

EXERCICES	POINTS
Exercise 1	10
Exercise 2	10
Exercise 3	30
Exercise 4	50
TOTAL	100

Exercise 1: Boolean expression

Demonstrate these equalities using the 7 simplification rules you have learnt.

$$\begin{aligned}
 1. \quad & (A \text{ or } B \text{ or } C) \text{ and } (!A \text{ or } B \text{ or } C) = B \text{ or } C \\
 & = (A \text{ or } !A) \text{ and } (B \text{ or } C) \\
 & = \text{True and } (B \text{ or } C)
 \end{aligned}$$

$$2. \quad (A \text{ and } B) \text{ or } (!A \text{ or } !B) = \text{True}$$

$$\text{False or true} = \text{True}$$

Exercise 2: Truth table

1. A and (A or B)

A	B	A and (A or B)
True	True	True
True	False	True
False	True	False
False	False	False

$$\begin{aligned}
 A \text{ and } (A \text{ or } B) &= (A \text{ and } A) \text{ or } (A \text{ and } B) \\
 &= A \text{ or } (\text{True and } A) \\
 &= A
 \end{aligned}$$

2. (A and B) or !C or [C and (!A or !B)]

A	B	C	(A and B) or !C or [C and (!A or !B)]
True	True	True	(True and True) or !True or [True and (! True or !True)] = True
True	True	False	(True and true) or !False or [False and (!True or !True)] = True
True	False	True	(True and False) or !True or [True and (!True or !False)] = True
True	False	False	(True and False) or !False or [False and (!True or !False)] = True
False	True	True	(False and True) or !True or [True and (!False or ! True)] = True
False	True	False	(false and True) or !False or [false and (!False or !True)] = True
False	False	True	(false and False) or !True or [true and (!Fasle or !false)] = true
False	False	False	(Fasle and False) or !false or [False and (!False or !False)] =True

$$\begin{aligned}
 (A \text{ and } B) \text{ or } !C \text{ or } [C \text{ and } (!A \text{ or } !B)] &= [A \text{ and } (B \text{ or true})] \text{ or } [(C \text{ and } !A) \text{ or } (C \text{ and } !B)] \\
 &= (A \text{ and True}) \text{ or } (\text{ False or false}) \\
 &= \text{True}
 \end{aligned}$$

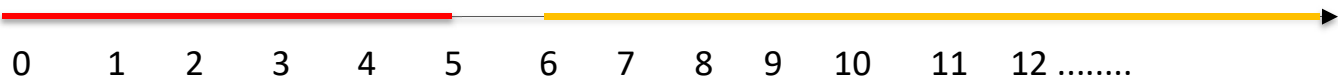
Exercise 3: Ranges

1. **Simplify** the expressions

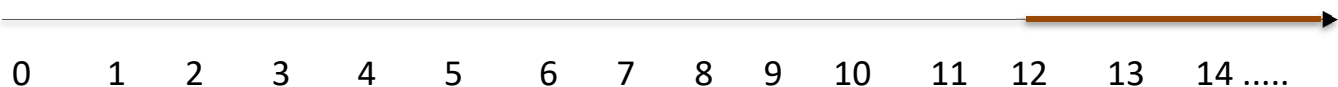
a) $a < 3 \text{ or } a > 3$



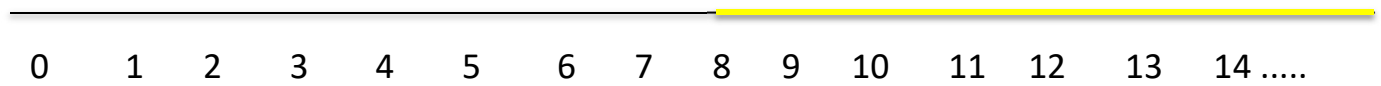
b) $a > 5 \text{ or } a < 6$



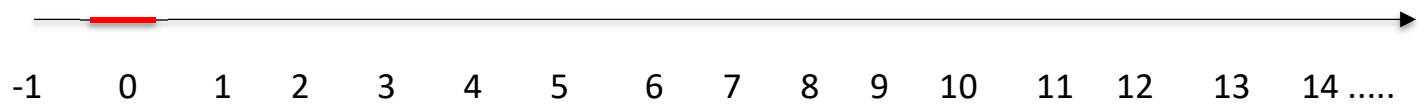
c) $a > 2 \text{ and } a > 12$



d) $a \geq 8$ or $a > 8$

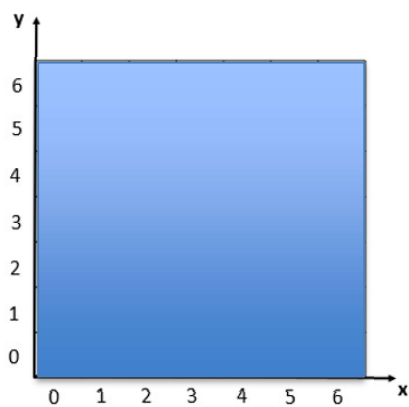


e) $a \geq 0$ and $a \leq 0$

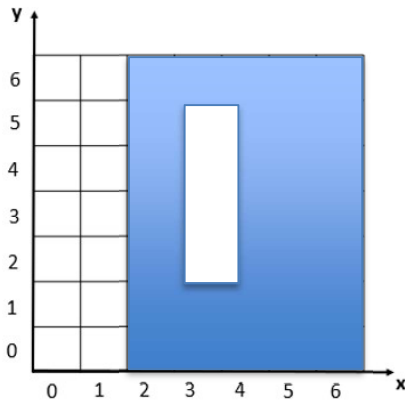


2. Draw the shape corresponding to the boolean expression

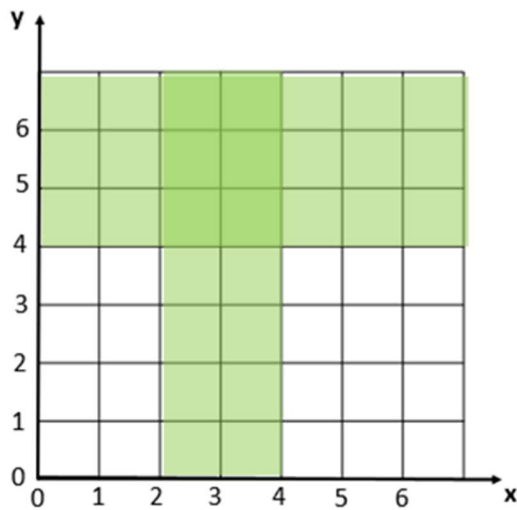
a) $(x = y)$



b) $(x > 2)$ and not($(x > 3$ and $x < 4)$ and $(y > 2$ and $y < 6)$)



a) Write the boolean condition for this grid

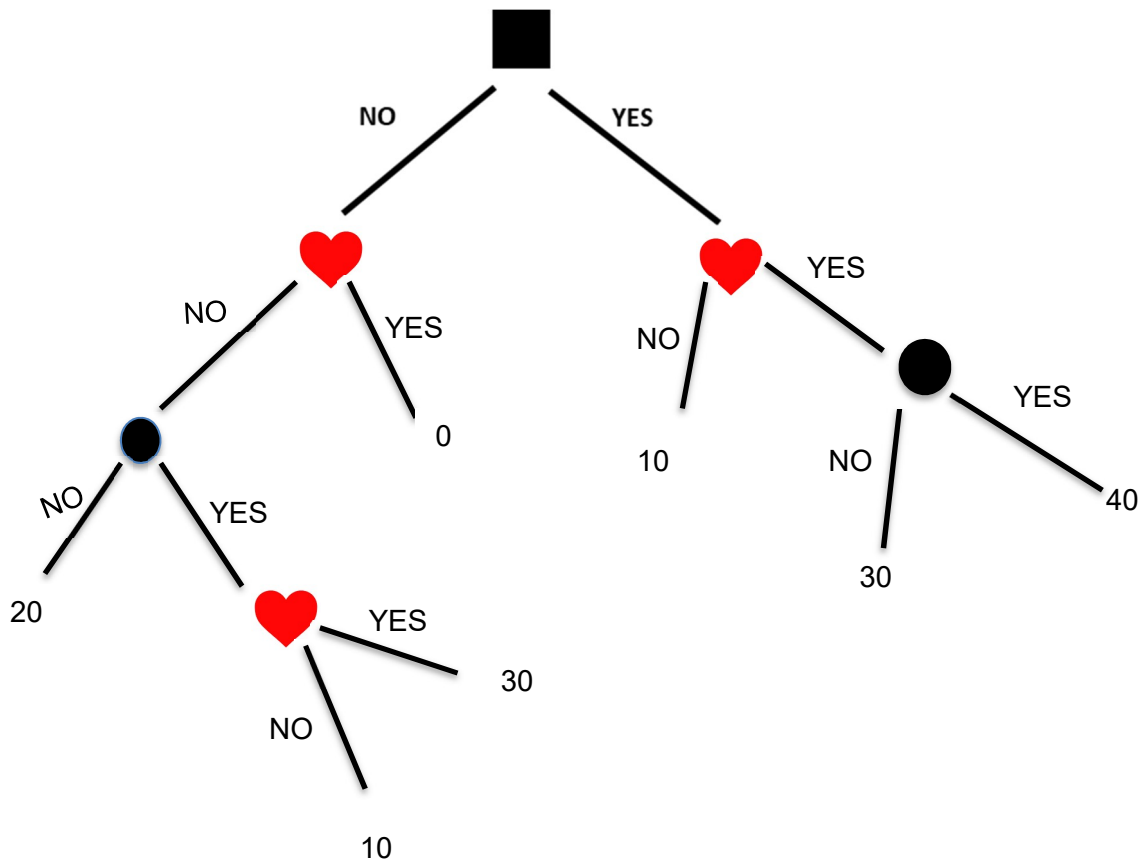


Expression: $(X > 2 \text{ and } X < 4) \text{ or } (Y > 4 \text{ or } Y > 6)$

Exercise 4: Flowcharts

1. Draw the tree of conditions

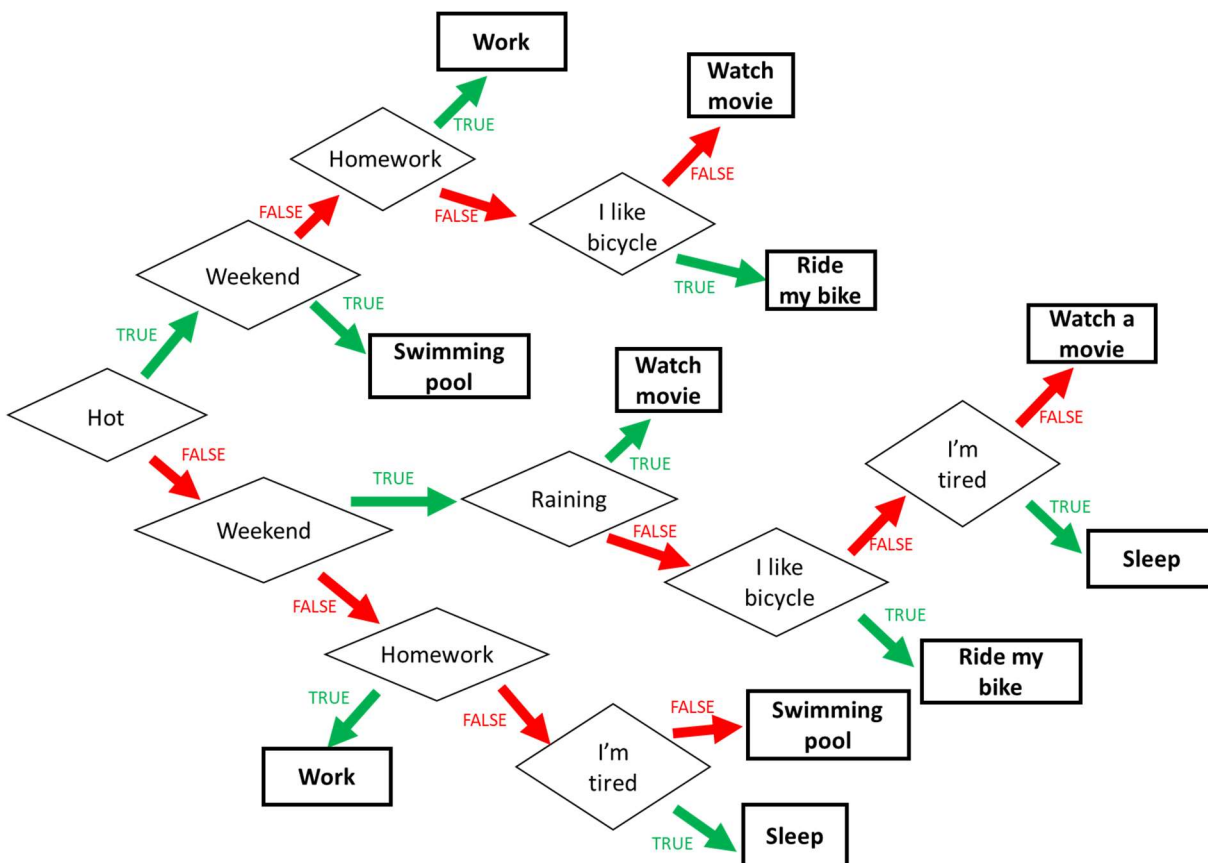
CELLS CONTENT EXACTLY	POINTS
■	10
■ ♥ ●	40
■ ♥	30
<NOTHING>	20
●	10
● ♥	30



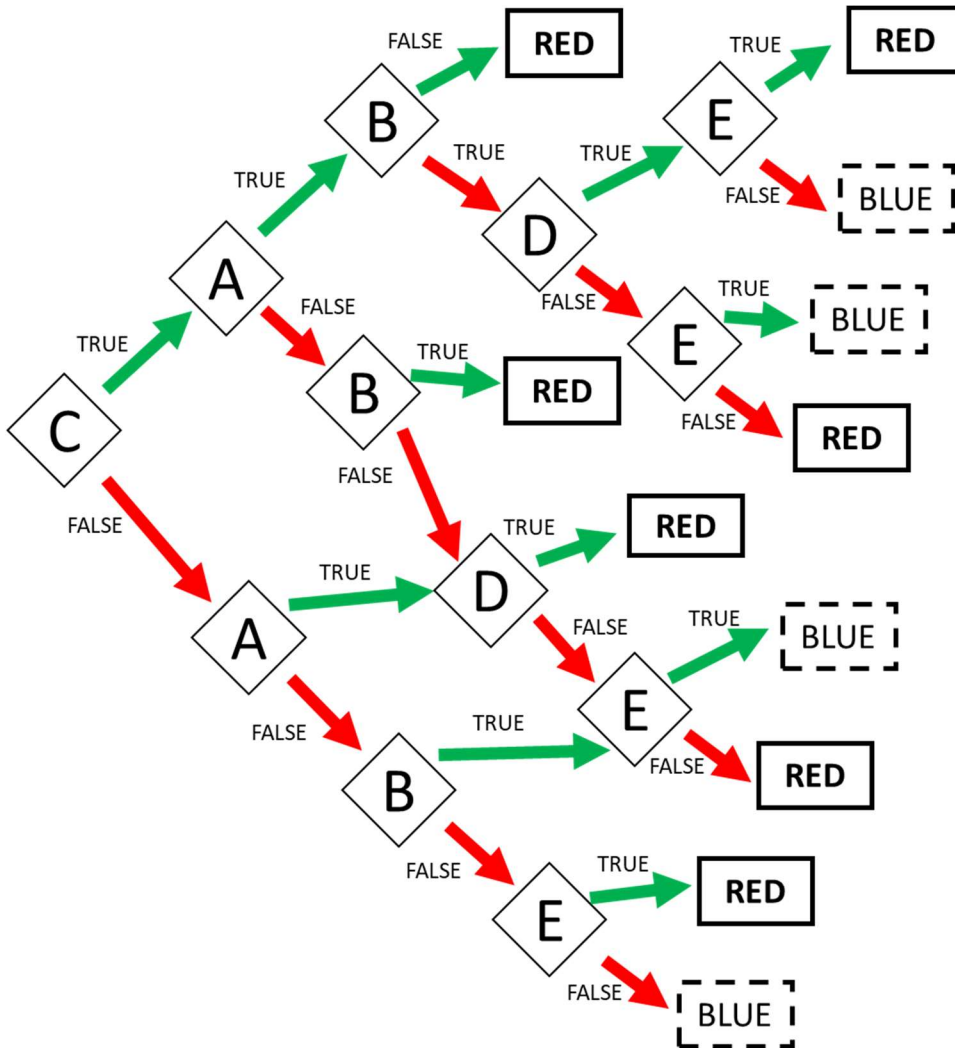
2. Say what I do thanks to the flowchart below?

- a. It is Monday, it's hot and I have homework. What I do? **work**
- b. It's Sunday, it's cold, it's not raining, I don't like bicycle and I'm not tired. What I do? **Watch movie**
- c. It's Friday, it's cold and raining, I'm tired but I don't have homework. What I do? **sleep**
- d. When do I ride my bike? **Give a boolean expression**

Hot and not weekend and don't have homework and I like bicycle OR
Not hot and weekend and not raining and I like bicycle



3. Find the boolean expression of **RED** of this flowchart



Expression: $RED = CAB \text{ or } CA!BDE \text{ or } CA!B!D!E \text{ or } C!AB \text{ or } C!A!BD \text{ or } C!A!B!D!E \text{ or } !CAD \text{ or } !C!AB!E \text{ or } !C!A!BE$