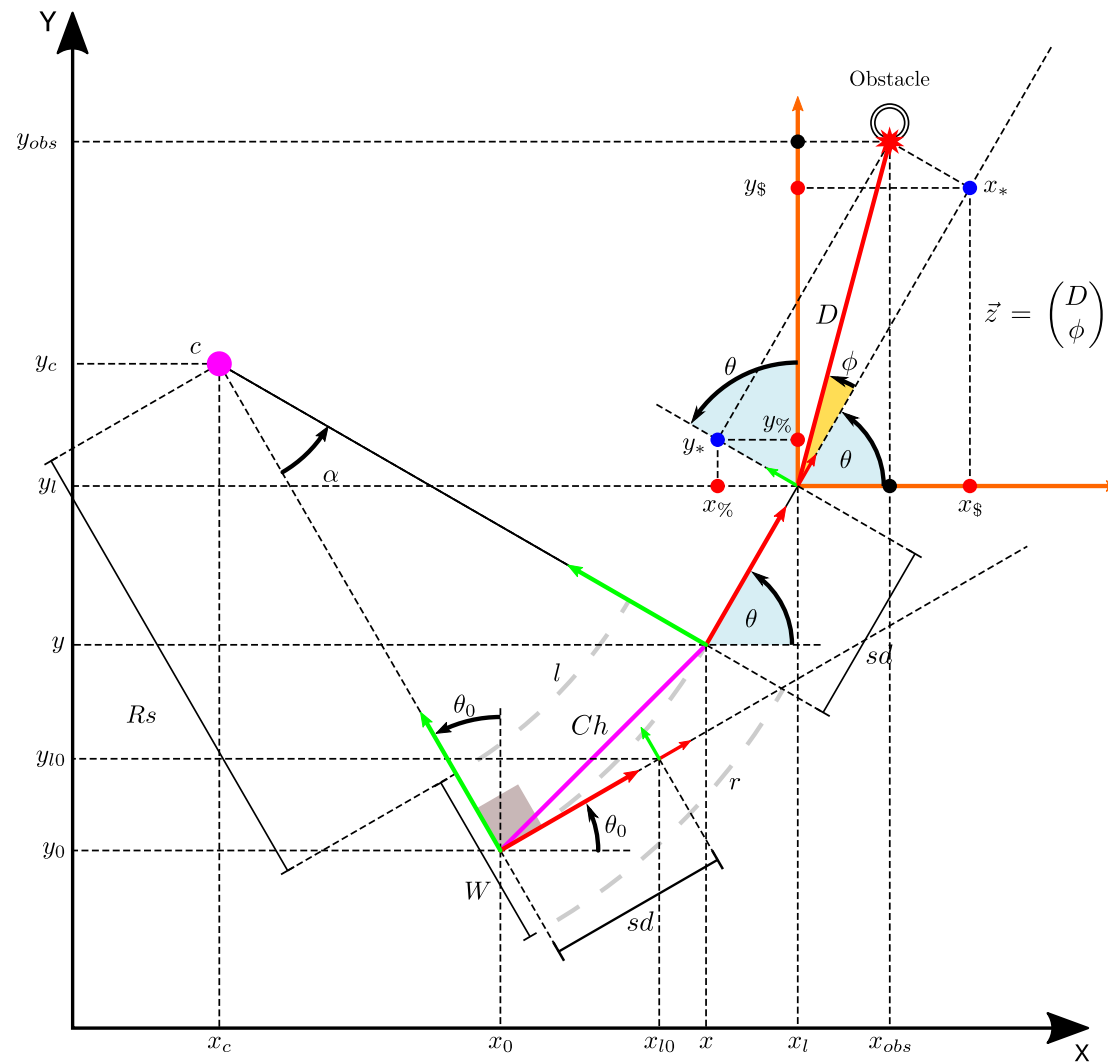


Obstacle's coordinates in the global reference frame



$$\begin{aligned}
r &= (Rs + W) \alpha \\
l &= Rs \alpha \\
r - l &= W \alpha
\end{aligned}$$

$$\begin{aligned}
\alpha &= \frac{r - l}{W} \\
Rs &= \frac{l}{\alpha}
\end{aligned}$$

$$\begin{aligned}
x_l &= x + sd \cos(\theta) \\
y_l &= y + sd \sin(\theta)
\end{aligned}$$

$$\begin{aligned}
\cos(u \pm v) &= \cos u \cos v \mp \sin u \sin v \\
\sin(u \pm v) &= \sin u \cos v \pm \cos u \sin v
\end{aligned}$$

$$\begin{aligned}
\cos(\theta + 90^\circ) &= -\sin(\theta) \\
\sin(\theta + 90^\circ) &= +\cos(\theta)
\end{aligned}$$

$$\begin{aligned}
x_{obs} &= x_l + x_{\S} + x_{\%} \\
&= x + sd \cos(\theta) + x_* \cos(\theta) + y_* \cos(\theta + 90^\circ) \\
&= x + sd \cos(\theta) + D \cos(\phi) \cos(\theta) + D \sin(\phi) \cos(\theta + 90^\circ) \\
&= x + sd \cos(\theta) + D \cos(\phi) \cos(\theta) - D \sin(\phi) \sin(\theta) \\
&= x + sd \cos(\theta) + D \cos(\theta + \phi)
\end{aligned}$$

$$\begin{aligned}
y_{obs} &= y_l + y_{\S} + y_{\%} \\
&= y + sd \sin(\theta) + x_* \sin(\theta) + y_* \sin(\theta + 90^\circ) \\
&= y + sd \sin(\theta) + D \cos(\phi) \sin(\theta) + D \sin(\phi) \sin(\theta + 90^\circ) \\
&= y + sd \sin(\theta) + D \cos(\phi) \sin(\theta) + D \sin(\phi) \cos(\theta) \\
&= y + sd \sin(\theta) + D \sin(\theta + \phi)
\end{aligned}$$