

## Data Mining (Week 1)

# MSc Data Mining

## Topic 07 : Advanced Classification

### Part 01 : Classification2-Overview

Foundational

Exploratory Data  
Analysis

Data Modelling  
Fundamentals

Data Modelling  
Advanced

Rule Based

Association Rules

Recommender Systems

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Supervised

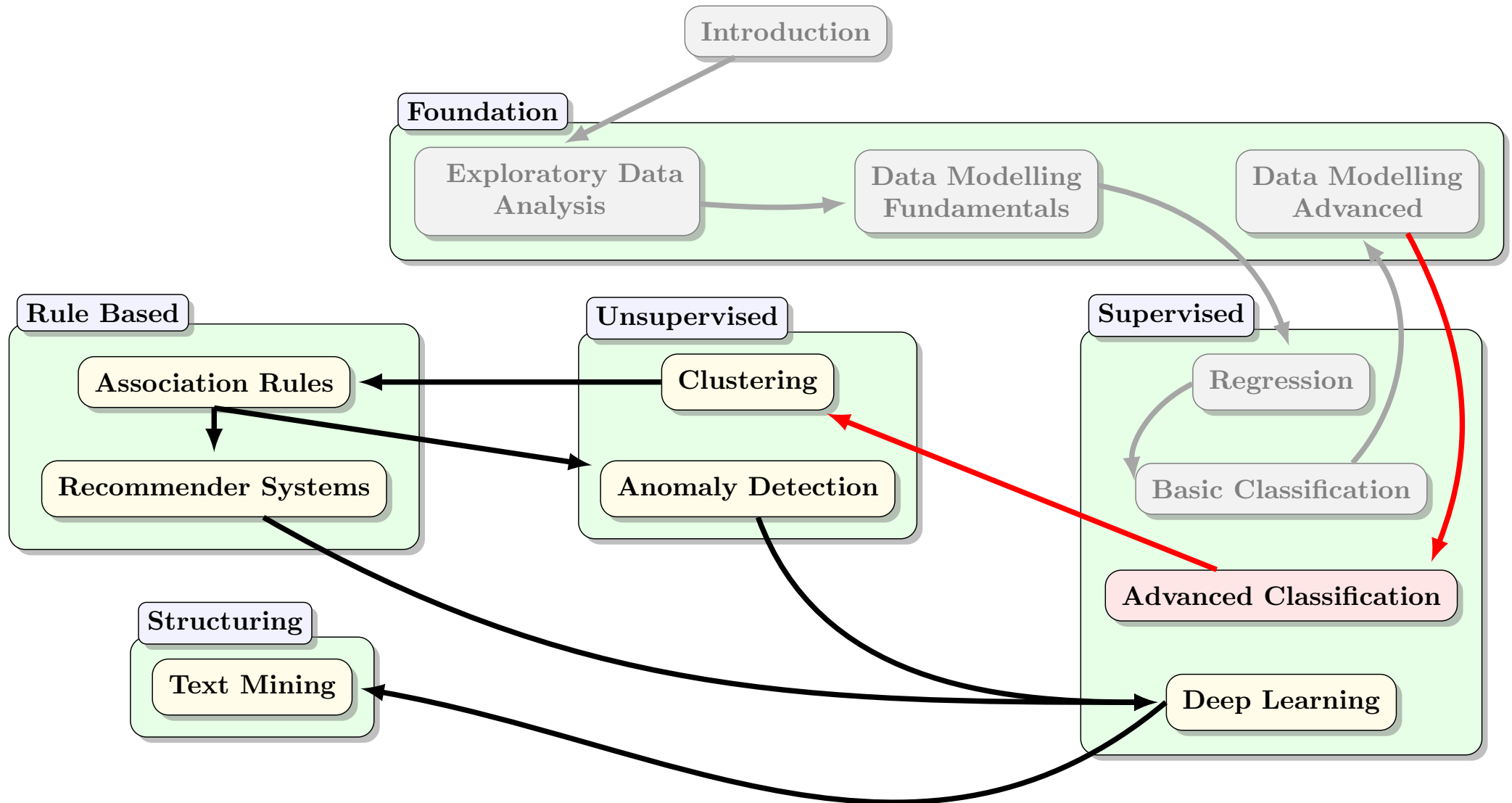
Regression

Basic Classification

### Outline

- Decision Trees
- Ensemble classifiers (Bagging and Boosting)
- Support vector machines (SVM)

# Data Mining (Week 7)



# Classification2-Overview — Summary

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## This Week's Aim

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This week's aim is to discuss advanced techniques used for **classification**. Remember: you have already met *logistic regression*, *Naive Bayes* and *k nearest neighbours* in Week 5 with Kieran, and ensemble *methods* (because of all their hyperparameters) in week 6 with Kieran.

The approaches are:

- A technique that uses a series of questions to classify a data set (Decision Trees)
- A technique that combines a suite of weak classifiers into a strong classifier (ensemble *classifier*)
- A technique that “pushes the boundary”: Support Vector Machine (SVM) classifier

These are three of the Top 10 algorithms in data mining (**WuKumarRossQuinlanEtAl2008**), each with its own strengths and weaknesses.

## This Week's Data

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Remember that Classification is concerned with predicting an entity's class membership (its label) based on attributes of that entity. The following data sets are used in the notes and lab

- Iris data: predicting which of three species a given flowering plant is, based on measurements of its sepals and petals. You have seen this with Kieran.
- NIST handwritten digits data: recognising a digit based on its scanned raster image of pixel intensities
- Pima Indians diabetes dataset: predicting whether someone has diabetes or not, based on their BP, BMI, etc.

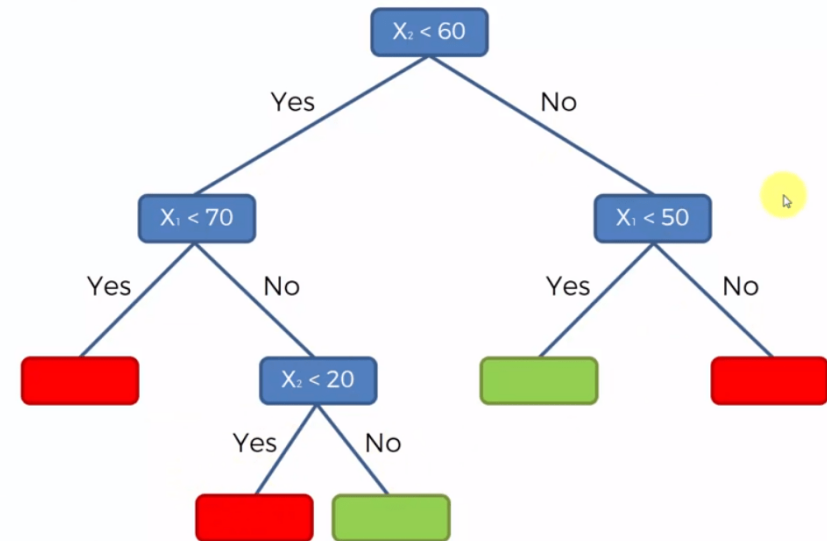
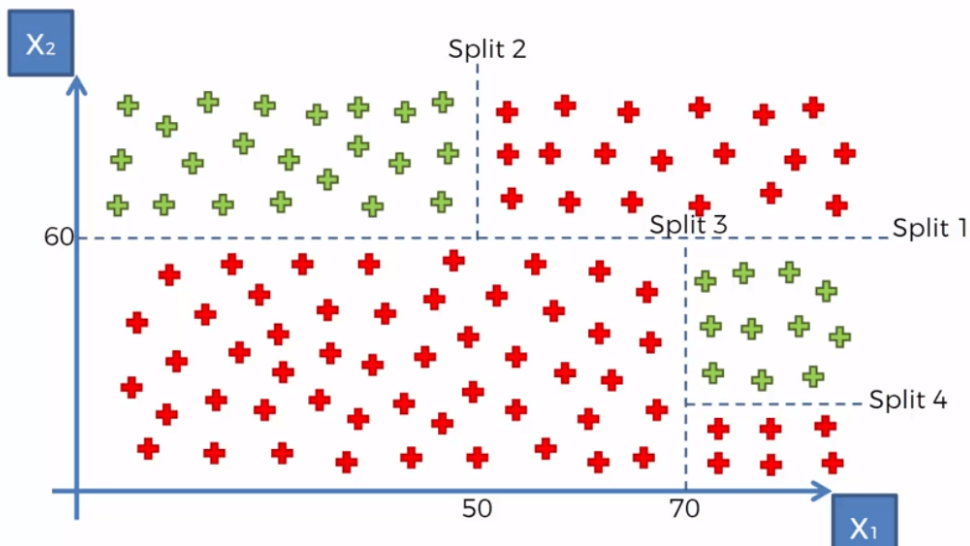
# Motivation

Twenty Questions is a powerful way of learning (identifying something)

## Can it be used to predict categorical variables?

- Assume we have a set of  $l$  labels to assign to  $n_{\text{test}}$  data observations
- During training we repeatedly partition the training set using a sequence of ever finer rules
- The resulting decision tree generates a mapping from *features* of an item (the mapping is defined by a path from root to leaf) to conclusions about the item's target value (represented in the leaves).
- The rules which generate the binary splits are applied in a greedy fashion and are intended to reduce the *impurity* in each nodes' children as quickly as possible
- the algorithm proceeds top-down from the root (all data), recursively generating rules as it goes
- Prediction is simple: the rules are applied along the path from root to leaf. The predicted class value is either the most frequent value at the leaf, or the leaf's probability vector.

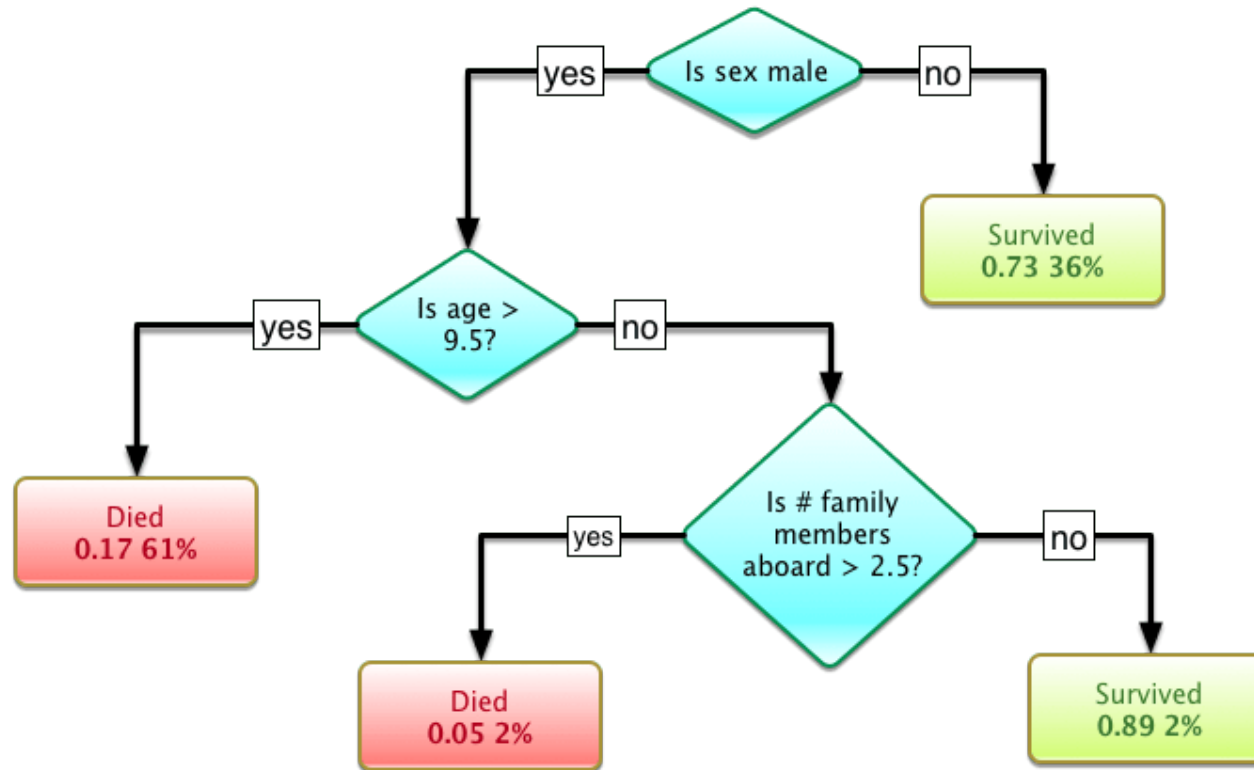
# Classification tree visualisation



Source: <http://diamondclover.com/dtc.html>

➤ Note how successive splits reduce the mixing between the red and green symbols.

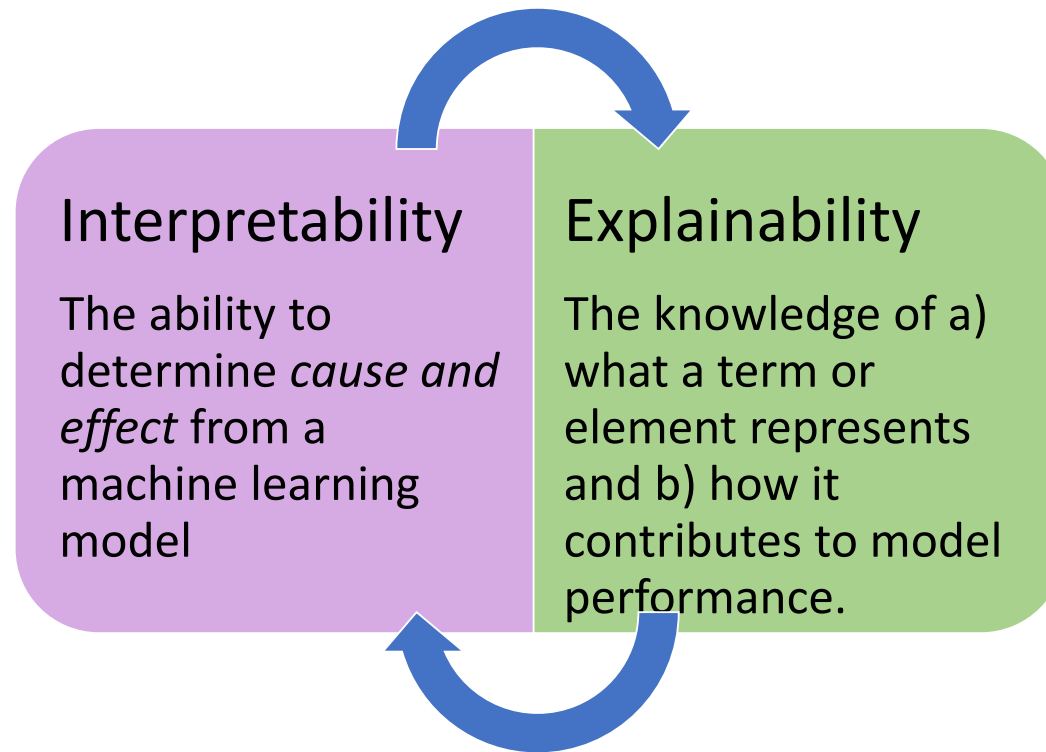
# Classification tree example: Titanic survival



- First split is on Sex, as that feature was the most important predictor of survival.
- Leaves show the probability of survival and the percentage of training observations in the leaf.
- Percentages sum to 100% (approximately), as the leaves partition the training data.
- Leaf colour indicates  $p(\text{survival}) \approx 1$  (green) or  $p(\text{survival}) \approx 0$  (red)



# Decision tree classifiers have benefits beyond accuracy



- Decision tree model for Titanic is *interpretable* because the splits are consistent with human intuition (humans overlay cause and effect models on reality).
- Decision tree model for Iris is *explainable* because the splits are based on flower shape (measurable so meaning is clear) and exclude unnecessary features automatically (feature engineering).

For more info, see Kieran's notes on these concepts.

## Information Entropy: intuition

Probability	Information	Perceived as
Low	High	Surprising
High	Low	Unsurprising

### Example

If it is winter in Ireland, and Met Éireann forecast that tomorrow's temperature will be 10 °C, nobody would pay much attention. If, on the other hand, they said it would be 40 °C, everyone would notice!

### Definition 1 (Entropy)

(Information) entropy is the average amount of information conveyed by an event, when considering all possible outcomes.

### How information is measured

Information is measured in bits, and is computed from the probability  $P(x)$  using  $h(x) = -\log_2(P(x))$ .

# Information Entropy: guessing—1

## Guessing game—equal probabilities

- Let's say Alice and Bob play a guessing game. Alice will pick a number between 0 and 3 ( $00_2$  and  $11_2$ ) (so  $n = 4$  possible values). Bob needs to guess the number.
- Bob can use *binary* search, recursively halving the range of numbers, until he finds the right one. He will need  $h(x_i) \equiv -\log_2(P(x_i)) = -\log_2(\frac{1}{4}) = \log_2(4) = \log_2(2^2) = 2$  questions to narrow it down to a single number ( $x_i$ ).
- That is how the **information** (measured in *bits*) to guess a single value is calculated when each of the  $n$  numbers is equally likely.
- But what if Bob knows that Alice has a preference for certain numbers?
- Let's say Alice is twice as likely to choose odd numbers. If the number she chose was 1, would that be more or less surprising than if she had chosen 2?
- What do you think? Hint - refer to the table in the previous slide...

# Information Entropy: guessing—2

## Guessing game—**unequal** probabilities

- What if there is no uncertainty and no surprise - say Alice always chooses 3?
- Then the probability of choosing 3 is 1 and the probability of each of the other numbers is zero.
- The **entropy** of our guessing game (the distribution of all guesses  $\{x_i\}, i = 1, \dots, n$ ) is  $H(x_i) \equiv \sum (P(x_i)h(x_i)) \equiv - \sum (P(x_i) \log_2(P(x_i)))$ .
- In words: we need to weight the information values for each  $x_i$  by the probability that Alice chose  $x_i$  as the number, and sum over these weighted values to give the *entropy of the set of numbers* Alice chooses from.
- Entropy takes its minimum value (0) when there is certainty about the outcome.
- Entropy takes its maximum value (1) when every outcome is equally likely.
- More generally, the entropy for a given distribution of  $\{x_i\}, i = 1, \dots, n$  lies between 0 and 1.

# Information Entropy: Applied to classification

## Classification and entropy

- Given a set of observations with the same label, we wish to make membership of that set as unsurprising as possible as possible, given the training set.
- Can we partition a set of observations, so their assigned labels match the majority label of their partition?
- If we can do this for most elements of each partition, there is little surprise (low entropy)...

## Definition 2 ((Information) Entropy)

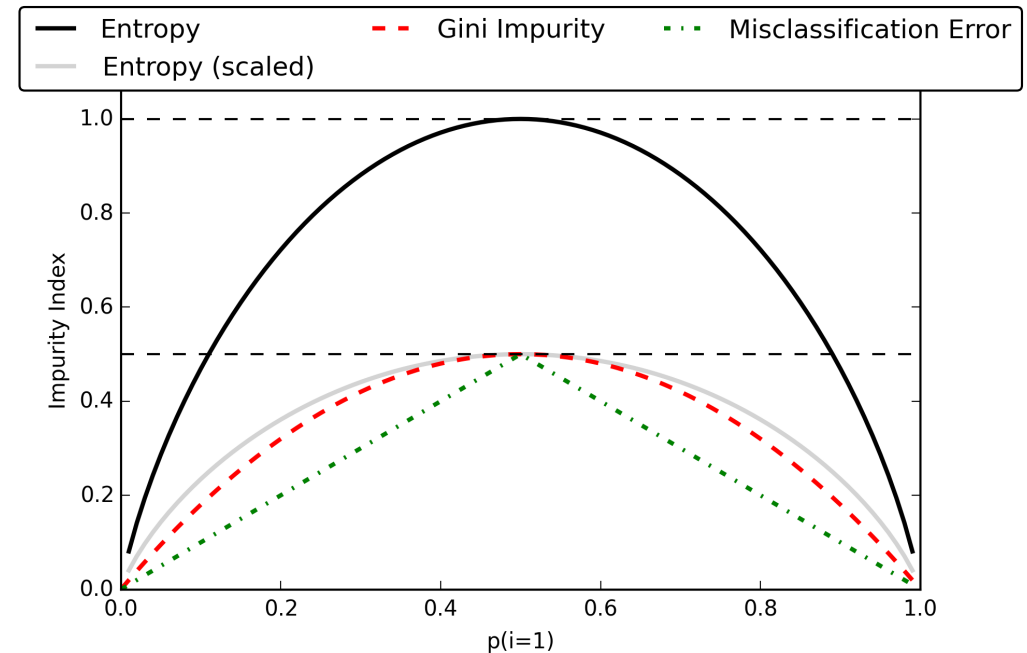
$$H(X) = - \sum_{i=1}^n P(x_i) \log_2(P(x_i))$$

where  $X = \{x_i\}$ . If all probabilities are equal ( $X$  is uniformly distributed),  $H(X) = 1$ . If they differ,  $H(X) < 1$ . Remember the weather forecasting and guessing examples!

A decision tree recursively partitions a set so as to increase the purity (equivalently: reduce the mixing) of the set of observations  $X$  at each node as we move from the root to the leaves.

# Classification tree metrics for rule building

Let  $p_i$  be the probability of an item with label  $1 < i < J$  being chosen. Then the *GINI* impurity is  $1 - \sum_{i=1}^J p_i^2$ . Worst case (maximum impurity): labels are uniformly distributed (entropy of the set is maximum: each value of the label appears the same number of times in the set of observations at that node). We wish to minimise this entropy.



The alternative *information gain* metric is the change in information entropy  $H$  from a prior state to a state that takes some information as given.

## Sidebar: Entropy and Information Gain

### Definition 3 (Entropy)

Entropy is a concept from *thermodynamics* and *information theory*. Here it measures the *impurity* of a collection of items. It ranges from 0 (only 1 item, possibly repeated) to 1 (equal numbers of each item type). Mathematically, it is defined for *one feature*  $T$  as  $H(T) = - \sum_{j=1}^J p_j \log_2 p_j$ , in a collection of size  $N$  where there are  $J$  unique elements of  $T$ , hence  $p_j = \frac{n_j}{N}$  where there are  $n_j$  elements of type  $j$ . For *two features*  $T$  and  $X$ ,  $H(T, X) = \sum_{c \in X} P(c) E(c)$  where each  $c$  represents a level of the  $X$  feature.

### Definition 4 (Information Gain)

Information Gain measures the decrease in entropy after a dataset is split on an feature. It is defined as  $G(T, X) = H(T) - H(T, X)$ , where  $H(T)$  is the entropy at the parent node, and  $H(T, X)$  is the entropy after the split by candidate feature  $X$ .

## Example: PlayTennis example data

outlook	temp	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

*Source: Mitchell, Machine Learning, 1997.*



## PlayTennis example calculations

### Example 5 ( $H(\text{play})$ )

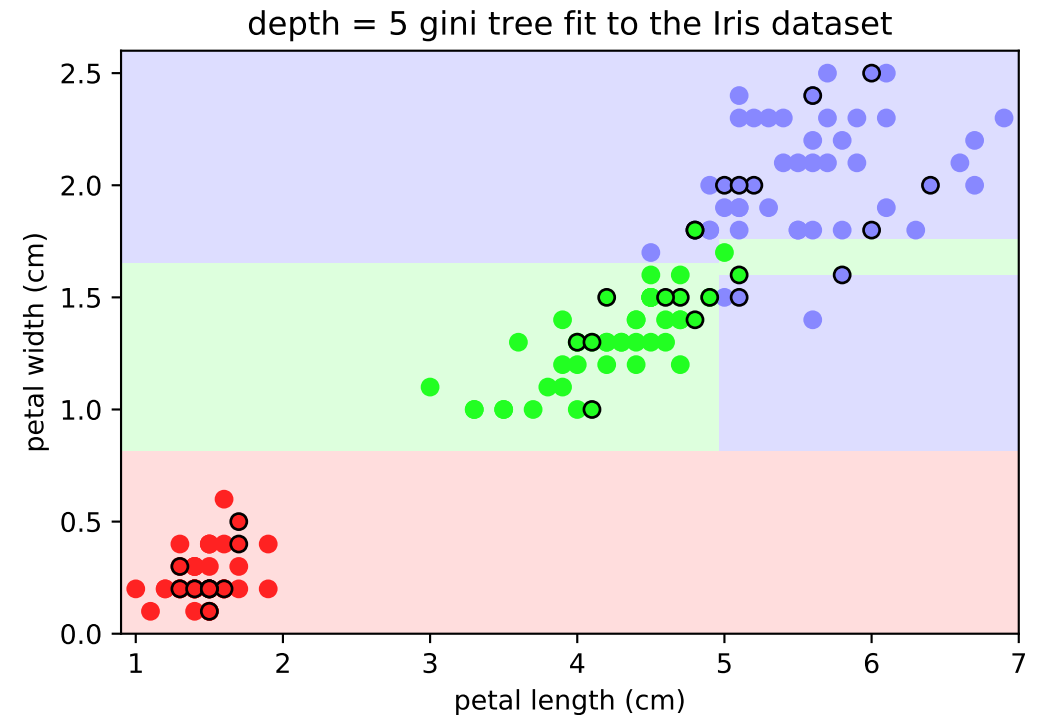
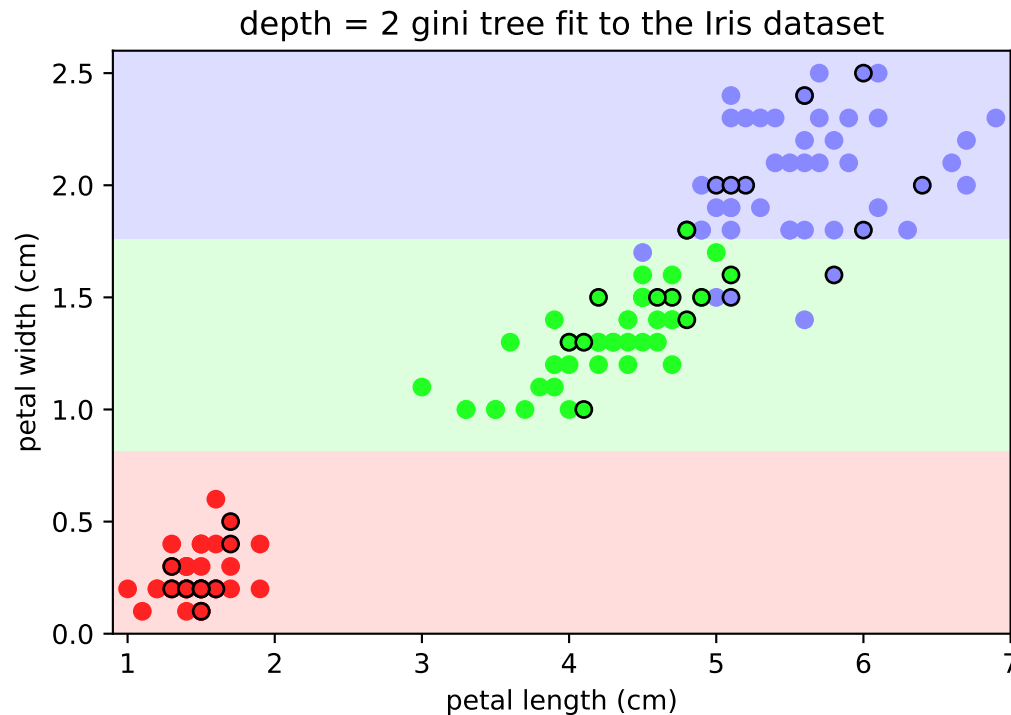
$$\begin{aligned} H(\text{play}) &= - (p(\text{play} = \text{yes}) \log_2 p(\text{play} = \text{yes}) + p(\text{play} = \text{no}) \log_2 p(\text{play} = \text{no})) \\ &= H_{9,5} \\ &= - \left( \frac{9}{14} \log_2 \left( \frac{9}{14} \right) + \frac{5}{14} \log_2 \left( \frac{5}{14} \right) \right) \approx 0.94 \end{aligned}$$

### Example 6 ( $H(\text{play}, \text{outlook})$ )

$$\begin{aligned} H(\text{play}, \text{outlook}) &= p(\text{outlook} = \text{sunny}) H(\text{play} \& (\text{outlook} = \text{sunny})) + \dots \\ &= p(\text{outlook} = \text{sunny}) H_{3,2} + p(\text{outlook} = \text{overcast}) H_{4,0} + \dots \\ &\approx \frac{5}{14} 0.97 + \frac{4}{14} 0 + \frac{5}{14} 0.97 \\ &\approx 0.69 \end{aligned}$$

When growing decision trees, at a given node we search over the features for splitting, and choose the one that gives the maximum information gain, until we reach a leaf, which has an entropy of zero.

# Classification tree examples: Iris Data

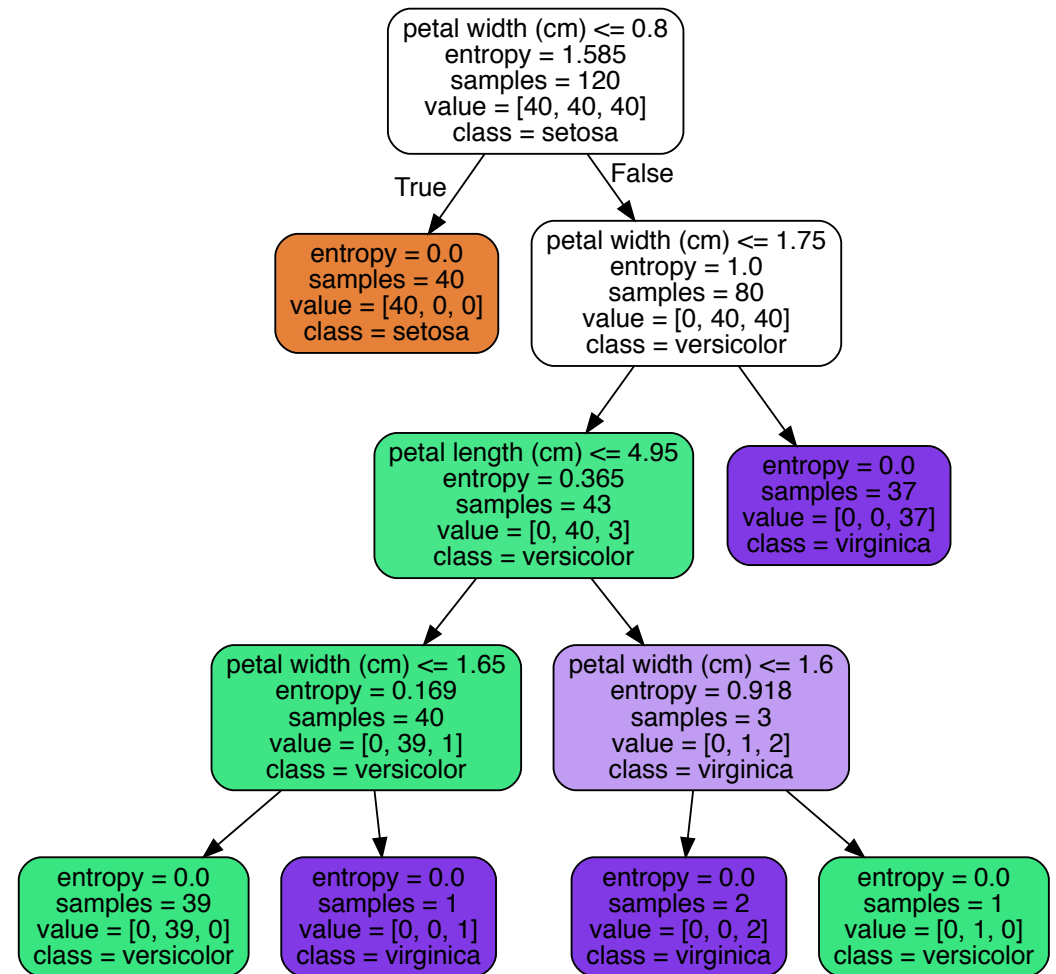


Note the rectangular regions (because each split is over one variable) and the greater complexity when the maximum depth of the tree increases.

Points within a dark circle represent test data, with the main colour of the point indicating its species label. The choice of metric (GINI impurity or Information Gain; `sklearn`'s `criterion` hyperparameter) makes only slight changes to the fit here.

# Classification tree view: Iris Data

Note that the leaf nodes are pure (entropy=0) and are coloured according to predicted value (species label): brown for *I. setosa*, green for *I. versicolor* and purple for *I. virginica*.



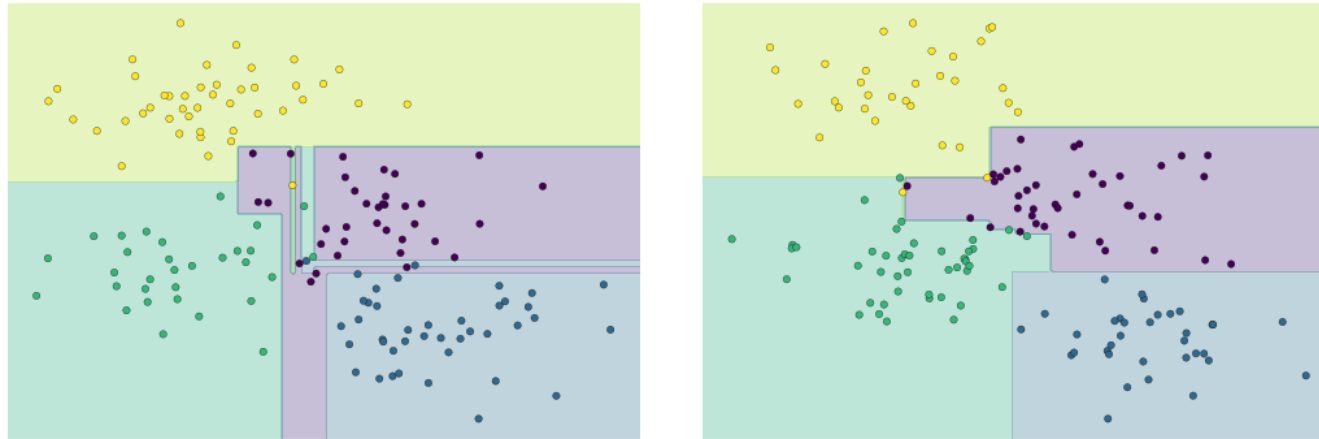
# Classification tree: Use for Prediction

Now that we have a decision tree, how do we use it to predict the label?

## Example: estimating the species of an iris plant

- Let `Petal_Width` = 1.5cm and `Petal_Length` = 5cm. The other (sepal) dimensions are ignored by the decision tree because they were not as useful for classification.
- The first split (`Petal_Width`  $\leq$  0.8) is `False` so we take the *right* branch.
- The second split (`Petal_Width`  $\leq$  1.75 is `True` so we take the *left* branch.
- The third split (`Petal_Length`  $\leq$  4.95 is `False` so we take the *right* branch.
- The fourth split (`Petal_Width`  $\leq$  1.6 is `True` so we take the *left* branch.
- We have reached a leaf (`entropy` = 0) and cannot split any further.
- Depending on where we stop, we would assign the prevalent label for that node (`versicolor`, `versicolor`, `virginica` or `virginica` if the `max_depth` was 2, 3, 4 or 5, respectively).

## Be careful of overfitting...



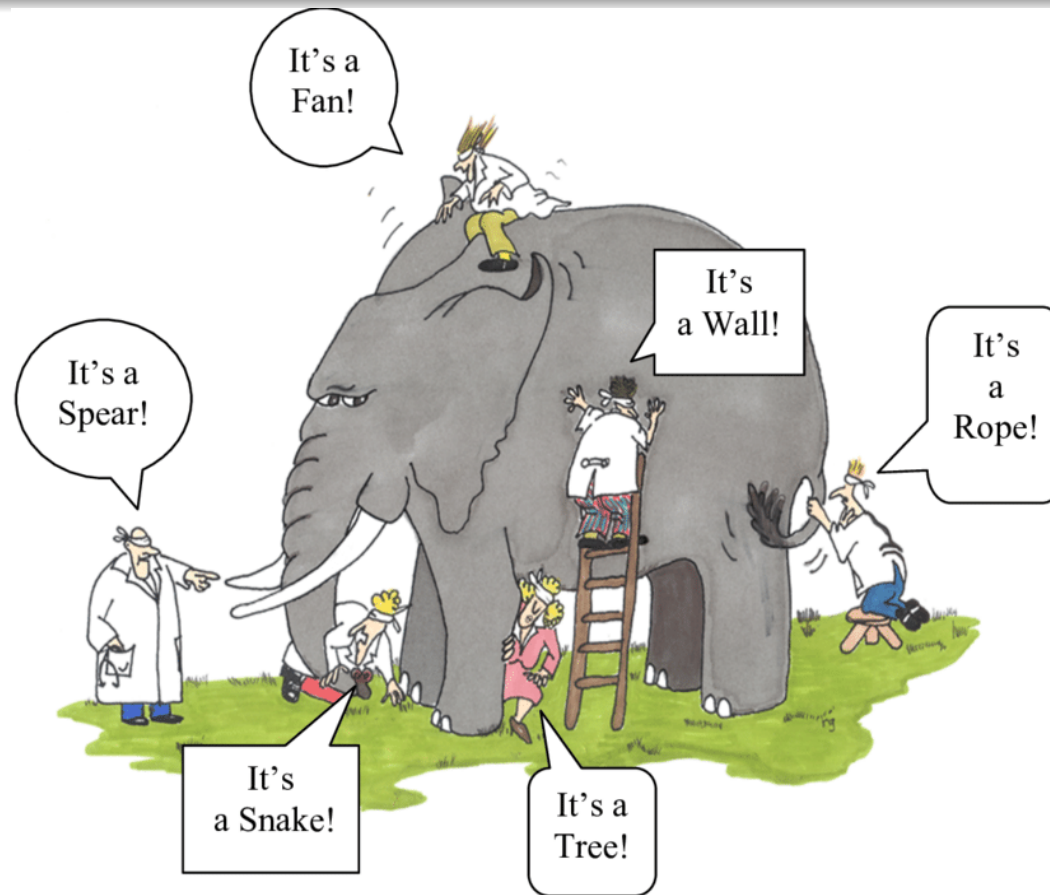
- Given two very similar (generated) data sets, all leaves in each fitted decision tree are *pure*.
- The resulting trees look very different.
- This sensitivity to the noise in the data is characteristic of *overfitting* (high variance).
- Control by a) limiting depth or b) limiting number of leaves (hyperparameters).
- Full depth trees often overfit, resulting in overly complex boundaries, suspiciously low training error and high variance.

# Classification trees in python

```
1 tree = DecisionTreeClassifier(criterion=criterion, max_depth=treeDepth, random_state=0)
2 tree.fit(Xtrain, ytrain)
3 y_treeTest = tree.predict(Xtest)
4 print(accuracy_score(ytest, y_treeTest))
5 print(confusion_matrix(ytest, y_treeTest))
6 print(classification_report(ytest, y_treeTest, digits=3))
```

- After creating the classifier object, fit the training data and then use the fit to predict yTest from xTest.
- Also see how to get some diagnostic output. Similar diagnostics can be obtained for other classifiers.
- `sklearn`'s consistent programming interface makes switching between classifiers trivial.

# Motivation: Combining Classifiers



Source: <https://bit.ly/3J6rApM>

By combining classifiers, we can get a better result than each classifier on its own...

# Ensemble learning overview

## Intuition

- Training a discriminative classifier is equivalent to searching for a function mapping features ( $X$ ) to classes ( $Y$ ).
- The function search space is **enormous**!
- Rather than finding a single *best* classifier, is it possible to find several *good* classifiers and combine them into a classifier that outperforms each of its components?

This is a **divide and conquer** approach. For example, *edge cases* can be handled by relatively simple classifiers, but they need to be combined with more general classifiers for good overall performance.

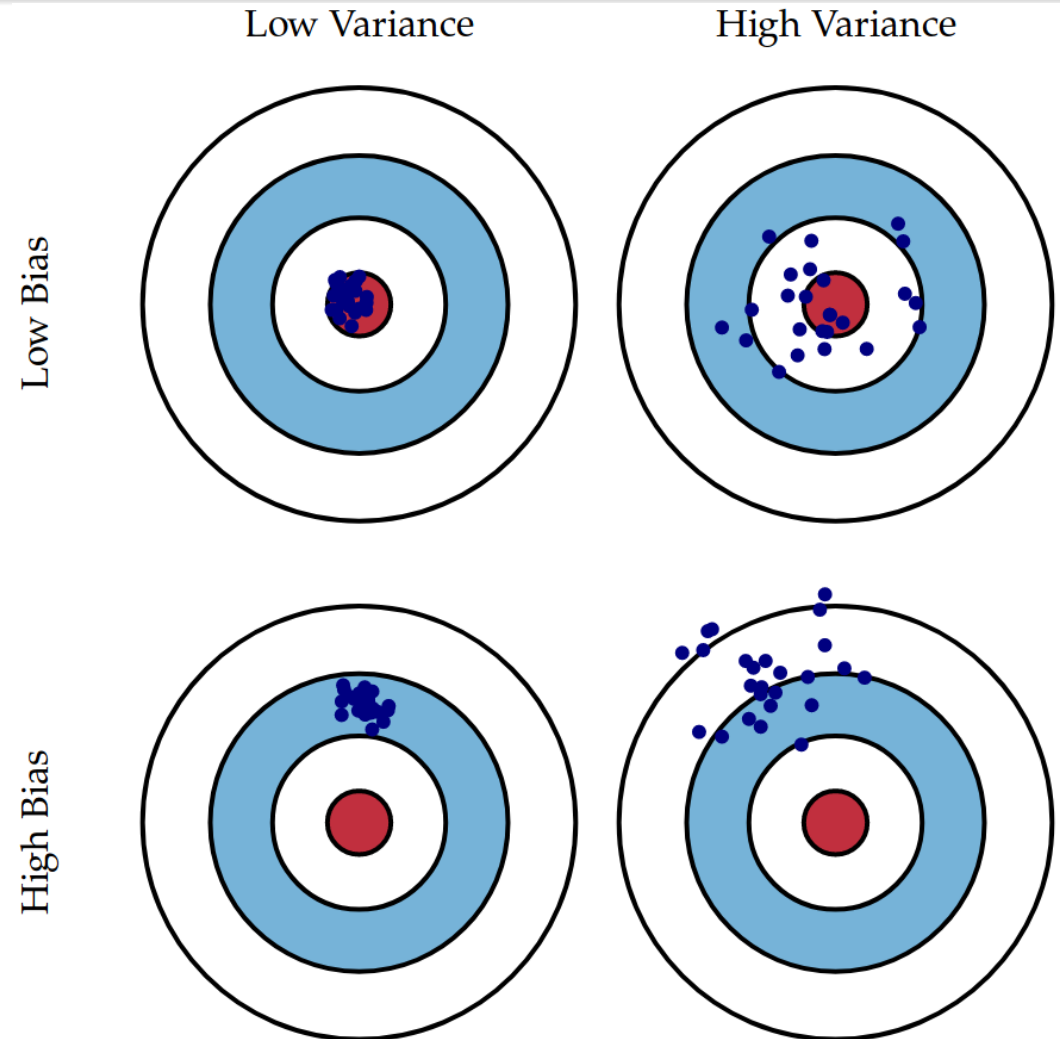
## General considerations

- weak versus strong learners - tradeoff on ensemble size hyperparameter
- learners need to be independent, so learner instability increases ensemble diversity
- high ensemble diversity is good, like high feature independence in regression and similar models
- ensemble size: when do we have enough learners?

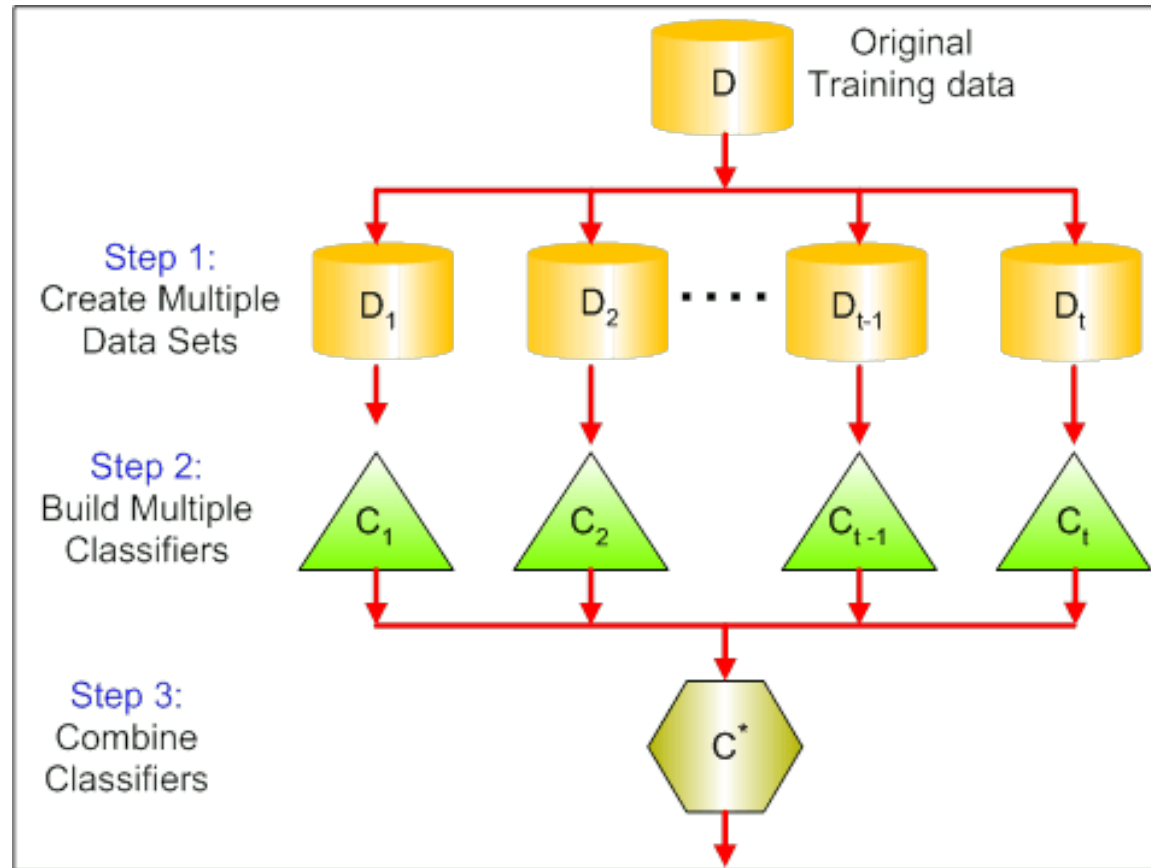


# Weak learners and ensemble learning

- A *weak learner* has high variance, high bias or both.
- Example: KNN with  $k$  set too high or too low, decision tree with too many or too few leaves
- Sometimes the weak learner is just slightly better than random guessing.
- Ensemble algorithms combine a suite of weak learners to act as a composite *strong learner*.
- Can be used for regression and classification, but classification is more common.
- Ensemble algorithms include *bagging*, *boosting* and variants.



# A canonical ensemble model



Source: [www.analyticsvidhya.com](http://www.analyticsvidhya.com)

This structure is used in **bagging** and **boosting** classifiers

# Samples and Bootstraps

## Definition 7 (Bootstrapping)

Given a sample (training data with  $N_0$  observations, say), **bootstrapping** (Efron1979) draws  $B$  samples, each of size  $N_s$ , with replacement from the original sample. Because of replacement,  $B$  is not limited by  $N_0$ , and an observation can appear in more than one bootstrap sample. By the *Law of Large Numbers*, statistics combined from the bootstrap samples can estimate those of the population.

## Example 8 (Sampling from a set of numbers)

Given the set of numbers  $\{1, 2, \dots, 10\}$ . If we sample *without* replacement, the maximum size of the sample is 10. However, if we sample *with* replacement, the maximum size of the sample is unbounded. If the sampling probability is not uniformly distributed, sampling with replacement will generate nonuniform samples (values will appear according to their probability). As that sample grows, it becomes representative of the underlying distribution from which the original set of 10 numbers is an example. We say that it **bootstraps** the population distribution.

➤ Bootstrapping allows samples to represent the full training set, so results can combine.

# Bagging background

## Definition 9 (Weak learner)

A weak learner is quick to learn and predict (e.g., a decision tree with restricted height, or Naive Bayes with a restricted feature set) and its error rate is strictly less than 0.5 for all training inputs.

## Definition 10 (Model Combination)

Given a set of predictions from many weak learners, the weighted average prediction generally is more correct and the *combined predictor* has lower variance than any of the individual predictors, c.f., “Wisdom of the crowd” phenomenon, which assumes independence, otherwise there is “groupthink”, resulting in low variance and high bias).

# Bagging algorithm

## Definition 11 (Bootstrap aggregation (Bagging))

```

 $k \leftarrow \text{numberOfBootstrapSamples}$ 
 $N \leftarrow \text{bootstrapSampleSize}$ 
 $X \leftarrow \text{trainingData}$ 
for  $i \leftarrow 1 : k$  do
     $D_i \leftarrow \text{deriveBootstrapSample}(X, N)$ 
     $C_i \leftarrow \text{trainClassifier}(D_i)$ 
end for
 $C^* \leftarrow \operatorname{argmax}_y \sum_i \delta(C_i(x) = y)$ 
where  $\delta(\cdot) = 1$  if  $\cdot$  is true and is 0 otherwise.

```

- The  $\delta(\cdot)$  aggregation function is used for classifiers and simple averaging is used for regression.
- The best known bagging algorithm for classification is **RandomForest** (equivalent to `BaggingClassifier` with `DecisionTreeClassifier` as the weak learner).
- In `sklearn`, it has basically the same API as other classifiers and is invoked using `from sklearn.ensemble import RandomForestClassifier` and `clf = RandomForestClassifier(n_estimators=10)`, where  $k = 10$  in this example.

# Boosting algorithm

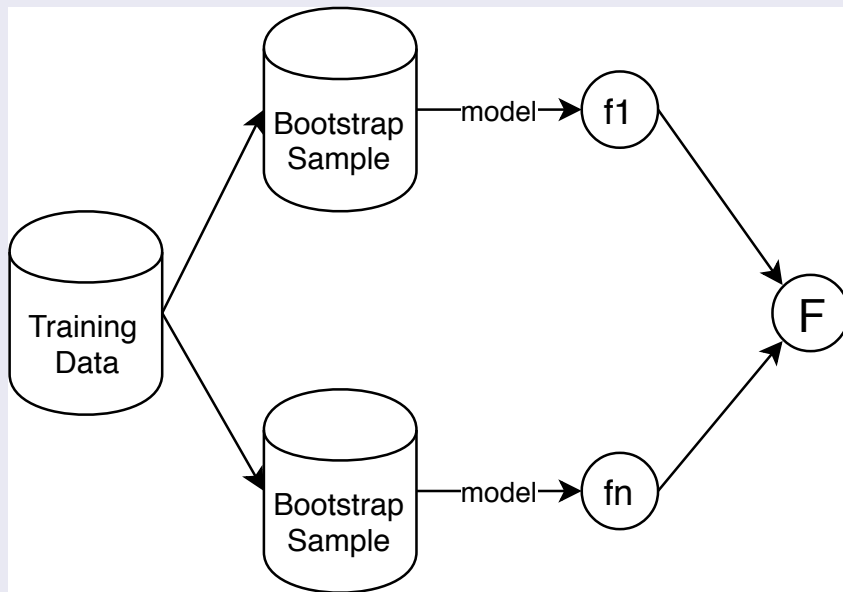
## Definition 12 (Boosting)

Boosting (**FreundSchapire1999**) is another ensemble classifier. Unlike boosting, observations are **reweighted** rather than **resampled**. Weak classifiers are applied *sequentially* to the training data. Records that were *misclassified* by the previous iteration/model are given *more weight*. Successive models are weighted according to their accuracy (AdaBoost) or gradient performance (rate of accuracy increase; e.g., GradientBoost). Variants include Adaboost, XGBoost, etc.

- The leading classification algorithms for the Netflix prize, many kaggle competitions, etc. tend to be boosted ensemble classifiers.
- They are available in sklearn: `from sklearn.ensemble import AdaBoostClassifier` and `clf = AdaBoostClassifier(n_estimators=100)`

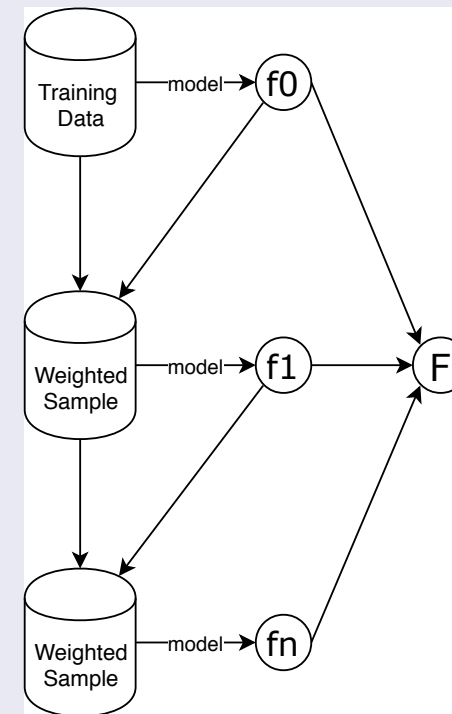
# Comparison of bagging and boosting

## Bagging



- Resamples the training data
- Observations are unweighted (uniform distribution)
- Classifiers work in parallel

## Boosting



- Reweights the training data
- Observations are weighted by “difficulty”
- Classifiers work in sequence

# Review of bagging and boosting

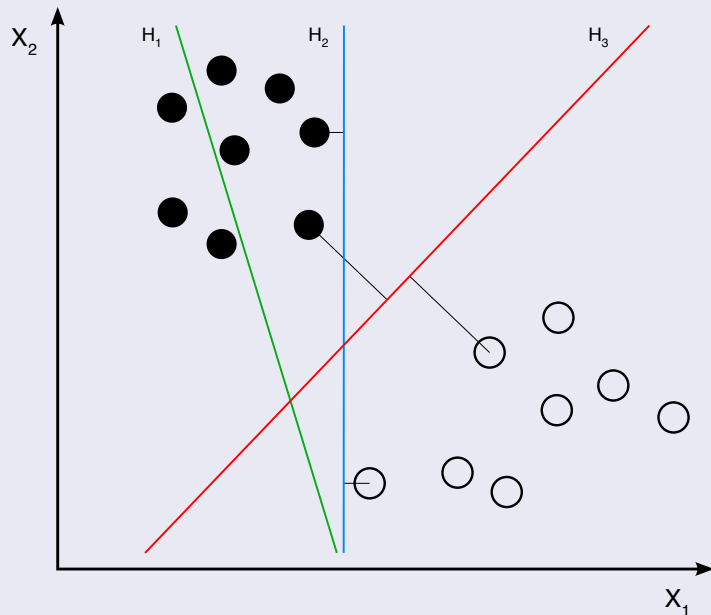
- Bagging uses weak learners with *high variance and low bias*, and *bagging reduces the variance* by statistical aggregation
- Boosting uses weak learners with *low variance and high bias*, and *boosting reduces the bias* by iteratively reweighting the learners
- Hyperparameters for each include: choice of weak learner type and number of estimators (weak learners)
- Hyperparameters for boosting include: learning rate (aka shrinkage factor); if less than 1, updated models are downweighted; stabilises the iteration but might slow convergence or even converge to local minimum
- **AdaBoost**: iterative reweighting classifiers by putting more weight on misclassified samples so that they tend to be tackled by the next classifier, keep doing this until convergence.
- **GradientBoosting**: Start with a constant learner, fit a weak learner to the negative gradient of the (approximate) loss function, take a downward step so that it minimises the loss function in that direction, and continue.
- In Adaboost, “shortcomings” of the fit at any stage are identified by high-weight data points.
- In Gradient Boosting, “shortcomings” of the fit at any stage are identified by gradients of the loss function.



# Classifier boundaries

Up to now, when considering classifiers, our focus has been on assigning data to classes, not on the boundaries between those classes.

## Comparison of separating planes

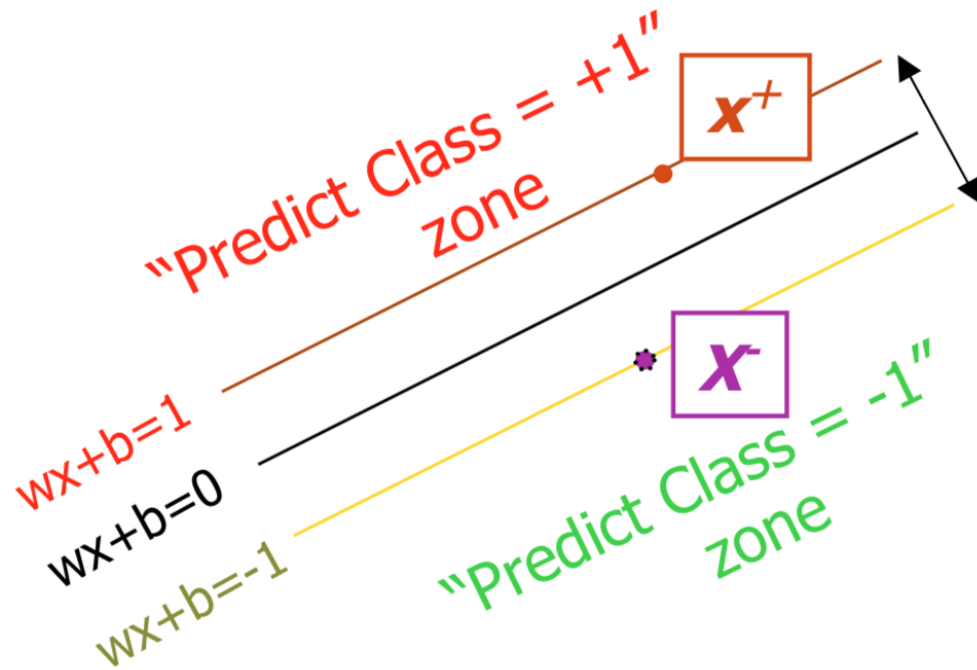


- $H_1$  does not separate the two classes
- $H_2$  does separate them, but only just!
- $H_3$  is the **maximum margin separating hyperplane** (line in 2-D) in this case
- the corresponding classifier is a **maximum margin classifier** that *minimises the generalisation error* when classifying new data from the test set

Source: wikipedia

Consequently,  $H_3$  is defined by a relatively small number of observations (points) which are known as the **support vectors** of the classifier

# Linear SVM geometry



- Assume we have one numeric-valued feature ( $x$ ) and one target ( $y$ )
- Suitably scaled and shifted, the margin lines are  $wx + b = 1$  and  $wx + b = -1$
- $x^+$  and  $x^-$  are the support vectors
- Note that  $(wx^+ + b = 1) - (wx^- + b = -1) = w(x^+ - x^-) = 2$ .
- Also the **Margin**  $M = (x^+ - x^-) \cdot w / |w|$ , i.e., the projection of the vector between the two support vectors onto a line perpendicular to the separating hyperplane
- Collecting terms, we have  $M = 2/|w|$

# Linear SVM optimisation

**We wish to find  $w$  and  $b$  so that each observation is assigned correctly to one of two classes, and the margin  $M$  is maximised (equivalently,  $|w|$  is minimised).**

## Definition 13 (SVM iteration)

**Feasibility** Start with an estimate of  $w$  and  $b$ , iterate to find new feasible  $w$  and  $b$  that ensure that all training data are classified correctly:  $y_i(wx_i + b) \geq 1, \forall i$ , where  $y_i = \pm 1$  depending on whether the point is in the +1 or -1 class.

**Optimality** Starting with feasible  $w$  and  $b$ , iterate to maximise  $M = \frac{2}{|w|}$  or equivalently, minimise  $w'w/2$  while maintaining feasibility.

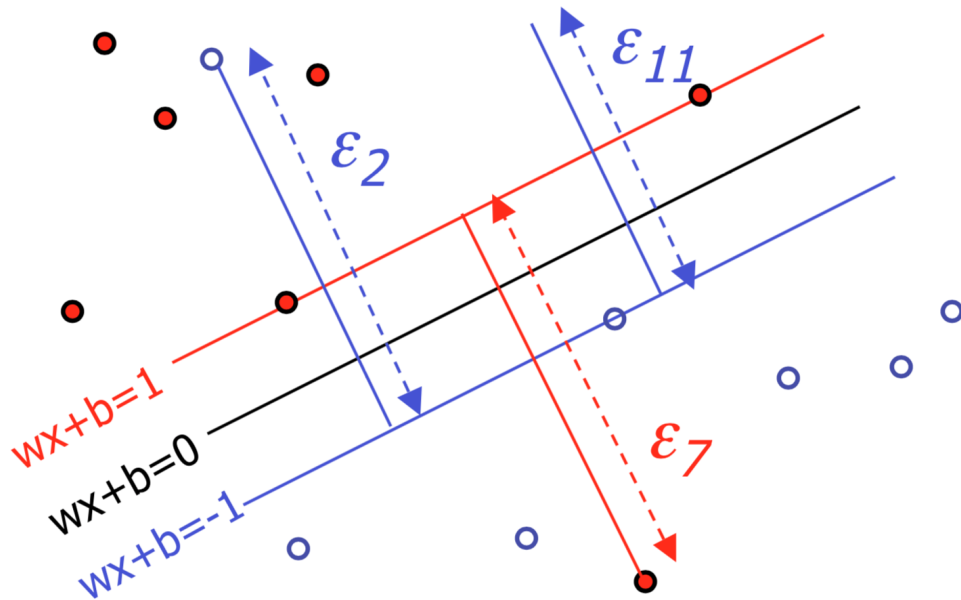
This is a constrained convex optimisation problem. Library software exists to solve it. Either there is no solution (because the classes are not linearly separable) or the solver will find the *unique* SVM classifier.

# Review of basic SVM

- The SVM solver we described can be extended to higher dimensions easily
- It can be extended to multiclass (not just binary classification), by running  $n$  SVMs and aggregating (this happens transparently)
- However, the use of a **hard margin** makes it sensitive to noisy support vectors (data that strays across the “true” separating hyperplane)
- Solution is to introduce a **soft margin**, so some points are allowed to be classified as “+”, say, even if they lie a small way inside the “-” region.

The soft margin is defined in terms of a set of  $\varepsilon$  vector lengths, which are nonzero for a small number of “noisy” points, some of which could otherwise be treated as support vectors and/or make the hard margin SVM problem infeasible.

# Soft margin linear SVM



$\varepsilon_2$  allows one point to be classified as blue even though it is on the “red side” and  $\varepsilon_7$  allows another point to be classified as red even though it is on the “blue side”.

**Hard** margin formulation is

- Find  $\mathbf{w}$  and  $b$  that minimise  $\frac{1}{2}\mathbf{w}'\mathbf{w}$
- Subject to  $y_i(\mathbf{w}'\mathbf{x}_i + b) \geq 1$  (hard margin feasibility)

**Soft** margin formulation is

- Find  $\mathbf{w}$  and  $b$  that minimise  $\frac{1}{2}\mathbf{w}'\mathbf{w} + \lambda \sum_i \varepsilon_i$
- Subject to  $y_i(\mathbf{w}'\mathbf{x}_i + b) \geq 1 - \varepsilon_i$  (soft margin feasibility), and
- $\varepsilon_i \geq 0$  for all points indexed by  $i$ , and
- $\lambda \geq 0$  is like a regularisation parameter

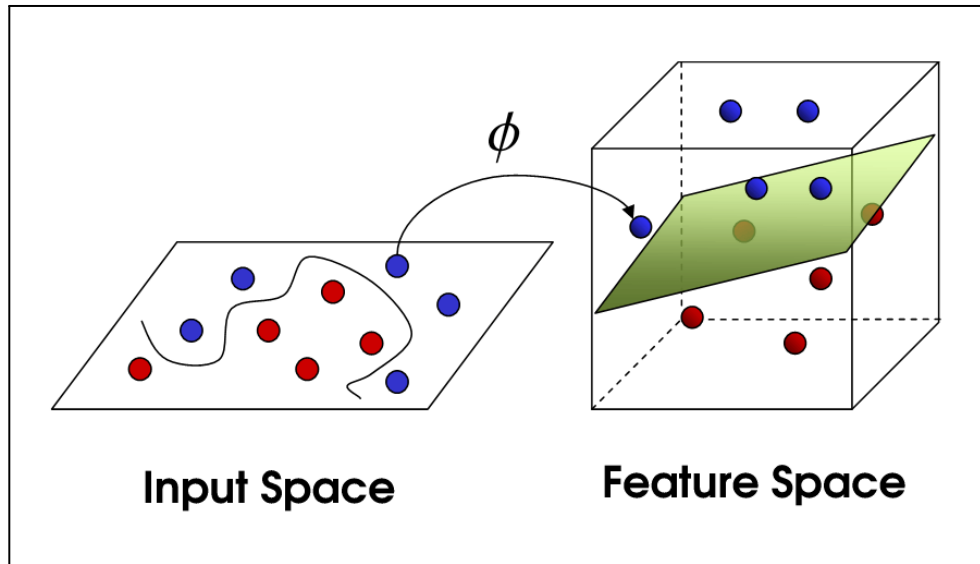
# Nonlinear boundaries: Kernel SVM

## Definition 14 (Kernel trick)

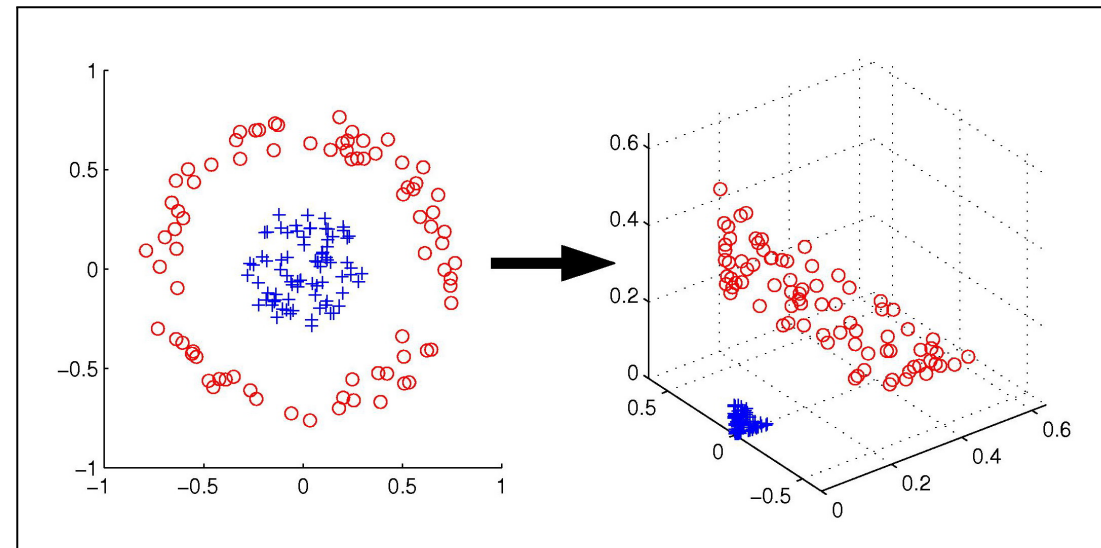
When the data is not linearly separable in the input space, a suitable transformation into a new feature space (often with more dimensions) can make it so.

- Example kernels include *linear* as seen already, *polynomial* (for curved boundaries), *radial basis function* (for classes “enclosing” others, etc.)
- By inspecting the data, the user should identify a suitable transformation, hence kernel and SVM can then work, as before, with the transformed data/generalised kernel
- SVM is available `sklearn: from sklearn import svm` and `clf = svm.SVC()`.

# Kernel transformation - Examples



We look for a transformation from 2-D to 3-D so the two classes can be separated by a plane. Often transformations map from  $n$  to  $n + 1$  dimensions.



If we transform from  $x, y$  to  $r, \theta$  representation, we can separate the two classes by a plane because the “outer class” has a larger radius  $r$ .

# Review of SVM

- Although Euclidean distance is frequently used, there is flexibility in choosing a similarity function
- Since the solution is defined in terms of (a relatively small number of) support vectors
  - even with large data sets, the solution is sparse
  - suited to high dimensional data because we calculate the inner product over the dimensions (“squashing them”) so complexity is largely independent of dimension
- Soft margin approach can help to deal with noisy data and to minimise overfitting
- Convex optimisation problem ensures the optimisation process leads to just a single global solution
- Very flexible regarding nonlinear boundaries and feature selection (kernel SVM)
- Often a good fit with text classification.
- *Kernel trick* also used in **artificial neural networks**, to enable them to classify even with nonlinear/piecewise-linear boundaries.



# Summary

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- Classification is one of the main tasks in data mining, and is a mature and well-studied field
  - Logistic regression is an extension of linear regression and benefits from its strengths
  - k-nearest-neighbours is conceptually simple (based on voting) and the lack of a model (lazy learning) means it responds better to data drift
  - Naïve Bayes offers a probability-based generative model, able to work from data summaries, ideal for text and email classification
- More advanced classifiers have their own advantages, especially in relation to high dimensional data:
  - Decision trees learn a representation that is often easily interpretable, but works better with linear boundaries
  - Ensemble methods were state of the art (2000-2012, say) and sacrifice interpretability for good performance with high dimensional data
  - SVM was state of the art (1985-2000, say) and is still extremely effective for very high dimensional problems like document classification

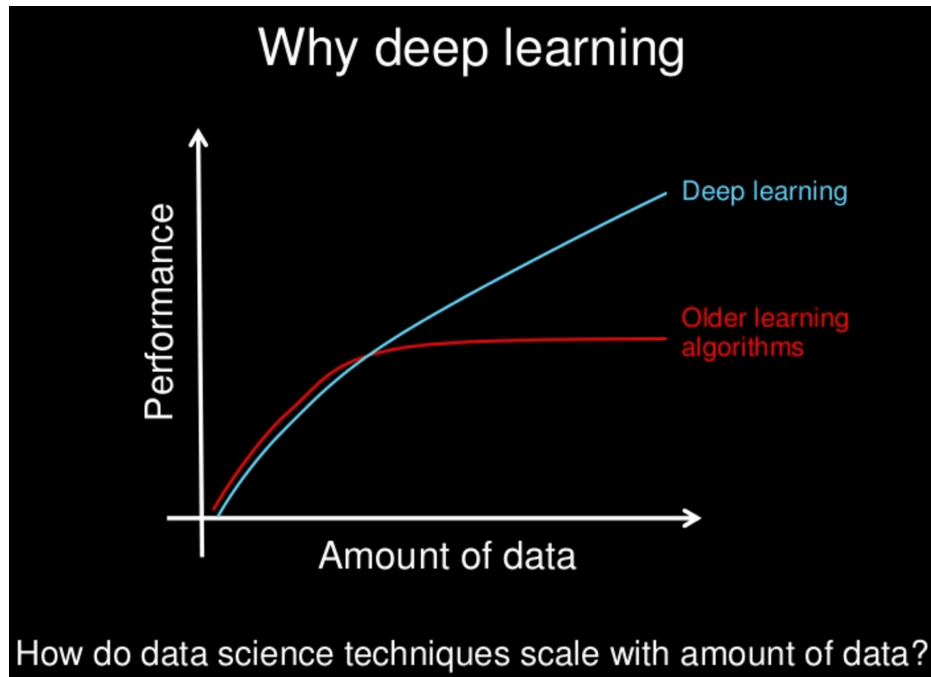
## Other considerations

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- KNN uses *lazy* learning, all other techniques above use *eager* learning (derive model from training data)
- Naive Bayes uses *generative* learning to learn how the data was generated, all other techniques above use *discriminative* learning to derive the function that assigns class labels
- For KNN and Decision Trees, the representation grows with the size of the data - that is not generally true in all other techniques above
- Always keep an eye on bias (more easily estimated using the training set) and variance. For high accuracy on the test set, they both need to be as low as possible.

Classification is sometimes confused with clustering - will cover this next time.

## But is that the last word on Classification?



Source: Andrew Ng, *Why Deep Learning*

### Learning from big data

- Traditional classification algorithms eventually run out of steam as data size increases
- Shallow neural networks had been discounted in the 1980s and 1990s when trained with small data
- Deep learning to the rescue!
- Kernel SVM and logistic regression lead nicely to perceptron models, hence ANNs, hence **deep learning**
- Deep learning requires lots of data but the models can scale better to take account of extra data

Kieran will cover Deep Learning as the topic in Week 11.

# General References

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