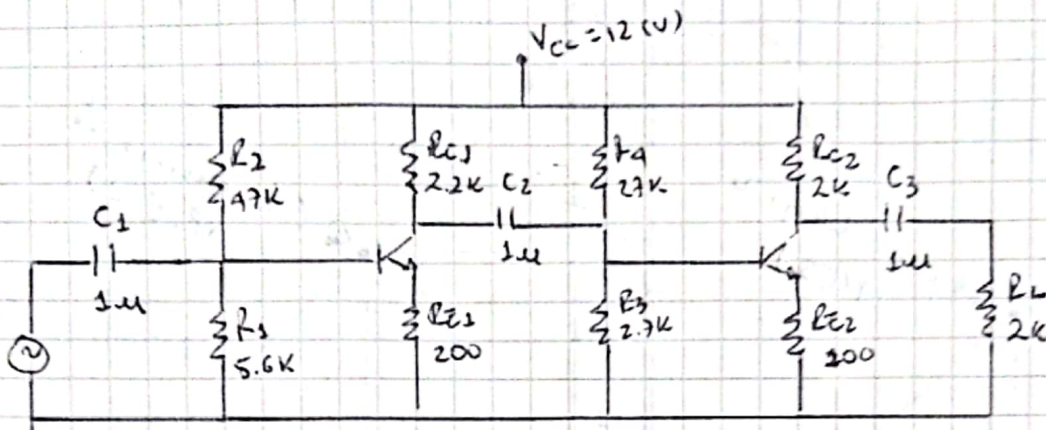


## Parcial 2B.

1.



$$\beta_1 = \beta_2 = 100$$

$$f_T = 500 \text{ MHz}$$

$$C_{bc} = 10 \text{ pF}$$

$$C_o: \text{despreciable.}$$

### Análisis D.C

Etapas 1:

$$R_{B1} = R_1 // R_2 \approx 5 \text{ K}\Omega$$

$$V_{BB1} = \frac{V_{CC} R_2}{R_1 + R_2} \approx 1.28 \text{ (V)}$$

L.V.K. mallo de entrada

$$V_{BB1} = \frac{I_{Q1} R_{B1}}{\beta} + V_{BE} + I_{Q1} R_{E1}$$

$$\Rightarrow I_{Q1} = \frac{V_{BB1} - V_{BE}}{\frac{R_{B1}}{\beta} + R_{E1}} = 2.32 \text{ mA}$$

L.V.K. mallo de salida:

$$V_{CC} = I_{Q1} R_{C1} + V_{CE1} + I_{Q1} R_{E1}$$

$$\Rightarrow V_{CE1} = V_{CC} - I_{Q1} (R_{C1} + R_{E1})$$

$$\Rightarrow V_{CE1} = 6.43 \text{ (V)}$$

$$I_{Cmax} (V_{CE1}=0) = \frac{V_{CC}}{R_{E1} + R_{C1}} = 5 \text{ mA}$$

$$V_{CEmax1} (I_{C1}=0) = V_{CC} = 12 \text{ (V)}.$$

Etapas 2:

$$R_{B2} = R_3 // R_4 = 2.45 \text{ K}\Omega$$

$$V_{BB2} = \frac{V_{CC} R_4}{R_3 + R_4} = 1.09 \text{ (V)}$$

L.V.K. mallo de entrada:

$$V_{BB2} = \frac{I_{Q2} R_{B2}}{\beta} + V_{BE} + I_{Q2} R_{E2}$$

$$\Rightarrow I_{Q2} = \frac{V_{BB2} - V_{BE}}{\frac{R_{B2}}{\beta} + R_{E2}} = 3.1 \text{ mA}$$

L.V.K. mallo de salida:

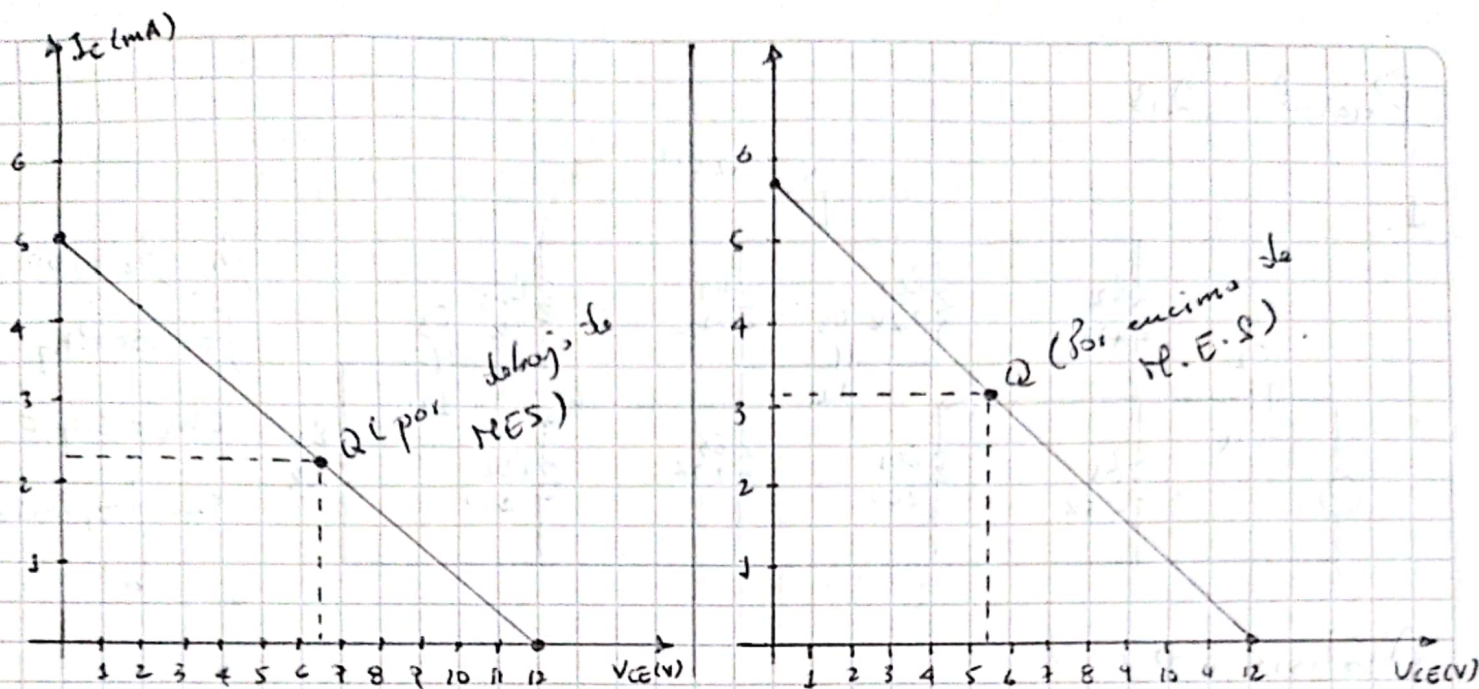
$$V_{CC} = I_{Q2} R_{C2} + V_{CE2} + I_{Q2} R_{E2}$$

$$\Rightarrow V_{CE2} = V_{CC} - I_{Q2} (R_{C2} + R_{E2})$$

$$\Rightarrow V_{CE2} = 5.49 \text{ (V)}$$

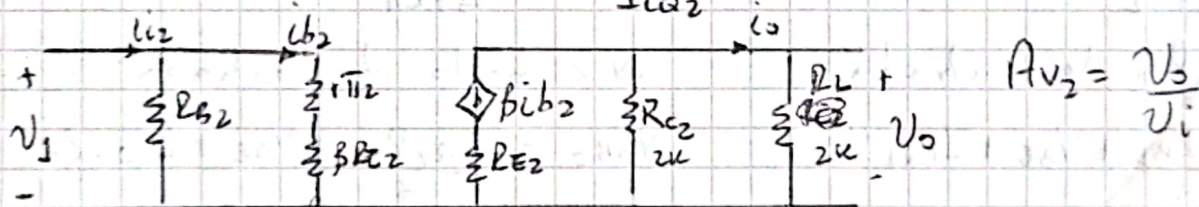
$$I_{Cmax2} (V_{CE2}=0) = \frac{V_{CC}}{R_{E2} + R_{C2}} = 5.71 \text{ mA}$$

$$V_{CEmax2} (I_{C2}=0) = V_{CC} = 12 \text{ (V)}$$



Análisis AC (Frecuencia media),

Etapas 2  $\Rightarrow r_{\pi 2} = \frac{\beta 26 \text{ mV}}{I_{CQ2}} = 838.3 \Omega$ ;  $R_{B2} = 2.45 \text{ k}\Omega$ .



$$v_o = -\beta i_{b2} R_{C2} \parallel R_L; \quad v_i = i_{i2} (r_{\pi 2} + \beta R_{E2})$$

$$\Rightarrow A_{v2} = \frac{v_o}{v_i} = \frac{-\beta i_{b2} R_{C2} \parallel R_L}{i_{i2} (r_{\pi 2} + \beta R_{E2})} = \frac{-\beta R_{C2} \parallel R_L}{(r_{\pi 2} + \beta R_{E2})} = -9.23$$

$$A_{i2} = \frac{i_o}{i_{i2}}; \quad i_o = \frac{-\beta i_{b2} R_{C2}}{R_{C2} + R_L}; \quad \text{pero } i_{b2} = \frac{i_{i2} R_{B2}}{R_{B2} + r_{\pi 2} + \beta R_{E2}}$$

$$\Rightarrow \frac{i_o}{i_{i2}} = A_{i2} = \frac{-\beta R_{C2} R_{B2}}{(R_{C2} + R_L)(R_{B2} + r_{\pi 2} + \beta R_{E2})} = -9.22$$

$$Z_{out2} = Z_{out} = R_{C2} = 2 \text{ k}\Omega$$

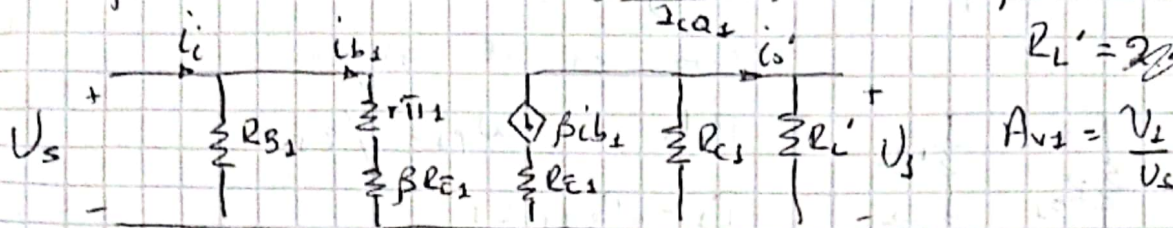
$$Z_{in2} = R_L' = (\beta R_{E2} + r_{\pi 2}) \parallel R_{B2} \approx 2.0 \text{ k}\Omega$$



Etapas 1.

$$\Rightarrow r_{\pi 1} = \frac{\beta 26 \text{ mV}}{I_{CQ1}} = 1.1 \text{ k}\Omega ; R_{B1} = 5 \text{ k}\Omega$$

$$R_{L1}' = 2.0 \text{ k}\Omega$$



$$V_{o1} = -\beta i_{b1} (R_{C1} \parallel R_{L1}') ; V_i = i_{b1} (r_{\pi 1} + \beta R_{E1})$$

$$\Rightarrow A_{v1} = \frac{V_{o1}}{V_i} = \frac{-\beta i_{b1} (R_{C1} \parallel R_{L1}')}{i_{b1} (r_{\pi 1} + \beta R_{E1})} = -5.05$$

$$A_{i1} = \frac{i_{o1}}{i_i} ; i_{o1} = -\frac{\beta i_{b1} R_{C1}}{R_{C1} + R_{L1}'} ; \text{pero } i_{b1} = \frac{i_i R_{B1}}{R_{B1} + r_{\pi 1} + \beta R_{E1}}$$

$$\Rightarrow \frac{i_{o1}}{i_i} = A_{i1} = \frac{-\beta R_{C1} R_{B1}}{(R_{C1} + R_{L1}') (R_{B1} + r_{\pi 1} + \beta R_{E1})} \approx -10$$

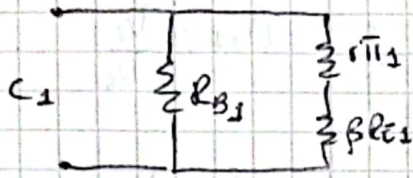
$$Z_{in1} = Z_{in} = (r_{\pi 1} + \beta R_{E1}) \parallel R_{B1} \approx 4.04 \text{ k}\Omega$$

$$A_{vT} = A_{v1} \times A_{v2} = (-9.23)(-505) = 46.6$$

$$A_{iT} = A_{i1} \times A_{i2} = (-9.22)(-10) = 92.2$$

## Análisis AC (frecuencias bajas).

Para  $C_1$ :



Cero en el origen

Polo en  $\omega_{p1} = 1/\tau_1$

$\tau_1 = R_{eq1} C_1$

$$R_{eq1} = (r\pi_1 + \beta R_{c1}) \parallel R_{B1} = 1k\Omega$$

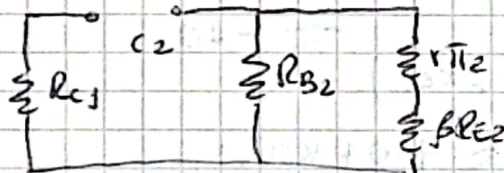
$$\Rightarrow \omega_{p1} = \frac{1}{1k\Omega \times 1\mu} = 250 \text{ rad/s}$$

Para  $C_2$ :

Cero en el origen

Polo en  $\omega_{p2} = 1/\tau_2$

$\tau_2 = R_{eq2} C_2$



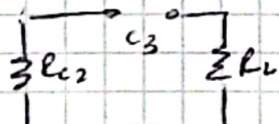
$$R_{eq2} = [(r\pi_2 + \beta R_{c2}) \parallel R_{B2}] + R_{c1}$$

$$R_{eq2} = 4.2k\Omega \Rightarrow \omega_{p2} = \frac{1}{4.2k\Omega \times 1\mu} = 238 \text{ rad/s}$$

Para  $C_3$ :

Cero en el origen

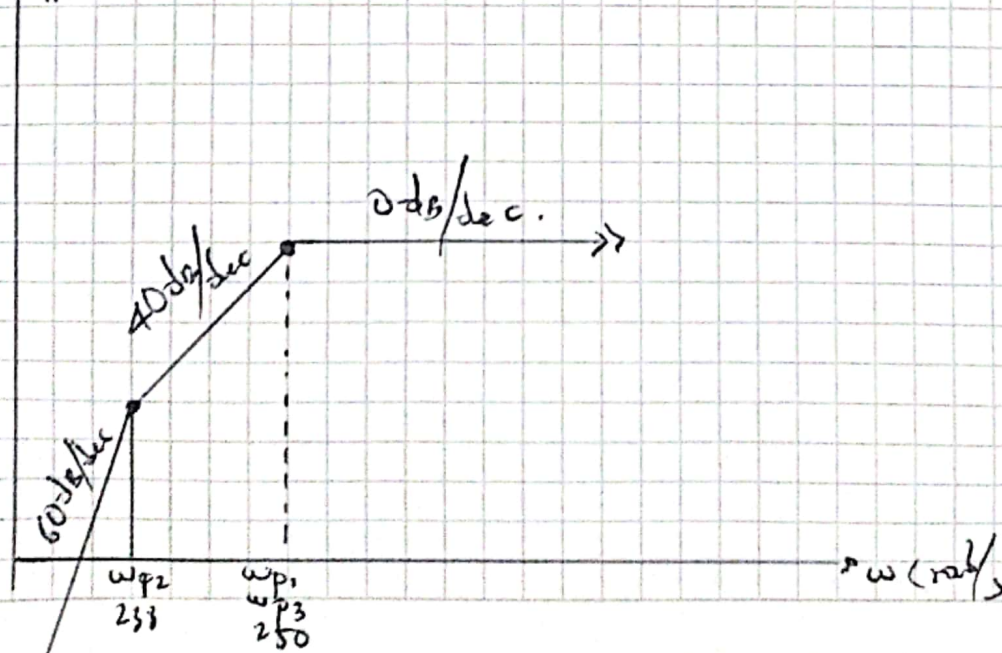
Polo en  $\omega_{p3} = \frac{1}{R_{eq3} C_3} = 250 \text{ rad/s}$



$$R_{eq3} = R_{c2} + R_{c1}$$

$$\Rightarrow \omega_c = \sqrt{\omega_{p1}^2 + \omega_{p2}^2 + \omega_{p3}^2} = 426.2 \text{ rad/s}$$

1A V/Dc





Análisis A-C para altas frecuencias

$$C_{bc1} = C_{bc2} = 10 \text{ pF}$$

$$\omega_T = 2\pi \times 500 \text{ MHz}$$

$$C_{bc1} = \frac{g_{m1}}{\omega_T}; \quad g_{m1} = \frac{1}{r_{e1}} \Rightarrow g_{m1} = \frac{1}{26 \text{ mV}/I_{CQ1}} = 0.089$$

$$\Rightarrow C_{bc1} = \frac{0.089}{2\pi \times 500 \text{ MHz}} = 28 \text{ pF}$$

$$C_{bc2} = \frac{g_{m2}}{\omega_T}; \quad g_{m2} = \frac{1}{r_{e2}} \Rightarrow g_{m2} = \frac{1}{26 \text{ mV}/I_{CQ2}} = 0.12$$

$$\Rightarrow C_{bc2} = \frac{0.12}{2\pi \times 500 \text{ MHz}} = 38 \text{ pF}$$

Aplicamos teorema de Miller para  $C_{bc1}$  y  $C_{bc2}$

Para  $C_{bc1}$ :

$$CM_1 = C_{bc1} (1 - A_{v1}) = 10 \text{ pF} (1 - (-5.05)) = 60.5 \text{ pF}$$

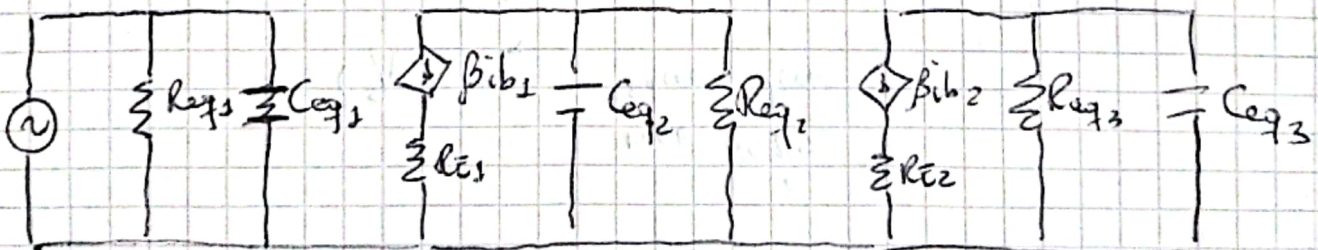
$$CM_2 = C_{bc1} (1 - (1/A_{v1})) = 10 \text{ pF} (1 - (-1/5.05)) \approx 12 \text{ pF}$$

Para  $C_{bc2}$ :

$$CM_3 = C_{bc2} (1 - A_{v2}) = 10 \text{ pF} (1 - (-9.23)) = 102 \text{ pF}$$

$$CM_4 = C_{bc2} (1 - 1/A_{v2}) = 10 \text{ pF} (1 - (-1/9.23)) \approx 11 \text{ pF}$$

Reduciendo los paralelos, se obtiene:



Polo para  $C_{eq1} \Rightarrow C_{eq1} = C_{be1} + C_{M1} = 88.5 \text{ pF}$

pero  $R_{eq1} \parallel C_{orto} = 0 \Rightarrow \omega_{p1} = \frac{1}{0} \approx \infty$  (No hay polo)

Polo para  $C_{eq2} \Rightarrow C_{eq2} = C_{M2} + C_{be2} + C_{M3} = 12 \text{ pF} + 38 \text{ pF} + 102 \text{ pF}$

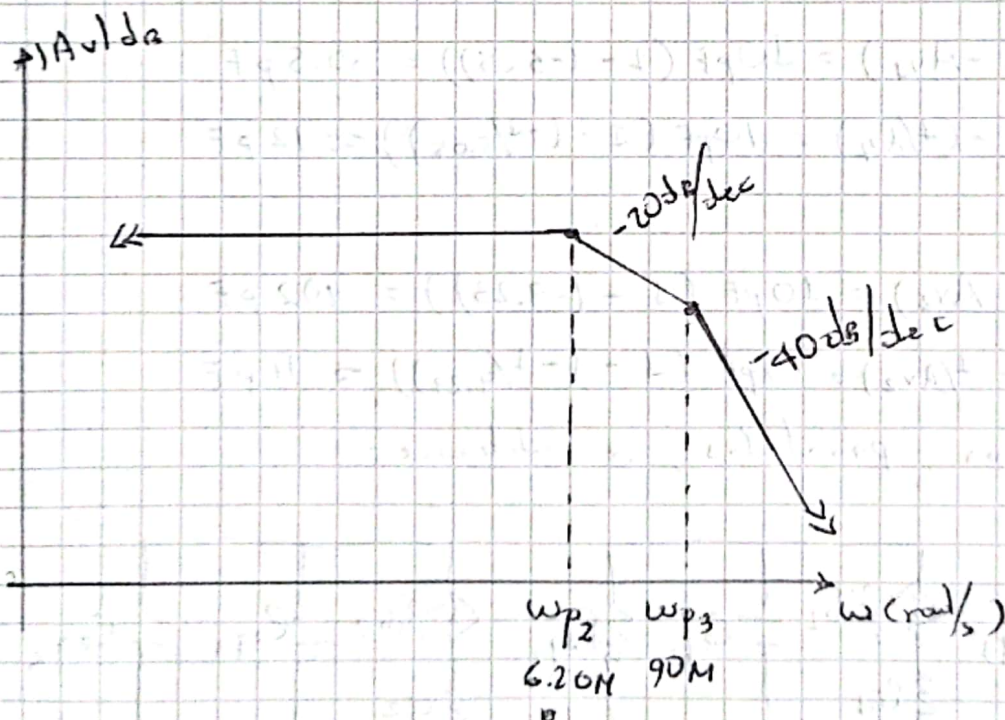
$R_{eq2} = R_{c1} \parallel R_{B2} \parallel (R_{H2} + R_{L2})$   $C_{eq2} = 152 \text{ pF}$

$R_{eq2} = 1.05 \text{ k}\Omega \Rightarrow \omega_{p2} = \frac{1}{1.05 \text{ k}\Omega \times 152 \text{ pF}} = 6.26 \text{ Mrad/s}$

Polo para  $C_{eq3} \Rightarrow C_{eq3} = C_{M4} = 11 \text{ pF}$  ;  $R_{eq3} = R_{c2} \parallel R_L = 1 \text{ k}\Omega$

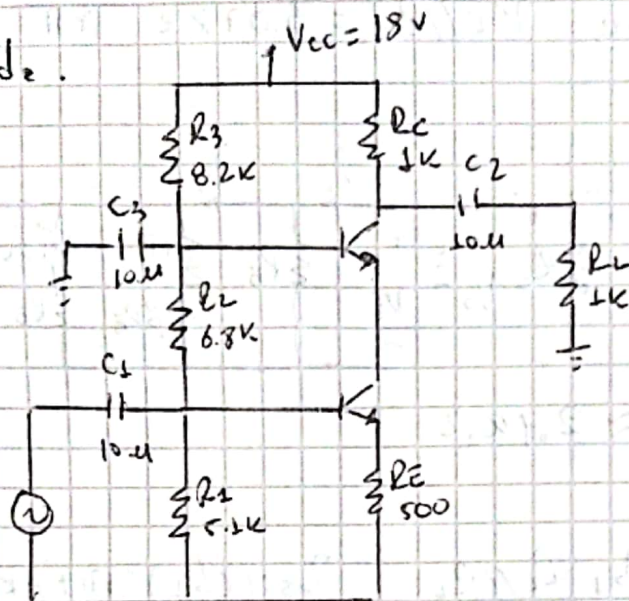
$\Rightarrow \omega_{p3} = \frac{1}{1 \text{ k}\Omega \times 11 \text{ pF}} = 90 \text{ Mrad/s}$

$\therefore \omega_H = \omega_{p2} = 6.26 \text{ Mrad/s}$



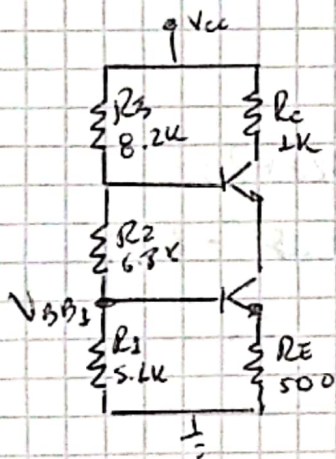


## 2. Cascode.



$$\beta = 100$$

## Análisis D.C



$$V_{BB3} = \frac{V_{CC} R_4}{R_3 + R_4} = 4.57 \text{ (V)}$$

L.V.K en Malla de entrada:

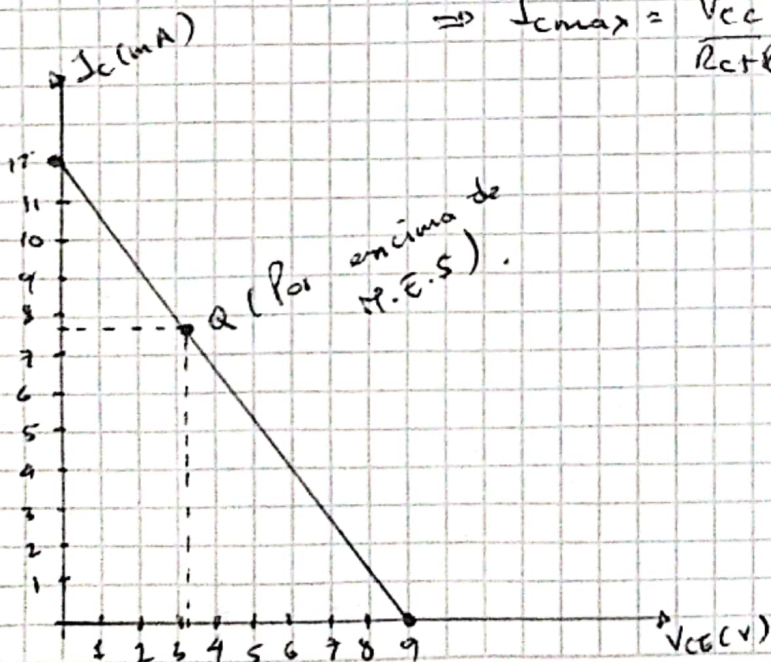
$$V_{BB1} = V_{BE} + I_{CQ} R_E \Rightarrow I_{CQ} = \frac{V_{BB1} - V_{BE}}{R_E} = 7.74 \text{ mA}$$

L.V.K en Malla de salida:

$$V_{CC} = 2V_{CEQ} + I_{CQ} (R_C + R_E) \Rightarrow V_{CEQ} = \frac{V_{CC} - I_{CQ} (R_C + R_E)}{2}$$

$$\Rightarrow V_{CEQ} = 3.2 \text{ (V)} \Rightarrow V_{CEmax} = \frac{V_{CC}}{2} = \frac{18 \text{ (V)}}{2} = 9$$

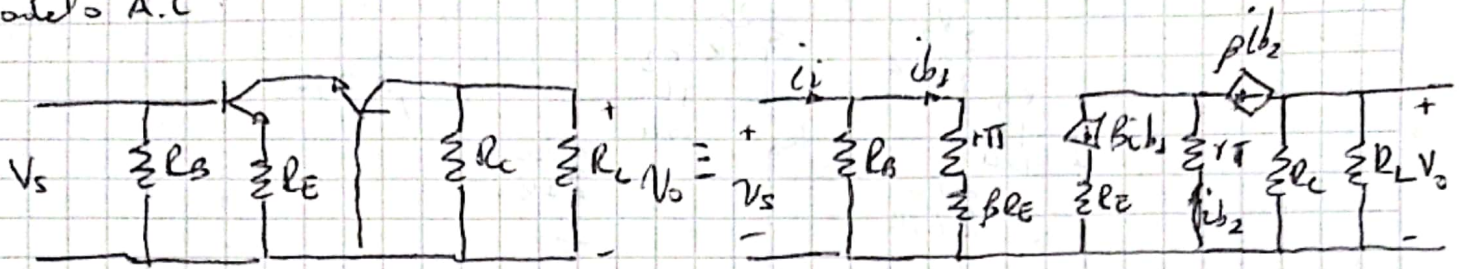
$$\Rightarrow I_{Cmax} = \frac{V_{CC}}{R_C + R_E} = 12 \text{ mA}$$





Analisis A.C:  $R_B = R_1 // R_2 = 3.07 k\Omega$   $r_{\pi} = \frac{\beta 26 mV}{I_{CQ}} \approx 338 \Omega$

Modelo A.C:



$$Z_{in} = (r_{\pi} + \beta R_E) // R_B \approx 2.9 k\Omega$$

$$Z_{out} = R_C = 1 k\Omega$$

$$A_v = \frac{V_o}{V_s} ; V_o = -\beta i_{b1} R_C // R_L ; V_s = (i_{b1})(r_{\pi} + \beta R_E)$$

$$\Rightarrow A_v = \frac{V_o}{V_s} = \frac{-\beta i_{b1} (R_C // R_L)}{i_{b1} (r_{\pi} + \beta R_E)} = 0.993$$

$$A_i = \frac{i_o}{i_i} , i_o = \frac{-\beta i_{b1} R_C}{R_C + R_L} ; i_{b1} = \frac{i_i R_B}{r_{\pi} + \beta R_E + R_B}$$

$$\Rightarrow \frac{i_o}{i_i} = A_i = \frac{-\beta R_C R_B}{(R_C + R_L)(r_{\pi} + \beta R_E + R_B)} = -2.87$$