Ch 13 Appendix - Riemann Sums

For each i, chaste x; E [1., 1.].

P- {10, ..., In } = patition of [0, b]

Then

(CF,P) & Z + Cx; 1 st; & UCF,P)

Any sum Ziscxi) Ot: 11 = Rigmann sum

The sent: Suppose I is interested in a set of the sent of the sent

for any Rieman sum James by choosing x; E[tim, ti]

Proof

Finless - I banded - 3M, It & M

Let po . {00, ... Un} s.t. UC. po) - L(), po) < E12

chanc 3 s.t. 3 < € 4Hk

For any Pr. 1. Al; (d we combled UCI.P) - L(I.P) . \(\sum_{i,j}^{\infty}(Mi-m;)\DI;\) into two sums

some of the DI, 's are completely contained in (Uj., Uj) be some j.

The pat of the sum bet such Dt. 4 W & Els.

The almos remaining Oh, 's have \$, , < U , < +; Sor same j=1, ..., h-1. Thus, there are at most h-1 of such Oh, is.

The sum besthere Oh, is is smeather than (h-1). (2M3). E12.

mus, oct.P)-14.P) (&

But we know that

10,9) < Z)(x,) DI, \$ = 00,9)

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