

# COMP 249 LC QUIZ ANSWERS

1.

$$x'y'z + w'xz + wxy'z' + wxz + w'xyz = y'z + xz + wxy$$

$$\rightarrow = x'y'z + xz(w+w') + wxyz' + w'xyz$$

$$= x'y'z + xz(1+w'y) + wxyz'$$

$$= z(x + x'y') + wxy z'$$

$$= z(x+y') + wxy z'$$

$$= xz + y'z + wxy'z'$$

$$= x(z + w y z') + y' z$$

$$= x(z + w y) + y' z$$

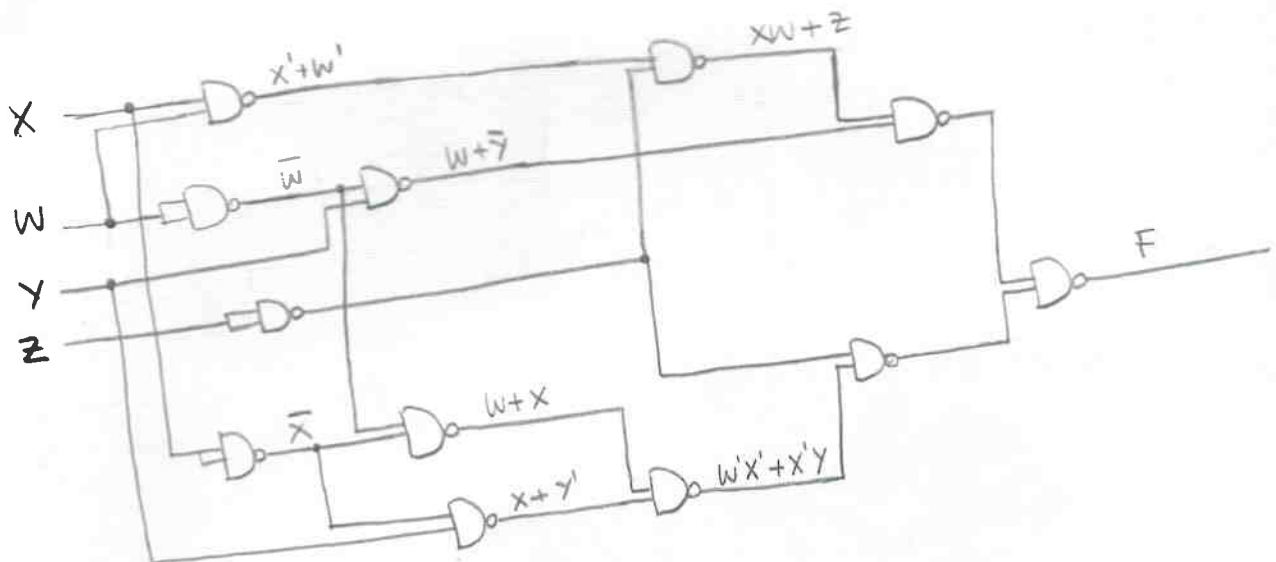
$$= xz + y'z + wxy \quad \checkmark$$

(30 points)

2.

$$f = z(x'y + w'x') + (w+y')(xw+z)$$

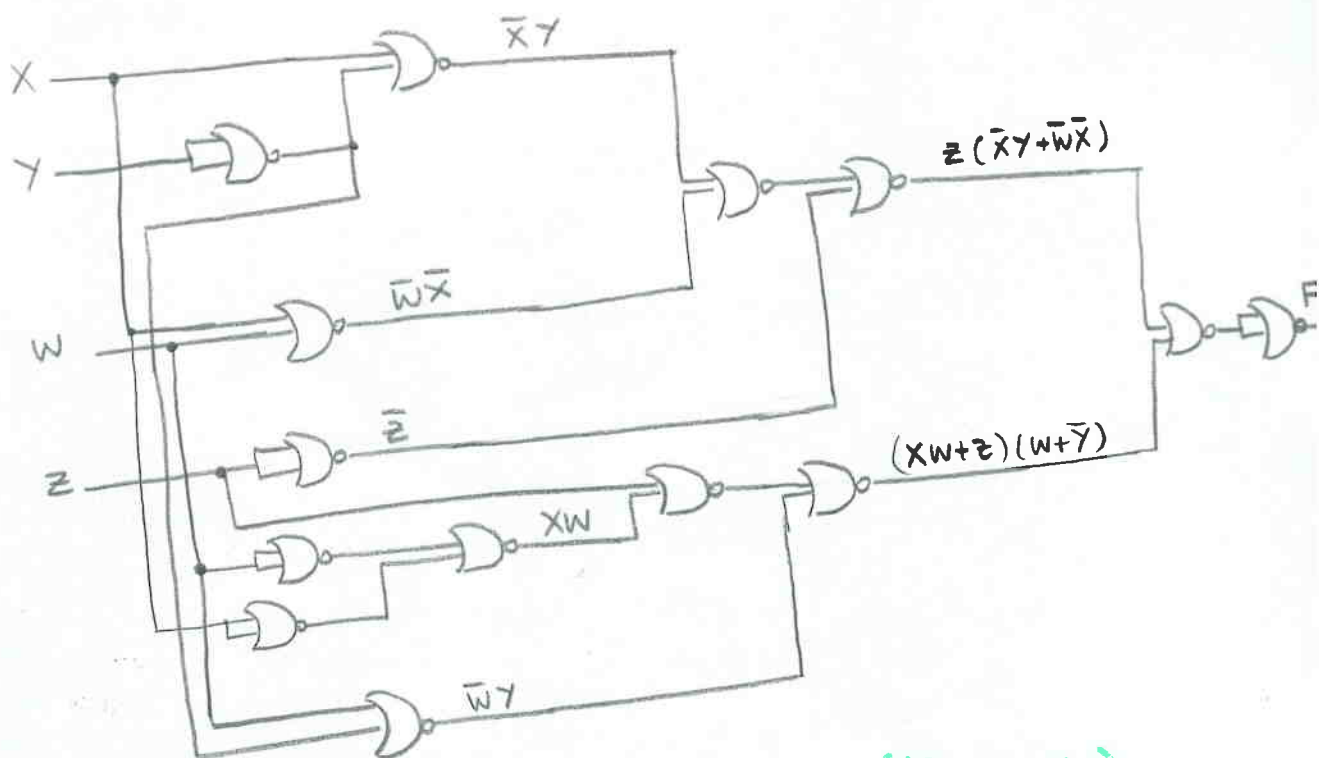
a.



- using only NAND gates -

(17 points)

b.  $f = z(x'y + w'x') + (w+y')(xw+z)$



(18 points)

3.  $f(a,b,c,d) = \sum m(0,2,4,5,6,7,8,9,10,14) + \sum d(3,13)$

(35 points)

List 1:

$m_i$	a	b	c	d	
0	0	0	0	0	✓
2	0	0	1	0	✓
4	0	1	0	0	✓
8	1	0	0	0	✓
3	0	0	1	1	✓
5	0	1	0	1	✓
6	0	1	1	0	✓
9	1	0	0	1	✓
10	1	0	1	0	✓
7	0	1	1	1	✓
13	1	1	0	1	✓
14	1	1	1	0	✓

List 2:

Product Terms	a	b	c	d	
(0,2)	0	0	-	0	✓
(0,4)	0	-	0	0	✓
(0,8)	-	0	0	0	✓
(2,3)	0	0	1	-	✓
(2,6)	0	-	1	0	✓
(2,10)	-	0	1	0	✓
(4,5)	0	1	0	-	✓
(4,6)	0	1	-	0	✓
(8,9)	1	0	0	-	PI6
(8,10)	1	0	-	0	✓
(3,7)	0	-	1	1	✓
(5,7)	0	1	-	1	✓
(5,13)	-	1	0	1	PI7
(6,7)	0	1	1	-	✓
(6,14)	-	1	1	0	✓
(9,13)	1	-	0	1	PI8
(10,14)	1	-	1	0	✓

List 3:

Product Terms	a	b	c	d	
(0,2,4,6)	0	-	-	0	PI1
(0,2,8,10)	-	0	-	0	PI2
(0,4,2,6)	0	-	-	0	PI2
(0,8,2,10)	-	0	-	0	PI2
(2,3,6,7)	0	-	1	-	PI3
(2,6,3,7)	0	-	1	-	PI3
(2,10,6,14)	-	-	1	0	PI4
(2,6,10,14)	-	-	1	0	PI4
(4,5,6,7)	0	1	-	-	PI5
(4,6,5,7)	0	1	-	-	PI5

PI Chart

PI	0	2 <sup>✓</sup>	4	5	6 <sup>✓</sup>	7	8	9	10 <sup>✓</sup>	14 <sup>✓</sup>
PI1	x	x	x		x					
PI2	x	x					x		x	
PI3		x			x	x				
PI4*		x			x				x	x
PI5			x	x	x	x				
PI6							x	x		
PI7				x						
PI8								x		

Reduced PI Chart

PI	0	4	5	7	8	9
PI1	x	x				
PI2	x				x	
PI4				x		
PI5		x	x	x		
PI6					x	x
PI7			x			
PI8						x

PI1 + PI6 → covers PI2

PI6 → covers PI8

PI5 → covers PI4 + PI7

EPI's : EPI1 + EPI4 + EPI5 + EPI6

$$= a'd' + cd' + a'b + ab'c'$$