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<b>Unit Number and Title</b>	<b>12: Data Analytics</b>
Academic Year	2020
Unit Tutor	Eduardo Caro
<b>Assignment Title</b>	<b>Data Analytics: Descriptive, inference, and predictive techniques</b>
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## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

### A. Introduction to data analytics

1. Give an example for the following terms:
  - a. Data. - Representación de un atributo o variable cuantitativa o cualitativa.
    - i. Nombres de las calles -
  - b. Information. - Datos procesados con significado.
    - i. Mapa -
  - c. Knowledge. - Integrar datos e información con experiencia para la toma de decisiones. - Inferencia.
    - i. Ruta -

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

2. Go to the web <https://www.teoalida.com/cardatabase/>, section "European Car Models", and download the "Demo/sample free" Excel database.  
Please, organize the data in the following categories:

- Categorical data
  - *Nominal data*
  - *Ordinal data*
- Numerical data
  - *Discrete data*
  - *Continuous data*

**Categorical data - Cualitativos** - NO medibles - determinan modalidades

- **Nominal data** - Nominales - no Ordinales - no se pueden ordenar, no tiene sentido ordenarlas, No puedo calcular la media, Los datos son principalmente alfabéticos, son datos "etiquetados" o "nombrados" que pueden dividirse en varios grupos

*European / World classification*

*Make*

*Model*

*Country of origin*

*Country*

*American classification*

*Description*

*Pre-1990 car models*

- **Ordinal data** - Ordinales - se pueden ordenar, tiene sentido ordenarlas, tienen un orden de categorías mientras que los nominales no.

*Platform / generation number*

*Sold in Western Europe*

*Sold in North America*

*Sold in Europe*

*Sold in North America*

*Sold in India*

*Timeline included*

*Class*

**Numerical data - Cuantitativos** - medibles

- **Discrete data** - Discretos - número finito de valores enteros. - barras

*Units produced*

*Production years*

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

*Model Years (US/Canada)*  
*Model Years (North America)*  
*Units produced*  
*Models included (WORLD)*  
*Models included (EURO)*  
*Company Founded*  
*First car produced*  
*Last car produced*  
*Years produced*  
*Year*  
*models*  
*Number of car models by the year of launch*

- **Continuous data** - Continuous - cualquier valor real infinito dentro de un intervalo. - histogramas

## B. Descriptive Analytics

3. For the data file "*Tablet Computer Sales.txt*", find the average number, standard deviation, variance, and interquartile range of units sold per week.

```
(base) hadoop@ubuntu-hokkaido-3568:~/R/Data$ cat Tablet_Computer_Sales
.txt
Week    Units_Sold
1        88
2        44
3        60
4        56
5        70
6        91
7        54
8        60
9        48
10       35
11       49
12       44
13       61
14       68
15       82
16       71
17       50
(base) hadoop@ubuntu-hokkaido-3568:~/R/Data$
```

Leer el fichero

```
> TablaVentas=read.table("Tablet_Computer_Sales.txt", header=T)
```

El fichero contiene 17 pares de valores Units\_Sold y Week:

```
> length(TablaVentas[[1]])
[1] 17
```

Los nombres de los campos de los ficheros son:

```
> names(TablaVentas)
[1] "Week"    "Units_Sold"
```

La media de las unidades vendidas es:

```
> mean(TablaVentas$Units_Sold)
[1] 60.64706
```

La varianza de las unidades vendidas es:

```
> var(TablaVentas$Units_Sold)
[1] 253.8676
```

La desviación estándar de las unidades vendidas es:

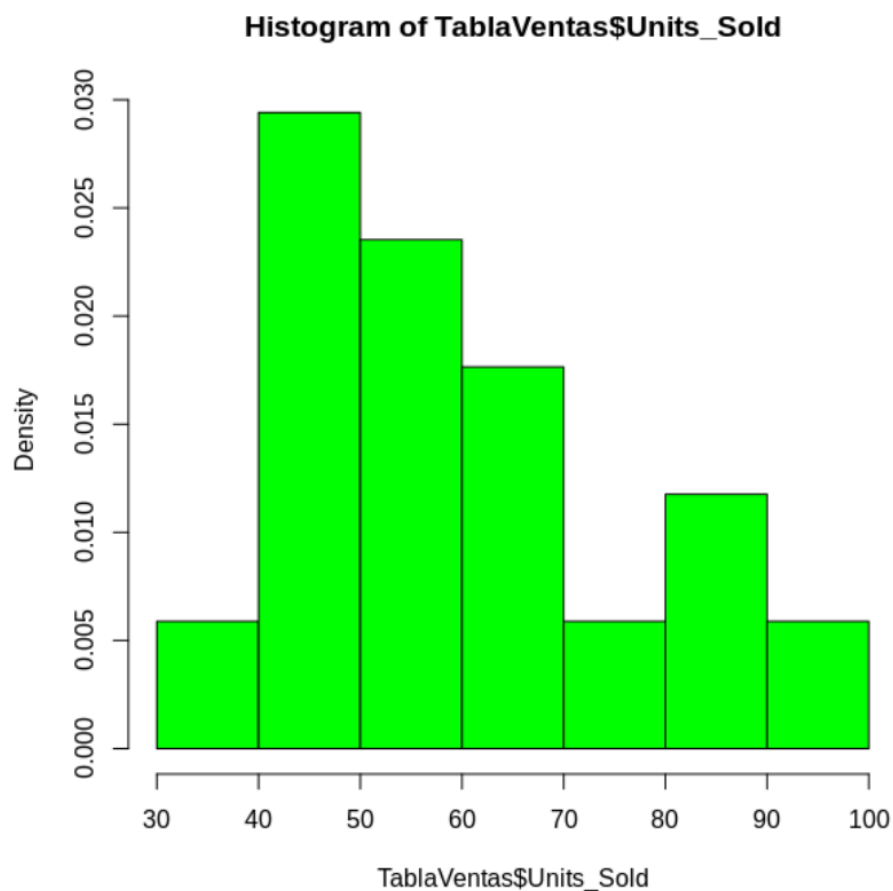
```
> sqrt(var(TablaVentas$Units_Sold))
[1] 15.93322
```

La mediana de las unidades vendidas es:

```
> median(TablaVentas$Units_Sold)
[1] 60
```

El eje x de la gráfica nos muestra las Unidades Vendidas y en el eje y podemos ver la frecuencia relativa de estas ventas por semana.

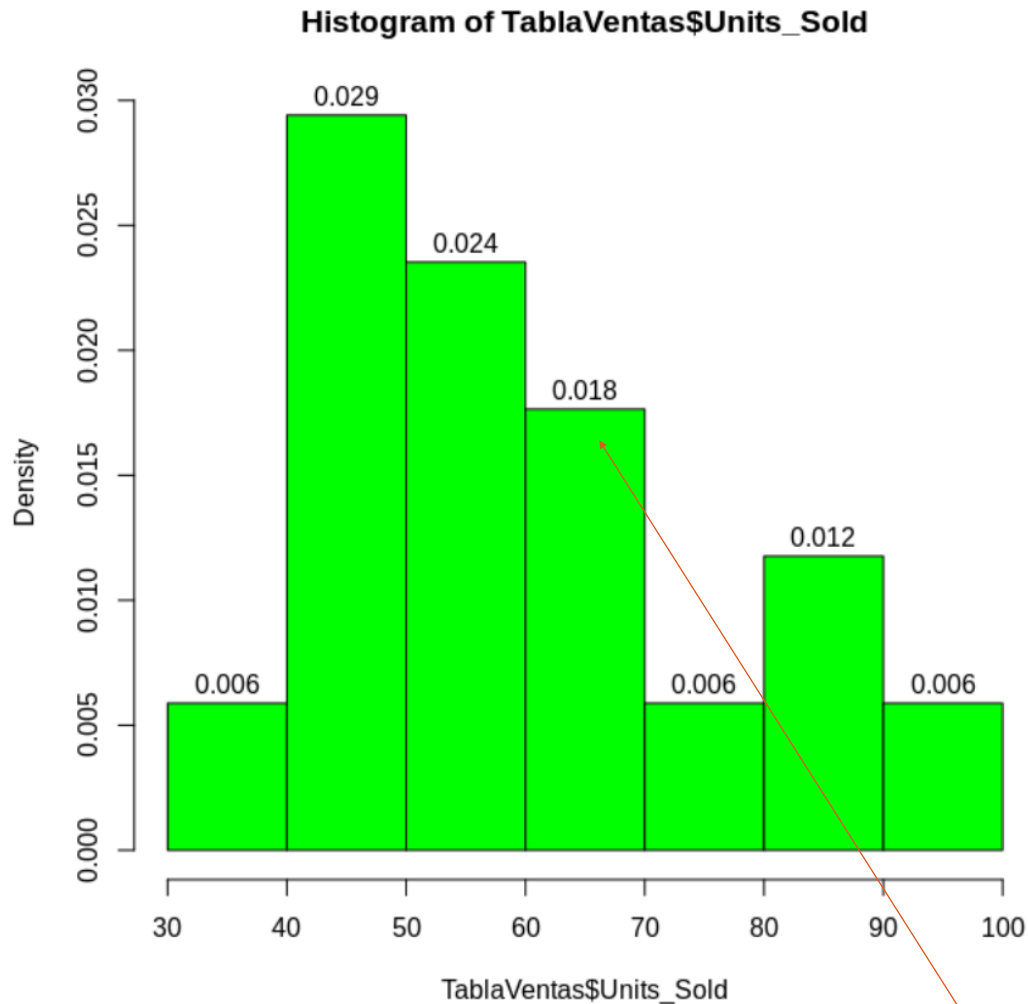
```
> hist(TablaVentas$Units_Sold, col = "green", freq=0)
```



```
> hist(TablaVentas$Units_Sold)
> hist(TablaVentas$Units_Sold, col = "green")
> hist(TablaVentas$Units_Sold, col = "green", freq=0)
```

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

```
> hist(TablaVentas$Units_Sold, labels = T, freq = F, col="green")
```

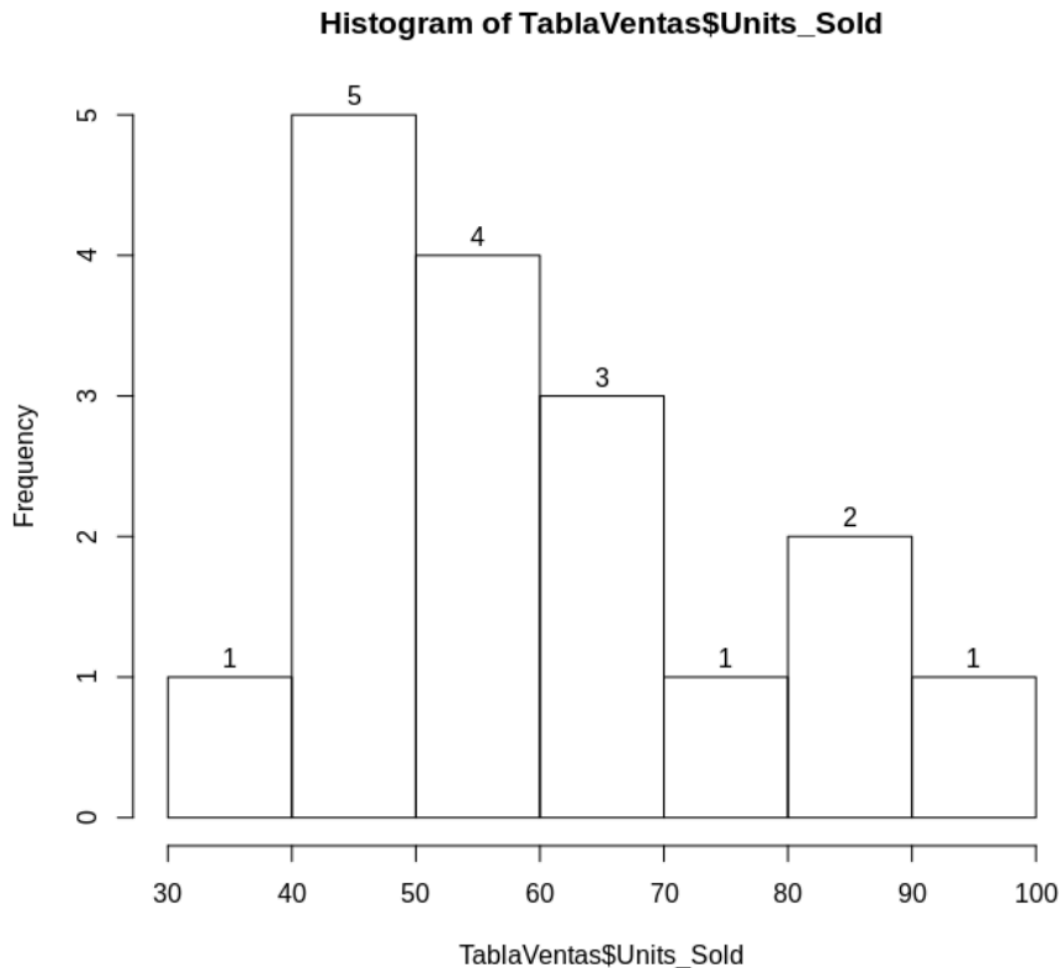


```
> hist(TablaVentas$Units_Sold, labels = T, freq = F, col="green")
```

esta frecuencia se multiplica por la amplitud del rango (el ancho de la base) y nos indica que el 18% de las unidades vendidas esta entre 60 y 70.

En el Histograma podemos ver el comportamiento de las ventas

```
> hist(TablaVentas$Units_Sold, labels = T)
```



```
> TablaVentas=read.table("Tablet_Computer_Sales.txt", header=T)
> hist(TablaVentas$Units_Sold, labels = T)
```

El eje x de la gráfica nos muestra las Unidades Vendidas y en el eje y podemos ver la frecuencia absoluta de estas ventas.

El 50% de las unidades vendidas están por debajo de la mediana, entre 30 y 60,  
El 50% de las unidades vendidas están por encima de la mediana, entre 60 y 100.

Por debajo de la mediana se han hecho  $1+5+4 = 9$  ventas, el 25%.

Por encima de la mediana se han hecho  $3+1+2+1 = 7$  ventas, el 25%

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

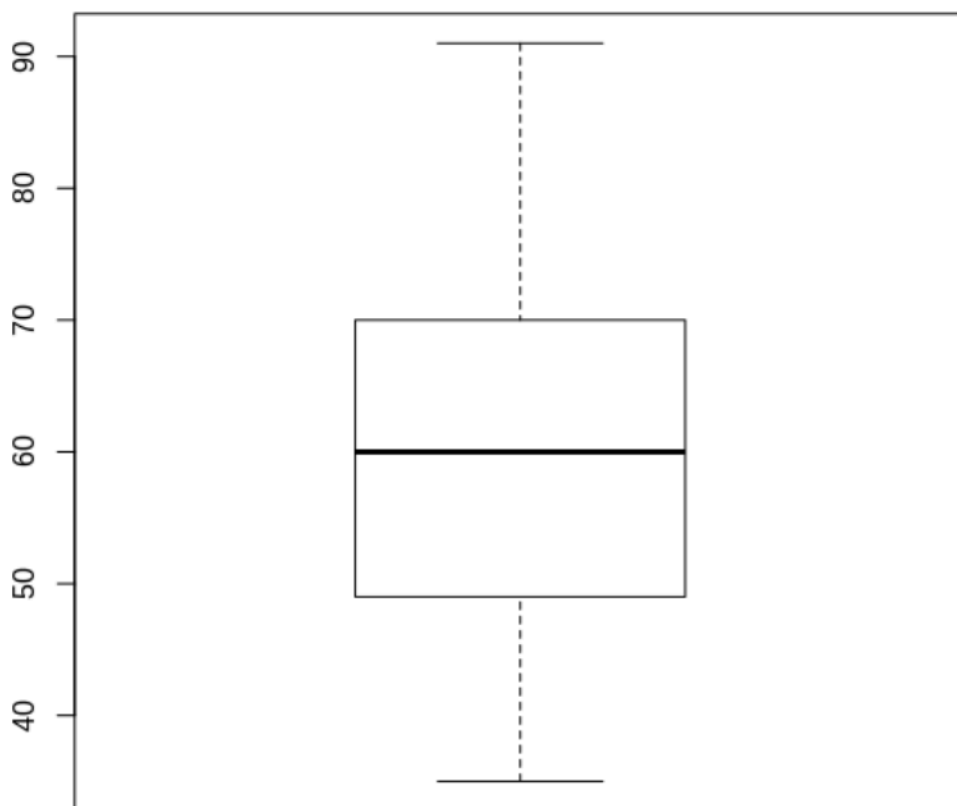
```
> quantile(TablaVentas$Units_Sold)
 0% 25% 50% 75% 100%
  Q1 60 Q3
 35 49 60 70 91
```

El 25% de las unidades vendidas están por debajo de el Q1= y

El 25% de las unidades vendidas están por encima de el Q3

La mitad de las ventas se hacen entre el Q1=50 y el Q3=70.

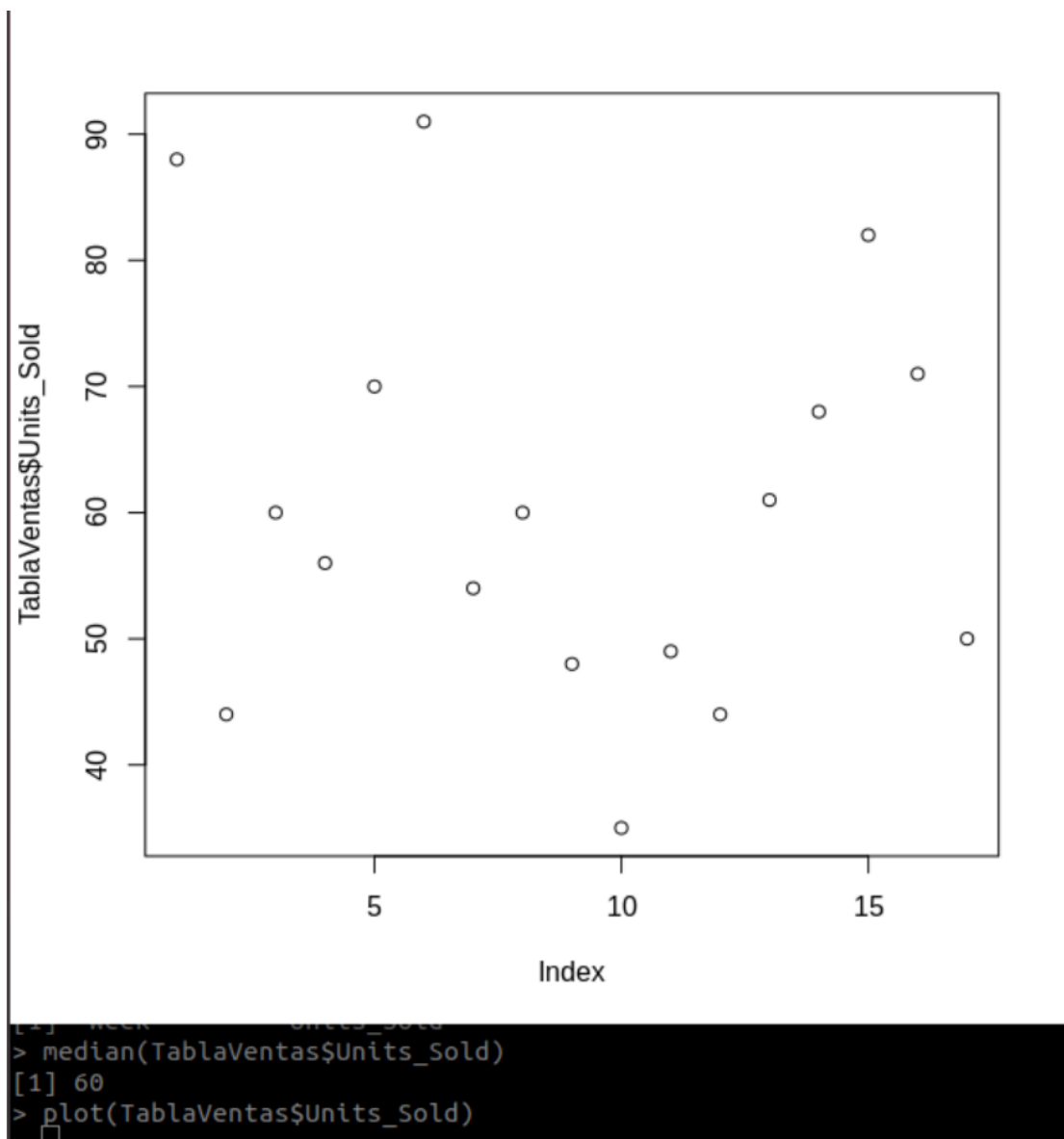
El Rango InterQuartil =  $Q3 - Q1 = 20$  que nos indica la dispersión de los datos.



```
median(TablaVentas$Units_Sold)
[1] 60
> plot(TablaVentas$Units_Sold)
> boxplot(TablaVentas$Units_Sold)
```

No tenemos puntos atípicos.





**C. Probability -**

4. Let us define  $X$  as a random variable Gaussian-distributed with  $\mu = 4$  and  $\sigma = 3$ .
  - Compute  $P(X \leq 6)$
  - Compute  $P(3 \leq X \leq 6)$
  - Compute  $a$  such as  $P(X \leq a) = 0.85$
  - Generate 1000 random numbers distributed as  $X$ .
    - Plot a histogram with these numbers, and superimpose the theoretical density function
    - Compute the proportion of the numbers that has been generated in the interval  $[3, 6]$ , and compare with the probability computed above in  $P(3 \leq X \leq 6)$
    - Check if the generated random numbers have a Gaussian distribution.

RNORM -> Crea  $n$  valores aleatorios con un  $\mu$  y un  $\sigma$  dado.  
 rnorm random de la distribución normal  
 rnorm( $n$ , mean, sd)

Generate 1000 random numbers distributed as  $X$ .

```
> x = rnorm( 1000, 4, 3)
```

```
> x
```

```
[1] 9.722570951 6.211427198 2.508262913 4.139724814 4.677790110
[6] 1.230995381 1.965396672 6.488571367 3.072921287 6.790270359
[11] 8.320486977 7.315415223 9.037359923 6.458714038 6.009824193
[16] 4.607721569 4.207768344 4.719899337 2.479265433 2.602571266
[21] 5.671424456 5.444647257 3.723626253 1.837756028 2.930583570
[26] 7.917282936 3.012074310 5.188248465 8.024267729 5.421459376
[31] 3.981487017 6.361560591 4.271581798 1.243004533 1.944055671
[36] 1.530621602 2.480864685 4.240728436 1.882294691 1.337529812
[41] -1.882293641 3.585676118 6.929947789 7.849017666 0.339912836
[46] 1.983010350 2.730427892 3.896994672 5.918259763 7.162565008
[51] -0.287221541 5.187820980 3.548050820 4.830088653 3.311645221
[56] 0.915211273 3.612222944 9.842090769 4.742765099 -0.835973072
[61] 1.766909070 1.671513668 6.495753925 5.129725893 3.918217479
[66] 6.768604611 5.834482601 1.516918895 6.140512728 8.874400451
[71] 4.514966635 2.532810399 5.432233809 0.726443464 4.271291944
[76] 1.774256967 7.597992599 13.055332535 3.576914728 1.751239379
[81] 4.952006568 2.370382055 1.079241610 6.795152411 3.321105427
```

[86] -0.576366567 4.409198008 -1.238873051 -0.335542623 2.932252428  
 [91] -0.822976474 5.862416781 5.224077734 1.298535381 5.560786148  
 [96] 1.726152640 4.405386415 6.062141376 6.933085281 0.083971564  
 [101] 5.939252510 0.712851474 8.258705038 6.061144946 4.468130686  
 [106] 0.289010919 0.525983395 2.998358336 0.514076221 3.643954712  
 [111] 7.995448922 3.230590080 4.657879228 2.641335486 3.178088515  
 [116] 7.152351631 4.917588796 4.092624350 3.149892615 0.869055959  
 [121] 8.543357113 9.895700597 9.641745611 -0.903208267 1.698466801  
 [126] 3.741987027 2.600176448 8.851360217 5.114223753 3.378683645  
 [131] -5.468752355 0.219529107 4.177014481 7.445974180 1.282261997  
 [136] 6.364841480 4.158220335 2.429991719 7.112274650 1.523045448  
 [141] 0.177278636 2.817009377 3.879597499 1.458014354 8.364717483  
 [146] 2.626763080 5.992223951 1.497974660 1.471208855 2.472373746  
 [151] 2.140080913 -0.173138318 0.738701084 1.100190538 3.093848425  
 [156] 2.614752807 -1.269680625 4.113679107 0.630165691 8.225266756  
 [161] 0.390878421 1.328138590 4.312852878 4.624936995 -0.638777809  
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 [171] 0.811697070 10.765247879 1.208862971 4.663853639 6.174358129  
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 [206] -0.233199808 1.037190762 1.558937496 -0.686512648 3.841825701  
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 [221] -0.114112348 5.079776356 -3.809169347 7.036561787 -1.514828920  
 [226] 3.360214337 4.365131538 4.461060799 7.383020658 11.699878215  
 [231] 6.186755272 6.123775530 6.539739394 1.794553599 2.485610905  
 [236] 2.608139050 3.566808815 0.497721853 2.866089227 5.828394493  
 [241] 2.178345540 5.093038819 4.961607481 2.437286659 1.363423225  
 [246] 7.491729676 2.414379528 0.106438284 4.265413101 0.681171206  
 [251] 3.482857725 2.574357004 4.548963722 10.896553245 0.959729015  
 [256] 6.357540064 -2.745009234 6.829742809 0.721179865 6.199110413  
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[576] 0.049168339 4.865983276 5.728722430 8.603317305 3.228644984  
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 [596] -0.619837891 3.967382207 0.785835133 2.896925374 0.447481059  
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 [656] 4.902163835 -0.405603491 2.348873931 6.286238261 6.236264022  
 [661] 6.689746628 -2.311298212 1.150579425 1.052796893 1.666651591  
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 [681] 1.318825090 3.113127101 7.149866598 6.353973581 4.041625919  
 [686] 6.540997495 5.657859450 5.784999260 4.921612570 0.569106047  
 [691] 6.899596937 8.278806612 9.418848635 4.667785765 5.010480439  
 [696] 6.849067150 2.998923418 0.194999569 0.830643034 -1.703665134  
 [701] 4.423620743 5.530128807 5.832168866 7.295113537 5.430939950  
 [706] 3.798712695 -0.659069454 5.064475439 8.981936789 3.448453669  
 [711] 5.931427932 7.547698140 -0.068651111 0.876545805 4.311691798  
 [716] 2.782839192 4.436149155 3.657116238 2.400586382 6.195525581  
 [721] 5.433768829 -0.419938931 4.776671529 6.977721657 9.252854790  
 [726] 1.188472478 8.622609738 3.676219656 2.918144141 3.462001367  
 [731] 3.192548547 4.633496694 6.686889015 2.423551924 4.858554560  
 [736] -3.826658525 2.016617221 6.294495910 0.742242710 5.513646668  
 [741] 3.682213357 2.432986208 1.714940422 8.536148499 1.727820631  
 [746] 7.400382993 6.268730238 -0.100547394 2.992598117 10.239088016  
 [751] 0.377079593 1.307163822 9.481052138 -0.610184480 3.409957928  
 [756] -0.157292930 6.301604399 4.216543625 9.533605964 8.633555938  
 [761] 6.096183524 3.638639635 0.975317044 5.125299917 7.725145457  
 [766] 2.039650909 3.473240677 -3.823699615 4.323735351 9.584445785  
 [771] 8.441958706 4.973996546 1.391446783 0.197915150 2.350267556  
 [776] 6.655826449 3.217182008 8.403025471 1.762704936 2.328387307  
 [781] -0.800270146 2.572068771 2.386047458 3.241964880 -0.366419675  
 [786] 2.256641122 2.875214488 7.341394895 -0.055212531 6.525665636  
 [791] 3.616757834 2.775267178 2.881864591 1.461219143 3.106719755  
 [796] 4.390606324 4.407141063 3.214795843 9.033697695 4.700564903  
 [801] 4.275098151 2.738830189 4.457127847 -0.201995279 7.033111677  
 [806] 6.893747737 0.298077240 0.112085491 -1.195432870 3.454119713  
 [811] 1.669384094 7.257897452 3.736462251 3.308560151 4.574995281  
 [816] 3.559881939 3.275774048 5.772927225 3.315348544 2.619204467

[821] 6.174814610 4.741439332 0.990673810 -0.609219512 2.734989995  
 [826] 10.145072186 7.147153262 4.832156640 5.850977952 0.599510927  
 [831] 5.947160676 0.666216323 6.676434553 -0.482537939 -1.900172763  
 [836] 3.048900638 7.838839390 5.851302513 6.823795786 7.622565426  
 [841] 2.155805800 4.454464392 -2.864232298 3.730787576 1.120894235  
 [846] 0.104634148 -2.498893482 8.550164250 5.903829403 -0.780464293  
 [851] 0.833347259 3.743421608 4.654216211 4.112404714 6.452046902  
 [856] 2.115153668 3.292777150 4.460443593 5.803095809 1.986178477  
 [861] 3.651534724 2.209781762 3.061074017 6.125712681 7.652292576  
 [866] 5.954147369 0.641963218 -2.030439149 -0.221400731 5.813850201  
 [871] 7.807039328 6.772659234 3.810651952 5.726720584 -0.127383625  
 [876] 0.220868545 3.839319307 9.391743706 3.294372582 7.543433686  
 [881] 6.240118606 9.815001498 4.164777359 2.643334865 4.923317586  
 [886] 3.086636336 3.322454892 8.085314508 3.169242515 -0.292071627  
 [891] 5.928410471 3.623712369 0.809973052 6.922605274 7.403139386  
 [896] 7.094559573 5.496784410 2.855290592 2.978759222 -1.044969746  
 [901] 2.410711240 3.870699755 6.478521724 1.187777273 5.772889807  
 [906] 7.154531467 4.284654211 3.201363701 4.896757445 2.732244214  
 [911] 7.676932284 3.289225515 2.501054648 4.199085588 8.234579629  
 [916] 8.959128329 3.620792197 6.739632937 1.195287454 6.378219374  
 [921] 1.169563754 -0.989844446 1.913297041 -2.248200791 3.369106795  
 [926] 5.229325213 6.424564818 7.271546502 0.306133700 5.245739608  
 [931] 6.541283057 0.532106227 8.508294597 9.272515031 -3.964967504  
 [936] 5.908047796 0.329210230 0.851137323 4.710201587 3.689213706  
 [941] 3.425921543 3.725367522 10.072711343 7.826463739 3.373082876  
 [946] 2.211918808 5.076166422 1.831917174 4.838812525 1.821511528  
 [951] 10.055279490 9.085432287 6.226849496 5.378771335 4.440647634  
 [956] 0.898951431 8.990225899 8.137731194 10.412555275 1.548484348  
 [961] 6.427600105 3.785829083 3.665892064 3.483239993 8.124939878  
 [966] 8.236620858 4.214459737 5.700270755 6.415499418 6.353337432  
 [971] 9.115362245 4.316094520 5.997749778 5.719000083 8.863206817  
 [976] 5.727793109 3.708372726 2.664170473 1.084940086 -0.424586902  
 [981] 2.033561889 2.115813583 4.310248773 1.551119406 4.185972246  
 [986] 2.867766666 3.386759483 -1.161971444 6.829082800 4.699670773  
 [991] 3.621348788 6.557779893 2.022140773 7.489283598 10.234863323  
 [996] -0.466739909 8.887104089 4.004537421 6.949013300 2.850796691

pnorm —> Calcula la probabilidad - AREA - dando un mu y un sigma - sólo calcula las areas a la izquierda

- **Compute**  $P(X \leq 6)$

pnorm(6, 4, 3) = 0.7475

- **Compute**  $P(3 \leq X \leq 6)$

pnorm(6, 4, 3) = 0.7475

pnorm(3, 4, 3) = 0.3694

pnorm(6, 4, 3) - pnorm(3, 4, 3) = 0.7475 - 0.3694 = 0.3780

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

- Compute a such as  $P(X \leq a) = 0.85$

qnorm —> devuelve la altura de la curva, con un  $\mu = 4$  y un  $\sigma = 3$ .

qnorm(0.85,4,3) = 7.1093 —> por tanto el 0,85% de los números están por debajo de 7.1093

Plot a histogram with these numbers, and superimpose the theoretical density function -

- Compute the proportion of the numbers that has been generated in the interval  $[3, 6]$ , and compare with the probability computed above in  $P(3 \leq X \leq 6)$

pnorm —> me devuelve p; la probabilidad

pnorm(1000, 4, 3) = 1 —> Teorico

Partiendo de que la muestra es de 1000 datos y sabiendo que se trata de una distribución normal...

Calculo la suma de los números que son mayores ó iguales a 3 de la muestra x

```
> sum(x >= 3)
```

```
[1] 646
```

Calculo la suma de los números menores ó iguales a 6 de la muestra x

```
> sum(x <= 6)
```

```
[1] 732
```

Saco la diferencia y lo divido entre la muestra 1000 y tenemos una probabilidad de:

$$732 - 368 = 364$$

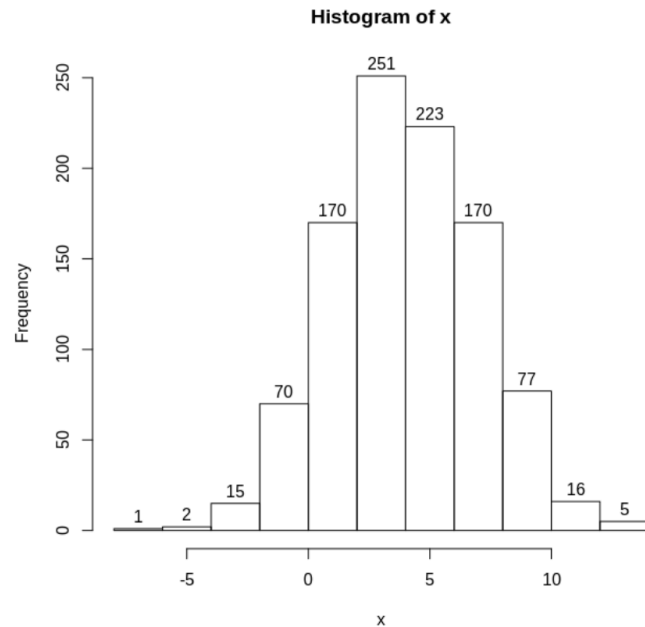
$$364/1000 = 0,364$$

Al realizar la comparación obtenida del calculo de los random de la variable Gaussian-distributed nos damos cuenta que la variación de la probabilidad es mínima.

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

Este histograma tiene una distribución normal "Experimental", —> tomando todos los x generados. (el histograma representa la curva de la muestra).

```
> hist(x, labels=T, freq=F)
```



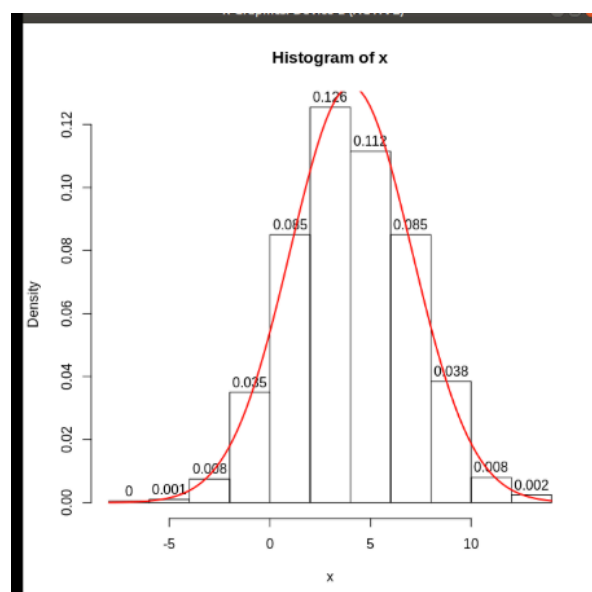
```
> hist(x)
> hist(x, labels = T)
> 
```

Check if the generated random numbers have a Gaussian distribution.

```
> media = mean(x) # calculo la media de x
```

```
> desv = sd(x) # calculo la desviación típica de x
```

```
> curve(dnorm(x,media, desv), add = T, col = "red", lwd = 2) # superpongo la función de la densidad, previamente calculada la media y la desviación típica.
```





De esta manera defino de forma unívoca la distribución normal.

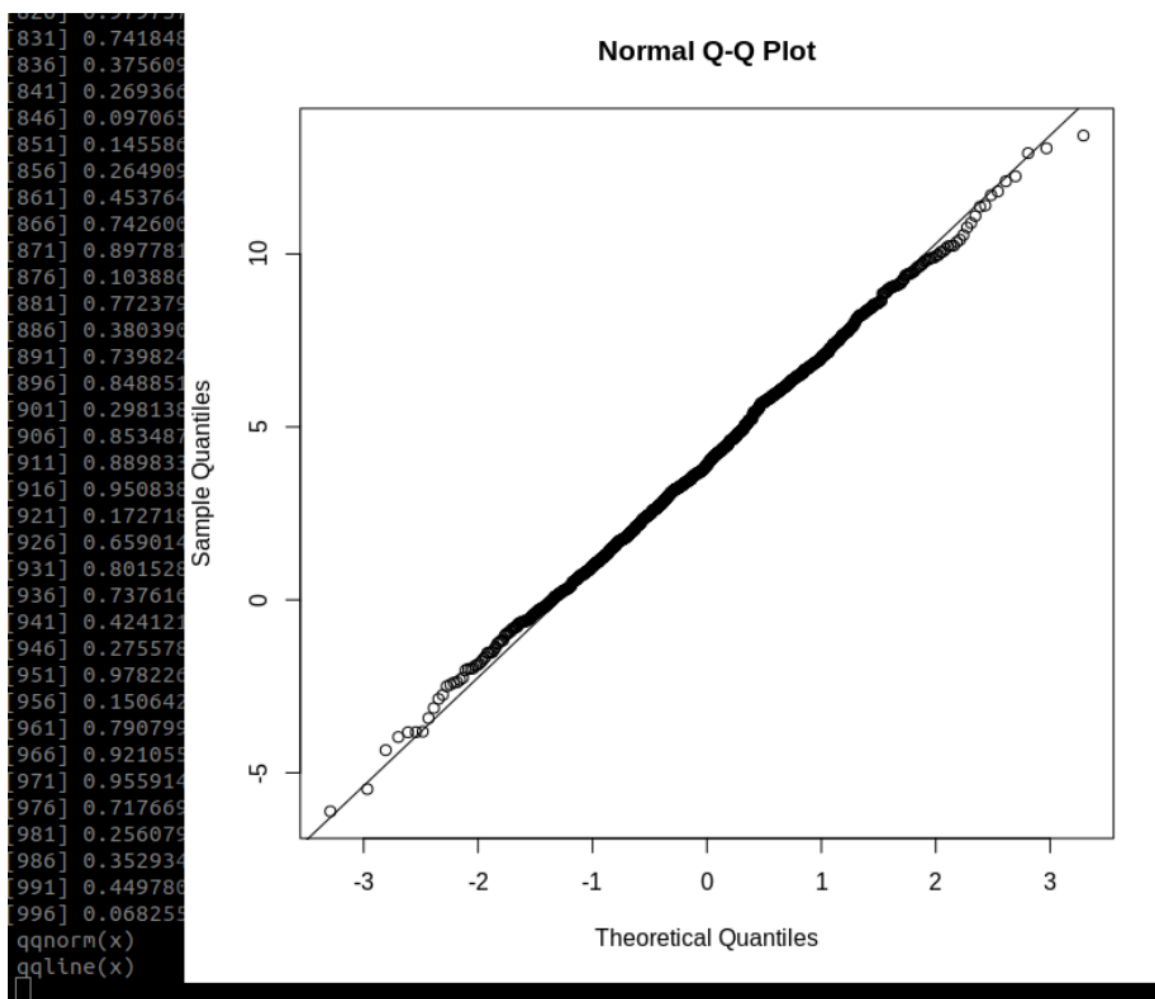
Curve me genera una gráfica de la función distribución de la distribución normal (Teórica con infinitos datos..), en función de  $x$ , con la media y desviación calculadas previamente.

Con el Q-QPlot —> Quantile-Quantile Plots - podemos ver gráficamente por medio de qqnorm y qqline.

Aquí podemos comprobar que las observaciones siguen una distribución normal siempre que los puntos de la gráfica de la distribución real "siguen" bastante bien la línea de la gráfica de la distribución teórica.

> qqnorm(x) # calculo de qq normal para x - distribución real -

> qqline(x) # adiciona la qqline al plot - distribución teórica



**D. Inference**

5. Some studies suggest that there is a relationship between the cheese's flavour and their chemical composition, especially with the lactic acid content.

The lactic acid content has been measured in ten cheeses, resulting the following values:

0.86, 1.53, 1.57, 1.81, 0.99, 1.09, 1.29, 1.78, 1.29, 1.58

Assuming that the lactic acid content can be modelled as a Gaussian distributed random variable:

- Estimate a value for the mean  $\mu$  and variance  $\sigma^2$
- Compute a confidence interval for the mean  $\mu$  ( $\alpha = 0.05$ )
- Compute a confidence interval for the variance  $\sigma^2$  ( $\alpha = 0.05$ )
- Solve the following hypothesis test ( $\alpha = 0.05$ ):

$$H_0 : \mu = 1$$

$$H_1 : \mu \neq 1$$

**- Estimate a value for the mean and variance**

```
> acidL # lactic acid
> acidL = c( 0.86, 1.53,1.57, 1.81, 0.99, 1.09, 1.29, 1.78, 1.29, 1.58 )
> acidL
[1] 0.86 1.53 1.57 1.81 0.99 1.09 1.29 1.78 1.29 1.58

> summary (acidL)
  Min. 1st Qu.  Median    Mean 3rd Qu.   Max.
0.860  1.140  1.410 1.379  1.577  1.810

> media = mean(acidL)
> media
[1] 1.379

> var(acidL)
[1] 0.1073656

> sqrt(var(acidL))
```

```
[1] 0.3276668
```

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

```
> desv = sd(acidL)
```

```
> desv
```

```
[1] 0.3276668
```

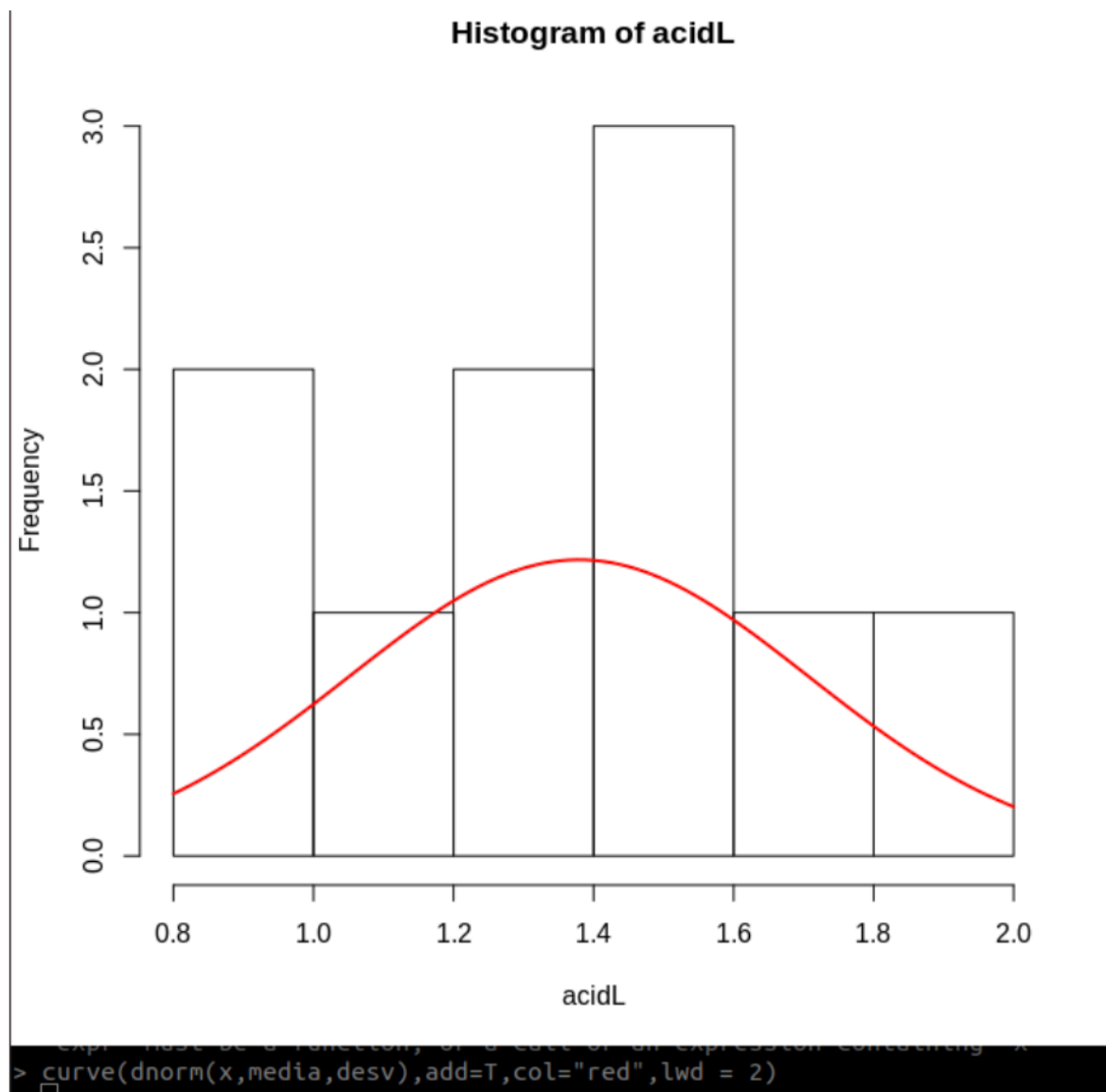
```
> n = length(acidL)
```

```
> n
```

```
[1] 10
```

```
> hist( acidL ) —> curva de la muestra
```

```
> curve( dnorm ( x, media, desv ), add=T, col="red", lwd = 2 ) —> curva de la distribución normal
```



## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

-Compute a confidence interval for the mean  $\mu$  ( variance = 0,05 )

$$IC(\mu) = \bar{x} \pm \hat{s} \cdot t_{n-1} \cdot \frac{1}{\sqrt{n}}$$

> # Intervalo de confianza de la media con un 99,9 % es:

```
media + desv * ( tstudent ( 0.05 ) , ( n-1 ) ) * ( 1 / sqrt ( n ) )  
media - desv * ( tstudent ( 0.05 ) , ( n-1 ) ) * ( 1 / sqrt ( n ) )
```

```
> media-desv*qt(0.05,n-1)/sqrt(n)  
[1] 1.568942
```

```
> media+desv*qt(0.05,n-1)/sqrt(n)  
[1] 1.189058
```

```
> 1.568942-1.189058  
[1] 0.379884
```

Con un **99 %** de confianza puedo afirmar que la media del acidL está entre el **1.568942-1.189058**, con una precisión aproximada de: **0.379884**.

Sé que entre **1.568942-1.189058** está la media del acidL # lactic acid, con una precisión aproximada de **0.379884**.

-Compute a confidence interval for the variance  $\sigma^2$  ( variance = 0,05 )

$$IC(\sigma^2) = \left( \frac{(n-1)\hat{s}^2}{\chi_b^2}, \frac{(n-1)\hat{s}^2}{\chi_a^2} \right)$$

> # Intervalo de confianza para la varianza

```
( n-1 ) * desv ^ 2 / qchisq ( 1-0.05 , n-1 )  
( n-1 ) * desv ^ 2 / qchisq ( 0.05 , n-1 )
```

```
> ( n-1 ) * desv ^ 2 / qchisq ( 1 - 0.05, n-1 )  
[1] 44.76498
```

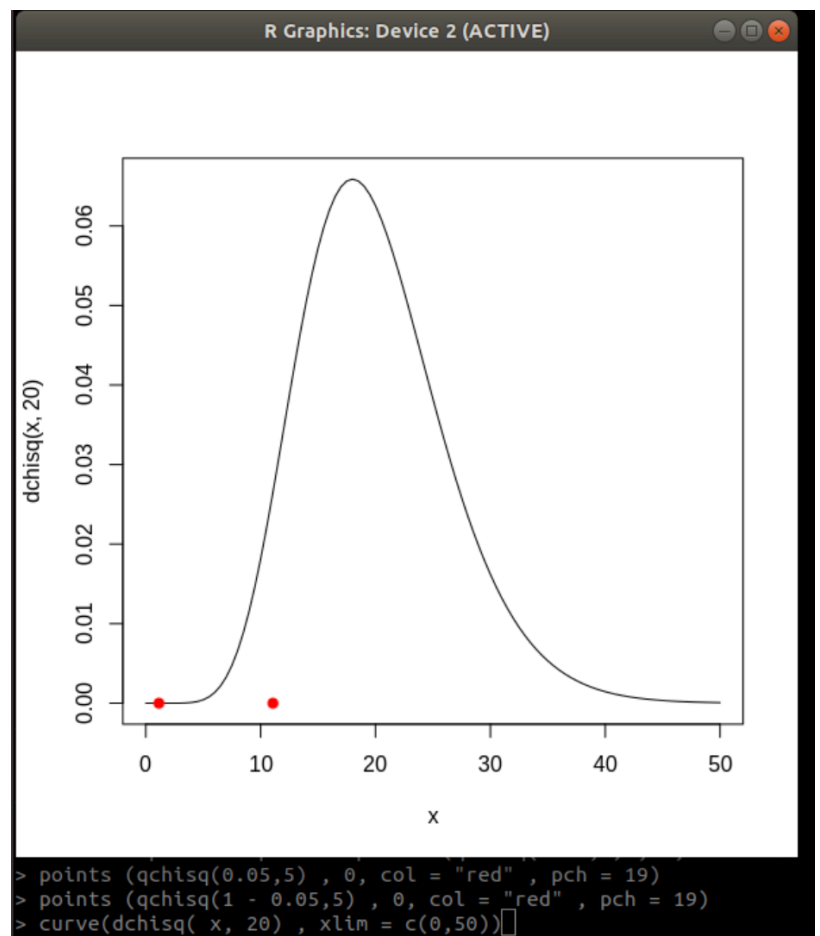
## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

```
> (n-1) * desv ^ 2 / qchisq ( 0.05, n-1 )  
[1] 60.25382
```

Con un **99%** de confianza puedo afirmar que la la varianza sigma del acidL está entre **44.76498 y 60.25382**

Con un **99%** de confianza puedo afirmar que (sigma), esta entre estos valores

```
> Xa = qchisq(0.05 , n-1)  
> Xa  
[1] 210.6873  
  
> Xb = qchisq(1 - 0.05 , n-1)  
> Xb  
[1] 283.5858  
  
> (n-1) * desv ^ 2 / Xb  
[1] 44.76498  
  
> (n-1) * desv ^ 2 / Xa  
[1] 60.25382  
  
curve(dchisq (x, 20) , xlim = c(0, 50))  
  
points (qchisq(0.05,5) , 0, col =  
"red" , pch = 19)  
  
points (qchisq(1 - 0.05,5) , 0, col =  
"red" , pch = 19)
```



## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES

- Solve the following hypothesis test ( $\alpha = 0.05$ ):

$$H_0 : \mu = 1$$

$$H_1 : \mu \neq 1$$

## DATA ANALYTICS: DESCRIPTIVE, INFERENCE, AND PREDICTIVE TECHNIQUES



**Student declaration**

I certify that the assignment submission is entirely my own work and I fully understand the consequences of plagiarism. I understand that making a false declaration is a form of malpractice.

Student signature:

Date: