
                           -0.1099
 21.00
          1.401
                  0.2590
                           -0.1169
 22.00
          1.359
                  0.2799
                           -0.1190
          1.300
                  0.3004
 23.00
                           -0.1235
 24.00
          1,220
                  0.3204
                           -0.1393
 25.00
          1.168
                  0.3377
                           -0.1440
 26.00
          1.116
                   0.3554
                           -0.1486
 28.00
          1.015
                   0.3916
                           -0.1577
 30.00
          0.926
                   0.4294
                           -0.1668
 32.00
          0.855
                  0.4690
                           -0.1759
 35.00
          0.800
                  0.5324
                           -0.1897
```

```
40.00
            0.804
                     0.6452 -0.2126
 45.00
            0.793
                     0.7573
                               -0.2344
 50.00
            0.763
                     0.8664
                              -0.2553
 55.00
            0.717
                     0.9708
                               -0.2751
 60.00
            0.656
                     1.0693
                               -0.2939
 65.00
           0.582
                     1.1606
                               -0.3117
           0.495
0.398
0.291
                              -0.3285
-0.3444
-0.3593
 70.00
75.00
                     1.2438
                     1.3178
 80.00
                     1.3809
 85.00
           0.176
                     1.4304
                              -0.3731
 90.00
           0.053
                     1.4565
                               -0.3858
 95.00
           -0.074
                     1.4533
                               -0.3973
100.00
          -0.199
                     1.4345
                               -0.4075
                     1.4004
105.00
          -0.321
                               -0.4162
          -0.321
-0.436
-0.543
-0.640
-0.723
-0.790
                              -0.4231
-0.4280
-0.4306
-0.4304
110.00
                     1.3512
                     1.2874
115.00
                     1.2099
1.1196
1.0179
120.00
125.00
130.00
                               -0.4270
135.00
          -0.840
                     0.9064
                               -0.4196
140.00
          -0.868
                     0.7871
                               -0.4077
145.00
          -0.872
                     0.6627
                               -0.3903
150.00
          -0.850
                     0.5363
                              -0.3665
155.00
160.00
170.00
          -0.798
                     0.4116
                              -0.3349
          -0.714
-0.749
                              -0.2942
-0.3771
                     0.2931
                     0.0971
175.00
          -0.374
                     0.0334
                               -0.1879
180.00
           0.000
                     0.0198
                                0.0000
```

# Appendix C Source Code for the Control System DLL

```
|-----
SUBROUTINE DISCON ( avrSWAP, aviFAIL, accINFILE, avcOUTNAME, avcMSG )
!DEC$ ATTRIBUTES DLLEXPORT, ALIAS: 'DISCON' :: DISCON
   ! This Bladed-style DLL controller is used to implement a variable-speed
     generator-torque controller and PI collective blade pitch controller for
   ! the NREL Offshore 5MW baseline wind turbine. This routine was written by ! J. Jonkman of NREL/NWTC for use in the IEA Annex XXIII OC3 studies.
IMPLICIT
                                  NONE
   | Passed Variables:
REAL(4),
            INTENT(INOUT)
                              :: avrSWAP
                                            (*)
                                                                                    ! The swap array, used to pass data to, and r
INTEGER(4), INTENT( OUT)
                                                                                    ! A flag used to indicate the success of this
                              :: aviFAIL
INTEGER(1), INTENT(IN
                              :: accINFILE (*)
                                                                                    ! The address of the first record of an array
INTEGER(1), INTENT( OUT)
INTEGER(1), INTENT(IN )
                               :: avcMSG
                                                                                    ! The address of the first record of an array
                              :: avcOUTNAME(*)
                                                                                    ! The address of the first record of an array
   ! Local Variables:
REAL(4)
                              :: Alpha
                                                                                    ! Current coefficient in the recursive, singl
                                                                                      Current values of the blade pitch angles, r
REAL(4)
                               :: BlPitch
REAL(4)
                               :: ElapTime
                                                                                      Elapsed time since the last call to the con
REAL(4), PARAMETER
                               :: CornerFreq
                                                         1.570796
                                                                                      Corner frequency (-3dB point) in the recurs
REAL(4)
                               :: GenSpeed
                                                                                      Current HSS (generator) speed, rad/s.
REAL(4), SAVE
                              :: GenSpeedF
                                                                                      Filtered HSS (generator) speed, rad/s.
REAL(4)
                              :: GenTrq
                                                                                      Electrical generator torque, N-m.
                                                                                      Current value of the gain correction factor
REAL(4)
                              :: GK
                                                                                      Horizontal hub-heigh wind speed, m/s.
REAL(4)
                              :: HorWindV
REAL(4), SAVE
                              :: IntSpdErr
                                                                                      Current integral of speed error w.r.t. time
REAL(4), SAVE
                                                                                      Commanded electrical generator torque the 1
                              :: LastGenTrq
REAL(4), SAVE
                                                                                      Last time this DLL was called, sec.
                              :: LastTime
REAL(4), SAVE
                              :: LastTimePC
                                                                                      Last time the pitch controller was called,
                              :: LastTimeVS
REAL(4), SAVE
                                                                                      Last time the torque controller was called,
REAL(4), PARAMETER
                                                = 1.0 + EPSILON(OnePlusEps)
                                                                                      The number slighty greater than unity in si
Communication interval for pitch controlle
                              :: OnePlusEps
REAL(4), PARAMETER
                              :: PC DT
                                                         0.00125
REAL(4), PARAMETER
REAL(4), PARAMETER
                              :: PC_KI
                                                         0.008068634
                                                                                      Integral gain for pitch controller at rated
                                                         0.1099965
                                                                                      Pitch angle were the the derivative of the
REAL(4), PARAMETER
                                                         0.01882681
                                                                                      Proportional gain for pitch controller at r
                              :: PC_KP
REAL(4), PARAMETER
                               :: PC_MaxPit
                                                         1.570796
                                                                                      Maximum pitch setting in pitch controller,
REAL(4), PARAMETER
                               :: PC_MaxRat
                                                         0.1396263
                                                                                      Maximum pitch rate (in absolute value) in
REAL(4), PARAMETER
                              :: PC_MinPit
:: PC_RefSpd
                                                         9.9
                                                                                      Minimum pitch setting in pitch controller,
REAL(4), PARAMETER
                                                       122,9096
                                                                                      Desired (reference) \mbox{HSS} speed for pitch con
                               :: PitCom
REAL(4), SAVE
                                            (3)
                                                                                      Commanded pitch of each blade the last time
                                                                                      Integral term of command pitch, rad.
REAL(4)
                              :: PitComI
REAL(4)
                              :: PitComP
                                                                                      Proportional term of command pitch, rad.
REAL(4)
                              :: PitComT
                                                                                      Total command pitch based on the sum of the
REAL(4)
                              :: PitRate
                                            (3)
                                                                                      Pitch rates of each blade based on the curr
REAL(4), PARAMETER
                               :: R2D
                                                        57.295780
                                                                                      Factor to convert radians to degrees.
REAL(4), PARAMETER
                               :: RPS2RPM
                                                         9.5492966
                                                                                      Factor to convert radians per second to rev
                                                                                      Current speed error, rad/s.
REAL(4)
                               :: SpdErr
REAL(4)
                               :: Time
                                                                                      Current simulation time, sec.
REAL(4)
                                 TraRate
                                                                                      Torque rate based on the current and last t
                              ::
                                                                                      Transitional generator speed (HSS side) bet
REAL(4), PARAMETER
                              :: VS CtInSp
                                                        70.16224
REAL(4), PARAMETER
REAL(4), PARAMETER
                                 VS DT
                                                         0.00125
                                                                                      Communication interval for torque controlle
                                 VS_MaxRat
                                                     15000.0
                                                                                      Maximum torque rate (in absolute value) in
REAL(4), PARAMETER
                                                                                      Maximum generator torque in Region 3 (HSS s
                                 VS_MaxTq
                                                     47402.91
REAL(4), PARAMETER
                                                                                      Generator torque constant in Region 2 (HSS
                                 VS_Rgn2K
                                                         2.332287
REAL(4), PARAMETER
                                 VS_Rgn2Sp
                                                        91.21091
                                                                                      Transitional generator speed (HSS side) bet
REAL(4), PARAMETER
                                                                                      Minimum pitch angle at which the torque is
                               :: VS_Rgn3MP
                                                         0.01745329
REAL(4), PARAMETER
                                                                                      Rated generator speed (HSS side), rad/s. --
                              :: VS RtGnSp
                                                       121.6805
REAL(4), PARAMETER
REAL(4), SAVE
                                                = 5296610.0
                               :: VS RtPwr
                                                                                      Rated generator generator power in Region 3
                              :: VS Slope15
                                                                                      Torque/speed slope of region 1 1/2 cut-in t
REAL(4), SAVE
REAL(4), PARAMETER
                              :: VS_Slope25
                                                                                      Torque/speed slope of region 2 1/2 inductio
                              :: VS_S1Pc
                                                        10.0
                                                                                      Rated generator slip percentage in Region 2
REAL(4), SAVE
                                                                                      Synchronous speed of region 2 1/2 induction
                               :: VS_SySp
REAL(4), SAVE
                               :: VS_TrGnSp
                                                                                    ! Transitional generator speed (HSS side) bet
INTEGER(4)
                                                                                    ! Generic index.
INTEGER(4)
                              :: iStatus
                                                                                    ! A status flag set by the simulation as foll
INTEGER(4)
                                                                                      Loops through blades.
                              :: K
                              :: NumBl
                                                                                    ! Number of blades, (-).
INTEGER(4)
```

```
INTEGER(4), PARAMETER
                             :: UnDb
                                               = 85
                                                                                   ! I/O unit for the debugging information
                                                                                   ! CHARACTER string cInFile stored as a 1-byt
INTEGER(1)
                             :: iInFile ( 256)
                              :: iMessage ( 256)
INTEGER(1)
                                                                                   ! CHARACTER string cMessage stored as a 1-byt
INTEGER(1), SAVE
                             :: iOutName (1024)
                                                                                   ! CHARACTER string cOutName stored as a 1-byt
LOGICAL(1), PARAMETER
                              :: PC_DbgOut
                                               = .FALSE.
                                                                                   ! Flag to indicate whether to output debuggin
CHARACTER( 256)
                              :: cInFile
                                                                                   ! CHARACTER string giving the name of the par
CHARACTER( 256)
                              :: cMessage
                                                                                   ! CHARACTER string giving a message that will
CHARACTER(1024), SAVE
                             :: cOutName
                                                                                   ! CHARACTER string giving the simulation run
CHARACTER( 1), PARAMETER :: Tab = CHAR( 9 ) ! The tab character.

CHARACTER( 25), PARAMETER :: FmtDat = "(F8.3,99('"//Tab//"',ES10.3E2,:))" ! The format of the debugging data
   ! Set EQUIVALENCE relationships between INTEGER(1) byte arrays and CHARACTER strings:
EQUIVALENCE (iInFile , cInFile )
EQUIVALENCE (iMessage, cMessage)
EQUIVALENCE (iOutName, cOutName)
   ! Load variables from calling program (See Appendix A of Bladed User's Guide):
iStatus
             = NINT( avrSWAP( 1) )
NumB1
             = NINT( avrSWAP(61) )
BlPitch (1) =
                     avrSWAP(4)
                     avrSWAP(33)
BlPitch (2) =
BlPitch (3) =
                      avrSWAP(34)
GenSpeed
                      avrSWAP(20)
HorWindV
             =
                      avrSWAP(27)
Time
                     avrSWAP(2)
   ! Initialize aviFAIL to 0:
aviFAIL
   ! Read any External Controller Parameters specified in the User Interface
      and initialize variables:
IF ( iStatus == 0 ) THEN ! .TRUE. if were on the first call to the DLL
   ! Convert byte arrays to CHARACTER strings, for convenience:
   DO I = 1,MIN( 256, NINT( avrSWAP(50) ) )
     iInFile (I) = accINFILE (I) ! Sets cInfile by EQUIVALENCE
   ENDDO
   DO I = 1,MIN( 1024, NINT( avrSWAP(51) ) )
      iOutName(I) = avcOUTNAME(I) ! Sets cOutName by EQUIVALENCE
   ! Inform users that we are using this user-defined routine:
   aviFAIL = 1
   ! Determine some torque control parameters not specified directly:
   VS_SYSp = VS_RtGnSp/( 1.0 + 0.01*VS_S1Pc )
VS_Slope15 = ( VS_Rgn2K*VS_Rgn2Sp*VS_Rgn2Sp )/( VS_Rgn2Sp - VS_CtInSp )
VS_Slope25 = ( VS_RtPwr/VS_RtGnSp )/( VS_RtGnSp - VS_SYSp )
   IF ( VS_Rgn2K == 0.0 ) THEN ! .TRUE. if the Region 2 torque is flat, and thus, the denominator in the ELSE condition is
      VS_TrGnSp = VS_SySp
   ELSE
                                  ! .TRUE. if the Region 2 torque is quadratic with speed
     VS\_TrGnSp = ( VS\_Slope25 - SQRT( VS\_Slope25*( VS\_Slope25 - 4.0*VS\_Rgn2K*VS\_SVSp ) ) )/( 2.0*VS\_Rgn2K )
   ENDTE
   ! Check validity of input parameters:
   IF ( CornerFreq <= 0.0 ) THEN</pre>
      aviFAIL = -1
```

```
cMessage = 'CornerFreq must be greater than zero.'
ENDIF
cMessage = 'VS_DT must be greater than zero.'
IF ( VS\_CtInSp < 0.0 ) THEN
   aviFAIL = -1
cMessage = 'VS_CtInSp must not be negative.'
\label{eq:if_constraint} \mbox{IF ( VS\_Rgn2Sp <= VS\_CtInSp ) } \mbox{ THEN}
   aviFAIL = -1
   cMessage = 'VS_Rgn2Sp must be greater than VS_CtInSp.'
IF \ (\ VS\_TrGnSp \ < \ VS\_Rgn2Sp \ ) \quad THEN
   aviFAIL = -1
   cMessage = 'VS_TrGnSp must not be less than VS_Rgn2Sp.'
IF ( VS_S1Pc  <= 0.0 ) THEN</pre>
   aviFAIL = -1
   cMessage = 'VS_S1Pc must be greater than zero.'
IF ( VS_MaxRat <= 0.0 ) THEN</pre>
   aviFAIL = -1 cMessage = 'VS_MaxRat must be greater than zero.'
IF ( VS_RtPwr < 0.0 ) THEN
  aviFAIL = -1
  cMessage = 'VS_RtPwr must not be negative.'</pre>
IF ( VS_Rgn2K < 0.0 ) THEN
   aviFAIL = -1
   cMessage = 'VS_Rgn2K must not be negative.'
\label{eq:constraint}  \mbox{IF ( VS_Rgn2K*VS_RtGnSp*VS_RtGnSp > VS_RtPwr/VS_RtGnSp ) } \mbox{ THEN } 
   aviFAIL = -1 cMessage = 'VS_Rgn2K*VS_RtGnSp^2 must not be greater than VS_RtPwr/VS_RtGnSp.'
ENDIF
IF ( VS_MaxTq
                                    < VS_RtPwr/VS_RtGnSp ) THEN
   aviFAIL = -1
   cMessage = 'VS_RtPwr/VS_RtGnSp must not be greater than VS_MaxTq.'
ENDIF
cMessage = 'PC_DT must be greater than zero.'
IF ( PC_KI \leftarrow 0.0 ) THEN aviFAIL = -1
   cMessage = 'PC_KI must be greater than zero.'
cMessage = 'PC_KK must be greater than zero.'
IF ( PC_RefSpd \leftarrow 0.0 ) THEN
   aviFAIL = -1
   cMessage = 'PC_RefSpd must be greater than zero.'
IF ( PC_MaxRat <= 0.0 ) THEN</pre>
   aviFAIL = -1
   cMessage = 'PC_MaxRat must be greater than zero.'
IF ( PC\_MinPit >= PC\_MaxPit ) THEN
   aviFAIL = -1
cMessage = 'PC_MinPit must be less than PC_MaxPit.'
```

```
! header:
     IF ( PC DbgOut ) THEN
          OPEN ( UnDb, FILE=TRIM( cOutName )//'.dbg', STATUS='REPLACE' )
          WRITE (UnDb,'(////)')
WRITE (UnDb,'(A)') 'Time '//Tab//'ElapTime'//Tab//'HorWindV'//Tab//'GenSpeed'//Tab//'GenSpeedF'//Tab//'RelSpdErr'//Tab//
WRITE (UnDb,'(A)') 'Time '//Tab//'ElapTime'//Tab//'HorWindV'//Tab//'BitComP'//Tab//'PitComI'//Tab//'PitComI'//Tab//'PitComI'//Tab//
                                               SpdErr '//Tab//'IntSpdErr'//Tab//'GK '//Tab//'PitComP'//Tab//'PitComI'//Tab//'PitComT'//Tab//
                                               'PitRate1'//Tab//'PitCom1'
                                              '(sec)'//Tab//'(sec) '//Tab//'(m/sec) '//Tab//'(rpm) '//Tab//'($'(rad/s)'//Tab//'(ad) '//Tab//'(deg) '//Tab//'(
                                                                                                                                                                                   '//Tab//'(%) '
Tab//'(deg) '//Tab//
          WRITE (UnDb, '(A)')
     ENDIF
     ! Initialize the SAVEd variables:
     ! NOTE: LastGenTrq, though SAVEd, is initialized in the torque controller
                  below for simplicity, not here.
     GenSpeedF = GenSpeed
                                                                                     ! This will ensure that generator speed filter will use the initial value of
     PitCom
                      = BlPitch
                                                                                      ! This will ensure that the variable speed controller picks the correct contr
                        = 1.0/( 1.0 + PitCom(1)/PC_KK ) ! This will ensure that the pitch angle is unchanged if the initial SpdErr is
     IntSpdErr = PitCom(1)/( GK*PC_KI )
                                                                                     ! This will ensure that the pitch angle is unchanged if the initial SpdErr is
    LastTime = Time
LastTimePC = Time - PC_DT
LastTimeVS = Time - VS_DT
                                                                                     ! This will ensure that generator speed filter will use the initial value of
                                                                                     ! This will ensure that the pitch controller is called on the first pass ! This will ensure that the torque controller is called on the first pass
ENDIF
    ! Main control calculations:
IF ( ( iStatus >= 0 ) .AND. ( aviFAIL >= 0 ) ) THEN ! Only compute control calculations if no error has occured and we are
     ! Abort if the user has not requested a pitch angle actuator (See Appendix A
          of Bladed User's Guide):
     IF ( NINT(avrSWAP(10)) /= 0 ) THEN ! .TRUE. if a pitch angle actuator hasn't been requested
          aviFAIL = -1
cMessage = 'Pitch angle actuator not requested.'
     ! Set unused outputs to zero (See Appendix A of Bladed User's Guide):
     avrSWAP(36) = 0.0 ! Shaft brake status: 0=off
     avrSWAP(41) = 0.0 ! Demanded yaw actuator torque
     avrSWAP(46) = 0.0 ! Demanded pitch rate (Collective pitch)
     avrSWAP(48) = 0.0 ! Demanded nacelle yaw rate
     avrSWAP(65) = 0.0 ! Number of variables returned for logging
     avrSWAP(72) = 0.0 ! Generator startup resistance
     avrSWAP(79) = 0.0 ! Request for loads: 0=none
     avrSWAP(80) = 0.0 ! Variable slip current status
     avrSWAP(81) = 0.0 ! Variable slip current demand
! Filter the HSS (generator) speed measurement:
     ! NOTE: This is a very simple recursive, single-pole, low-pass filter with
                  exponential smoothing.
     ! Update the coefficient in the recursive formula based on the elapsed time
          since the last call to the controller:
                      = EXP( ( LastTime - Time )*CornerFreq )
     Alpha
     ! Apply the filter:
     GenSpeedF = ( 1.0 - Alpha )*GenSpeed + Alpha*GenSpeedF
|-----
     ! Variable-speed torque control:
```

```
! Compute the elapsed time since the last call to the controller:
  ElapTime = Time - LastTimeVS
  ! Only perform the control calculations if the elapsed time is greater than
      or equal to the communication interval of the torque controller:
  ! NOTE: Time is scaled by OnePlusEps to ensure that the contoller is called
          at every time step when VS_DT = DT, even in the presence of
          numerical precision errors.
  IF ( ( Time*OnePlusEps - LastTimeVS ) >= VS_DT ) THEN
  ! Compute the generator torque, which depends on which region we are in:
     GenTrq = VS_RtPwr/GenSpeedF
     ELSEIF ( GenSpeedF <= VS_CtInSp ) THEN</pre>
                                                                                ! We are in region 1 - torque is zero
        GenTrq = 0.0
     ELSEIF ( GenSpeedF < VS_Rgn2Sp ) THEN
                                                                                ! We are in region 1 1/2 - linear ramp in to
        GenTrq = VS_Slope15*( GenSpeedF - VS_CtInSp )
     ELSEIF ( GenSpeedF < VS_TrGnSp ) THEN
                                                                                ! We are in region 2 - optimal torque is pro
        GenTrq = VS_Rgn2K*GenSpeedF*GenSpeedF
     ELSE
                                                                                ! We are in region 2 1/2 - simple induction
        GenTrq = VS_Slope25*( GenSpeedF - VS_SySp )
     ENDIF
  ! Saturate the commanded torque using the maximum torque limit:
     GenTrq = MIN( GenTrq
                                              , VS_MaxTq ) ! Saturate the command using the maximum torque limit
  ! Saturate the commanded torque using the torque rate limit:
     IF ( iStatus == 0 ) LastGenTrq = GenTrq
                                                               ! Initialize the value of LastGenTrq on the first pass only
     TrqRate = ( GenTrq - LastGenTrq )/ElapTime ! Torque rate (unsaturated)

TrqRate = MIN( MAX( TrqRate, -VS_MaxRat ), VS_MaxRat ) ! Saturate the torque rate using its maximum absolute value
                                                              ! Saturate the command using the torque rate limit
     GenTrq = LastGenTrq + TrqRate*ElapTime
  ! Reset the values of LastTimeVS and LastGenTrq to the current values:
     LastTimeVS = Time
     LastGenTrq = GenTrq
  ENDIF
  ! Set the generator contactor status, avrSWAP(35), to main (high speed)
  ! variable-speed generator, the torque override to yes, and command the generator torque (See Appendix A of Bladed User's Guide):
  avrSWAP(35) = 1.0
                             ! Generator contactor status: 1=main (high speed) variable-speed generator
  avrSWAP(56) = 0.0
                             ! Torque override: 0=yes
  avrSWAP(47) = LastGenTrq ! Demanded generator torque
1-----
  ! Pitch control:
  ! Compute the elapsed time since the last call to the controller:
  ElapTime = Time - LastTimePC
  ! Only perform the control calculations if the elapsed time is greater than ! or equal to the communication interval of the pitch controller:
  ! NOTE: Time is scaled by OnePlusEps to ensure that the contoller is called
          at every time step when PC_DT = DT, even in the presence of
          numerical precision errors.
  IF ( ( Time*OnePlusEps - LastTimePC ) >= PC_DT ) THEN
  ! Compute the gain scheduling correction factor based on the previously
     commanded pitch angle for blade 1:
     GK = 1.0/(1.0 + PitCom(1)/PC_KK)
```

```
! Compute the current speed error and its integral w.r.t. time; saturate the
      integral term using the pitch angle limits:
               = GenSpeedF - PC_RefSpd
                                                                        ! Current speed error
      IntSpdErr = IntSpdErr + SpdErr*ElapTime
                                                                        ! Current integral of speed error w.r.t. time
      IntSpdErr = MIN( MAX( IntSpdErr, PC_MinPit/( GK*PC_KI ) ), &
                                       PC MaxPit/( GK*PC KI )
                                                                 ) ! Saturate the integral term using the pitch angle li
   ! Compute the pitch commands associated with the proportional and integral
      gains:
      PitComP
              = GK*PC KP* SpdErr
                                                                        ! Proportional term
      PitComI = GK*PC_KI*IntSpdErr
                                                                        ! Integral term (saturated)
   ! Superimpose the individual commands to get the total pitch command;
      saturate the overall command using the pitch angle limits:
     PitComT = PitComP + PitComI
PitComT = MIN( MAX( PitComT, PC_MinPit ), PC_MaxPit )
                                                                        ! Overall command (unsaturated)
                                                                        ! Saturate the overall command using the pitch angle
    Saturate the overall commanded pitch using the pitch rate limit:
     NOTE: Since the current pitch angle may be different for each blade
           (depending on the type of actuator implemented in the structural
           dynamics model), this pitch rate limit calculation and the
          resulting overall pitch angle command may be different for each
          blade.
      DO K = 1, NumBl ! Loop through all blades
        PitRate(K) = ( PitComT - BlPitch(K) )/ElapTime
PitRate(K) = MIN( MAX( PitRate(K), -PC_MaxRat ), PC_MaxRat )
PitCom (K) = BlPitch(K) + PitRate(K)*ElapTime
                                                                        ! Pitch rate of blade K (unsaturated)
                                                                       ! Saturate the pitch rate of blade K using its maximu
                                                                        ! Saturate the overall command of blade K using the p
      ENDDO
                     ! K - all blades
   ! Reset the value of LastTimePC to the current value:
      lastTimePC = Time
   ! Output debugging information if requested:
     ENDIF
   ! Set the pitch override to yes and command the pitch demanded from the last
      call to the controller (See Appendix A of Bladed User's Guide):
   avrSWAP(55) = 0.0
                           ! Pitch override: 0=yes
   avrSWAP(42) = PitCom(1) ! Use the command angles of all blades if using individual pitch
  avrSWAP(43) = PitCom(2) ! "
avrSWAP(44) = PitCom(3) ! "
   avrSWAP(45) = PitCom(1) ! Use the command angle of blade 1 if using collective pitch
|-----
   ! Reset the value of LastTime to the current value:
  LastTime = Time
FNDTF
   ! Convert CHARACTER string to byte array for the return message:
DO I = 1,MIN( 256, NINT( avrSWAP(49) ) ) avcMSG(I) = iMessage(I) ! Same as cMessage by EQUIVALENCE
ENDDO
```

RETURN
END SUBROUTINE DISCON

#### REPORT DOCUMENTATION PAGE

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|--|--|----------|--------------------------------------|--|---|--|--|--|
| 1.   | REPORT DATE (DD-MM-YYYY)   | 2. RE    | PORT TYPE                            |  |   | 3. DATES COVERED (From - To)                               |  |  |
|  | February 2009  | te       | chnical report                       |  |   |  |  |  |
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| 14. ABSTRACT (Maximum 200 Words) This report describes a three-bladed, upwind, variable-speed, variable blade-pitch-to-feather-controlled multimegawatt wind turbine model developed by NREL to support concept studies aimed at assessing offshore wind technology. |  |          |                                      |  |   |  |  |  |
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