

# Manufacturing System Analysis Experiment

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Variability

# 1. Experiment Overview

- Title

**Understanding of variability basic concept**

- Objective

- Understand the effects of the process time variability (availability & setup) on jobs
- Observe the changes in variability from different parameter values using ARENA simulation

## 2. Theoretical Background

- Coefficient of Variation (CV)

- $c_0 = \frac{\sigma_0}{t_0}$  ( $t_0$ : base process mean time)

- Availability

- $A = \frac{m_f}{m_f + m_r}$  ( $m_f$ : mean time between failures,  $m_r$ : mean time to repair)

## 2. Theoretical Background

- Variability from breakdown

- $t_e = \frac{t_0}{A}$  ( $t_e$  : *mean process time of a job*)

- $\sigma_e^2 = \frac{\sigma_0^2}{A^2} + \frac{(m_r^2 + \sigma_0^2)(1-A)t_0}{Am_r}$ ,  $c_r = \frac{\sigma_r}{m_r}$

- $c_e^2 = c_0^2 + \frac{(1+c_r^2)A(1-A)m_r}{t_0}$

➤ Decreasing MTTF (Mean Time To Failure) and MTTR (Mean Time To Repair) reduces the variability

## 2. Theoretical Background

- Variability from setup

- $t_e = t_0 + \frac{t_s}{N_s}$  ( $t_s$  : *average setup time*,  $N_s$  :  
*average number of parts between setups*)

- $\sigma_e^2 = \sigma_0^2 + \frac{\sigma_s^2}{N_s} + \frac{N_s-1}{N_0^2} t_0^2$

- $c_e^2 = \frac{\sigma_e^2}{t_e^2}$

➤ Decreasing setup time and cycle time reduces the variability

# 3. Experiment Design

1. Yonsei Electronics plant manager is trying to buy a new machine to replace the old machine. Each machine has the same conditions except for the few minor differences shown in the table below. Do a experiment to decide which machine is more effective.

- Variability from breakdown

	MTTF	MTTR		Process time (Constant)
Hare X19	774 minutes	248 minutes	$Cr = 0$	$t_0 = 15\text{ minutes}$
Tortoise 2000	114 minutes	38 minutes		

- Calculate  $t_e$  (effective mean process time),  $\sigma_e^2$  (effective variance process time),  $c_e^2$  (effective squared coefficient), and  $r_e$  (effective capacity) with given equations, and calculate which machine has bigger variability.

- Based on the calculation, compare the WIP and TH and explain which machine is better.

### 3. Experiment Design

2. Under same situation, machine replacement for different production line has a machine with longer process time and no setup time, and other machine with shorter process time and setup time. Calculate the variability using the equations given like the first problem, and compare the results.

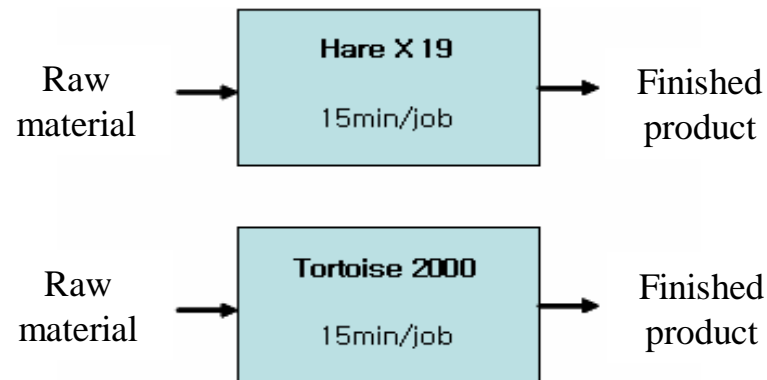
	Process time (NORM)		Setup
Machine 1	$t_0 = 1.2$ hours	$\sigma = 0.25$	-
Machine 2	$t_0 = 1.0$ hours	$\sigma = 0.125$	$N_s = 10, t_s = 2 \text{ hours}, \sigma = 0.125$

## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ▪ Step 1-1. Simulation summary

- Simulation consists of two systems with one machine
- Each system has same arrival interval and processing time
- Each system has different MTTF and MTTR
- Statistics on WIP and TH of two systems with same availability, but different MTTR and MTTF
- Simulation runs for one week (7 days x 24 hr/day) and is repeated 30 times



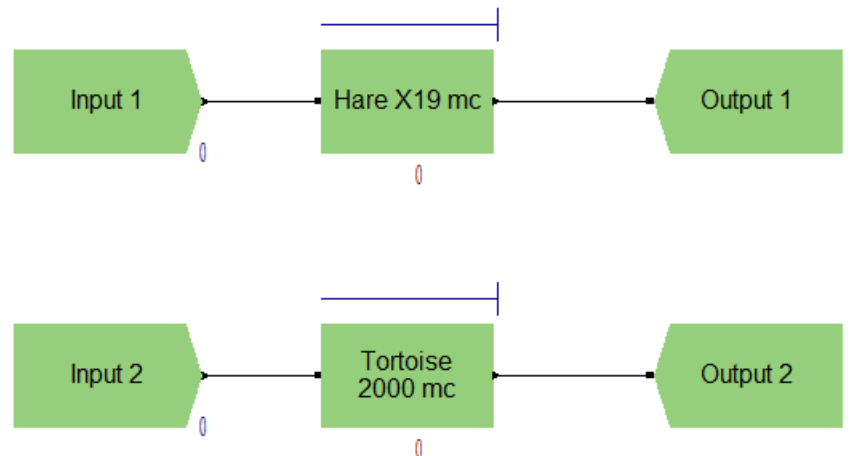


## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ▪ Step 1-2. Creating the model

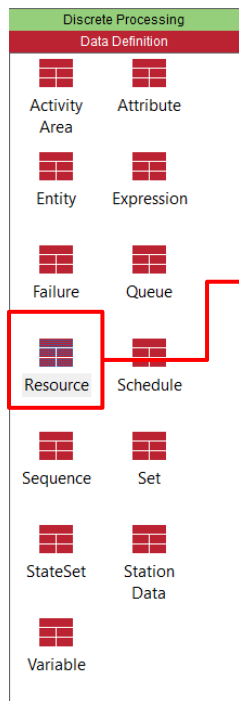
- Basic simulation model is as the picture shown below
- Modules used: 1 Create, 1 Process, 1 Dispose for each system



# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

- **Step 1-2. Creating the model (cont.)**
  - Add resources (M/C) for each system



	Name	Type	Capacity	Busy / Hour	Idle / Hour	Per Use	StateSet Name	Failures	Report Statistics
1	Hare X19	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>
2	Tortoise 2000	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>

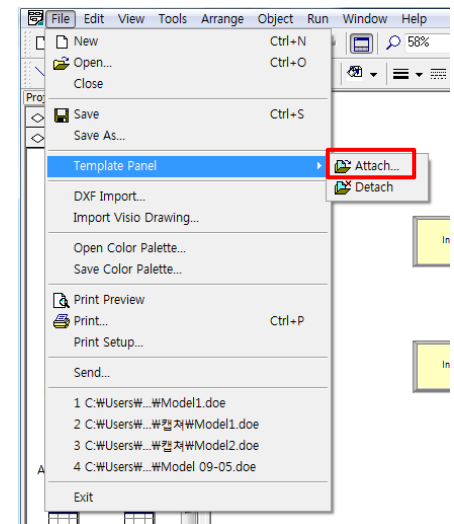
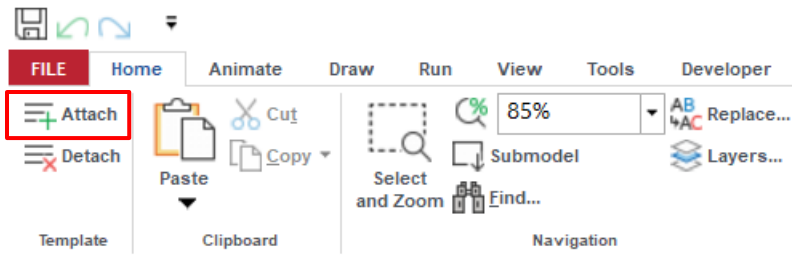
# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ▪ Step 1-2. Creating the model (cont.)

- Each resource has different Break time
- Use Failure module from Advanced process

- File → Template Panel → Attach, open 'Advanced process'

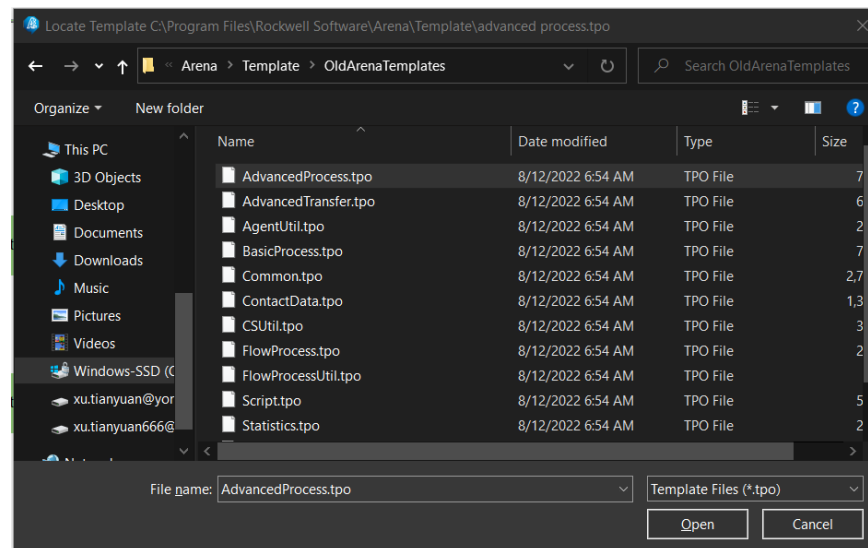


# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ▪ Step 1-2. Creating the model (cont.)

- Each resource has different Break time
- Use Failure module from Advanced process (cont.)
  - File → Template Panel → Attach, open ‘Advanced process’



# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ■ Step 1-2. Creating the model (cont.)

- Set MTTR and MTTF for each machine using Failure module

Activity Area

Attribute

Entity

Expression

Failure

Queue

Resource

Schedule

Sequence

Set

StateSet

Station Data

Variable

	Name	Type	Up Time	Up Time Units	Down Time	Down Time Units	Uptime in this State only
1	Hare_Failure	Time	774	Minutes	248	Minutes	
2	Tortoise_Failure	Time	114	Minutes	38	Minutes	

	MTTF	MTTR
Hare X19	774 minutes	248 minutes
Tortoise 2000	114 minutes	38 minutes

# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ■ Step 1-2. Creating the model (cont.)

- Add failure to each resource

Activity Area

Attribute

Entity

Expression

Failure

Queue

**Resource**

Schedule

Sequence

Set

StateSet

Station Data

Variable

	Name	Type	Capacity	Busy / Hour	Idle / Hour	Per Use	StateSet Name	Failures	Report Statistics	Comment
1	Hare X19	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>	
2	Tortoise 2000	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>	

Double-click here to add a new row

# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

- Step 1-2. Creating the model (cont.)
  - Select failure name (already made) for each resource
  - Set Failure Rule as Ignore

	Name	Type	Capacity	Busy / Hour	Idle / Hour	Per Use	StateSet Name
1	Hare X19	Fixed Capacity	1	0.0	0.0	0.0	
2	Tortoise 2000	Fixed Capacity	1	0.0	0.0	0.0	

Failures

	Failure Name	Failure Rule
1	Failure_Hare	Ignore

Double-click here to add a new row.

	Failure	Report Statistics	Comment
1 rows	<input checked="" type="checkbox"/>		
1 rows	<input checked="" type="checkbox"/>		

## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ■ Step 1-2. Creating the model (cont.)

- Create raw material entities
  - Different entities for each system
  - Each entity will have a statistics in Arena Report
- Time between Arrivals = 0.5 hours

Create

Name: Input 1 Entity Type: Entity 1

Time Between Arrivals

Type: Constant Value: 0.5 Units: Hours

Entities per Arrival: 1 Max Arrivals: Infinite First Creation: 0.0

Comment:

OK Cancel Help

Create

Name: Input 2 Entity Type: Entity 2

Time Between Arrivals

Type: Constant Value: 0.5 Units: Hours

Entities per Arrival: 1 Max Arrivals: Infinite First Creation: 0.0

Comment:

OK Cancel Help



# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ■ Step 1-2. Creating the model (cont.)

- Set action as 'Seize Delay Release'  
= Station seize, process, and return the resource

Process

Name: Hare X19 mc Type: Standard

Logic

Action: Seize Delay Release Priority: Medium(2)

Resources:

Resource: Hare X19, 1  
<End of list>

Add...  
Edit...  
Delete

Delay Type: Constant Units: Hours Allocation: Value Added

Value: 0.25

☒ Report Statistics

Comment:

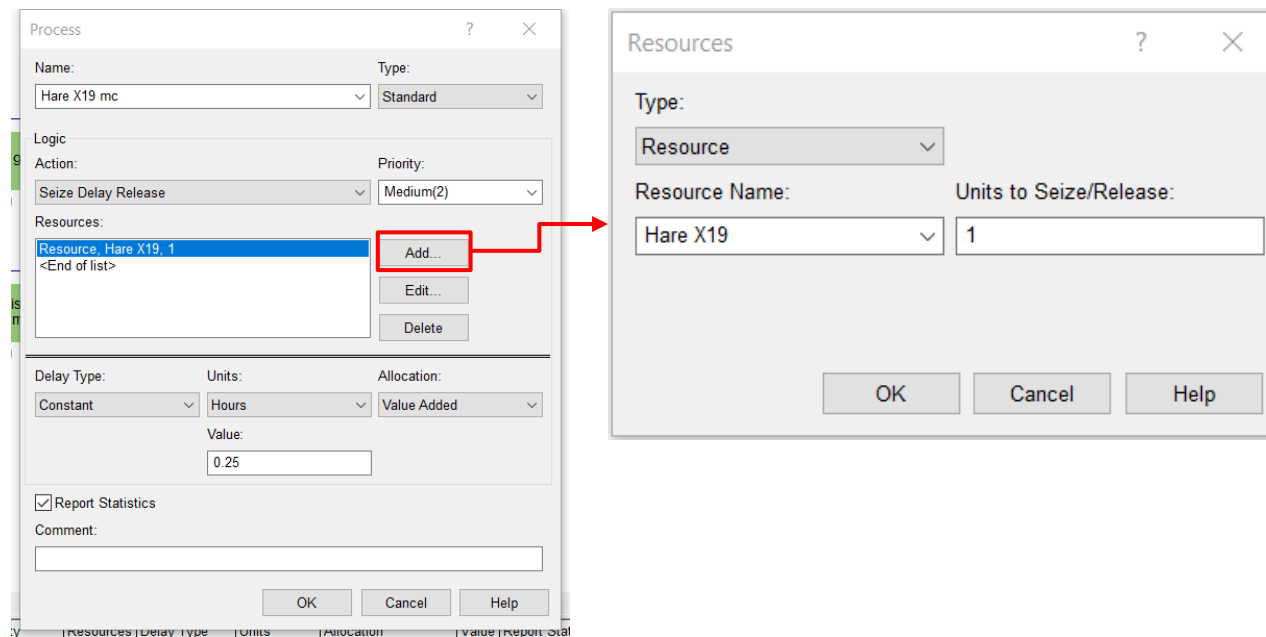
OK Cancel Help

## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ■ Step 1-2. Creating the model (cont.)

- Use Add button to assign resources
- Quantity is the number of resource



## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ■ Step 1-2. Creating the model (cont.)

- Delay Type decides how long a station seizes the resources (actual production time)
- Processing time for both system = 15 minutes

The screenshot shows the 'Process' dialog box with the following settings:

- Name: Hare X19 mc
- Type: Standard
- Logic: Seize Delay Release
- Priority: Medium(2)
- Resources: Resource, Hare X19, 1
- Delay Type: Constant
- Units: Hours
- Allocation: Value Added
- Value: 0.25
- Report Statistics: ☒

The 'Delay Type' section, including the 'Constant' dropdown, 'Hours' units, 'Value Added' allocation, and '0.25' value, is highlighted with a red rectangle.

# 4. Experiment Procedure

## Experiment 1. Variability from breakdown

### ■ Step 2. Compare the performance of two machines

1) Run setup (Run → Setup)

- Set up the repetitive experiment
- Replication length = 1 week (7 days), Number of replications = 30

The screenshot shows the 'Run Setup' dialog box in the Arena simulation software. The left sidebar contains a menu with options: Run Speed, Run Control, Reports, Project Parameters, Replication Parameters (highlighted in red), Array Sizes, and Arena Visual Designer. The main area is titled 'Replication Parameters' and contains the following fields:

- Number of Replications: 30 (highlighted with a red box)
- Start Date and Time: Friday, May 5, 2023 2:14:35 PM
- Warm-up Period: 0.0 Hours
- Replication Length: 7 Days (highlighted with a red box)
- Hours Per Day: 24
- Terminating Condition: (empty field)
- Base Time Units: Hours

At the top of the main area, there is a descriptive text: 'Establish replication-related options for the current model. Settings include the number of simulation replications to be run, the length of the replication, the start date and time of the simulation, warm-up time length, time units, and the type of initialization to be performed between replications.'

## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ■ Step 2. Compare the performance of two machines

2) Analysis of result report

- To analyze the variability of two machines,
  - Use [*Waiting time*  $\approx V \times U \times t_e$ ]
  - $V$  = variability,  $U$  = utilization ( $u/(1 - u)$ ),  $t_e$  = production time

## 4. Experiment Procedure

### Experiment 1. Variability from breakdown

#### ■ Step 3. Change time intervals & analyze the performance

- Compare the performance of each system by changing time interval from Create module

The screenshot shows a 'Create' dialog box with the following fields and values:

Name:		Entity Type:
Input 1		Entity 1

Time Between Arrivals		
Type:	Value:	Units:
Constant	0.5	Hours

Entities per Arrival:	Max Arrivals:	First Creation:
1	Infinite	0.0

Comment:

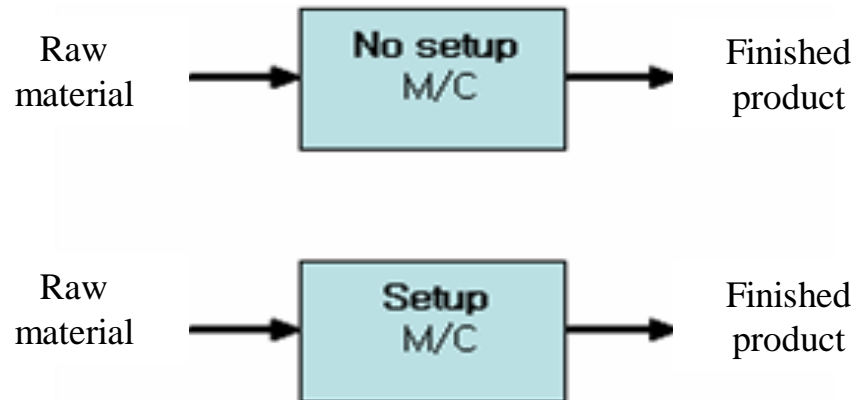
OK Cancel Help

## 4. Experiment Procedure

### Experiment 2. Variability from setup

#### ■ Step 1-1. Simulation summary

- Simulation consists of a system with setup and a system without setup
- Analyzing variability of each system with one M/C
- Simulation runs for one week (7 days x 24 hr/day) and is repeated 30 times



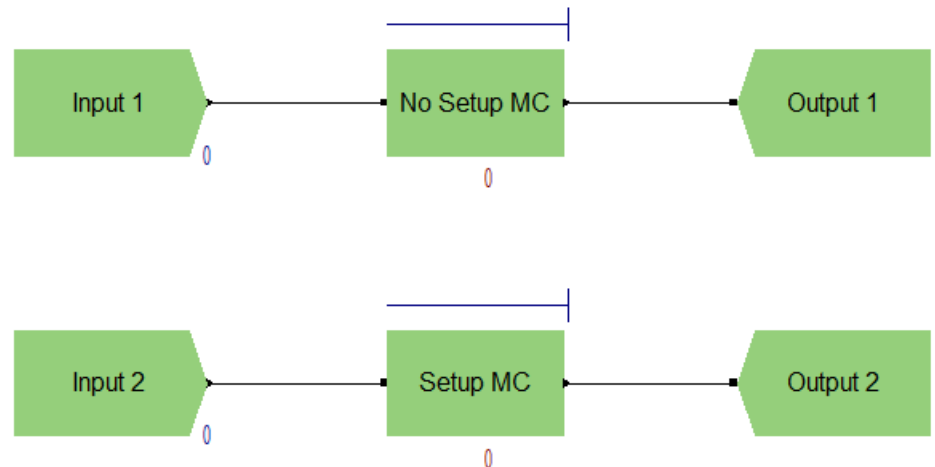
<Picture 2> Production system (2)

# 4. Experiment Procedure

## Experiment 2. Variability from setup

### ■ Step 1-2. Creating the model

- Basic simulation model is as the picture below
- Modules: 1 Create, 1 Process, 1 Dispose for each system





# 4. Experiment Procedure

## Experiment 2. Variability from setup

- Step 1-2. Creating the model (cont.)
  - Add resources (M/C) for each system

Discrete Processing

Data Definition

Activity Area

Attribute

Entity

Expression

Failure

Queue

Resource

Schedule

Sequence

Set

StateSet

Station Data

Variable

	Name	Type	Capacity	Busy / Hour	Idle / Hour	Per Use	StateSet Name	Failures	Report Statistics	Comment
1 ▶	No Setup	Fixed Capacity	1	0.0	0.0	0.0		0 rows	<input checked="" type="checkbox"/>	
2	Setup	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>	

Double-click here to add a new row.

# 4. Experiment Procedure

## Experiment 2. Variability from setup

### ■ Step 1-2. Creating the model (cont.)

- Add setup time using Failure module
- Set Type as count (Resource works on the number of counts and becomes down = machine is idle for setup)

Activity Area

Attribute

Entity

Expression

**Failure**

Queue

Resource

Schedule

Sequence

Set

StateSet

Station Data

Variable

	Name	Type	Count	Down Time	Down Time Units	Comment
1 ▶	Setup time	Count	10	NORM(2,0.125)	Hours	
Double-click here to add a new row.						

	Setup
Machine 1	-
Machine 2	$N_s = 10, t_s = 2 \text{ hours}, \sigma = 0.125$

# 4. Experiment Procedure

## Experiment 2. Variability from setup

### ■ Step 1-2. Creating the model (cont.)

- Add failure to each resource
- Select failure name (already made) for each resource
- Set Failure Rule as Ignore



	Name	Type	Capacity	Busy / Hour	Idle / Hour	Per Use	StateSet Name	Failures	Report Statistics	Comment
1 ▶	No Setup	Fixed Capacity	1	0.0	0.0	0.0		0 rows	<input checked="" type="checkbox"/>	
2	Setup	Fixed Capacity	1	0.0	0.0	0.0		1 rows	<input checked="" type="checkbox"/>	

Double-click here to add a new row.

# 4. Experiment Procedure

## Experiment 2. Variability from setup

### ■ Step 1-2. Creating the model (cont.)

- Create raw material entities (different entities for each system)
- Time between Arrivals = 1.2 hours
- Set up Process modules same as experiment 1

**Create**

Name:  Entity Type:

Time Between Arrivals

Type:  Value:  Units:

Entities per Arrival:  Max Arrivals:  First Creation:

Comment:

OK Cancel Help

**Process**

Name:  Type:

Logic

Action:  Priority:

Resources:

Add... Edit... Delete

<End of list>

Delay Type:  Units:  Allocation:

Value:

☒ Report Statistics

Comment:

OK Cancel Help

## 4. Experiment Procedure

### Experiment 2. Variability from setup

#### ■ Step 2. Compare the performance of two machines

1) Run setup (Run  $\rightarrow$  Setup)

- Set up the repetitive experiment
- Replication length = 1 week (7 days), Number of replications = 30

## 4. Experiment Procedure

### Experiment 2. Variability from setup

#### ■ Step 2. Compare the performance of two machines

1) Analysis of result report

- To analyze the variability of two machines,
  - Use *Waiting time*  $\approx V \times U \times t_e$
  - $V$  = variability,  $U$  = utilization ( $u/(1 - u)$ ),  $t_e$  = production time

## 4. Experiment Procedure

### Experiment 2. Variability from setup

#### ■ Step 3. Change time intervals & analyze the performance

- Like experiment 1, compare the performance of each system by changing time interval from Create module

#### ■ Step 4. Change Setup & analyze the performance

- Change set up frequency ( $N_s$ ) and time ( $t_s$ )
- Analyze the performance

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***Q & A***

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