

### Assignment 1

1) Convert the following binary numbers to decimal: 10011101, 1011011.1011.

$$10011101 = 2^7 + 2^4 + 2^3 + 2^2 + 1 = 128 + 16 + 8 + 4 + 1 = 157$$

$$10110101,1011 = 2^7 + 2^5 + 2^4 + 2^2 + 1 + 2^{-1} + 2^{-3} + 2^{-4} = 128 + 32 + 16 + 4 + 1 + (\frac{1}{2}) + (1/8) + (1/16) = 181 + (11/16)$$

2) Convert the following decimal numbers to binary: 1854, 1904 .

$$1854 = [ (1854 - 1024 = 830 - 512 = 318 - 256 = 62 - 32 = 30 - 16 = 14 - 8 = 6 - 4 = 2 - 2 = 0 ) ] \\ = 11100111110$$

$$1904 = [ 1904 - 1024 = 880 - 512 = 368 - 256 = 112 - 64 = 48 - 32 = 16 - 16 = 0 ] \\ = 11101110000$$

3) Convert the following decimal numbers to the indicated bases: 4539.61 to octal, 8961.459 to hexadecimal

$$4539.61 [ 4539 = 8 * 567 + 3 \quad 867 = 8 * 70 + 7 \quad 70 = 8 * 8 + 6 \quad 8 = 8 * 1 ] , [ 0,61 * 8 = 4,88 \quad 0,88 * 8 = 7,04 \\ 0,04 * 8 = 0,32 ] = 10673_8 , 470_8$$

$$8961.459 [ 8961 = 16 * 560 + 1 \quad 560 = 16 * 35 \quad 35 = 16 * 2 + 3 ] , [ 0,459 * 16 = 7,344 \quad 0,344 * 16 = 5,504 \\ 0,504 * 16 = 8,064 ] = 2301,426_8$$

4) Perform the following binary multiplication: 111001\*1010111

$$\begin{array}{r} 111001 \\ 1010111 \\ * \hline 111001 \\ 111001 \\ 111001 \\ 111001 \\ 111001 \\ 111001 \\ + \hline 1001101011111_2 \end{array}$$

5) The following calculation was performed by a particular breed of unusually intelligent chicken. If the base  $r$  used by the chicken corresponds to its total number of toes, how many toes does the chicken have on each foot?

$$[ 43_r + 61_r ] * 35_r = 5416_r$$

$$[3 + 4r + 1 + 6r] * [5 + 3r] = 6 + r + 4 * r^2 + 5 * r^3$$

$$[10r + 4] * [5 + 3r] = 6 + r + 4 * r^2 + 5 * r^3$$

$$30 * r^2 + 62 * r + 20 = 6 + r + 4 * r^2 + 5 * r^3$$

$$5 * r^3 - 26 * r^2 - 61 * r - 14 = 0$$

r must be greater than 6...

6) Represent the decimal numbers 651 and 1904 in BCD, then show the steps necessary to form their sum.

$$651 = (110)(101)(001)_{BCD}$$

$$1904 = (0001)(1001)(0000)(0100)_{BCD}$$

$$+ \text{-----}$$

$$(0001)(1010)(1010)(1101)_{BCD}$$