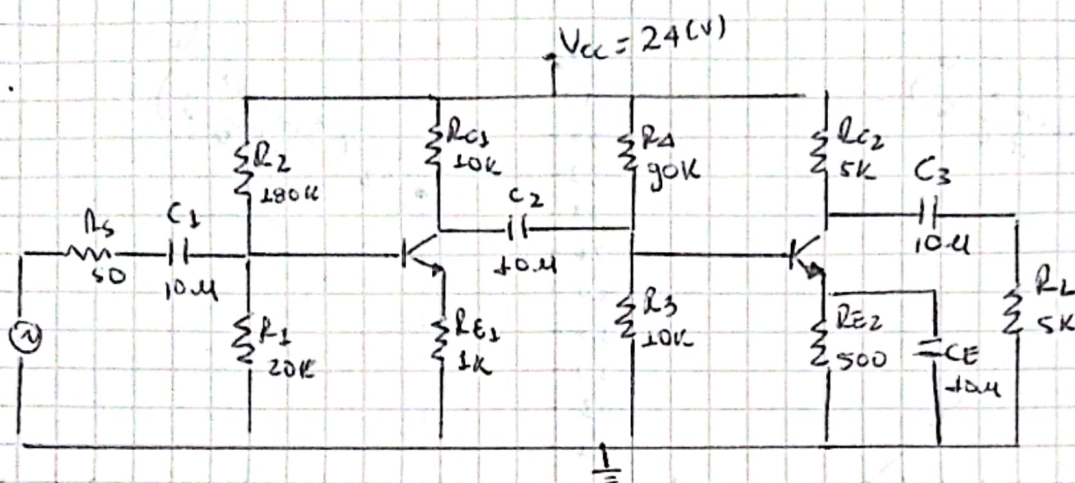


Parcial 2A.

J.



$$\beta_1 = \beta_2 = 200$$

$$f_T = 500 \text{ MHz}$$

$$C_{bc} = 10 \text{ pF}$$

$$C_o: \text{despreciable}$$

Análisis D.C

Etapa 1.

$$R_{B1} = R_1 // R_2 = 18 \text{ K}$$

$$V_{BB1} = \frac{V_{CC} R_1}{R_1 + R_2} = 2.4 \text{ (V)}$$

L.V.K malla de entrada:

$$V_{BB1} = \frac{I_{CQ1} R_{B1}}{\beta} + V_{BE} + I_{CQ1} R_{E1}$$

$$\Rightarrow I_{CQ1} = \frac{V_{BB1} - V_{BE}}{\frac{R_{B1}}{\beta} + R_{E1}} = 1.56 \text{ mA}$$

L.V.K Malla de salida:

$$V_{CC} = I_{CQ1} R_{E1} + V_{CE1} + I_{CQ1} R_{E1}$$

$$\Rightarrow V_{CE1} = V_{CC} - I_{CQ1} (R_{E1} + R_{E1})$$

$$\Rightarrow V_{CE1} = 6.84 \text{ (V)}$$

$$I_{Cmax1} (V_{CE1}=0) = \frac{V_{CC}}{R_{E1} + R_{E1}} = 2.18 \text{ mA}$$

$$V_{CEmax1} = V_{CC} = 24 \text{ (V)}$$

Etapa 2.

$$R_{B2} = R_3 // R_4 = 9 \text{ K}$$

$$V_{BB2} = \frac{V_{CC} R_3}{R_3 + R_4} = 2.4 \text{ (V)}$$

L.V.K malla de entrada:

$$V_{BB2} = \frac{I_{CQ2} R_{B2}}{\beta} + V_{BE} + I_{CQ2} R_{E2}$$

$$\Rightarrow I_{CQ2} = \frac{V_{BB2} - V_{BE}}{\frac{R_{B2}}{\beta} + R_{E2}} = 3.12 \text{ mA}$$

L.V.K malla de salida:

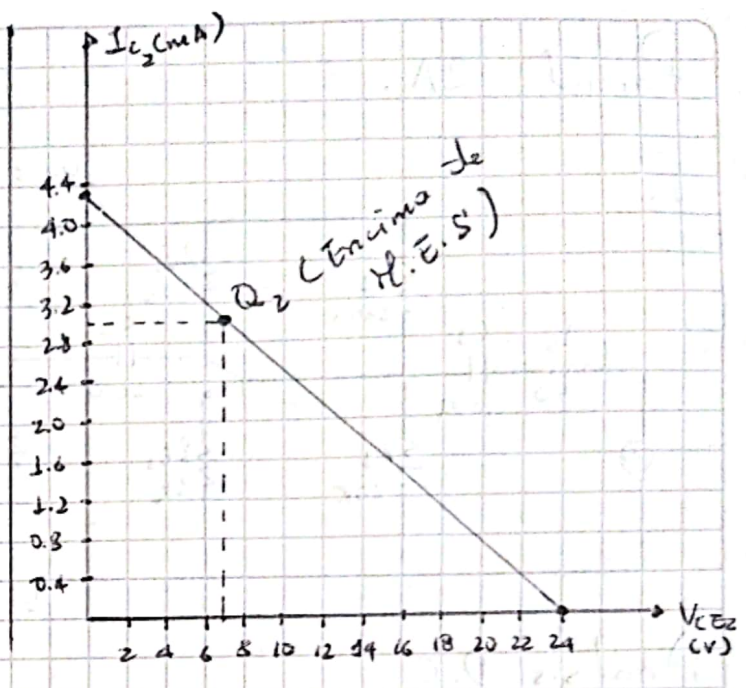
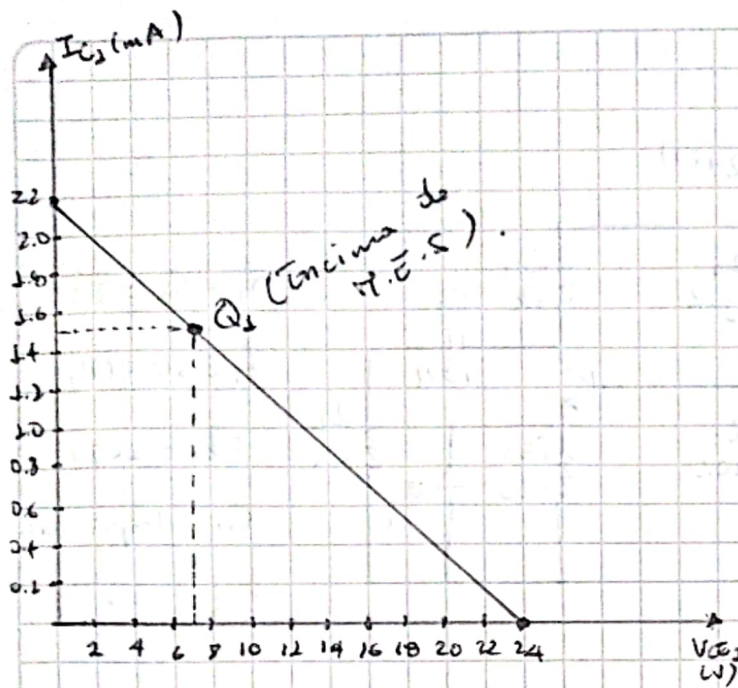
$$V_{CC} = I_{CQ2} R_{E2} + V_{CE2} + I_{CQ2} R_{E2}$$

$$\Rightarrow V_{CE2} = V_{CC} - I_{CQ2} (R_{E2} + R_{E2})$$

$$\Rightarrow V_{CE2} = 6.84 \text{ (V)}$$

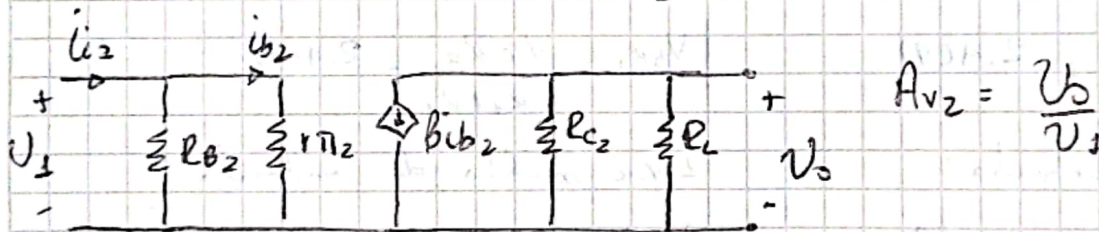
$$I_{Cmax2} (V_{CE2}=0) = \frac{V_{CC}}{R_{E2} + R_{E2}} = 4.36 \text{ mA}$$

$$V_{CEmax2} = V_{CC} = 24 \text{ (V)}$$



Análisis AC (Frecuencias medias).

Etapas 2. $\Rightarrow r_{\pi 2} = \frac{\beta 26mV}{I_{CQ2}} = 1.66k\Omega$. $R_{B2} = 9k\Omega$.



$$A_{v2} = \frac{V_0}{V_1}$$

$$V_0 = -\beta i_{b2} R_{C2} \parallel R_L ; \quad V_1 = i_{b2} r_{\pi 2}$$

$$\Rightarrow A_{v2} = \frac{V_0}{V_1} = -\frac{\beta i_{b2} R_{C2} \parallel R_L}{i_{b2} r_{\pi 2}} = -\frac{\beta R_{C2} \parallel R_L}{r_{\pi 2}} = -301.2$$

$$A_{i2} = \frac{i_0}{i_{i2}} ; \quad i_0 = -\frac{\beta i_{b2} R_{C2}}{R_{C2} + R_L}, \text{ pero } i_{b2} = \frac{i_{i2} R_{B2}}{r_{\pi 2} + R_{B2}}$$

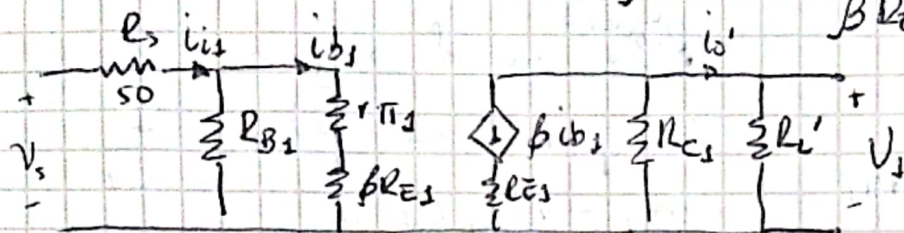
$$\Rightarrow \frac{i_0}{i_{i2}} = A_{i2} = -\frac{\beta R_{B2} R_{C2}}{(R_{C2} + R_L)(r_{\pi 2} + R_{B2})} = -84.4$$

$$Z_{out2} = Z_{out} = R_{C2} = 5k\Omega.$$

$$Z_{in2} = R_L' = r_{\pi 2} \parallel R_{B2} = 1.4k\Omega.$$

Etapas $\Rightarrow r_{\pi 1} = \frac{\beta 26 \text{ mV}}{I_{C1}} \approx \frac{3.33 \text{ k}\Omega}{200 \mu\text{A}}; R_{B1} = 18 \text{ k}\Omega.$

$\beta R_{E1} = 200 \text{ k}\Omega; R_{L'} = 1.4 \text{ k}\Omega$



Calculamos $(r_{\pi 1} + \beta R_{E1}) \parallel R_{B1} = 16.5 \text{ k}\Omega \gg R_S$
 \Rightarrow Se puede despreciar R_S de A_{V1} y Z_{in1}

$A_{V1} = \frac{V_1}{V_S}$

$V_1 = -\beta i_{b1} R_{C1} \parallel R_{L'}; V_S = i_{b1} (r_{\pi 1} + \beta R_{E1})$

$\Rightarrow A_{V1} = \frac{V_1}{V_S} = \frac{-\beta i_{b1} R_{C1} \parallel R_{L'}}{i_{b1} (r_{\pi 1} + \beta R_{E1})} = \frac{-\beta R_{C1} \parallel R_{L'}}{(r_{\pi 1} + \beta R_{E1})} = \frac{-(200)(1.23 \text{ k})}{(203.3 \text{ k})}$

$A_{V1} = -1.20$

$A_{i1} = \frac{i_{o1}}{i_{i1}}; i_{o1} = \frac{-\beta i_{b1} R_{C1}}{R_{C1} + R_{L'}}; \text{ pero } i_{b1} = \frac{i_{i1} R_{B1}}{(R_{B1} + r_{\pi 1} + \beta R_{E1})}$

$\Rightarrow A_{i1} = \frac{i_{o1}}{i_{i1}} = \frac{-\beta R_{C1} R_{B1}}{(R_{C1} + R_{L'})(R_{B1} + r_{\pi 1} + \beta R_{E1})} = -14.3$

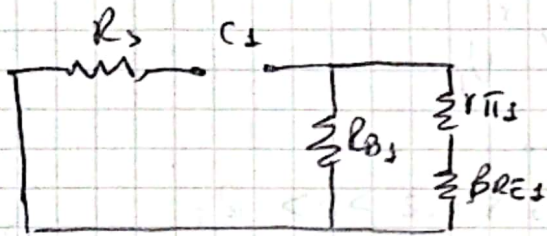
$Z_{in} = (r_{\pi 1} + \beta R_{E1}) \parallel R_{B1} = 16.5 \text{ k}\Omega.$

$\Rightarrow A_{VT} = A_{V1} \times A_{V2} = (-1.20)(-301.2) = 361.4$

$\Rightarrow A_{iT} = A_{i1} \times A_{i2} = (-14.3)(84.4) = 1206.9$

Análisis AC (frecuencias bajas).

Para C_1 :



Cero en el origen

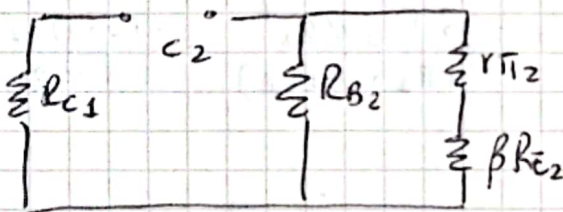
polo en $\omega_{p1} = \frac{1}{\tau_1}$

$$\tau_1 = R_{eq1} C_1$$

$$R_{eq1} = [(r_{\pi 1} + \beta R_{E1}) \parallel R_{B1}] + R_s$$

$$R_{eq1} = 16.55 \text{ k}\Omega \Rightarrow \omega_{p1} = \frac{1}{16.55 \text{ k}\Omega \times 10 \mu\text{F}} = 6.04 \text{ rad/s.}$$

Para C_2



Cero en el origen

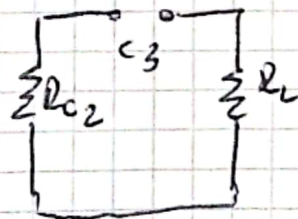
polo en $\omega_{p2} = \frac{1}{\tau_2}$

$$\tau_2 = R_{eq2} C_2$$

$$R_{eq2} = [(\beta R_{E2} + r_{\pi 2}) \parallel R_{B2}] + R_{C1}$$

$$R_{eq2} = 18.27 \text{ k}\Omega \Rightarrow \omega_{p2} = \frac{1}{18.27 \text{ k}\Omega \times 10 \mu\text{F}} = 5.47 \text{ rad/s.}$$

Para C_3



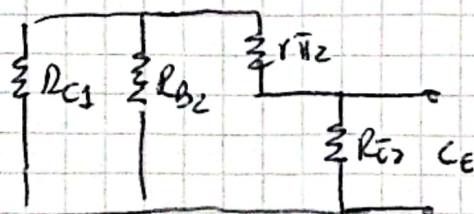
Cero en el origen

polo en $\omega_{p3} = \frac{1}{\tau_3}$

$$\tau_3 = R_{eq3} C_3 ; R_{eq3} = R_{C2} + R_L = 10 \text{ k}\Omega.$$

$$\Rightarrow \omega_{p3} = \frac{1}{10 \text{ k}\Omega \times 10 \mu\text{F}} = 10 \text{ rad/s.}$$

Para C_E .



Polo en $\omega_{z1} = \frac{1}{R_{E2} C_E} = 200 \text{ rad/s.}$

Polo en $\omega_{p4} = \frac{1}{\tau_4} = \frac{1}{R_{eq4} C_E}$

$$R_{eq4} = [(R_{C1} \parallel R_{B2}) + r_{\pi 2}] \parallel R_{E2}$$

$$R_{eq4} \approx 30 \Omega \Rightarrow \omega_{p4} = \frac{1}{(30)(10 \mu\text{F})} = 3.33 \text{ krad/s.} \Rightarrow \omega_L = \omega_{p4}$$

polo dominante = 3.33 krad/s.

Análisis A.C (para alta frecuencia) , $C_{bc1} = C_{bc2} = 10 \text{ pF}$
 $\omega_f = 2\pi \times 500 \text{ MHz}$

$$C_{be1} = \frac{g_{m1}}{\omega_f}, \quad g_{m1} = \frac{1}{r_{e1}} \Rightarrow g_{m1} = \frac{1}{26 \text{ mV} / I_{CQ1}} = 0.06$$

$$\Rightarrow C_{be1} = \frac{0.06}{(2\pi \times 500 \text{ MHz})} = 19 \text{ pF}$$

$$C_{be2} = \frac{g_{m2}}{\omega_f}, \quad g_{m2} = \frac{1}{r_{e2}} \Rightarrow g_{m2} = \frac{1}{26 \text{ mV} / I_{CQ2}} = 0.12$$

$$\Rightarrow C_{be2} = \frac{0.12}{(2\pi \times 500 \text{ MHz})} = 38 \text{ pF}$$

Aplicamos teorema de Miller para C_{bc1} y C_{bc2}
 Para C_{bc1} :

$$C_{M1} = C_{bc1} (1 - A_{V1}) = 10 \text{ pF} (1 - (-1.20)) = 22 \text{ pF}$$

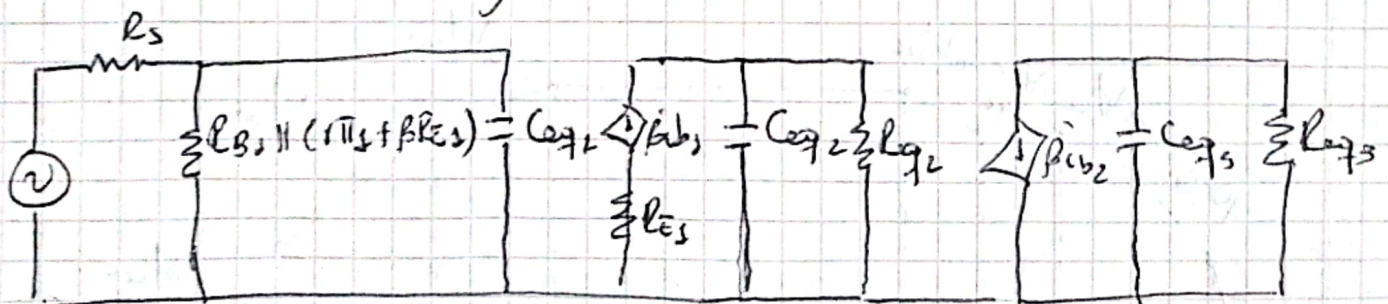
$$C_{M2} = C_{bc1} (1 - 1/A_{V1}) = 10 \text{ pF} (1 - (-1/1.2)) = 18.3 \text{ pF}$$

Para C_{bc2} :

$$C_{M3} = C_{bc2} (1 - A_{V2}) = 10 \text{ pF} (1 - (-304.2)) \approx 3 \text{ nF}$$

$$C_{M4} = C_{bc2} (1 - 1/A_{V2}) = 10 \text{ pF} (1 - (-1/304.2)) \approx 10 \text{ pF}$$

Reduciendo los paralelos se obtiene:



Polo para C_{eq1} : $C_{eq1} = C_{be1} + C_{M1} = 22pF + 19pF = 41pF$

$$\omega_{p1} = \frac{1}{C_{eq1} R_{eq1}} \quad R_{eq1} = R_s \parallel R_{B1} \parallel (r_{\pi1} + \beta R_{E1}) = 49.8 \Omega$$

$$\Rightarrow \omega_{p1} = \frac{1}{49.8 \times 41pF} = 489.8 \text{ Mrad/s}$$

Polo para C_{eq2} : $C_{eq2} = C_{M2} + C_{be2} + C_{M3} = 18.3pF + 3nF + 38pF \approx 3nF$

$$\Rightarrow \omega_{p2} = \frac{1}{C_{eq2} R_{eq2}} \quad R_{eq2} = R_{c1} \parallel R_{B2} \parallel r_{\pi2} = 1.23k$$

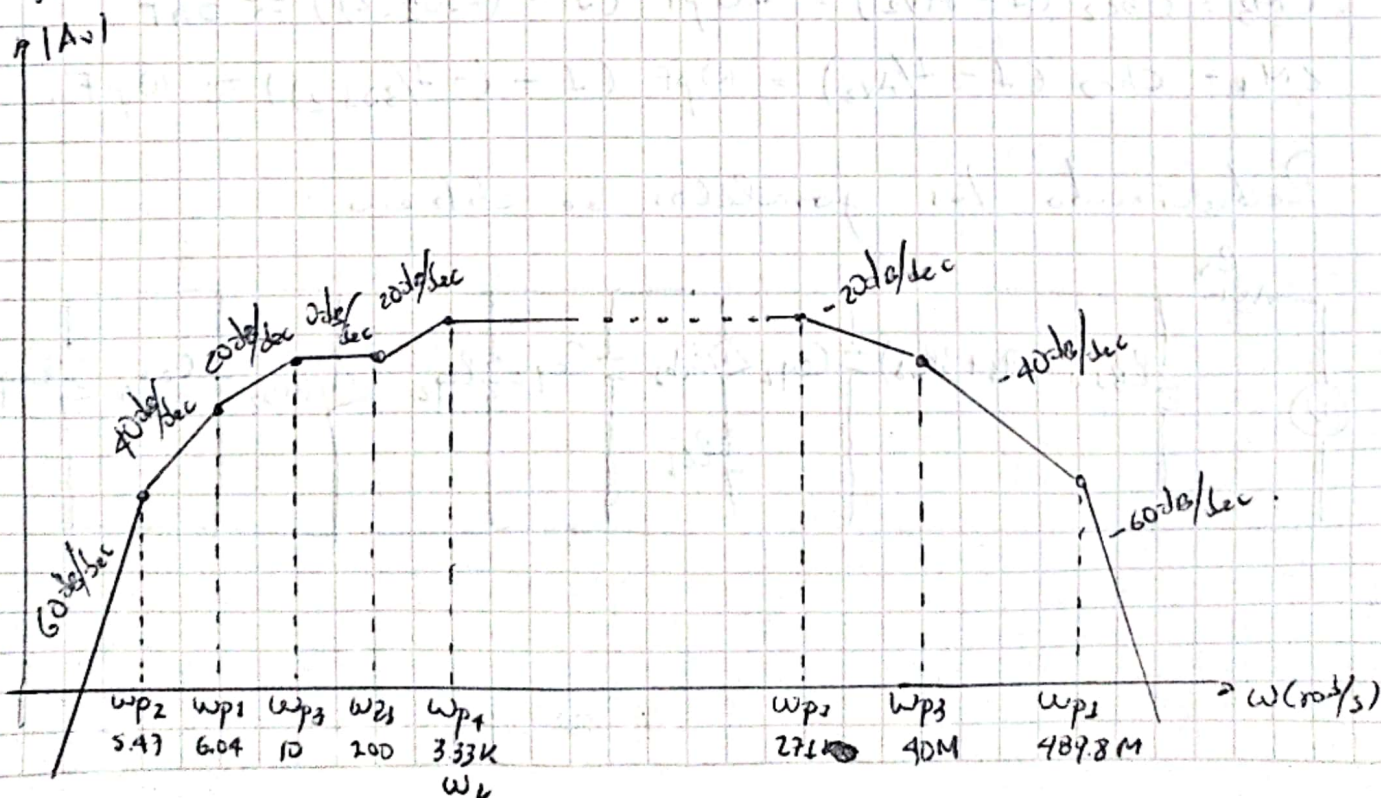
$$\omega_{p2} = \frac{1}{3nF \times 1.23k} = 271 \text{ Krad/s} \quad \Rightarrow \left| \omega_H = 271 \text{ Krad/s} \right|$$

Polo para C_{eq3} : $C_{eq3} = C_{M4} = 10pF$

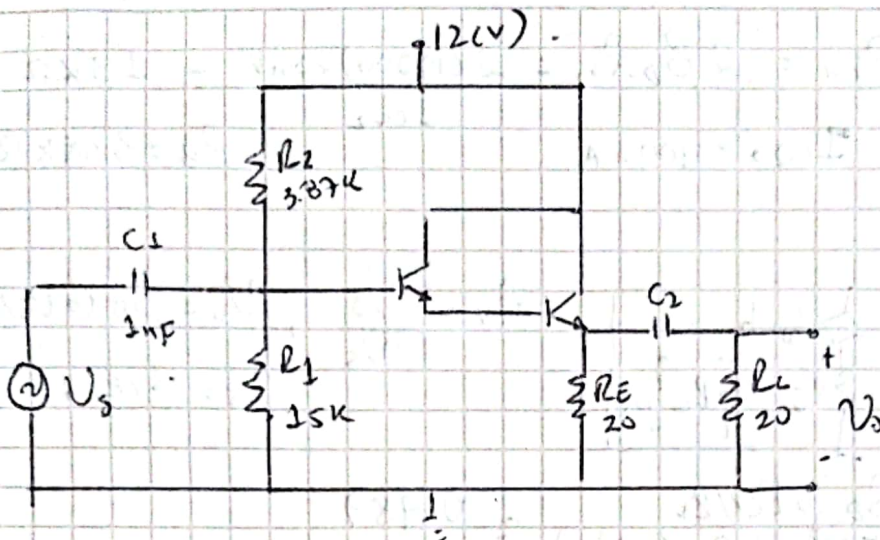
$$\omega_{p3} = \frac{1}{C_{eq3} R_{eq3}} \quad R_{eq3} = R_{c2} \parallel R_L = 2.5k\Omega$$

$$\omega_{p3} = \frac{1}{10pF \times 2.5k\Omega} = 40 \text{ Mrad/s}$$

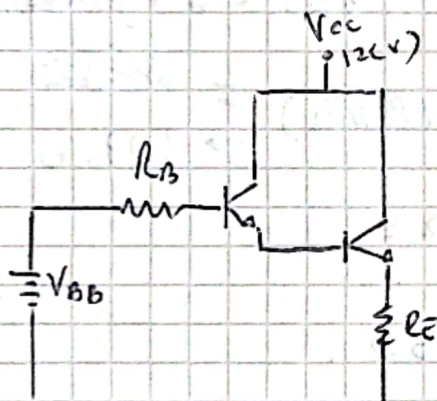
Resposta en frecuencia.



2.



Analisis D.C



$$R_B = R_1 // R_2 = 3.08 k\Omega$$

$$V_{BB} = \frac{V_{CC} R_1}{R_1 + R_2} = 9.53 (V)$$

L.V.K. malla de entrada

$$V_{BB} = \frac{I_{CQ2} R_B}{\beta_D} + 2V_{BE} + I_{CQ2} R_E$$

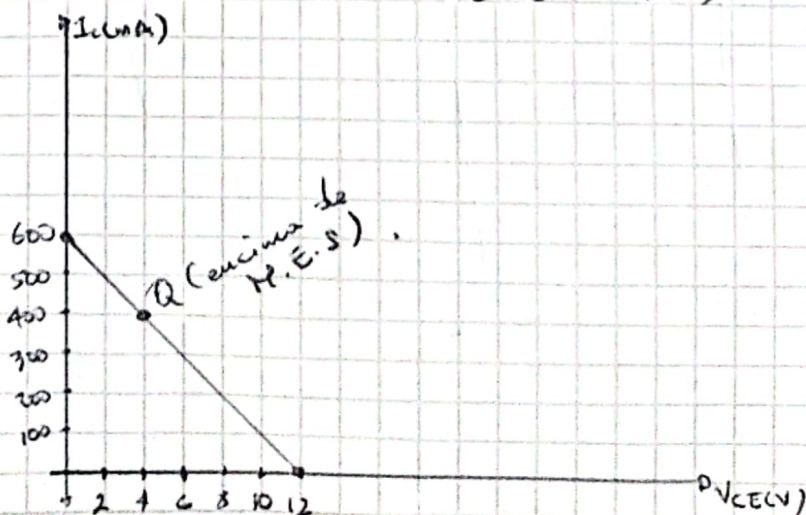
$$\Rightarrow I_{CQ2} = \frac{V_{BB} - 2V_{BE}}{\frac{R_B}{\beta_D} + R_E} = 0.4 (A) = 400 mA$$

L.V.K. malla de salida:

$$V_{CC} = V_{CE} + I_{CQ2} R_E \Rightarrow V_{CE} = V_{CC} - I_{CQ2} R_E = 4 (V)$$

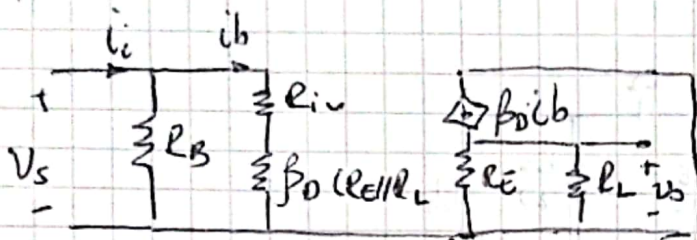
$$I_{Cmax} = \frac{V_{CE}}{R_E} = 600 mA$$

$$V_{CEmax} = V_{CC} = 12 (V)$$



Análisis A.C $R_{in} = 2\beta_D R_{E2} = \frac{2(10000)26mV}{I_{CQ2}} = 1.3k\Omega$

Modelo híbrido $I_{CQ2} = 400\mu A$ $R_B = 3.08k\Omega$



$A_v = \frac{V_o}{V_s}$; $V_o = \beta_D i_b R_E \parallel R_L$
 $V_s = i_b (R_{in} + \beta_D R_E \parallel R_L)$

$\Rightarrow A_v = \frac{V_o}{V_s} = \frac{\beta_D i_b R_E \parallel R_L}{i_b (R_{in} + \beta_D R_E \parallel R_L)} \approx 0.987$

$A_i = \frac{i_o}{i_i}$; $i_o = \frac{\beta_D i_b R_E}{R_E + R_L}$; pero $i_b = \frac{i_i R_B}{R_B + R_{in} + \beta_D (R_E \parallel R_L)}$

$\Rightarrow \frac{i_o}{i_i} = A_i = \frac{\beta_D R_E R_B}{(R_E + R_L)(R_B + R_{in} + \beta_D (R_E \parallel R_L))} \approx 147.6$

$Z_{in} = [R_{in} + \beta_D (R_E \parallel R_L)] \parallel R_B \approx 3k\Omega$

$Z_{out} = \frac{R_{in}}{\beta_D} \parallel R_E = \frac{1.3k\Omega}{10000} \parallel 20 \approx 0.13\Omega$

