

# HOMEWORK

## EXERCICE 1

Determine the values of A, B, C, and D that makes this expression **false**:

**!A and B and !C and D**

- A. A = 1, B = 0, C = 0, D = 0 false
- B. A = 1, B = 0, C = 1, D = 0 true
- C. A = 0, B = 1, C = 0, D = 0 false
- D. A = 1, B = 0, C = 1, D = 1 false

## EXERCICE 2

Determine the values of A, B, C, and D that makes this expression **true**:

**!A . B . !C . D**

- A. A = 0, B = 1, C = 0, D = 1 true
- B. A = 0, B = 0, C = 0, D = 1 false
- C. A = 1, B = 1, C = 1, D = 1 false
- D. A = 0, B = 0, C = 1, D = 0 false

## EXERCICE 3

True or false?

**AC + ABC = AC true**

To solve this problem:

1- Try using a TRUTH table

A	B	C	$AC + ABC$	AC
False	false	false	false	False
false	True	False	false	false
True	true	false	false	False
True	True	True	True	True
True	False	False	False	False

2- Try using the 7 rules of simplification

$$\begin{aligned}AC + ABC &= AC \text{ or } (AC \text{ and } B) \\&= AC \text{ and } (B \text{ or True}) \\&= AC \text{ and True} \\&= AC\end{aligned}$$

## EXERCICE 5

True or false?

$$A + AB = A \text{ true}$$

To solve this problem:

1- Try using a TRUTH table

A	B	$A + AB$
False	True	False
False	False	False
True	False	False
True	True	True

2- Try using the 7 rules of simplification

$$\begin{aligned}A + AB &= A \text{ or } (A \text{ and } B) \\&= A \text{ and } (B \text{ or True}) \\&= A \text{ and true}\end{aligned}$$

## EXERCICE 6

True or false?

$$A + \neg AB = A + B$$

To solve this problem:

1- Try using a TRUTH table

A	B	$A + \neg AB$	$A + B$
False	False	False	False
False	True	True	True
True	True	true	True
True	False	True	true

2- Try using the 7 rules of simplification

$$\begin{aligned} A + \neg AB &= A \text{ or } (\neg A \text{ and } B) \\ &= A \text{ or } B \\ &= A + B \end{aligned}$$

In the following exercises: you need to use the table of truth to simplify the expression as much as possible

### EX-14

$$A == \text{True and } (B == \text{False or } A == \text{False}) \text{ and } B == \text{True}$$

a	b	$a == \text{True and } (b == \text{False or } a == \text{False}) \text{ and } b == \text{True}$
True	True	$\text{True} == \text{True and } (\text{True} == \text{False or } \text{True} == \text{False}) \text{ and } \text{True} == \text{True} : \text{true}$
True	False	$\text{True} == \text{True and } (\text{False} == \text{False or } \text{True} == \text{False}) \text{ and } \text{False} == \text{True} : \text{False}$
False	True	$\text{False} == \text{True and } (\text{True} == \text{False or } \text{False} == \text{false}) \text{ and } \text{True} == \text{True} : \text{False}$
False	False	$\text{False} == \text{true and } (\text{False} == \text{False or } \text{False} == \text{False}) \text{ and } \text{False} == \text{True} : \text{False}$

The expression is equivalent to:

$$\begin{aligned} A == A \text{ and } (B == \neg B \text{ or } A == \neg B) \text{ and } A == \neg A \\ A == A \text{ and } (B == B \text{ or } A == \neg A) \text{ and } B == A \\ A == \neg A \text{ and } (B == \neg B \text{ or } A == A) \text{ and } B == B \\ A == \neg A \text{ and } (A == A \text{ or } B == B) \text{ and } A == \neg A \end{aligned}$$

## EX-15

$(A == \text{True} \text{ and } B == \text{False}) \text{ or } (A == \text{False} \text{ and } B == \text{True})$
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a	b	$(a == \text{True} \text{ and } b == \text{False}) \text{ or } (a == \text{False} \text{ and } b == \text{True})$
True	True	$(\text{True} == \text{True} \text{ and } \text{True} == \text{False}) \text{ or } (\text{True} == \text{False} \text{ and } \text{True} == \text{True})$
True	False	$(\text{True} == \text{True} \text{ and } \text{False} == \text{False}) \text{ or } (\text{True} == \text{False} \text{ and } \text{False} == \text{True})$
False	True	$(\text{False} == \text{True} \text{ and } \text{True} == \text{False}) \text{ or } (\text{False} == \text{False} \text{ and } \text{True} == \text{True})$
False	False	$(\text{False} == \text{True} \text{ and } \text{False} == \text{False}) \text{ or } (\text{False} == \text{False} \text{ and } \text{False} == \text{True})$

The expression is equivalent to:

$(A == A \text{ and } A == !A) \text{ or } (A == !A \text{ and } A == A)$

$(A == A \text{ and } B == B) \text{ or } (A == !A \text{ and } B == !B)$

$(A == !A \text{ and } B == !B) \text{ or } (A == A \text{ and } B == B)$

$(A == !A \text{ and } B == B) \text{ or } (A == A \text{ and } B == !B \text{ or } == !A)$

## EX-16

$(B \text{ or } !B) \text{ and } A$
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a	b	$(B \text{ or } !B) \text{ and } A$
True	True	$(\text{True} \text{ or } !\text{true}) \text{ and true}$
True	False	$(\text{False} \text{ or } !\text{false}) \text{ and true}$
False	True	$(\text{true} \text{ or } !\text{true}) \text{ and false}$
False	False	$(\text{false} \text{ or } !\text{true}) \text{ and false}$

The expression is equivalent to:

$(A \text{ or } !A \text{ and } !B) \text{ and } A \text{ or } B$

$(B \text{ or } !B) \text{ and } A$