# project2-tangential

#### November 18, 2024

```
[1]: import pandas as pd
     import numpy as np
     import matplotlib.pyplot as plt
     import seaborn as sns
     import copy
     import scipy as sp
     import scipy.stats as stats
     import time
     import itertools
     from sklearn.model_selection import GridSearchCV
     from sklearn.decomposition import NMF, TruncatedSVD
     from sklearn.cluster import AgglomerativeClustering, KMeans, __
      →SpectralClustering, OPTICS
     from sklearn.mixture import GaussianMixture
     from sklearn.metrics import accuracy_score, confusion_matrix, silhouette_score
     from scipy.cluster.hierarchy import dendrogram
     from sklearn.preprocessing import StandardScaler, MinMaxScaler
     df = pd.read_excel("data/titanic3.xls")
     RANDOMSTATE = 42
     NCLUST = 2
     td = df[['pclass',
             'sex',
             'age',
             'sibsp',
             'parch',
             'fare',
             'embarked',
             'survived']].copy()
     td.sex = td.sex.map({'male': 0, 'female': 1})
     td.age = td.age.fillna(td.groupby('sex')['age'].transform('mean'))
     td.fare = td.fare.fillna(td.fare.median())
     td.embarked = td.embarked.fillna('S').map({'S': 0, 'C': 1, 'Q': 2})
     gtruth = df.survived
```

Picking through data was necessary to catch as many issues as possible. Some values were simple transcription errors, such as a seemingly random 'T' under 'embarked'. Thankfully, the dataset featured no actual duplicates of passengers. However, two pairs of passengers did share an identical name.

```
df.name[df.name.duplicated()]
[2]:
[2]: 726
             Connolly, Miss. Kate
                 Kelly, Mr. James
     925
     Name: name, dtype: object
     df[df.name == 'Connolly, Miss. Kate']
                                                                      sibsp
[3]:
          pclass
                   survived
                                                name
                                                                             parch
                                                          sex
                                                                age
     725
                3
                              Connolly, Miss. Kate
                                                      female
                                                               22.0
                                                                          0
                                                                                  0
     726
                3
                              Connolly, Miss. Kate
                                                      female
                                                               30.0
                                                                          0
                                                                                  0
           ticket
                      fare cabin embarked boat
                                                  body home.dest
     725
          370373
                   7.7500
                             NaN
                                                   NaN
                                                          Ireland
                                              13
     726
          330972
                   7.6292
                             NaN
                                            NaN
                                                   NaN
                                                          Ireland
     df[df.name == 'Kelly, Mr. James']
                                                               sibsp
[4]:
                   survived
                                                                       parch
                                                                              ticket
          pclass
                                           name
                                                          age
                                                   sex
     924
                3
                              Kelly, Mr. James
                                                  male
                                                         34.5
                                                                    0
                                                                           0
                                                                               330911
     925
                3
                                                  male
                              Kelly, Mr. James
                                                         44.0
                                                                    0
                                                                           0
                                                                              363592
             fare cabin embarked boat
                                         body home.dest
     924
          7.8292
                    NaN
                                Q
                                    NaN
                                         70.0
                                                     NaN
     925
          8.0500
                    NaN
                                S
                                    NaN
                                          NaN
                                                     NaN
```

## 0.0.1 Manipulating The Projection

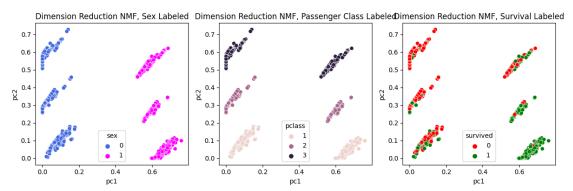
Whether we look to NMF or SVD it is possible to observe how the outcome of a projection can change by preemptively controlling for the scale of some features. This alters the angle and spread among datapoints. Scroll down to observe how the preprocessed data transitions between six and three groupings when 'sex' and 'pclass' are scaled between 0-1 and 0-.5.

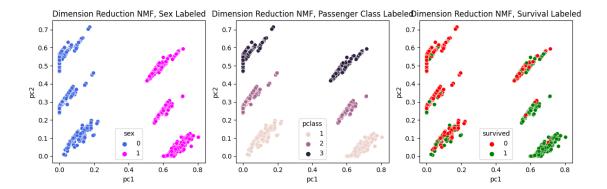
```
[5]: def cycle_scaling(X):
    for i in range(10):
        X = MinMaxScaler(feature_range=(0, 1)).fit_transform(X)
```

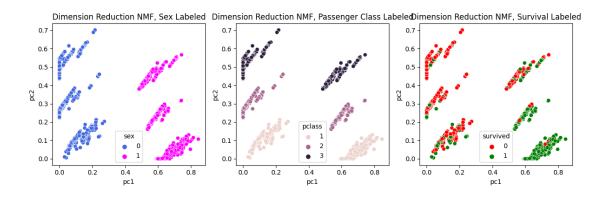
```
X[:, 1] = \text{np.vectorize(lambda } x: x/(i/10+1))(X[:, 1]) \# reducing spread/
    \hookrightarrow tightness
                        X[:, 0] = \text{np.vectorize(lambda } x: x/(i/10+1))(X[:, 0]) \# scaling_{\square}
    \rightarrow adjustment
                         \#X\_svd = pd.DataFrame(TruncatedSVD(n\_components=2, algorithm='arpack', \sqcup svd = pd.DataFrame(TruncatedSVD(n\_components=2, algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', ultimatedSVD(n\_components=2, algorithm='arpack', ultimatedSVD(n\_components=2, algorit
    ⇔random_state=RANDOMSTATE).fit_transform(X),
                                                                    columns=['pc1', 'pc2'])
                         X_nmf = pd.DataFrame(NMF(n_components=2, init='random', max_iter=600,__
    →random_state=RANDOMSTATE).fit_transform(X),
                                                                 columns=['pc1', 'pc2'])
                        fig, axes = plt.subplots(1, 3, figsize=(12, 4), sharey=False)
                         sns.scatterplot(x='pc1', y='pc2', data=X_nmf, hue=td.sex, palette={0:___

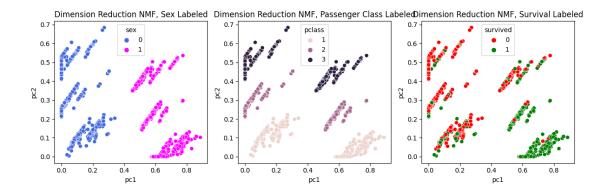
¬'royalblue', 1: 'magenta'}, ax=axes[0])
                         axes[0].set_title('Dimension Reduction NMF, Sex Labeled')
                         sns.scatterplot(x='pc1', y='pc2', data=X_nmf, hue=td.pclass, ax=axes[1])
                        axes[1].set_title('Dimension Reduction NMF, Passenger Class Labeled')
                         sns.scatterplot(x='pc1', y='pc2', data=X_nmf, hue=gtruth, palette={0:___

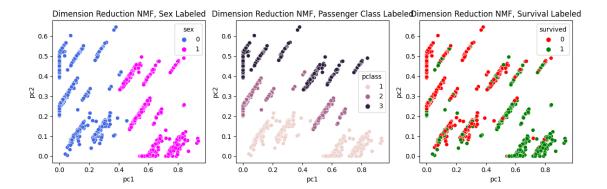
¬'red', 1: 'green'}, ax=axes[2])
                        axes[2].set_title('Dimension Reduction NMF, Survival Labeled')
                        plt.tight_layout()
                        plt.show()
cycle_scaling(td)
```

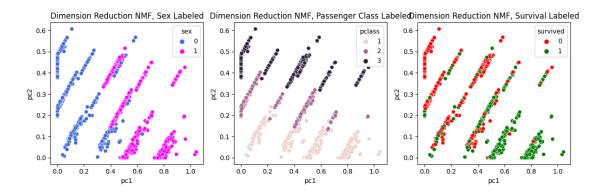


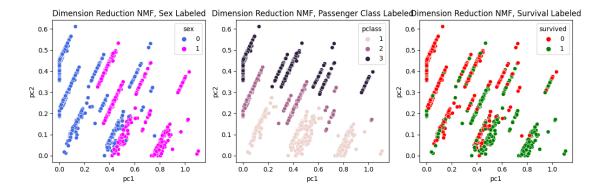


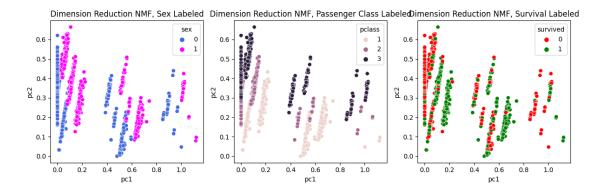


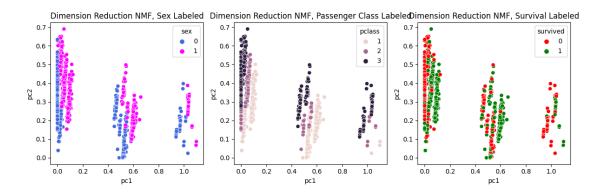


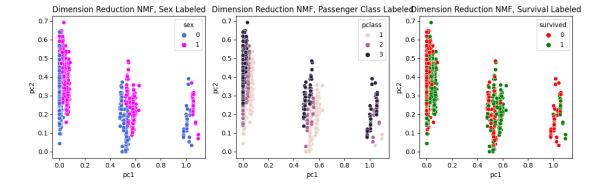












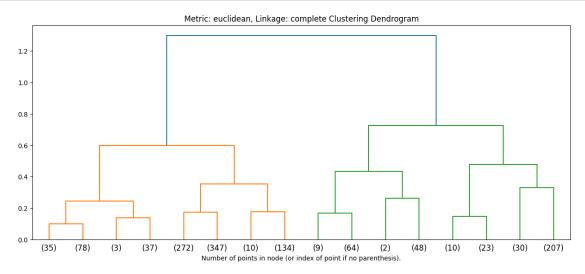
# 0.0.2 Complete Vs. Ward Dendrogram

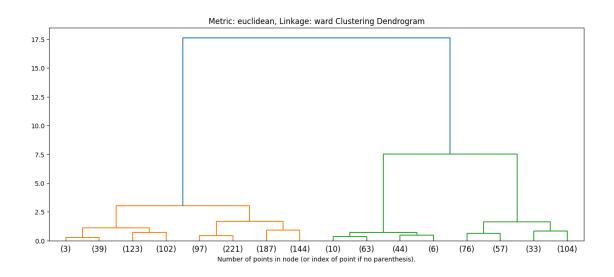
In our case 'complete' linkage won out over 'ward' fairly significantly. From the dendrogram, the complete scheme interprets groupings more evenly, with agglomeration occurring at more consistant distances. The ward scheme is comparitively squashed, and percieves the final two groups as significantly farther apart.

```
[8]: X_zo[:, 1] = np.vectorize(lambda x: x/1.4)(X_zo[:, 1]) # 'sex'
     X_{zo}[:, 0] = np.vectorize(lambda x: x/1.4)(X_{zo}[:, 0]) # 'pclass'
     X_svd = pd.DataFrame(TruncatedSVD(n_components=2, algorithm='arpack',_
      →random_state=RANDOMSTATE).fit_transform(X_zo),
                          columns=['pc1', 'pc2'])
     X_nmf = pd.DataFrame(NMF(n_components=2, init='random', max_iter=400,
                              beta_loss='frobenius', solver='cd',
                              random_state=RANDOMSTATE).fit_transform(X_zo),
                          columns=['pc1', 'pc2'])
     def plot_dendrogram(model, **kwargs):
         # Create linkage matrix and then plot the dendrogram
         # create the counts of samples under each node
         counts = np.zeros(model.children .shape[0])
         n_samples = len(model.labels_)
         for i, merge in enumerate(model.children_):
             current_count = 0
             for child_idx in merge:
                 if child_idx < n_samples:</pre>
                     current_count += 1 # leaf node
                 else:
                     current_count += counts[child_idx - n_samples]
             counts[i] = current_count
         linkage_matrix = np.column_stack(
             [model.children_, model.distances_, counts]
         ).astype(float)
         dendrogram(linkage matrix, **kwargs)
     metrics = ['euclidean']
     linkages = ['complete', 'ward']
     for linkage in linkages:
         model = AgglomerativeClustering(metric=metrics[0],
                                         distance_threshold=0,
                                         n_clusters=None,
                                         linkage=linkage).fit(X_nmf)
         plt.figure(figsize=(15, 6))
         plt.title(f"Metric: {metrics[0]}, Linkage: {linkage} Clustering Dendrogram")
         plot dendrogram(model, truncate mode="level", p=3)
```

```
plt.xlabel("Number of points in node (or index of point if no parenthesis).

→")
plt.show()
```





```
[9]: from sklearn.feature_selection import RFECV
from sklearn.ensemble import GradientBoostingClassifier
from sklearn.model_selection import StratifiedKFold

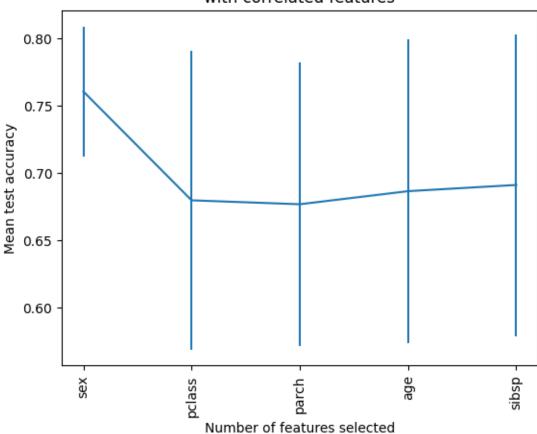
min_features_to_select = 1
clf = GradientBoostingClassifier()
cv = StratifiedKFold(4)

rfecv = RFECV(
```

```
estimator=clf,
    step=1,
    cv=cv,
    scoring="balanced_accuracy",
    min_features_to_select=min_features_to_select,
    n_{jobs=2},
X = pd.DataFrame(X_zo, columns=td.columns).drop(columns=['embarked','fare'])
rfecv.fit(X, gtruth)
print(f"Optimal number of features: {rfecv.n_features_}")
cv_results = pd.DataFrame(rfecv.cv_results_)
plt.figure()
plt.xlabel("Number of features selected")
plt.ylabel("Mean test accuracy")
plt.errorbar(
    x=rfecv.feature_names_in_,
    y=cv_results["mean_test_score"],
    yerr=cv_results["std_test_score"],
plt.xticks(rotation=90)
plt.title("Recursive Feature Elimination \nwith correlated features")
plt.show()
```

Optimal number of features: 1

# Recursive Feature Elimination with correlated features



## 0.0.3 Cabin Subset

```
cabins = df[df.cabin.notna()].cabin.str[0].map({'A': 0, 'B': 1, 'C': 2, 'D': 3,__
      tdc = td[df.cabin.notna()]
[11]: tdc = tdc.reset_index(drop=True)
     tdc
[11]:
          pclass
                  sex
                           fare
                                 embarked
                                                 age parch
                                                            sibsp
                       211.3375
               1
                    1
                                        0
                                           29.000000
     1
               1
                    0
                       151.5500
                                        0
                                            0.916700
                                                          2
                                                                 1
     2
               1
                       151.5500
                                            2.000000
                                                          2
                                                                 1
                    1
                                        0
                                                          2
     3
               1
                    0 151.5500
                                        0 30.000000
                                                                 1
     4
                       151.5500
                                        0 25.000000
                                                          2
                                                                 1
               1
     290
                    1
                        16.7000
                                            4.000000
                                                          1
                                                                 1
               3
     291
                    0
                        7.6500
                                        0 19.000000
                                                          0
                                                                 0
               3
     292
               3
                    1
                        10.4625
                                        0
                                           2.000000
                                                          1
                                                                 0
     293
               3
                   1
                        10.4625
                                        0 29.000000
                                                          1
                                                                 1
     294
                    0
                                                                 0
               3
                        7.7500
                                        2 30.585233
                                                          0
     [295 rows x 7 columns]
[12]: for column in list(tdc.columns):
         print(column, len(tdc[column].unique()))
     pclass 3
     sex 2
     fare 112
     embarked 3
     age 73
     parch 5
     sibsp 4
[15]: from sklearn.decomposition import PCA
     X std = StandardScaler(with_mean=True, with_std=True).fit_transform(tdc)
     X_zo = MinMaxScaler(feature_range=(0, 1)).fit_transform(tdc)
     X_svd = pd.DataFrame(PCA(n_components=2, svd_solver='full',_
      →random_state=RANDOMSTATE).fit_transform(X_std),
                          columns=['pc1', 'pc2'])
     X_nmf = pd.DataFrame(NMF(n_components=2, init='random',__
       →random_state=RANDOMSTATE).fit_transform(X_zo),
                          columns=['pc1', 'pc2'])
     fig, axes = plt.subplots(3, 2, figsize=(20, 20), sharey=False)
```

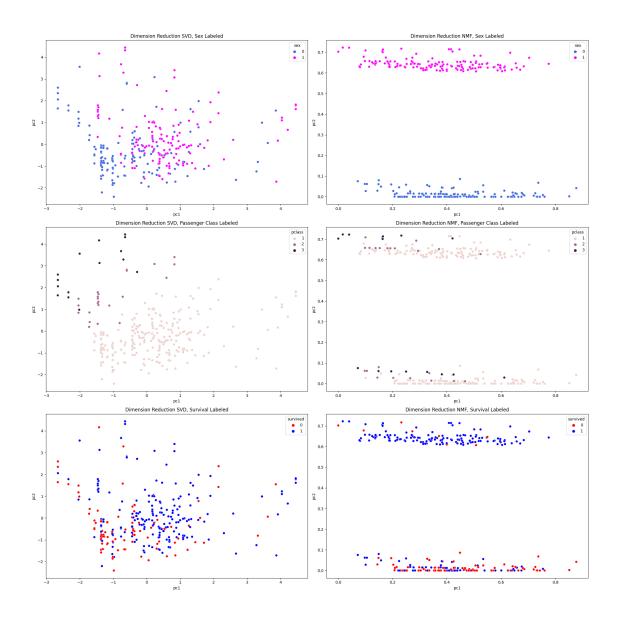
```
sns.scatterplot(x='pc1', y='pc2', data=X_svd, hue=tdc.sex, palette={0:__

¬'royalblue', 1: 'magenta'}, ax=axes[0][0])

axes[0][0].set_title('Dimension Reduction SVD, Sex Labeled')
sns.scatterplot(x='pc1', y='pc2', data=X nmf, hue=tdc.sex, palette={0:11

¬'royalblue', 1: 'magenta'}, ax=axes[0][1])

axes[0][1].set_title('Dimension Reduction NMF, Sex Labeled')
sns.scatterplot(x='pc1', y='pc2', data=X svd, hue=tdc.pclass, ax=axes[1][0])
axes[1][0].set_title('Dimension Reduction SVD, Passenger Class Labeled')
sns.scatterplot(x='pc1', y='pc2', data=X_nmf, hue=tdc.pclass, ax=axes[1][1])
axes[1][1].set_title('Dimension Reduction NMF, Passenger Class Labeled')
sns.scatterplot(x='pc1', y='pc2', data=X_svd, hue=df[df.cabin.notna()].survived.
_reset_index(drop=True), palette={0: 'red', 1: 'blue'}, ax=axes[2][0])
axes[2][0].set_title('Dimension Reduction SVD, Survival Labeled')
sns.scatterplot(x='pc1', y='pc2', data=X_nmf, hue=df[df.cabin.notna()].survived.
oreset_index(drop=True), palette={0: 'red', 1: 'blue'}, ax=axes[2][1])
axes[2][1].set title('Dimension Reduction NMF, Survival Labeled')
plt.tight_layout()
plt.show()
```



[]: