

$$= \sum_{\mathbf{a} \in [0, n]^m} \prod_{i=1}^m p(a_i \mid a_{i-1}) \times p(e_i \mid f_{a_i})$$