# Guidance to fit the model to the polar bear data, R code, and additional results.

# Sarah Cubaynes

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We fitted our model to the Polar bear data in a Bayesian framework using Markov Chain Monte Carlo (MCMC) simulation implemented in program JAGS (Hornik et al. 2003) called from R using package jagsUI (Kellner 2015). We ran two MCMC in parallel with different initial values, we used 20.000 iterations with an initial burn-in of 9.000 iterations, thinning every 5 iterations, to reach convergence to a stationary distribution, assessed by visual inspection of trace plots for each model parameter to ensure adequate mixing and by using the Gelman and Rubin diagnostic (R-hat < 1.02). We used non-informative priors on the model parameters, with uniform distribution between 0 and 1 for probabilities, and normal distribution with mean 0 and variance of 1 for regression coefficients. To help estimation of the parameters in the model, we introduced the constraint that survival of cubs was lower than that of yearling survival (Amstrup and Durner, 1995). The constraint was enough to reach convergence with satisfactory posterior distribution for each of the estimated parameters (see Figure below).

Below we provide the code to prepare the data, run the model and analyse the results.

# Prepare data and run jags model

Load data and useful packages:

```
load(file = "CRlocalbears_revision2MEE.Rdata") # family units CR histories
data <- data.matrix(CRlb)

load(file = "daylocalbears_revision2MEE.Rdata") # capture date in day of the yaer
daycapt <- daylb
load(file="initstatelocalbears_revision2MEE.Rdata") #matrix of initial states

alive1 <- data.matrix(initmatlb)

load(file = "dataweaning_revision2MEE.Rdata") # all two-year old bear captures

library(jagsUI) # to run jags model

## Loading required package: lattice

##
## Attaching package: 'jagsUI'

## The following object is masked from 'package:utils':
##
## View

library(jtools) # to make predict plot from glm</pre>
```

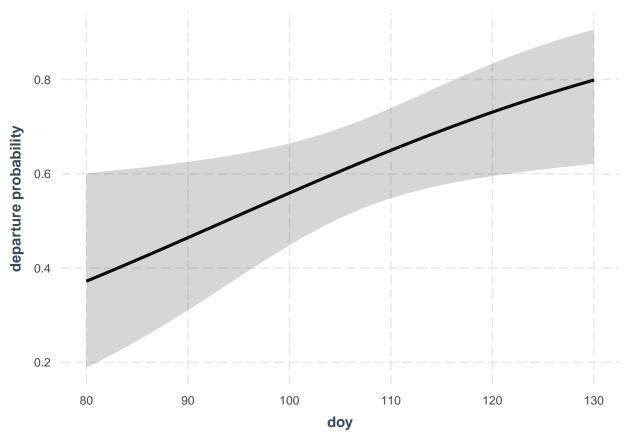
Define useful quantities:

```
N <- dim(data)[1] # number of family units
Years <- dim(data)[2] #number of sampling occasions

# Compute vector with occasion of first capture
get.first <- function(x) min(which(x!=0))
First <- apply(data, 1, get.first)</pre>
```

We use the ratio of two-year old bears captured alone versus still together with their mother (include all bears, not only resident females) to estimate the shape of the relationship between offspring departure probability and date within the field season:

```
nty <- dim(dataweaning)[[1]] # number of two-year old bears captured
status <- dataweaning$status #status of two-year old bears at the time of capture :
#1 alone (already departed from family unit),
#0 still together with mother (not yet departed from family unit)
doy <- dataweaning$daysinseason # date of capture</pre>
# qlm of departure probability as a function of date of capture
modeld<-glm(status~doy,family="binomial")</pre>
summary(modeld)
##
## Call:
## glm(formula = status ~ doy, family = "binomial")
##
## Deviance Residuals:
                      Median
##
       Min
                 1Q
                                    3Q
                                            Max
## -1.7056 -1.2304
                      0.7665
                                0.9143
                                         1.3215
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -3.56486
                           1.75383 -2.033
                                              0.0421 *
                                      2.310
                                              0.0209 *
                0.03803
                           0.01646
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 154.11 on 119 degrees of freedom
## Residual deviance: 137.99 on 118 degrees of freedom
## AIC: 141.99
## Number of Fisher Scoring iterations: 6
Plot predicted departure probability of two-year old bears as a function of date in day of the year (doy):
```



Departure probability increased throughout the field season. It was about 40% at the end of March and reached 80% at mid-May.

Predict departure probability from date of capture for resident family units (departure probability will be used in matrix E2 of the observation process to relate state to events for family units in states AS1 or AS2):

```
# Predict departure probability function of date of capture
daycapt <- daylb # dates of capture

# if not captured, replace with 80 (in date of capture) to avoid NAs
daycapt <- replace(daycapt,is.na(daycapt),80)

# create empty object to store predicted departure probability
alpha = matrix(0,nrow=N,ncol=Years)
# predict departure probability based on date of capture using modeld
for(i in 1:N){
   for(j in (First[i]):Years){
      alpha[i,j] <- predict(modeld,newdata=list(doy=daycapt[i,j]),type="response")
   }
}</pre>
```

Create a list containing the data to run the jags model:

```
# Bundle data for jags
mydatax <- list(N=N,First=First,Years=Years,mydata=data.matrix(data+1),alpha=data.matrix(alpha))</pre>
```

Generate initial values for each of the two chains:

```
set.seed(42)
# Initial values
```

```
init1 <- list(theta=rnorm(10, mean = 0, sd = 1),alive=alive1)
init2 <- list(theta=rnorm(10, mean = 0, sd = 1),alive=alive1)
inits <- list(init1,init2)</pre>
```

Create a list with names of the parameters to monitor:

```
# Parameters monitored
params <- c("phi", "s", "102", "112", "kappa", "beta", "gamma", "p", "prop")</pre>
```

Load the script of the jags model:

```
# JAGS MODEL
sink("Multieventmodel FitresidentBeardata.txt")
cat("
model {
  # Probabilities of events given states and states given states
  # vector of initial states
  SO[1] \leftarrow prop[1] / (1 + sum(prop[1:10])) # prob. of being in initial state J2
  SO[2] \leftarrow prop[2] / (1 + sum(prop[1:10])) # prob. of being in initial state J3
  SO[3] \leftarrow prop[3] / (1 + sum(prop[1:10])) # prob. of being in initial state SA4
  SO[4] \leftarrow prop[4] / (1 + sum(prop[1:10])) # prob. of being in initial state SA5
  SO[5] \leftarrow prop[5] / (1 + sum(prop[1:10])) # prob. of being in initial state A01
  SO[6] \leftarrow prop[6] / (1 + sum(prop[1:10])) # prob. of being in initial state AO2
  SO[7] \leftarrow prop[7] / (1 + sum(prop[1:10])) \# prob. of being in initial state A11
  SO[8] \leftarrow prop[8] / (1 + sum(prop[1:10])) # prob. of being in initial state A12
  SO[9] \leftarrow prop[9] / (1 + sum(prop[1:10])) # prob. of being in initial state AS1
  SO[10] \leftarrow prop[10] / (1 + sum(prop[1:10])) # prob. of being in initial state AS2
  SO[11] \leftarrow 1 / (1 + sum(prop[1:10])) # prob. of being in initial state A-
  SO[12] <- 0 # prob. of being in initial state dead
  # State process: define probabilities of S(t+1) given S(t)
  # define PHI matrix gathering survival of independent juveniles, subadults and adults
  PHI
        1
                    1
                        ]<- phi[1]</pre>
        Γ
                    2
                         1<- 0
  PHI
            1
  PHI
        1
                    3
                        1<- 0
  PHI
        Γ
            1
                    4
                        1<- 0
                    5
                        1<- 0
  PHI
        1
  PHI
        Γ
            1
                    6
                         1<- 0
        Ε
                    7
                        ]<- 0
  PHI
            1
  PHT
        Γ
            1
                    8
                        1<- 0
        Γ
                    9
                        1<- 0
  PHI
            1
        Γ
                    10 ]<- 0
  PHT
            1
  PHI
        1
                    11 ]<- 0
                    12 ]<- 1-phi[1]
  PHI
        1
  PHI
        Ε
            2
                    1
                         ]<- 0
  PHI
        Γ
            2
                    2
                        ]<- phi[1]</pre>
  PHI
        2
                    3
                        ]<- 0
        Γ
            2
                    4
                         ]<- 0
  PHI
        2
                    5
                        ]<- 0
  PHI
  PHI
        Γ
            2
                    6
                       1<- 0
        2
                    7
                         1<- 0
  PHI
  PHI
        [ 2 ,
                    8
                        1<- 0
```

```
PHI
      [
          2
                   9
                       ]<- 0
           2
                       ]<- 0
PHI
      10
      Г
           2
                       ]<- 0
PHI
                   11
PHI
      2
                       ]<- 1-phi[1]</pre>
                   12
PHI
      Ε
          3
                   1
                       ]<- 0
PHI
      3
                   2
                       ]<- 0
      Ε
          3
PHI
                   3
                       ]<- phi[1]</pre>
PHI
      Ε
          3
                       ]<- 0
                   4
      Ε
PHI
          3
                   5
                       ]<- 0
PHI
      3
                   6
                       ]<- 0
PHI
      Ε
          3
                   7
                       ]<- 0
      3
                       ]<- 0
PHI
                   8
PHI
      Γ
          3
                   9
                       ]<- 0
      [
          3
PHI
                      ]<- 0
                   10
PHI
      3
                   11
                       ]<- 0
PHI
      3
                   12
                       ]<- 1-phi[1]</pre>
PHI
      ]<- 0
           4
                   1
      2
                       ]<- 0
PHI
           4
PHI
      4
                   3
                       ]<- 0
PHI
      4
                   4
                       ]<- phi[1]</pre>
           4
                   5
PHI
      Ε
                       ]<- 0
PHI
      Е
           4
                   6
                       ]<- 0
PHI
      Ε
                   7
                       ]<- 0
           4
PHI
      Ε
           4
                   8
                       ]<- 0
PHI
      4
                   9
                       1<- 0
      Е
           4
                      ]<- 0
PHI
                   10
PHI
      Ε
           4
                   11
                       ]<- 0
PHI
      [
           4
                   12
                       ]<- 1 - phi[1]</pre>
PHI
      ]<- 0
           5
                   1
PHI
      5
                   2
                       ]<- 0
      [
PHI
          5
                   3
                       ]<- 0
      [
          5
                       ]<- 0
PHI
                   4
      5
PHI
                   5
                       ]<- phi[1]</pre>
      [
           5
PHI
                   6
                       ]<- 0
PHI
      5
                   7
                       ]<- 0
                       ]<- 0
PHI
      5
                   8
PHI
      5
                   9
                       ]<- 0
      Е
                       ]<- 0
PHI
          5
                   10
      Ε
           5
PHI
                   11
                       ]<- 0
PHI
      Ε
           5
                   12
                       ]<- 1 - phi[1]</pre>
PHI
      ]<- 0
           6
                   1
PHI
      Ε
           6
                   2
                       ]<- 0
      ]<- 0
PHI
           6
                   3
PHI
      6
                   4
                       ]<- 0
PHI
      [
           6
                   5
                       ]<- 0
PHI
      6
                   6
                       ]<- phi[1]</pre>
                   7
      6
                       ]<- 0
PHI
PHI
      Г
           6
                   8
                       ]<- 0
PHI
      ]<- 0
```

```
PHI
      [
          6
                   10 ]<- 0
                       ]<- 0
PHI
      6
                   11
PHI
      Е
           6
                   12
                       ]<- 1 - phi[1]</pre>
PHI
      7
                   1
                       ]<- 0
PHI
      Ε
           7
                   2
                       ]<- 0
PHI
      7
                   3
                       ]<- 0
      Ε
PHI
          7
                   4
                       ]<- 0
PHI
      Ε
          7
                   5
                       ]<- 0
      Ε
PHI
          7
                   6
                       ]<- 0
PHI
      7
                   7
                       ]<- phi[1]
PHI
      Ε
          7
                   8
                       ]<- 0
      7
                       ]<- 0
PHI
                   9
      [
          7
PHI
                   10
                       ]<- 0
      [
PHI
          7
                       ]<- 0
                   11
PHI
      7
                   12
                       ]<- 1-phi[1]</pre>
PHI
      ]<- 0
           8
                   1
      Е
                   2
PHI
           8
                       ]<- 0
      Е
PHI
           8
                   3
                       ]<- 0
PHI
      8
                   4
                       ]<- 0
PHI
      [
           8
                   5
                       ]<- 0
          8
PHI
      6
                       ]<- 0
                   7
PHI
      Е
          8
                       ]<- 0
      Ε
PHI
          8
                   8
                       ]<- phi[1]</pre>
PHI
      8
                   9
                       ]<- 0
PHI
      8
                   10
                       ]<- 0
      Е
                       ]<- 0
PHI
           8
                   11
PHI
      8
                   12
                       ]<- 1-phi[1]</pre>
      Е
PHI
           9
                   1
                       ]<- 0
      Е
                   2
                       ]<- 0
PHI
           9
PHI
      9
                   3
                       ]<- 0
PHI
      9
                   4
                       ]<- 0
      Е
           9
                   5
                       ]<- 0
PHI
      Е
           9
PHI
                   6
                       ]<- 0
      [
           9
                   7
                       ]<- 0
PHI
PHI
      9
                       ]<- 0
PHI
      9
                   9
                       ]<- phi[1]</pre>
                       ]<- 0
PHI
      9
                   10
      Е
                   11 ]<- 0
PHI
           9
PHI
      ]<- 1-phi[1]
           9
                   12
      Ε
                       1<- 0
PHI
           10
                   1
PHI
      Е
                   2
                       ]<- 0
           10
PHI
      Е
           10
                   3
                       ]<- 0
PHI
      Е
                       ]<- 0
           10
                   4
PHI
      10
                   5
                       ]<- 0
PHI
      [
                   6
                       ]<- 0
           10
      10
                   7
                       ]<- 0
PHI
      Е
           10
                   8
                       ]<- 0
PHI
      Г
           10
                   9
                       ]<- 0
PHI
PHI
      10
                   10 ]<- phi[1]
```

```
PHI
     [ 10 , 11 ]<- 0
PHI
                 12 ]<- 1-phi[1]
         10
                     ]<- 0
PHI
         11
                 1
PHI
     11
                 2
                    ]<- 0
PHI
     Ε
         11
                 3
                    ]<- 0
PHI
     11
                 4
                    ]<- 0
         11 ,
PHI
     5
                    ]<- 0
PHI
                    1<- 0
     6
         11
PHI
     Γ
         11
                 7
                     1<- 0
PHI
     11 ,
                 8
                    ]<- 0
     Γ
         11 ,
                 9
                    1<- 0
PHI
                 10 ]<- 0
     PHI
         11
PHI
     Γ
         11
                 11
                    ]<- phi[1]
PHI
     11
                 12 ]<- 1-phi[1]
PHI
     12
                 1
                    ]<- 0
     Е
                 2
                    ]<- 0
PHI
         12
PHI
     12
                 3
                    ]<- 0
PHI
     Γ
         12
                 4
                    ]<- 0
PHI
     Γ
         12
                 5
                    ]<- 0
PHI
     12
                 6
                    ]<- 0
PHI
         12 ,
                 7
                    ]<- 0
PHI
     12
                 8
                    ]<- 0
PHI
     12
                 9
                    ]<- 0
PHI
     10 ]<- 0
         12 ,
         12 ,
PHI
     Γ
                 11 1<- 0
     Ε
         12 ,
                 12 ]<- 1
PHI
# Define PSI matrices gathering state-to-state transition probabilities, it includes:
# PSI1: offspring survival and growth to next age, proba of sexual maturation:
PSI1 [
       1
                 1
                    ]<- 1
PSI1 [
                 2
                    1<- 0
         1
PSI1 [
         1
                 3
                    ]<- 0
     Γ
                    ]<- 0
PSI1
         1
                 4
     [
                 5
PSI1
         1
                    ]<- 0
     Ε
                    ]<- 0
PSI1
         1
                 6
                 7
PSI1 [
         1
                    ]<- 0
PSI1 [
                 8
                    ]<- 0
         1
PSI1 [
         1
                 9
                    ]<- 0
PSI1 Γ
                 10 ]<- 0
         1
PSI1
     1
                 11 ]<- 0
PSI1
     [
         1
                 12 ]<- 0
PSI1 Γ
         1
                 13
                    1<- 0
PSI1 Γ
         2
                 1
                    1<- 0
PSI1 [
         2
                 2
                    ]<- 1
PSI1
     [
         2
                 3
                    ]<- 0
PSI1 [
         2
                 4
                    ]<- 0
PSI1 [
         2
                 5
                    ]<- 0
         2
     [
                 6
                    ]<- 0
PSI1
     [
         2
                 7
                    ]<- 0
PSI1
PSI1
     [
                    ]<- 0
```

```
PSI1 [ 2 , 9 ]<- 0
PSI1 [
       2
             10 ]<- 0
PSI1 [ 2 , 11 ]<- 0
PSI1 [ 2
            12 ]<- 0
            13 ]<- 0
PSI1 [ 2
PSI1 [ 3 , 1 ]<- 0
PSI1 [ 3 ,
            2 ]<- 0
PSI1 [ 3
             3 ]<- 1-kappa#1 #
PSI1 [ 3 , 4 ]<- 0
PSI1 [ 3 , 5 ]<- 0
PSI1 [ 3
            6 1<- 0
          , 7 ]<- 0
PSI1 [ 3
PSI1 [ 3 , 8 ]<- 0
PSI1 [ 3 , 9 ]<- 0
PSI1 [ 3
            10 ]<- 0
PSI1 [ 3 , 11 ]<- 0
PSI1 [ 3 , 12 ]<- kappa #0
PSI1 [ 3 , 13 ]<- 0
PSI1 [
      4,
             1
                ]<- 0
PSI1 [ 4 ,
             2 ]<- 0
PSI1 [ 4 ,
            3 ]<- 0
PSI1 [ 4
            4 ]<- 0
PSI1 [ 4 , 5 ]<- 0
PSI1 [ 4 , 6 ]<- 0
PSI1 [ 4
            7 1<- 0
PSI1 [
      4
            8 ]<- 0
PSI1 [
      4 , 9 ]<- 0
PSI1 [ 4 , 10 ]<- 0
          , 11 ]<- 0
PSI1 [ 4
PSI1 [
      4 , 12 ]<- 1
PSI1 [ 4 , 13 ]<- 0
PSI1 [ 5 , 1 ]<- 0
            2 ]<- 0
PSI1 [
      5
PSI1 [ 5 ,
            3 ]<- 0
PSI1 [ 5 , 4 ]<- s[1] # litter of 1, cub survives
PSI1 [ 5
            5 ]<- 0
         , 6 ]<- 0
PSI1 [ 5
PSI1 [ 5 , 7 ]<- 0
PSI1 [ 5 , 8 ]<- 1-s[1] #litter of 1, cub dies
PSI1 [ 5
            9 1<- 0
PSI1 Γ
      5 , 10 ]<- 0
PSI1 [ 5 , 11 ]<- 0
            12 ]<- 0
PSI1 [ 5
PSI1 [ 5
          , 13 ]<- 0
       6 , 1 ]<- 0
PSI1 [
PSI1 [ 6
            2 ]<- 0
          ,
PSI1
    6
            3
               ]<- 0
PSI1 [ 6 , 4 ]<- 2*s[2]*(1-s[2]) # litter of 2, 1 cub survives
PSI1 [
            5 ]<- s[2]^2 # litter of 2, both cubs survive
```

```
PSI1 [ 6
                  6
                     ]<- 0
                  7
     [
                     ]<- 0
PSI1
          6
PSI1
     [
                  8
                     ] \leftarrow (1-s[2]^2 -2*s[2]*(1-s[2])) #litter of 2, both cubs die
PSI1
      6
                  9
                     ]<- 0
PSI1
      Ε
          6
                  10 ]<- 0
      Ε
          6
                     ]<- 0
PSI1
                  11
PSI1
     [
          6
                  12 ]<- 0
PSI1 [
                     ]<- 0
          6
                  13
PSI1
     [
          7
                  1
                     ]<- 0
      Γ
          7
                  2
                     1<- 0
PSI1
      Ε
          7
                  3
                     ]<- 0
PSI1
      Ε
         7
                  4
                     ]<- 0
PSI1
     5
PSI1
         7
                     ]<- 0
PSI1
     Ε
         7
                  6
                     ]<- s[3] # litter of 1, yearling survives</pre>
     [
         7
                 7
                     ]<- 0
PSI1
     Ε
                  8
                     ]<- 0
PSI1
         7
     [
         7
                  9
                     ] \leftarrow (1-s[3])  # litter of 1, yearling dies
PSI1
PSI1
     [
         7
                 10 ]<- 0
PSI1
     Ε
          7
                  11
                     ]<- 0
     [
         7
                  12 ]<- 0
PSI1
PSI1
     [
          7
                  13
                     ]<- 0
     [
PSI1
          8
                  1
                      ]<- 0
     [
                  2
                     1<- 0
PSI1
          8
     Γ
          8
                  3
                     1<- 0
PSI1
                     ]<- 0
PSI1
      8
                  4
     Ε
          8
                  5
                     ]<- 0
PSI1
PSI1
     8
                  6
                     ] \leftarrow 2*s[4]*(1-s[4]) # litter of 2, 1 yearling survives
                 7
                     ]<- s[4]^2 # litter of 2, both yearlings survive
PSI1
     [
         8
PSI1
     8
                  8
                     ]<- 0
     9
                     < (1-s[4]^2 -2*s[4]*(1-s[4])) #litter of 2, both yearlings die
PSI1
          8
     8
                  10 ]<- 0
PSI1
                     ]<- 0
PSI1
      Ε
          8
                  11
      [
                     ]<- 0
PSI1
          8
                  12
PSI1 [
          8
                  13
                     ]<- 0
PSI1
     [
                     ]<- 0
          9
                  1
PSI1
     [
          9
                  2
                     ]<- 0
     [
          9
                  3
                     ]<- 0
PSI1
PSI1
     9
                  4
                     ]<- 0
PSI1
     Ε
          9
                  5
                     1<- 0
PSI1
      Γ
          9
                  6
                     1<- 0
PSI1
     9
                  7
                     ]<- 0
                     1<- 0
PSI1
     Ε
         9
                  8
                     ]<- 0
PSI1
     [
          9
                  9
PSI1
     9
                  10
                     ]<- 1
     9
                  11 ]<- 0
PSI1
     Ε
                  12 ]<- 0
PSI1
          9
     [
PSI1
          9
                  13
                     ]<- 0
PSI1 [
         10 , 1
                     ]<- 0
```

```
PSI1 [ 10 , 2 ]<- 0
    [
PSI1
        10
               3
                  ]<- 0
PSI1 [
               4
                 ]<- 0
        10
PSI1 [
        10
               5
                 ]<- 0
PSI1
    10
               6
                 ]<- 0
PSI1
    [
        10
              7
                  ]<- 0
PSI1 [
        10
              8
                 ]<- 0
PSI1 [
        10
              9 ]<- 0
              10 ]<- 0
PSI1 [
        10
PSI1 Γ
        10
               PSI1 [
        10
               12 ]<- 0
PSI1 [
              13 ]<- 0
        10
PSI1 [
        11
                  ]<- 0
               1
PSI1 [
               2
                 ]<- 0
        11 ,
PSI1 [
        11 ,
               3
                 ]<- 0
PSI1
    [
               4
                  ]<- 0
        11
PSI1 [
        11 ,
                 ]<- 0
               5
PSI1 [
        11 ,
               6
                 ]<- 0
PSI1
    Ε
        11 ,
              7
                 ]<- 0
PSI1
    11
              8
                  ]<- 0
PSI1 [
        11 ,
              9
                 ]<- 0
        11 ,
PSI1 [
             10 ]<- 0
PSI1 [
              11 ]<- 0
        11 ,
PSI1 [
        11
               12 ]<- 1
PSI1 [
              13 ]<- 0
        11 ,
                  ]<- 0
PSI1 [
        12
               1
PSI1
    [
        12
               2
                  ]<- 0
PSI1
    [
        12
               3
                 ]<- 0
PSI1 [
                 ]<- 0
        12
              4
PSI1 [
        12
              5
                 ]<- 0
PSI1 [
              6
                 ]<- 0
        12
PSI1 [
        12 ,
             7
                 ]<- 0
PSI1 [
        12 ,
             8
                 ]<- 0
    [
        12
              9
                 ]<- 0
PSI1
PSI1 [
        12 ,
             10 ]<- 0
        12 ,
PSI1 [
             11 ]<- 0
PSI1 [
              12 ]<- 0
        12
PSI1 [
        12 ,
              13 ]<- 1
# PSI2: breeding probabilities:
PSI2 [ 1 , 1
                  ]<- 1
    Γ
               2
PSI2
        1
                  1<- 0
PSI2 [
      1
               3
                 ]<- 0
PSI2 [
              4
                 1<- 0
      1
PSI2 [
                 ]<- 0
        1
             5
PSI2 [
       1
              6
                 ]<- 0
PSI2 [ 1 ,
             7 ]<- 0
PSI2 [
             8 ]<- 0
        1
    [
PSI2
        1
             9
                 ]<- 0
PSI2 [
        1 , 10 ]<- 0
PSI2 [
        1
             11 ]<- 0
```

```
PSI2 [ 1 , 12 ]<- 0
     [
                13 ]<- 0
PSI2
         1
PSI2
     [
                14 ]<- 0
        1
PSI2
    1
                15 ]<- 0
PSI2
     [
         1
                16 ]<- 0
PSI2 [
        2
                   ]<- 0
                1
PSI2 [
         2
                2
                   ]<- 1
     Ε
                   ]<- 0
PSI2
         2
                3
PSI2
     [
         2
                4
                   ]<- 0
PSI2 [
         2
                5 ]<- 0
PSI2 [
        2
                6 ]<- 0
     [
         2
               7
                  ]<- 0
PSI2
PSI2
     2
               8
                  ]<- 0
         2
                9 ]<- 0
PSI2
    [
PSI2
     2
               10 ]<- 0
PSI2
     2
                11 ]<- 0
     [
                12 ]<- 0
PSI2
        2
    [
         2
                13 ]<- 0
PSI2
PSI2
     [
         2
               14 ]<- 0
PSI2
     2
               15 ]<- 0
PSI2 [
               16 ]<- 0
         2
PSI2 [
                   ]<- 0
         3
                1
     Ε
PSI2
        3
                2
                   ]<- 0
PSI2 [
                  ]<- 1
         3
                3
PSI2 [
        3
                4
                  1<- 0
                  ]<- 0
PSI2
     [
         3
                5
PSI2
     [
        3
                6
                   ]<- 0
               7
PSI2 [
         3
                  ]<- 0
PSI2
    [
        3
               8
                  ]<- 0
                  ]<- 0
PSI2
     [
         3
                9
     10 ]<- 0
PSI2
        3
PSI2 [
         3
                11 ]<- 0
               12 ]<- 0
PSI2
     [
         3
     [
         3
               13 ]<- 0
PSI2
PSI2 [
        3
               14 ]<- 0
PSI2
    [
        3
               15 ]<- 0
PSI2 [
               16 ]<- 0
        3
PSI2 [
                   ]<- 0
         4
                1
PSI2 [
         4
                2
                   ]<- 0
PSI2
     Ε
         4
                3
                   ]<- 0
PSI2
     Γ
         4
                4
                   ]<- 1
PSI2 [
         4
                5
                  ]<- 0
PSI2 [
                 ]<- 0
         4
               6
               7
                  ]<- 0
PSI2
     [
         4
PSI2
     [
        4
                8
                  ]<- 0
PSI2 [
                9 ]<- 0
         4
PSI2 [
               10 ]<- 0
         4
PSI2
     4
               11 ]<- 0
PSI2 [
         4
               12 ]<- 0
PSI2 [
                13 ]<- 0
```

```
PSI2 [ 4 , 14 ]<- 0
     [
                15 ]<- 0
PSI2
         4
PSI2
     [
                16
                   ]<- 0
         4
PSI2
     5
                1
                    ]<- 0
PSI2
     Ε
         5
                2
                    ]<- 0
PSI2
     [
         5
                3
                    ]<- 0
PSI2
     [
         5
                4
                   ]<- 0
                   ]<- 1
PSI2
     [
                5
         5
PSI2
     5
                6
                    ]<- 0
PSI2 [
         5
                7
                  ]<- 0
     [
                8 ]<- 0
PSI2
         5
     Ε
                9 ]<- 0
PSI2
         5
PSI2
     Ε
         5
                10 ]<- 0
PSI2
     5
                11 ]<- 0
PSI2
     Ε
         5
                12 ]<- 0
PSI2
     [
         5
                13 ]<- 0
     [
                14 ]<- 0
PSI2
         5
PSI2 [
         5
                15 ]<- 0
                16 ]<- 0
PSI2
     [
         5
PSI2
                    ]<- 0
     6
                1
PSI2
     Ε
         6
                2
                    ]<- 0
PSI2
     3
                   ]<- 0
         6
     [
PSI2
         6
                4
                    ]<- 0
PSI2 [
                  ]<- 0
         6
                5
PSI2 [
         6
                6
                  <- 1
                7
                   ]<- 0
PSI2
     6
PSI2
     Ε
         6
                8
                    ]<- 0
PSI2
     [
         6
                9
                   ]<- 0
PSI2
                10 ]<- 0
     [
         6
PSI2
     [
         6
                11 ]<- 0
     [
                12 ]<- 0
PSI2
         6
PSI2
     [
         6
                13 ]<- 0
                14 ]<- 0
PSI2
     Ε
         6
     15 ]<- 0
PSI2
         6
PSI2 [
         6
                16 ]<- 0
PSI2
     [
         7
                    ]<- 0
                1
PSI2
     Ε
         7
                2
                    ]<- 0
PSI2 [
         7
                3
                   ]<- 0
PSI2 [
         7
                4
                   ]<- 0
PSI2
     Ε
         7
                5
                   ]<- 0
PSI2
     Γ
         7
                6
                    ]<- 0
PSI2 [
         7
                7
                   ]<- 1
PSI2 [
         7
                8
                   ]<- 0
     [
         7
                   ]<- 0
PSI2
                9
PSI2
     [
         7
                10 ]<- 0
PSI2 [
                11 ]<- 0
         7
PSI2 [
         7
                12 ]<- 0
         7
PSI2
     13 ]<- 0
     [
         7
PSI2
                14 ]<- 0
PSI2 [
         7
                15 ]<- 0
```

```
PSI2 [ 7 , 16 ]<- 0
PSI2
                   ]<- 0
    [
         8
                1
                2
PSI2
    8
                   ]<- 0
PSI2
     Γ
         8
                3
                   ]<- 0
PSI2
     Ε
         8
                4
                   ]<- 0
PSI2 [
         8
                5
                   ]<- 0
PSI2 [
        8
                  ]<- 0
               7
                  ]<- 0
PSI2 [
        8
PSI2
    Γ
        8
                8
                  ]<- beta[1]
                9 ]<- 1-beta[1]
PSI2 [
        8
PSI2 [
                10 ]<- 0
        8
                11 ]<- 0
     Ε
PSI2
        8
PSI2
     8
                12 ]<- 0
PSI2 [
        8
               13 ]<- 0
PSI2 [
        8
               14 ]<- 0
PSI2
    [
               15 ]<- 0
        8
PSI2 [
                16 ]<- 0
        8
                   ]<- 0
PSI2
     9
                1
PSI2
     Γ
         9
                2
                   ]<- 0
PSI2
     [
         9
                3
                   ]<- 0
PSI2 [
         9
                4
                  ]<- 0
PSI2 [
                5
                  ]<- 0
        9
PSI2 [
        9
                6
                   ]<- 0
PSI2 [
                7 ]<- 0
        9
PSI2 [
        9
                8 1<- 0
                9 ]<- 0
PSI2
    9
PSI2 [
        9
                10 ]<- beta[2]
        9
                11 ]<- 1-beta[2]
PSI2 [
PSI2 [
               12 ]<- 0
        9
               13 ]<- 0
PSI2 [
        9
PSI2
    Г
                14 ]<- 0
        9
PSI2 [
         9
              15 ]<- 0
PSI2 [
               16 ]<- 0
         9
PSI2 [
         10
                1
                   ]<- 0
PSI2 [
         10
                2
                   ]<- 0
PSI2 [
                   ]<- 0
         10
                3
PSI2
    10
                4
                   ]<- 0
PSI2 [
                5
                  ]<- 0
         10
PSI2 [
         10
                6
                  ]<- 0
PSI2
    [
         10
                7
                   ]<- 0
PSI2
     Γ
         10
                8
                   1<- 0
PSI2 [
         10
                9
                  ]<- 0
PSI2 [
                10 ]<- 0
        10
                11 ]<- 0
PSI2 [
         10
        10
PSI2
    [
                12 ]<- beta[3]
PSI2 [
               13 ]<- 1-beta[3]
        10
PSI2 [
         10 ,
               14 ]<- 0
    [
PSI2
         10
               15 ]<- 0
PSI2 [
              16 ]<- 0
         10 ,
```

```
PSI2 [ 11 , 1 ]<- 0
PSI2 [ 11 ,
             2 ]<- 0
PSI2 [ 11 , 3 ]<- 0
PSI2 [ 11 , 4 ]<- 0
PSI2 [ 11 ,
            5 ]<- 0
      11 , 6 ]<- 0
PSI2 [
PSI2 [ 11 , 7 ]<- 0
PSI2 [ 11 , 8 ]<- 0
PSI2 [ 11 , 9 ]<- 0
PSI2 [ 11 , 10 ]<- 0
PSI2 [ 11 , 11 ]<- 0
PSI2 [ 11 , 12 ]<- beta[3]
PSI2 [ 11 , 13 ]<- 1-beta[3]
PSI2 [ 11 , 14 ]<- 0
PSI2 [ 11 , 15 ]<- 0
PSI2 [ 11 ,
            16 ]<- 0
PSI2 [ 12 , 1 ]<- 0
PSI2 [ 12 , 2 ]<- 0
PSI2 [ 12 ,
            3 ]<- 0
PSI2 [ 12 , 4 ]<- 0
PSI2 [ 12 , 5 ]<- 0
PSI2 [ 12 , 6 ]<- 0
PSI2 [ 12 , 7 ]<- 0
PSI2 [ 12 , 8 ]<- 0
PSI2 [ 12 , 9 ]<- 0
PSI2 [ 12 , 10 ]<- 0
PSI2 [ 12 , 11 ]<- 0
PSI2 [ 12 , 12 ]<- 0
PSI2 [ 12 , 13 ]<- 0
PSI2 [ 12 , 14 ]<- beta[3]
PSI2 [ 12 , 15 ]<- 1-beta[3]
PSI2 [ 12 , 16 ]<- 0
PSI2 [ 13 , 1 ]<- 0
PSI2 [ 13 , 2 ]<- 0
PSI2 [ 13 , 3 ]<- 0
PSI2 [ 13 , 4 ]<- 0
PSI2 [ 13 , 5 ]<- 0
PSI2 [ 13 , 6 ]<- 0
PSI2 [ 13 , 7 ]<- 0
PSI2 [ 13 , 8 ]<- 0
PSI2 [ 13 ,
            9 1<- 0
PSI2 [ 13 , 10 ]<- 0
PSI2 [ 13 , 11 ]<- 0
PSI2 [ 13 , 12 ]<- 0
PSI2 [ 13 , 13 ]<- 0
PSI2 [ 13 , 14 ]<- 0
PSI2 [ 13 , 15 ]<- 0
PSI2 [ 13 , 16 ]<- 1
# PSI3:litter size probabilities
PSI3 [ 1 , 1 ]<- 0
```

```
PSI3 [ 1 , 2 ]<- 1
                   ]<- 0
PSI3
     1
PSI3
    [
                4
                   ]<- 0
        1
PSI3
        1
                5
                   ]<- 0
PSI3
     [
        1
               6
                   ]<- 0
PSI3
     1
               7
                   ]<- 0
PSI3 [
               8
                  ]<- 0
        1
PSI3
    [
        1
               9
                 ]<- 0
               10 ]<- 0
PSI3
    [
        1
PSI3
    1
               11 ]<- 0
PSI3 [
        1
               12 ]<- 0
                   ]<- 0
PSI3
     2
               1
PSI3
     Ε
         2
                2
                   ]<- 0
        2
PSI3
     3
                   ]<- 1
PSI3
     2
               4
                  ]<- 0
PSI3
     [
        2
               5
                   ]<- 0
                  ]<- 0
PSI3
    [
        2
               6
    [
        2
               7 ]<- 0
PSI3
PSI3
    [
        2
               8 ]<- 0
PSI3
     2
               9
                  ]<- 0
PSI3 [
        2
               10 ]<- 0
PSI3
    2
               11 ]<- 0
PSI3
    [
        2
               12 ]<- 0
                   ]<- 0
PSI3 [
        3
               1
PSI3 [
        3
               2
                  1<- 0
            ,
                   ]<- 0
PSI3
     3
               3
PSI3
     Ε
        3
               4
                   ]<- 1
PSI3
    [
        3
               5
                  ]<- 0
PSI3
        3
                 ]<- 0
    6
PSI3
    [
        3
               7
                  ]<- 0
    [
               8
                  ]<- 0
PSI3
        3
PSI3 [
        3
               9 ]<- 0
               10 ]<- 0
PSI3
    3
     [
        3
               11 ]<- 0
PSI3
PSI3 [
               12 ]<- 0
         3
PSI3
    [
                   ]<- 0
         4
               1
PSI3
     4
               2
                   ]<- 0
PSI3
    [
               3
                  ]<- 0
        4
PSI3 [
        4
               4 ]<- 0
PSI3
    4
               5
                  ]<- 0
PSI3
     Γ
        4
               6
                   ]<- 0
PSI3 [
        4
               7
                 ]<- 1
PSI3 [
               8
                 ]<- 0
        4
                  ]<- 0
PSI3
    [
        4
               9
PSI3
    [
        4
               10 ]<- 0
        4 ,
               11 ]<- 0
PSI3 [
PSI3 [
               12 ]<- 0
        4
                   ]<- 0
PSI3 [
        5
               1
PSI3 [
               2 ]<- 0
```

```
PSI3 [
         5
                 3
                     ]<- 0
PSI3
     [
         5
                     ]<- 0
     [
PSI3
         5
                 5
                     ]<- 0
PSI3 [
                     ]<- 0
PSI3
     5
                 7
                     ]<- 0
PSI3
      Ε
         5
                 8
                     ]<- 1
PSI3 [
         5
                 9
                     ]<- 0
PSI3
     [
         5
                 10 ]<- 0
     [
                 11 ]<- 0
PSI3
         5
PSI3
     5
                 12
                    ]<- 0
PSI3
     Ε
                     ]<- 0
         6
                 1
                 2
PSI3
      Е
                     ]<- 0
         6
PSI3
      Γ
         6
                 3
                     ]<- 0
PSI3
     [
         6
                     ]<- 0
                 4
PSI3
     [
         6
                 5
                     ]<- 0
PSI3
     [
         6
                 6
                     ]<- 0
     [
                 7
                     ]<- 0
PSI3
         6
PSI3 [
         6
                 8
                     ]<- 0
PSI3
     [
         6
                 9
                     ]<- 1
PSI3
      Γ
         6
                 10 ]<- 0
PSI3 [
         6
                 11 ]<- 0
PSI3
     [
                 12
                    ]<- 0
PSI3 [
                     ]<- 0
         7
                 1
PSI3 [
                 2
                     ]<- 0
         7
PSI3 [
         7
                 3
                     ]<- 0
     Ε
         7
                     ]<- 0
PSI3
                 4
PSI3
     Ε
         7
                 5
                     ]<- 0
PSI3 [
                 6
                     ]<- 0
         7
PSI3 [
         7
                 7
                     ]<- 0
                     ]<- 0
PSI3 [
         7
                 8
PSI3 [
         7
                 9
                     ]<- 0
PSI3 [
         7
                 10 ]<- 1
PSI3 [
         7
                 11 ]<- 0
     Ε
         7
PSI3
                 12
                    ]<- 0
PSI3
      Γ
                     ]<- 0
         8
                 1
                     ]<- 0
PSI3
     [
         8
                 2
                     ]<- 0
PSI3
     8
                 3
                     ]<- 0
PSI3 [
         8
                 4
                     ]<- gamma[1]
PSI3 [
         8
                 5
PSI3
     Ε
         8
                 6
                     ]<- 1-gamma[1]
PSI3
     Ε
         8
                 7
                     ]<- 0
                     ]<- 0
PSI3 [
         8
                 8
PSI3 [
         8
                 9
                     ]<- 0
                 10 ]<- 0
     PSI3
         8
PSI3
     [
         8
                 11 ]<- 0
PSI3 [
                 12 ]<- 0
         8
PSI3
      ]<- 0
         9
                 1
PSI3 [
         9
                 2
                     ]<- 0
PSI3 [
                     ]<- 0
```

```
PSI3 [ 9
                4
                    ]<- 0
PSI3 [
                5
                    ]<- 0
         9
PSI3 [
                    ]<- 0
         9
                6
                7
PSI3 [
                    ]<- 0
PSI3 [
         9
                8
                   ]<- 0
PSI3
     [
         9
                9
                   ]<- 0
PSI3 [
         9
                10 ]<- 0
PSI3 [
         9
                11 ]<- 1
PSI3 [
                12 ]<- 0
         9
PSI3 [
         10
                1
                    ]<- 0
PSI3 [
         10
                2
                    ]<- 0
                    ]<- 0
     Ε
                3
PSI3
         10
PSI3
     10
                4
                    ]<- 0
PSI3 [
                    ]<- gamma[1]
         10
                5
PSI3 [
         10
                6
                   ]<- 1-gamma[1]
                    ]<- 0
PSI3 [
                7
         10
PSI3 [
                8
                   ]<- 0
         10
PSI3 [
                9 ]<- 0
         10
                10 ]<- 0
PSI3
     10
PSI3 [
         10
                11 ]<- 0
PSI3 [
                12 ]<- 0
         10
                    ]<- 0
PSI3 [
         11
                1
PSI3 [
                2
         11
                    ]<- 0
PSI3 [
                3
                    ]<- 0
         11
PSI3 [
         11 ,
                4
                    1<- 0
PSI3 [
                    ]<- 0
         11
                5
PSI3 [
         11
                6
                    ]<- 0
PSI3 [
                7
                    ]<- 0
         11
PSI3 [
         11 ,
                8
                    ]<- 0
                    ]<- 0
PSI3 [
         11
                9
PSI3 [
                10 ]<- 0
         11
PSI3 [
         11 ,
                11 ]<- 1
PSI3 [
         11 ,
                12 ]<- 0
                    ]<- 0
PSI3 [
         12
                1
PSI3 [
         12
                2
                    ]<- 0
                    ]<- 0
PSI3 [
         12
                3
PSI3 [
         12
                4
                    ]<- 0
PSI3 [
         12
                5
                    ]<- gamma[2]
PSI3 [
         12 ,
                6
                    ]<- 1-gamma[2]
PSI3 [
         12
                7
                    ]<- 0
PSI3 [
                    1<- 0
         12
                8
         12 ,
                9
                   ]<- 0
PSI3 [
PSI3 [
         12 ,
                10 ]<- 0
                11 ]<- 0
PSI3 [
         12
PSI3 [
         12
                12 ]<- 0
PSI3 [
         13 ,
                    ]<- 0
                1
                2
PSI3 [
                    ]<- 0
         13
PSI3 [
         13
                3
                    ]<- 0
PSI3 [
         13 ,
                    ]<- 0
```

```
PSI3 [ 13 , 5 ]<- 0
PSI3 [
       13
              6 ]<- 0
PSI3 [ 13 ,
             7
               ]<- 0
PSI3 [ 13 ,
            8 ]<- 0
PSI3 [ 13 ,
             9 ]<- 0
          , 10 ]<- 0
PSI3 [
       13
PSI3 [ 13 , 11 ]<- 1
PSI3 [ 13 ,
            12 ]<- 0
PSI3 [
      14 , 1 ]<- 0
PSI3 [ 14 , 2 ]<- 0
PSI3 [ 14 ,
            3 1<- 0
             4 ]<- 0
PSI3 [
      14
PSI3 [ 14 , 5 ]<- gamma[2]
PSI3 [ 14 , 6 ]<- 1-gamma[2]
PSI3 [ 14 ,
            7 ]<- 0
          , 8 ]<- 0
PSI3 [
      14
PSI3 [ 14 , 9 ]<- 0
PSI3 [ 14 , 10 ]<- 0
PSI3 [ 14 , 11 ]<- 0
PSI3 [
       14 , 12 ]<- 0
PSI3 [ 15 , 1 ]<- 0
PSI3 [ 15 ,
            2 ]<- 0
          , 3
PSI3 [ 15
                ]<- 0
PSI3 [ 15 , 4 ]<- 0
PSI3 [ 15 , 5 ]<- 0
PSI3 [
      15 ,
            6 ]<- 0
PSI3 [ 15 , 7 ]<- 0
PSI3 [ 15 , 8 ]<- 0
PSI3 [ 15 , 9 ]<- 0
          , 10 ]<- 0
PSI3 [
      15
PSI3 [ 15 , 11 ]<- 1
PSI3 [ 15 , 12 ]<- 0
                ]<- 0
PSI3 [
       16 , 1
PSI3 [
      16 , 2 ]<- 0
PSI3 [ 16 , 3 ]<- 0
            4 ]<- 0
      16 ,
PSI3 [
          , 5]<-0
PSI3 [
      16
PSI3 [ 16 , 6 ]<- 0
PSI3 [ 16 , 7 ]<- 0
PSI3 [ 16 ,
            8 1<- 0
          , 9 ]<- 0
PSI3 [
       16
       16 , 10 ]<- 0
PSI3 [
       16 ,
            11 ]<- 0
PSI3 [
PSI3 [
       16,
            12 ]<- 1
# Matrix product for state-to-state transitions S
S[1:12,1:12] <- PHI[1:12,1:12] %*% PSI1[1:12,1:13] %*% PSI2[1:13,1:16] %*% PSI3[1:16,1:12]
## Observation process: Define probabilities of E(t) given S(t).
```

```
#for initial capture, conditional on first capture
      [
                  1
                      ]<- 0
ΕO
          1
      Е
                  2
                      <- 1
ΕO
          1
                      1<- 0
ΕO
      Ε
          1
                  3
ΕO
      Е
                      ]<- 0
          1
                  4
ΕO
      Ε
          1
                  5
                      ]<- 0
ΕO
      ]<- 0
          1
                  6
ΕO
      Ε
          1
                  7
                      ]<- 0
                      ]<- 0
ΕO
      Ε
          1
                  8
ΕO
      Е
          1
                  9
                      ]<- 0
ΕO
      ]<- 0
          1
                  10
ΕO
      1
                  11
                      ]<- 0
ΕO
      ]<- 0
          1
                  12
ΕO
      2
                      ]<- 0
                  1
ΕO
      2
                  2
                      ]<- 0
      Е
          2
                      ]<- 1
ΕO
                  3
ΕO
      Е
          2
                  4
                      ]<- 0
ΕO
      2
                  5
                      ]<- 0
ΕO
      Ε
          2
                  6
                      ]<- 0
ΕO
      Ε
          2
                  7
                      ]<- 0
ΕO
      Ε
          2
                  8
                      ]<- 0
          2
      Ε
ΕO
                  9
                      ]<- 0
      2
                  10 ]<- 0
ΕO
      2
ΕO
                  11
                      ]<- 0
ΕO
      Е
          2
                  12
                      ]<- 0
ΕO
      Е
                      ]<- 0
          3
                  1
ΕO
      3
                  2
                      ]<- 0
ΕO
      3
                  3
                      ]<- 0
ΕO
      Е
          3
                  4
                      ]<- 1
      Е
          3
                  5
                      ]<- 0
ΕO
      Е
ΕO
          3
                  6
                      ]<- 0
      Е
          3
E0
                  7
                      ]<- 0
ΕO
      Е
          3
                  8
                      ]<- 0
      3
                      ]<- 0
ΕO
                  9
ΕO
      Ε
          3
                  10
                     ]<- 0
          3
ΕO
      Ε
                  11 ]<- 0
ΕO
      Ε
          3
                  12 ]<- 0
ΕO
      Е
          4
                  1
                      ]<- 0
ΕO
      4
                  2
                      ]<- 0
ΕO
      Е
                      ]<- 0
          4
                  3
      Е
ΕO
          4
                  4
                      ]<- 0
ΕO
      ]<- 1
          4
                  5
ΕO
      4
                      ]<- 0
ΕO
      4
                  7
                      ]<- 0
      Е
          4
ΕO
                  8
                      ]<- 0
ΕO
      Е
          4
                  9
                      ]<- 0
                  10
ΕO
      4
                     ]<- 0
      Е
                  11 ]<- 0
ΕO
          4
E0
      Е
          4
                  12 ]<- 0
```

```
ΕO
      5
                  1
                      ]<- 0
                  2
E0
          5
                      ]<- 0
ΕO
      [
          5
                      ]<- 0
                  3
ΕO
      5
                      ]<- 0
                  4
ΕO
      5
                  5
                      ]<- 0
ΕO
      Е
          5
                  6
                      ]<- 1
ΕO
      5
                  7
                      ]<- 0
ΕO
      Ε
          5
                      ]<- 0
                  8
ΕO
      Е
          5
                      ]<- 0
                  9
      Е
ΕO
          5
                  10
                      ]<- 0
ΕO
      Е
          5
                  11
                     ]<- 0
ΕO
      5
                  12
                     ]<- 0
ΕO
      6
                      ]<- 0
                  1
ΕO
      6
                  2
                      ]<- 0
ΕO
      6
                  3
                      ]<- 0
ΕO
      6
                  4
                      ]<- 0
ΕO
      6
                  5
                      ]<- 0
ΕO
      6
                      ]<- 0
      7
ΕO
          6
                      ]<- 1
E0
      6
                  8
                      ]<- 0
ΕO
      6
                  9
                      ]<- 0
ΕO
          6
      10
                     ]<- 0
ΕO
      6
                      ]<- 0
                  11
      Ε
ΕO
          6
                  12
                      ]<- 0
ΕO
      7
                  1
                      ]<- 0
      Е
          7
                  2
                      ]<- 0
ΕO
ΕO
      Е
          7
                  3
                      ]<- 0
      ΕO
          7
                      ]<- 0
                  4
E0
      7
                  5
                      ]<- 0
      7
ΕO
                  6
                      ]<- 0
ΕO
      7
                  7
                      ]<- 0
      ΕO
          7
                  8
                      ]<- 1
ΕO
      7
                      ]<- 0
                  9
          7
      ΕO
                      ]<- 0
                  10
ΕO
      7
                      ]<- 0
                  11
ΕO
      7
                  12
                      ]<- 0
      Ε
ΕO
          8
                  1
                      ]<- 0
ΕO
      [
          8
                  2
                      ]<- 0
      Е
ΕO
          8
                  3
                      ]<- 0
ΕO
      Е
          8
                  4
                      ]<- 0
      Е
ΕO
          8
                  5
                      ]<- 0
ΕO
      Е
          8
                  6
                      ]<- 0
ΕO
      8
                  7
                      ]<- 0
      ΕO
          8
                      ]<- 0
                  8
ΕO
      8
                  9
                      ]<- 1
ΕO
      8
                     ]<- 0
                  10
ΕO
      ]<- 0
          8
                  11
      ΕO
          8
                  12
                      ]<- 0
      ΕO
          9
                      ]<- 0
```

```
ΕO
      9
                 2
                     ]<- 0
E0
          9
                      ]<- 0
ΕO
      Е
          9
                  4
                     ]<- 0
ΕO
      9
                  5
                     ]<- 0
ΕO
      9
                  6
                     ]<- 0
ΕO
      Е
          9
                 7
                      ]<- 0
ΕO
      9
                 8
                     ]<- 0
ΕO
      Ε
          9
                     ]<- 0
                 9
ΕO
      Е
          9
                 10 ]<- 1
ΕO
      9
                  11
                     ]<- 0
ΕO
      Е
          9
                  12
                     ]<- 0
                      ]<- 0
ΕO
      10
                  1
      2
ΕO
          10
                      ]<- 0
ΕO
      10
                  3
                     ]<- 0
ΕO
      10
                 4
                     ]<- 0
ΕO
      10
                 5
                      ]<- 0
ΕO
      6
                     ]<- 0
          10
      ΕO
                 7
                      ]<- 0
          10
      ΕO
          10
                 8
                     ]<- 0
ΕO
      10
                 9
                      ]<- 0
ΕO
      10
                     ]<- 0
                 10
ΕO
      10
                  11
                     ]<- 1
ΕO
      Е
                 12
                     ]<- 0
          10
ΕO
      Е
                      ]<- 0
          11
                  1
ΕO
      11
                  2
                      ]<- 0
      Е
                 3
                      ]<- 0
ΕO
          11
ΕO
      Е
          11
                 4
                     ]<- 0
      ΕO
                  5
                     ]<- 0
          11
E0
      6
                     ]<- 0
          11
      ΕO
          11
                 7
                      ]<- 0
ΕO
      8
                     ]<- 0
          11
ΕO
      11
                  9
                     ]<- 0
      ]<- 0
E0
          11
                 10
      ΕO
          11
                     ]<- 0
                  11
ΕO
      11
                  12
                     ]<- 1
      ΕO
          12
                  1
                      ]<- 1
ΕO
      12
                  2
                      ]<- 0
ΕO
      12
                  3
                     ]<- 0
      Е
ΕO
          12
                  4
                     ]<- 0
ΕO
      Ε
          12
                 5
                      ]<- 0
      Ε
ΕO
          12
                 6
                      ]<- 0
ΕO
      Е
          12
                 7
                     ]<- 0
ΕO
      Е
          12
                 8
                     ]<- 0
                      ]<- 0
ΕO
      Е
                 9
          12
ΕO
      12
                  10
                     ]<- 0
ΕO
      ]<- 0
          12
                  11
ΕO
      12 ,
                 12 ]<- 0
# departure probability of a2 offspring
for(i in 1:N){
```

```
for(t in 1:(Years-1)){
     [ 1 , 1 ,i,t]<- 1
 E1
      [
         1
                 2
                    ,i,t]<-0
                 3, i,t] < 0
 E1
       1
 E1
       [
          1
                 4, i,t] < 0
 E1
       [
          1
                 5
                    ,i,t]<- 0
 E1
       [
          1
                 6, i,t] < 0
 E1
       [
          1
                 7, i,t] < 0
       Ε
                 8, i,t] < 0
 E1
          1
 E1
       Ε
          1
                 9,i,t]<-0
 E1
      [
          1
                 10,i,t] < 0
       [
                 11,i,t]<- 0
 E1
          1
                 12,i,t]<- 0
       E1
          1
          2
                 1, i,t] < 0
 E1
      [
 E1
       [
          2
                 2, i,t] < -1
       [
          2
                 3, i,t] < 0
 E1
      [
          2
 E1
                 4 , i,t] < 0
      [
          2
                 [5, i,t] < 0
 E1
          2
       [
                 6, i,t] < 0
 E1
 E1
       Ε
          2
                 7 ,i,t] <- 0
 E1
      [
          2
                 8, i,t] < 0
          2
 E1
     [
                 9, i,t] < 0
      [
          2
                 10,i,t] < 0
 E1
                 11,i,t]<- 0
      Ε
 E1
          2
      [
          2
                 12,i,t] < 0
 E1
       [
 E1
          3
                 1, i,t] < 0
       Ε
          3
                 2, i,t] < 0
 E1
      3
 E1
                 3, i,t] < -1
      [
          3
                 4, i,t] < 0
 E1
      [
 E1
          3
                 [5, i,t] < 0
      [
          3
                    ,i,t]<- 0
 E1
                 6
                 7 , i,t] < -0
      [
          3
 E1
      [
          3
                 8 ,i,t]<- 0
 E1
       [
          3
                 9,i,t]<-0
 E1
      [
 E1
          3
                 10,i,t] < -0
 E1
      3
                 11,i,t]<-
       Ε
          3
                 12,i,t] < 0
 E1
      [
          4
                 1, i,t] < 0
 E1
 E1
     [
          4
                 2, i,t] < 0
       Ε
          4
                 3, i,t] < 0
 E1
 E1
       Γ
          4
                 4 , i,t] < -1
     [
 E1
          4
                 5, i,t] < 0
      Ε
          4
                 [6, i,t] < 0
 E1
      Ε
                 7
                     ,i,t]<-0
 E1
          4
                    ,i,t]<- 0
 E1
      4
                 8
      [
          4
                 9, i,t] < 0
 E1
       [
          4
                 10,i,t] < -0
 E1
                 11,i,t]<- 0
       E1
          4
       [
                 12,i,t]<- 0
 E1
          4,
```

```
E1
   [
         5
                 1,i,t]<-
                             0
      5
                 2,i,t] < -
E1
     [
E1
         5
                 3,i,t] < -
                             0
                 4,i,t] < -
E1
     E1
      5
                 5,i,t]<-
                             1
E1
      Ε
         5
                 6,i,t]<-
                             0
E1
     [
         5
                 7,i,t]<-
                             0
E1
     Ε
         5
                 8,i,t]<-
                             0
     [
                 9,i,t]<-
         5
                             0
E1
E1
     Ε
         5
                 10,i,t]<-
                             0
E1
     [
         5
                 11,i,t]<-
                             0
     5
                 12,i,t]<-
                             0
E1
E1
     [
         6
                    ,i,t]<-0
                 1
     [
         6
                 2, i,t] < 0
E1
E1
     [
         6
                 3, i,t] < 0
E1
     [
         6
                    ,i,t]<-0
                 4
     [
E1
         6
                 5
                    ,i,t]<- 0
     [
         6
                 6, i,t] < -1
E1
                 7, i,t] < -0
     [
         6
E1
                    ,i,t]<- 0
E1
     [
         6
                 8
     [
         6
                 9, i,t] < 0
E1
E1
     Ε
         6
                 10,i,t] < 0
                 11,i,t]<-
     [
         6
                             0
E1
     Ε
                 12,i,t]<-
E1
         6
     Ε
         7
                 1
                    ,i,t]<-0
E1
     [
         7
E1
                 2, i,t] < 0
                    ,i,t]<- 0
E1
     [
         7
                 3
     [
         7
                 4, i,t] < 0
E1
E1
     [
         7
                 [5, i,t] < 0
     [
         7
E1
                 [6, i,t] < 0
E1
     [
         7
                 7
                     ,i,t]<- 1
         7
E1
     8, i,t] < 0
     [
         7
                 9, i,t] < 0
E1
         7
     [
                 10,i,t] < -0
E1
     [
         7
                 11,i,t]<-
E1
                             0
                 12,i,t]<-
E1
     7
                    ,i,t]<-0
E1
     Ε
         8
                 1
                 [2, i,t] < 0
     [
         8
E1
     Ε
E1
         8
                 3, i,t] < 0
      Ε
         8
                 4, i,t] < 0
E1
                   ,i,t]<-0
E1
     Ε
         8
                 5
E1
     8
                 6, i,t] < 0
     [
         8
                 7 , i,t] <- 0
E1
     [
                    ,i,t]<- 1
E1
         8
                 8
                    ,i,t]<- 0
E1
     [
         8
                 9
     [
E1
         8
                 10,i,t] < 0
     [
                 11,i,t]<-
E1
         8
                             0
      12,i,t]<-
E1
         8
            , 1 ,i,t]<- 0
     [
```

```
E1
      [
          9
                  2
                    ,i,t]<- 0
      ,i,t]<-0
E1
          9
                  3
      E1
          9
                  4
                     ,i,t]<-0
      Γ
          9
E1
                  5
                     ,i,t]<-0
E1
      9
                  6
                     ,i,t]<-0
E1
      Ε
          9
                  7
                      ,i,t]<-0
E1
      [
          9
                      ,i,t]<-0
                  8
                    ,i,t]<- 1-alpha[i,t+1]
E1
      Ε
          9
                  9
      [
                  10,i,t]<-
          9
                             0
E1
E1
      9
                  11,i,t]<-
                              alpha[i,t+1]
E1
      [
          9
                  12,i,t]<-
      Е
                  1,i,t]<-
E1
          10
                              0
E1
      Γ
          10
                  2,i,t] < -
                              0
      [
                  3,i,t]<-
                              0
E1
          10
E1
      Ε
          10
                  4,i,t] < -
                              0
E1
      [
          10
                  5,i,t]<-
                              0
      Е
                  6,i,t] < -
E1
          10
                              0
      [
                  7,i,t] < -
                              0
E1
          10
E1
      10
                  8,i,t]<-
                              0
E1
      Γ
          10
                  9,i,t] < -
                              2*(1-alpha[i,t+1])*alpha[i,t+1]
E1
     [
                  10,i,t]<-
                              1 - (2*(1-alpha[i,t+1])*alpha[i,t+1]) - (alpha[i,t+1])^2
          10
E1
      10
                  11,i,t]<-
                              (alpha[i,t+1])^2
      [
          10
                  12,i,t]<-
E1
                     ,i,t]<- 0
E1
     Ε
          11 ,
                  1
          11 ,
                    ,i,t]<- 0
E1
      Ε
                  2
      Ε
E1
          11
                  3
                     ,i,t]<-0
                     ,i,t]<-0
E1
      Ε
          11
                  4
      [
          11
                    ,i,t]<- 0
E1
                  5
      [
          11
                  6
                     ,i,t]<-0
E1
E1
      [
          11
                  7
                      ,i,t]<-0
      [
          11
                      ,i,t]<-0
E1
                  8
                     ,i,t]<-0
E1
     [
          11
                  9
      E1
          11
                  10,i,t]<-
      E1
          11
                  11,i,t]<-
                              1
                  12,i,t]<-
E1
      [
          11
      [
          12
                  1
                     ,i,t]<-0
E1
E1
      12
                  2
                      ,i,t]<-0
     [
                     ,i,t]<- 0
E1
          12
                  3
     Ε
          12 ,
E1
                  4
                     ,i,t]<-0
E1
      [
          12
                  5
                      ,i,t]<-0
                      ,i,t]<-0
E1
      Γ
          12
                  6
     Ε
E1
          12
                  7
                      ,i,t]<-0
      [
          12
                  8
                     ,i,t]<- 0
E1
      [
          12
                  9
                      ,i,t]<-0
E1
E1
      12
                  10,i,t]<-
                              0
      [
          12 ,
                  11,i,t]<-
E1
                              0
          12 ,
      12,i,t]<-
E1
# for recapture probability
    [ 1 , 1 ,i,t] \leftarrow 1-p
```

```
E2
     [
         1
                 2 ,i,t]<- p
      E2
         1
                    ,i,t]<-0
                 3
      ,i,t]<- 0
E2
         1
                 4
                    ,i,t]<- 0
         1
E2
      5
E2
      1
                 6
                    ,i,t]<-0
E2
      Ε
         1
                 7
                     ,i,t]<-0
E2
     [
         1
                 8
                    ,i,t]<-0
E2
     Ε
         1
                 9, i,t] < 0
     [
                 10,i,t] < -0
E2
         1
                 11,i,t]<-
E2
     Ε
         1
                             0
E2
     [
         1
                 12,i,t]<-
                             0
      Е
         2
                    ,i,t]<- 1 -p
E2
                 1
E2
     [
         2
                 2
                    ,i,t]<-0
     [
         2
E2
                    ,i,t] \leftarrow p
                 3
E2
     2
                 4 , i,t] <- 0
E2
     [
         2
                 5
                     ,i,t]<-0
     [
         2
                    ,i,t]<- 0
E2
                 6
     [
         2
                 7
                     ,i,t]<- 0
E2
      2
                    ,i,t]<-0
E2
                 8
         2
                 9, i,t] < 0
E2
      E2
     [
         2
                 10,i,t] < -0
         2
                 11,i,t]<-
E2
      Е
                             0
E2
     [
         2
                 12,i,t]<-
                             0
                    ,i,t]<- 1 -p
E2
     3
                 1
E2
     Ε
         3
                 2
                   ,i,t]<- 0
      Е
                 3, i,t] < 0
E2
         3
E2
     [
         3
                 4
                    ,i,t]<- p
     [
         3
                 [5, i,t] < 0
E2
E2
     [
         3
                 6, i,t] < 0
     [
                 7
                     ,i,t]<-0
E2
         3
E2
     [
         3
                    ,i,t]<- 0
                 8
                 9, i,t] < 0
E2
     [
         3
                 10,i,t] < -0
     Е
         3
E2
      [
                 11,i,t]<-
E2
         3
                             0
     [
                 12,i,t]<-
E2
         3
                             0
      E2
         4
                    ,i,t]<- 1 -p
                 1
E2
      4
                 2
                     ,i,t]<-0
     [
                    ,i,t]<- 0
E2
         4
                 3
     Ε
E2
                 4
                    ,i,t]<- 0
E2
      Ε
         4
                 5
                    ,i,t]<- p
     [
E2
         4
                 6
                    ,i,t]<-0
     [
         4
                 7 , i,t] < -0
E2
E2
     [
         4
                 8, i,t] < 0
     Ε
E2
         4
                     ,i,t]<-0
                 9
E2
     [
         4
                 10,i,t]<-
                             0
E2
     [
         4
                 11,i,t]<-
                             0
E2
      4
                 12,i,t]<-
                             0
     [
         5
                 1,i,t]<-
E2
                            1 -p
      5
                 2,i,t]<-
                             0
```

```
E2
    [
         5
                 3,i,t] < -
                             0
E2
      5
                 4,i,t] < -
     [
E2
         5
                 5,i,t]<-
                             0
                 6,i,t] < -
E2
     p
E2
      5
                 7,i,t] < -
                             0
E2
      Ε
         5
                 8,i,t] < -
                             0
E2
     [
         5
                 9,i,t] < -
                             0
E2
     Ε
         5
                 10,i,t]<-
                             0
      Е
                 11,i,t]<-
E2
         5
                             0
E2
     Ε
         5
                 12,i,t]<-
                             0
     [
                    ,i,t]<- 1 -p
E2
         6
                 1
      2, i,t] < 0
E2
         6
                    ,i,t]<- 0
E2
      6
                 3
E2
     [
                    ,i,t]<-0
         6
                    ,i,t]<-0
E2
     [
         6
                 5
E2
     [
         6
                 6
                     ,i,t]<-0
     [
                 7
                    ,i,t]<- p
E2
         6
     [
         6
                    ,i,t]<-0
E2
                 9, i,t] < -0
E2
     [
         6
E2
      6
                 10,i,t] < 0
E2
     [
                 11,i,t]<-
                             0
         6
                 12,i,t]<-
E2
     6
     [
         7
E2
                 1
                    ,i,t]<- 1 -p
     [
         7
                   ,i,t]<- 0
E2
                 2
E2
     Ε
         7
                 3
                   ,i,t]<- 0
      7
E2
                 4, i,t] < 0
                    ,i,t]<- 0
E2
     [
         7
                 5
     [
         7
                 6, i,t] < -0
E2
E2
     [
         7
                 7
                     ,i,t]<-0
         7
                    ,i,t]<- p
E2
     [
                 8
E2
     [
         7
                    ,i,t]<- 0
                 9
E2
     [
         7
                 10,i,t] < 0
     [
         7
                 11,i,t]<- 0
E2
      [
         7
                 12,i,t]<-
E2
E2
     8
                 1
                    ,i,t]<- 1 -p
E2
      8
                   ,i,t]<-0
                 2
                    ,i,t]<- 0
E2
     Ε
         8
                 3
                    ,i,t]<- 0
E2
     [
         8
                 4
E2
     Ε
         8
                 5
                   ,i,t]<- 0
E2
      Ε
         8
                 6, i,t] < -0
E2
     Ε
         8
                 7
                     ,i,t]<-0
E2
     Ε
         8
                 8, i,t] < 0
     [
         8
                 9 ,i,t]<- p
E2
     [
                 10,i,t]<- 0
E2
         8
E2
     [
         8
                 11,i,t]<-
                            0
E2
     [
                 12,i,t]<-
         8
      E2
         9
                 1
                     ,i,t] <- 1-p
      2
                     ,i,t]<-0
E2
         9
      ,i,t]<-0
```

```
E2
          9
                      4
                         ,i,t]<- 0
          E2
              9
                          ,i,t]<-0
                      5
          E2
              9
                      6
                          ,i,t]<-0
          E2
                      7
                          ,i,t]<-0
    E2
          9
                      8
                          ,i,t]<-0
    E2
          Ε
              9
                      9
                          ,i,t]<-0
    E2
          [
              9
                      10,i,t]<-
                                  р
    E2
          9
                      11,i,t]<-
                                  0
                      12,i,t]<-
    E2
          9
                                  0
    E2
          10
                      1,i,t]<-
                                  1-p
          [
                      2,i,t] < -
                                  0
    E2
              10
          3,i,t]<-
    E2
              10
                                  0
    E2
          10
                      4,i,t] < -
                                  0
          [
                      5,i,t]<-
                                  0
    E2
              10
    E2
          10
                      6,i,t]<-
                                  0
    E2
          [
              10
                      7,i,t] < -
                                  0
          Е
    E2
              10
                      8,i,t]<-
                                  0
          [
                      9,i,t]<-
                                  0
    E2
              10
    E2
          10
                      10,i,t]<-
                                  0
    E2
          10
                      11,i,t]<-
                                  p
    E2
          12,i,t]<-
              10
                                  0
    E2
          [
                          ,i,t] < -1 - p
              11
                      1
                          ,i,t]<-0
    E2
          11
                      2
                         ,i,t]<-0
          [
    E2
              11
                      3
    E2
          11
                      4
                         ,i,t]<-0
          Е
    E2
              11
                      5
                          ,i,t]<-0
                          ,i,t]<-0
    E2
          Ε
              11
                      6
          [
                      7
                          ,i,t]<-0
    E2
              11
                          ,i,t]<-0
    E2
          [
                      8
              11
    E2
          [
              11
                      9
                           ,i,t]<-0
    E2
          11
                      10,i,t]<-
                                  0
    E2
          [
                      11,i,t]<-
                                  0
              11
          Е
                      12,i,t]<-
    E2
              11
                                  p
    E2
          [
              12
                      1
                          ,i,t]<-1
    E2
          Ε
              12
                      2
                          ,i,t]<-0
    E2
          [
              12
                          ,i,t]<-0
                      3
    E2
          12
                      4
                          ,i,t]<-0
                          ,i,t]<- 0
    E2
          [
              12
                      5
          [
    E2
              12
                      6
                          ,i,t]<-0
    E2
          Ε
              12
                      7
                          ,i,t]<-0
          [
                          ,i,t]<-0
    E2
              12
                      8
          [
    E2
              12
                      9
                          ,i,t]<-0
          Е
                      10,i,t]<-
                                  0
    E2
              12
          Е
              12
                      11,i,t]<-
    E2
                                  0
    E2
          12
                      12,i,t]<-
                                  0
    # Matrix product for offspring independence and recapture
    E[1:12,1:12,i,t] <- E1[1:12,1:12,i,t] %*% E2[1:12,1:12,i,t]
  }
}
```

```
## LIKELIHOOD
for (i in 1:N) # for each individual
  # The estimated probabilities of initial states SO are the proportions in each state at first captu
  alive[i,First[i]] ~ dcat(S0[1:12])
  mydata[i,First[i]] ~ dcat(E0[alive[i,First[i]],1:12])
  for (j in (First[i]+1):Years)
    ## STATE EQUATIONS ##
    # draw S(t) given S(t-1)
    alive[i,j] ~ dcat(S[alive[i,j-1],1:12])
    ## OBSERVATION EQUATIONS ##
    # draw events E(t) given states S(t)
    mydata[i,j] ~ dcat(E[alive[i,j],1:12,i,j-1])
 }
}
## PRIORS
# capture probability
p \sim dunif(0,1)
# juveniles, subadults and adult survival
#for(i in 1:2){phi[i] ~ dunif(0,1)}
phi[1] ~ dunif(0,1)
# initial states
for (i in 1:10){ log(prop[i]) <- theta[i]</pre>
theta[i] ~ dnorm(0,1)}
# offspring survival
# litter survival n=2 offspring
102 \leftarrow 1 - (1 - s[2]^2 - 2*s[2]*(1-s[2]))
112 \leftarrow 1 - (1 - s[4]^2 - 2*s[4]*(1 - s[4]))
# indiviual offspring survival
#for(i in 1:4){s[i]~ dunif(0,1)}
for(i in 1:2){s[i]~ dunif(0,1)}
  # Set constraints
  for(u in 1:2){ X[u] \sim dunif(0,1)} # with X \sim U[0,1] then (a + (b - a) * X)
  \#so that s[1] < s[3] < phi[1] for litter of 1
  s[3] \leftarrow s[1] + (phi[1] - s[1]) * X[1]
  # and s[2] < s[4] < phi[1] for litters of 2
  s[4] \leftarrow s[2] + (phi[1] - s[2]) * X[2]
# Breeding probability
kappa ~ dunif(0,1)
```

```
for(i in 1:3){beta[i]~ dunif(0,1)}

# Litter size probability
for(i in 1:2){gamma[i]~ dunif(0,1)}

} # end model
")
```

This model differs from the model used for the simulations in just a few points. It assumes breeding probability and litter size probability does not vary between successful breeders (states AS1 and AS2) and female without dependent offspring (state A) by setting  $beta_3 = beta_4$  (in the code beta[3]) and  $gamma_3 = gamma_4$  (in the code gamma[2]). It also assumes that litter size probability is the same among failed breeders (loss of cub versus yearling litter), by setting  $gamma_1 = gamma_2$  (in the code gamma[1]).

Run the jags model and save the results:

# Analyse the results

Load useful packages:

```
library(jagsUI)
library(MCMCvis)
```

Load model results and print a summary:

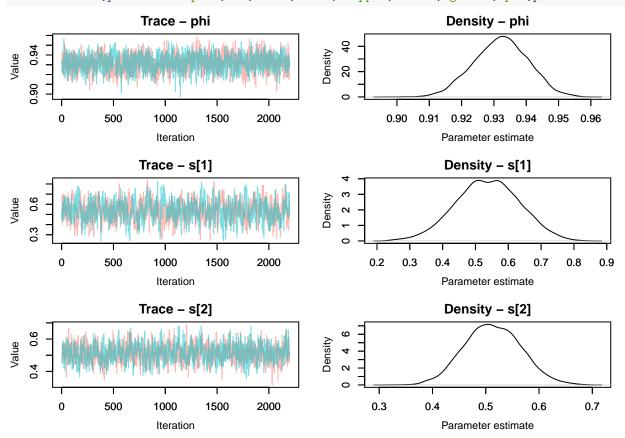
```
load(file='Fit_beardata.RData')
MCMCsummary(out,round=2)
```

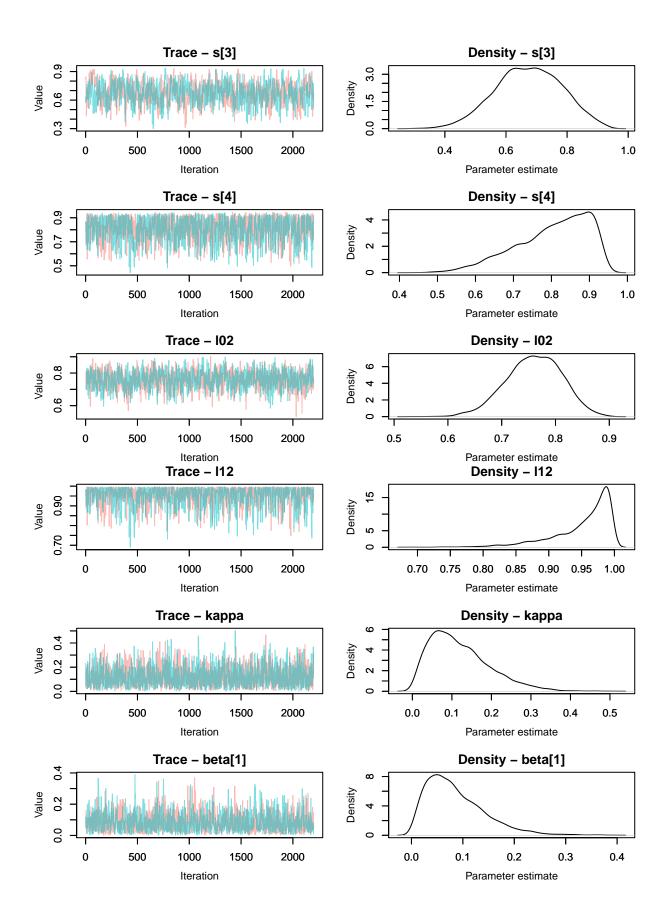
```
##
                mean
                         sd
                               2.5%
                                         50%
                                                97.5% Rhat n.eff
## phi
                0.93
                      0.01
                               0.92
                                        0.93
                                                0.95 1.00
                                                            2027
                0.54
                      0.10
                               0.34
                                        0.54
                                                            4400
## s[1]
                                                0.72 1.00
## s[2]
                0.51
                      0.05
                               0.41
                                        0.51
                                                0.62 1.00
                                                            4400
## s[3]
                0.67
                      0.11
                               0.46
                                        0.68
                                                 0.87 1.00
                                                             1458
## s[4]
                      0.09
                               0.59
                                        0.82
                                                              422
                0.80
                                                 0.93 1.01
## 102
                0.76
                      0.05
                               0.65
                                        0.76
                                                 0.85 1.00
                                                            4400
## 112
                0.95
                      0.04
                               0.83
                                        0.97
                                                 0.99 1.01
                                                              331
## kappa
                0.12
                      0.08
                               0.02
                                        0.11
                                                 0.30 1.00
                                                             4400
## beta[1]
                0.09
                      0.06
                               0.01
                                        0.07
                                                 0.23 1.00
                                                            2978
## beta[2]
                0.58
                      0.21
                               0.19
                                        0.57
                                                 0.96 1.00
                                                            4400
## beta[3]
                0.52
                      0.04
                               0.43
                                        0.52
                                                0.61 1.00
                                                            1763
## gamma[1]
                0.35
                      0.17
                               0.07
                                        0.34
                                                0.71 1.00
                                                            2652
## gamma[2]
                      0.05
                               0.30
                                                            4400
                0.40
                                        0.40
                                                0.51 1.00
                                                0.27 1.01
## p
                      0.01
                               0.22
                0.25
                                        0.25
                                                              182
                0.56
                      0.16
                               0.30
                                        0.54
                                                0.92 1.00
                                                            4400
## prop[1]
## prop[2]
                0.46
                      0.14
                               0.24
                                        0.44
                                                 0.79 1.00
                                                            4400
## prop[3]
                0.66
                      0.18
                               0.37
                                        0.63
                                                 1.08 1.00
                                                            4400
## prop[4]
                0.42
                      0.14
                               0.21
                                        0.40
                                                 0.74 1.00
                                                            4400
## prop[5]
                0.80
                      0.21
                               0.45
                                        0.77
                                                1.28 1.00 4400
```

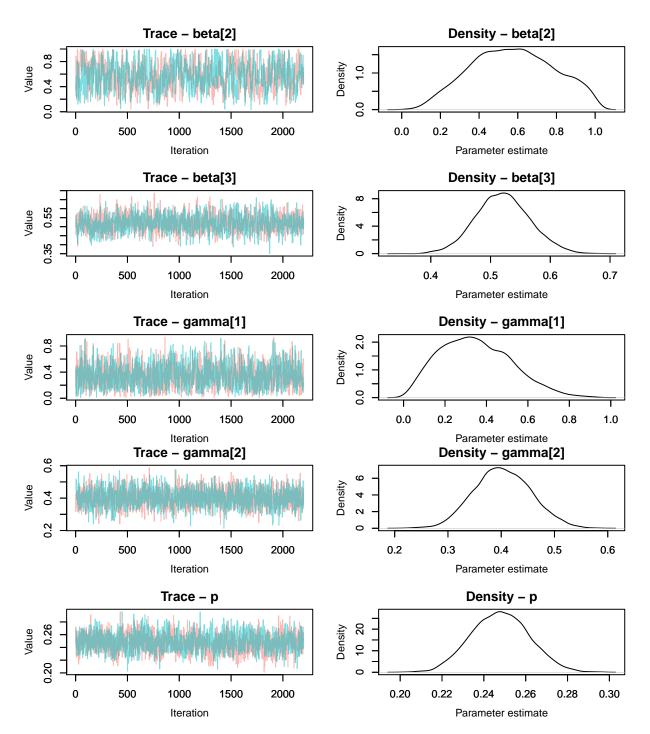
```
## prop[6]
                0.76
                      0.20
                               0.43
                                        0.74
                                                1.22 1.00
                                                            4400
## prop[7]
                0.46
                               0.24
                                                0.80 1.00
                                                            4400
                      0.15
                                        0.44
## prop[8]
                0.20
                      0.08
                               0.08
                                        0.19
                                                0.40 1.00
                                                            4400
## prop[9]
                0.20
                      0.08
                               0.08
                                        0.19
                                                0.40 1.00
                                                            4400
                0.09
## prop[10]
                      0.05
                               0.02
                                        0.08
                                                0.22 1.00
                                                            4400
## deviance 1611.02 25.81 1563.30 1609.45 1664.85 1.02
                                                             133
```

Check mixing of the chains and posterior distributions:

MCMCtrace(out,params = c('phi','s','102','112','kappa','beta','gamma','p'),pdf=FALSE)







Plot a summary of the posterior distribution for each model parameter:

```
expression(gamma[1]),expression(gamma[3]),expression(p)),
col = 'black',
sz_labels = 1.5,
sz_med = 1.5,
sz_thick = 4,
sz_thin = 2,
sz_ax = 4,
sz_main_txt = 2)
```

# Estimates φ S1 S2 S3 S4 12 12 12 71 73 P 0.0 0.0 0.2 0.4 0.6 0.8 1.0 Value

Dots represent posterior medians, thick lines represent 50 percent credible intervals while thin lines represent 95 percent credible intervals.

Calculate the probabilities of successfully raising 1 or 2 or 0 offspring to independence over a three-year period for an adult female without dependent offspring at the start of the period:

```
prx0 <- 1 -prx1 -prx2
```

Make a table with the median value and 95% credible interval for the probabilities of successfully raising 1 or 2 or 0 offspring to independence over a three-year period for an adult female without dependent offspring at the start of the period:

```
# Summary of results
tabres <- matrix(NA,3,3)
tabres[1,]<-quantile(prx0,probs=c(0.025,0.5,0.975))
tabres[2,]<-quantile(prx1,probs=c(0.025,0.5,0.975))
tabres[3,]<-quantile(prx2,probs=c(0.025,0.5,0.975))
rownames(tabres)=c("Pr(X=0)","Pr(X=1)","Pr(X=2)")
colnames(tabres)=c("Q 2.5%","Median","Q 97.5%")
round(tabres,2)</pre>
```

```
## Pr(X=0) 0.57 0.67 0.76

## Pr(X=1) 0.20 0.29 0.38

## Pr(X=2) 0.02 0.04 0.07
```

### References

Amstrup, S. C., & Durner, G. M. (1995). Survival rates of radio-collared female polar bears and their dependent young. Canadian Journal of Zoology, 73, 1312–1322. doi:10.1139/z95-155

Hornik, K., Leisch, F., & Zeileis, A. (2003). JAGS: A program for analysis of Bayesian graphical models using Gibbs sampling. In Proceedings of DSC (Vol. 2, No. 1).

Kellner, K. (2015). jagsUI: a wrapper around rjags to streamline JAGS analyses. R package version, 1(1).