

Data Mining (Week 1)

MSc Data Mining

Topic 11 : Deep Learning

Part 01 : Neural Networks

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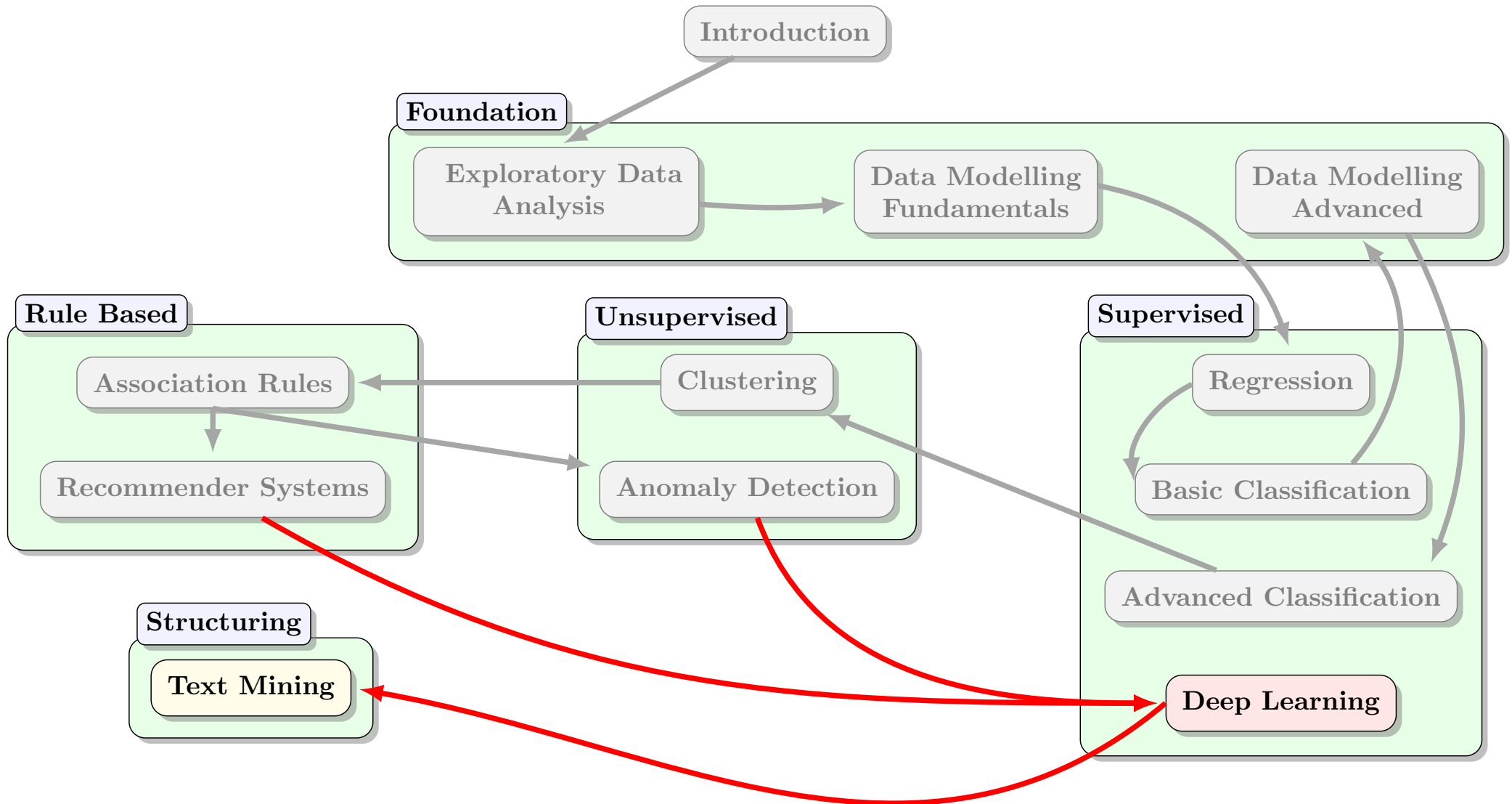
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Spring Semester, 2023

Outline

- Fundamental concepts in neural networks
- Neural networks using scikit-learn.

Data Mining (Week 11)



Introduction

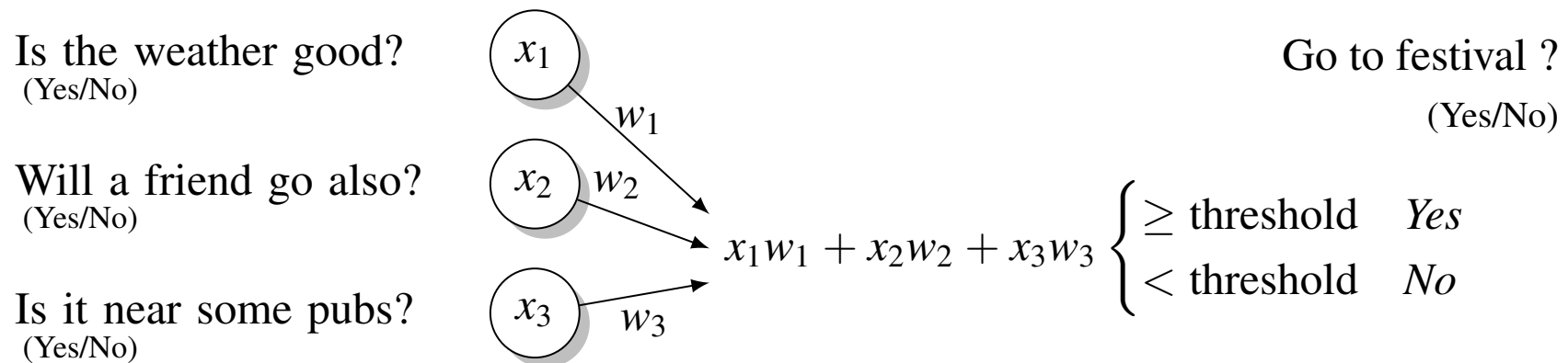
Aim

Introduce the fundamental concepts in neural networks and deep learning, and demonstrate the basics of modelling and training of networks using `scikit` using toy data sets (XOR, ...) and the MIST Handwritten Digits dataset.

Formalising a Simple Decision Process

I

Say you want to decide whether you are going to attend a cheese festival this weekend. And say, the following three factors go into your decision:

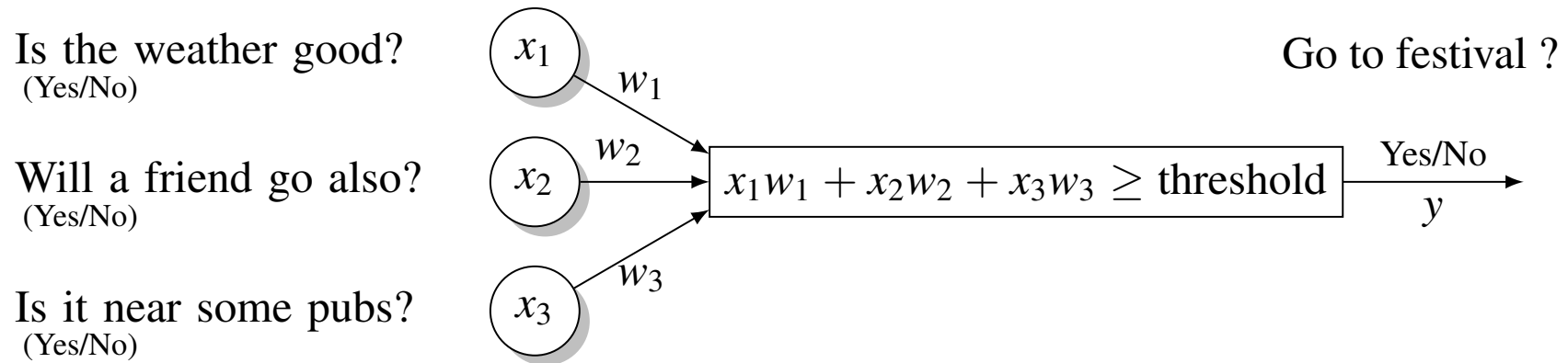


Assume

- Factors are binary: No/Yes, False/True, ... \implies
- Each input factor has its relative importance, given by its **weight** and importance is additive.
- We have an initial threshold (inertial/bias...) that we need to exceed before we will decide "Yes".

0/1

Formalising a Simple Decision Process



For given input vector, \mathbf{x} , the decision is controlled by the weights and threshold:

- If you want decision to be 'Yes' whenever any two input factors are 'Yes', then set

$$w_1 = w_2 = w_3 = 1 \quad \text{and} \quad \text{threshold} = 2$$

- Fear of dying of thirst dominates your decision making process, then set

$$w_1 = w_2 = 1, \quad w_3 = 10 \quad \text{and} \quad \text{threshold} = 11$$

Formalising a Simple Decision Process

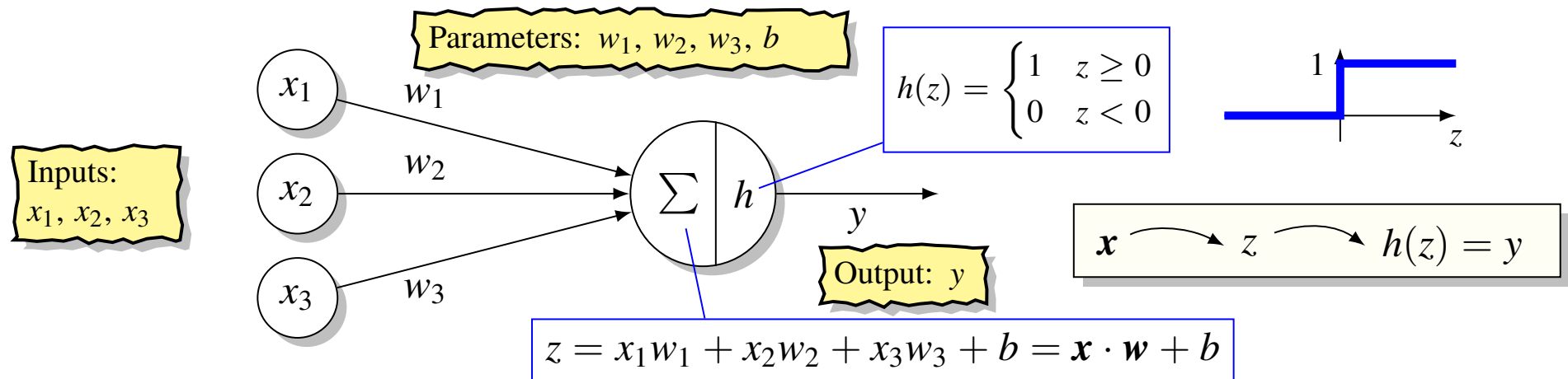
Rewriting function

$$y = \begin{cases} 1 & \text{if } x_1w_1 + x_2w_2 + x_3w_3 \geq \text{threshold} \\ 0 & \text{otherwise} \end{cases}$$

so that the comparison is against zero we have

$$y = \begin{cases} 1 & \text{if } x_1w_1 + x_2w_2 + x_3w_3 + b \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

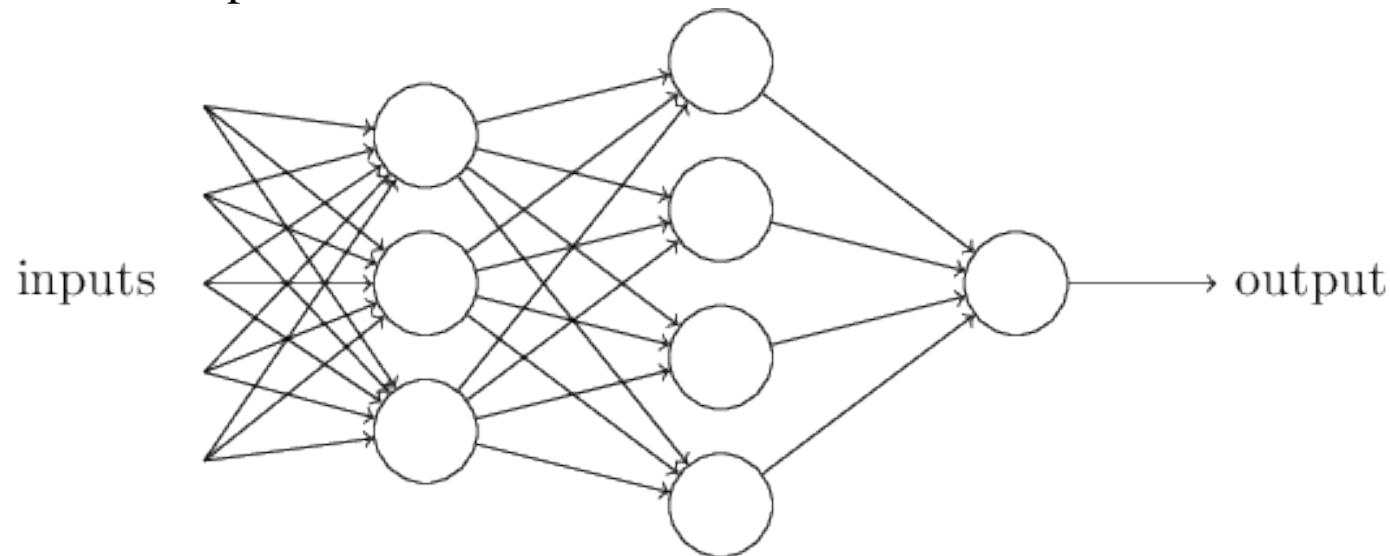
where $b = -\text{threshold}$ is called the **bias**. This **binary, multi-rule function** can be treated as a **(smooth) summation function** followed by a **(non-linear) activation function**.



Arbitrary Complex Decisions \rightsquigarrow Neural Networks

I

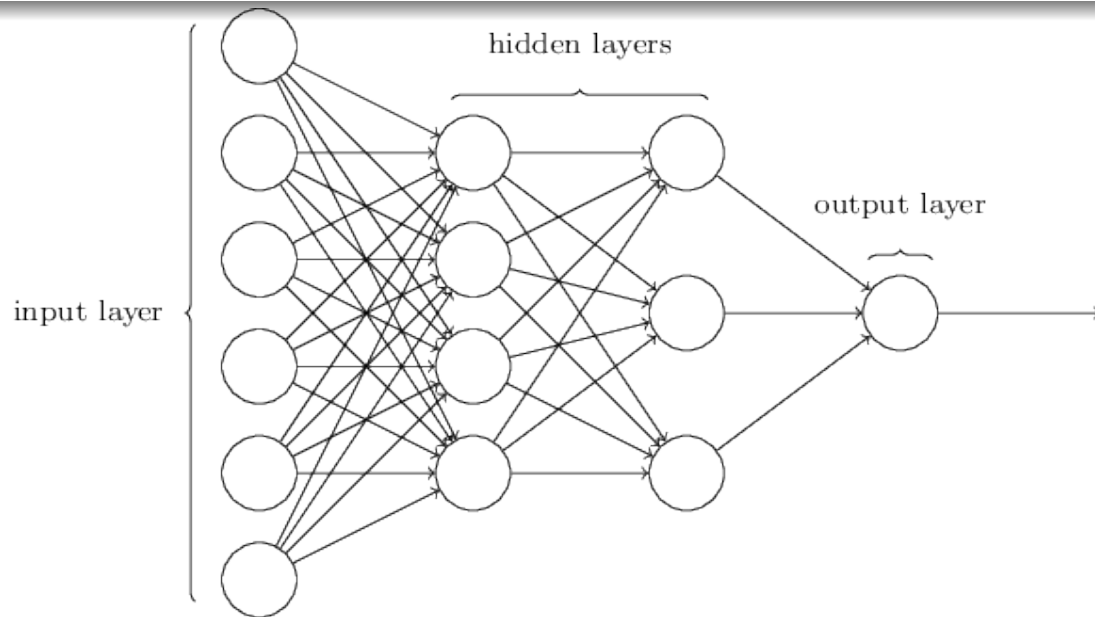
Arbitrary complex decisions can be constructed by chaining/linking simple decisions, where the output of some decisions are used as input for other decisions.



- Each simple decision node is called a **neuron**.
- While a decision might have arbitrary number of inputs it only has one output. (The multiple links out represent the same output.)
- In the simplest network the effect of decisions moves in one direction, this is called a **feed forward network**.

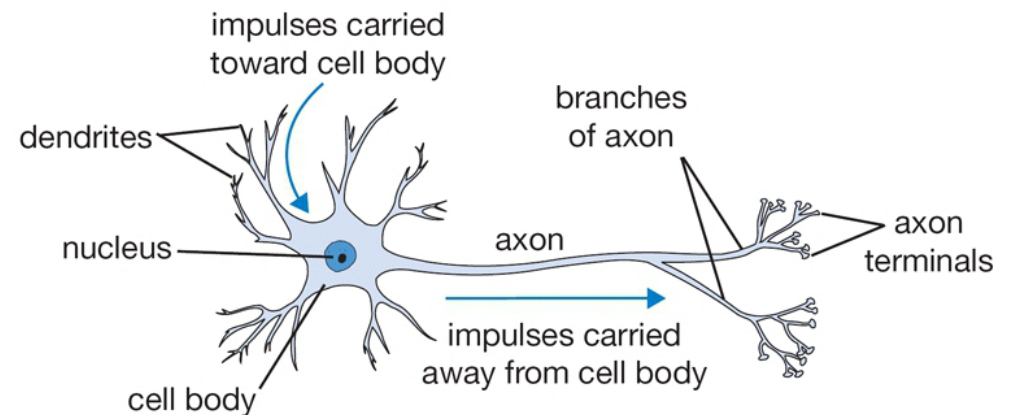
Arbitrary Complex Decisions \rightsquigarrow Neural Networks

II



More than one hidden layer is
"Deep learning"

- The input and outputs are typically represented as their own neurons, with the other neurons named **hidden layers**
- The biological interpretation of a neuron is this: when it emits a 1 this is equivalent to 'firing' an electrical pulse, and when it is 0 this is when it is not firing. The bias indicates how difficult it is for this particular node to send out a signal.



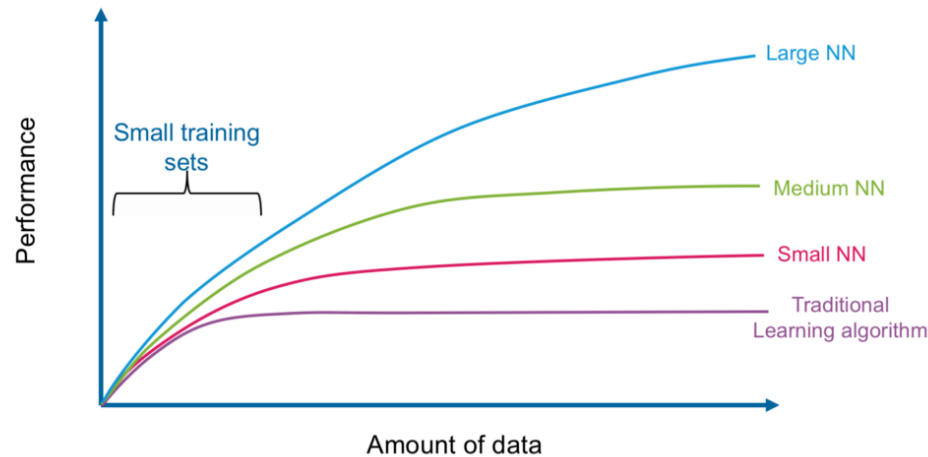
When to Consider Neural Networks?

- Input is high-dimensional discrete or real-valued (e.g. raw sensor input)
- Output is discrete or real valued
- Output is a vector of values
- Possibly noisy data
- Form of target function is unknown
- Human readability of result is unimportant.

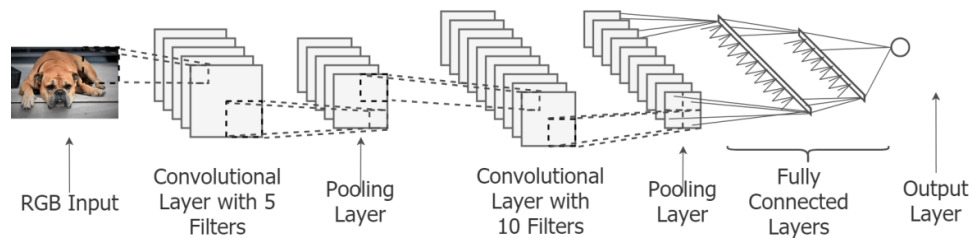
Examples

- Financial modelling — predicting the stock market
- Time series prediction — climate, weather, seizures
- Computer games — intelligent agents, chess, backgammon
- Robotics — autonomous adaptable robots
- Pattern recognition — speech recognition, seismic activity, sonar signals
- Data analysis — data compression, data mining
- Bioinformatics — DNA sequencing, alignment

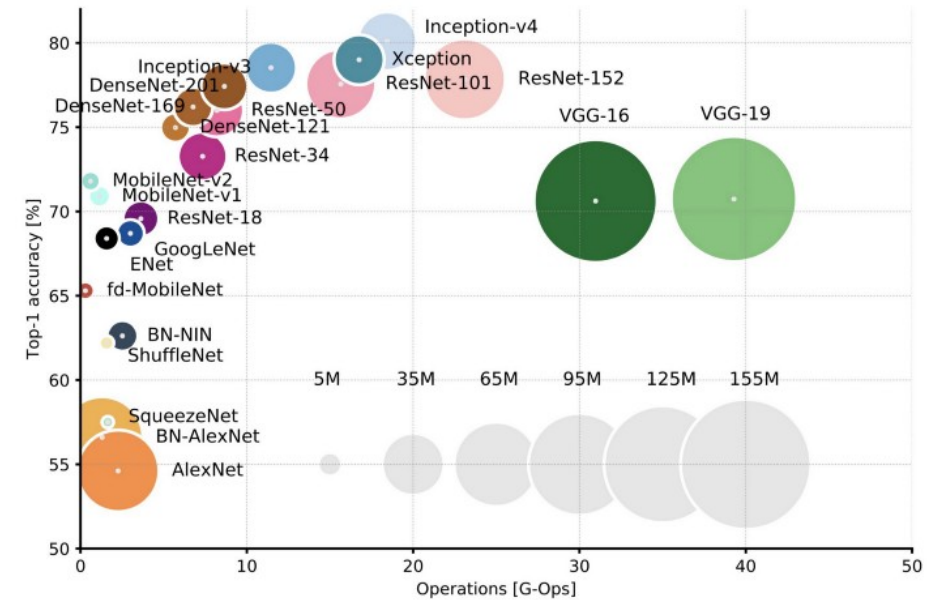
Deep Learning Models Scale with Data



- Deep neural networks scale well with large data sets.



- In addition to size, deep NN have more complicated structure.



- Size of deep NN models on ImageNet competition.

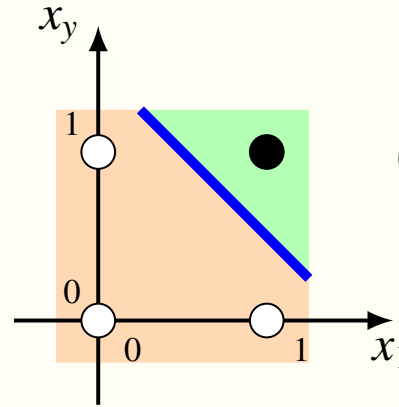
towards data science **Neural Network Architectures**

Implementation of Simple Logic Gates — AND

Function AND

x_1	x_2	y
0	0	0
0	1	0
1	0	0
1	1	1

SVM

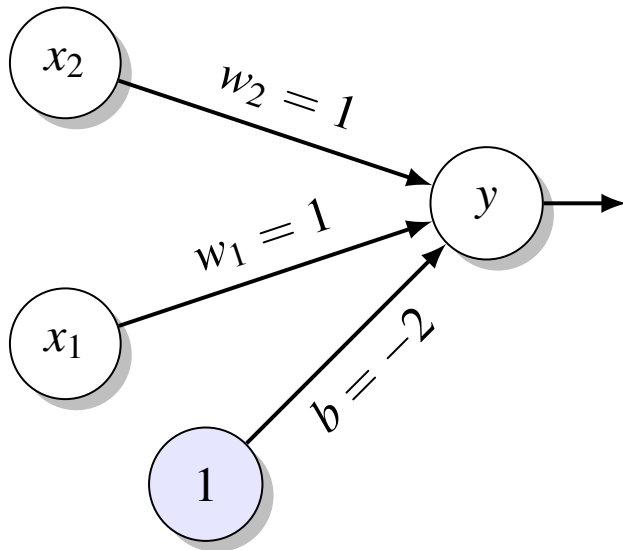


Linearly separable

Calculation

x_1	x_2	y	$z = \vec{x} \cdot \vec{w} + b$	$y = h(z)$
0	0	0	-2	0
0	1	0	-1	0
1	0	0	-1	0
1	1	1	0	1

Solution not unique — how many lines can separate classes in above SVM?

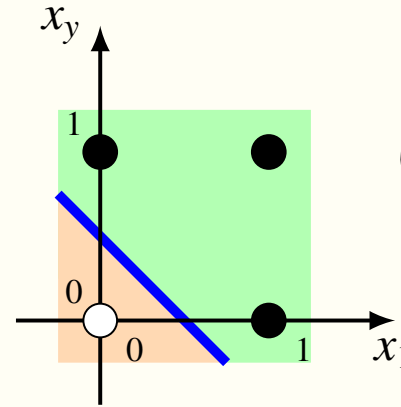


Implementation of Simple Logic Gates — OR

Function OR

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	1

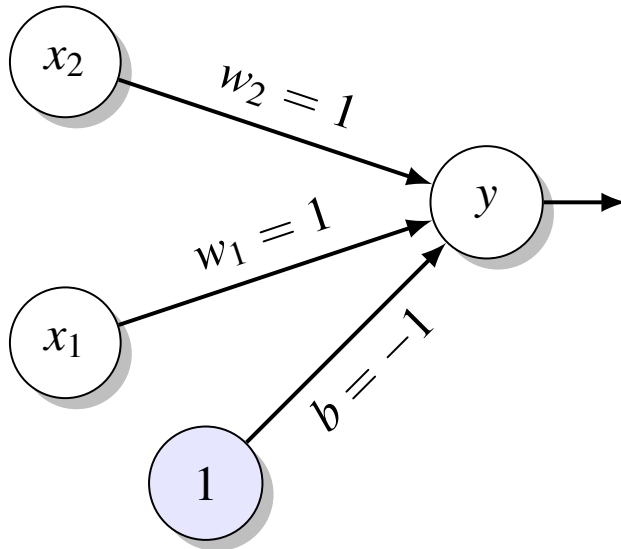
SVM



Calculation

x_1	x_2	y	$z = \vec{x} \cdot \vec{w} + b$	$y = h(z)$
0	0	0	-1	0
0	1	0	0	1
1	0	0	0	1
1	1	1	0	1

Solution not unique — how many lines can separate classes in above SVM?

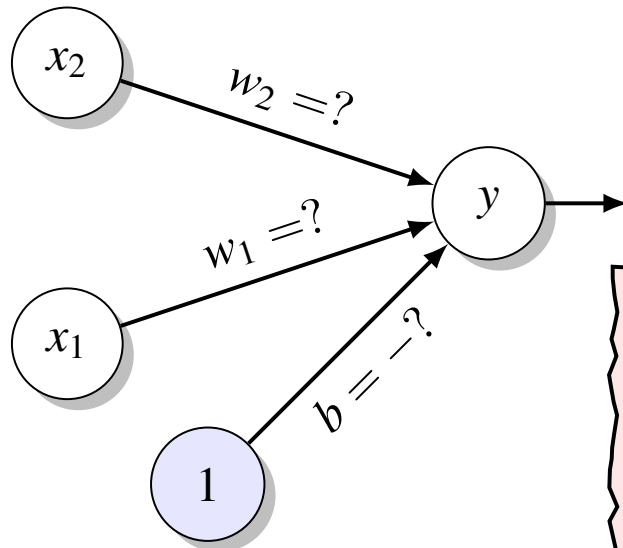
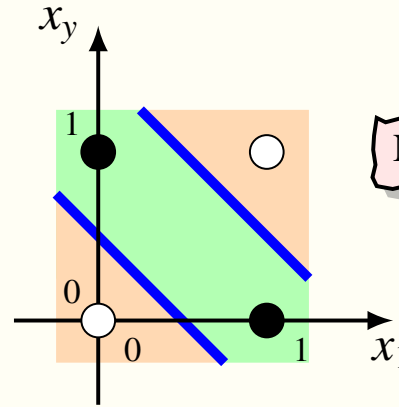


Implementation of Simple Logic Gates — XOR

Function OR

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	0

SVM



Calculation

$$x_1 \quad x_2 \quad y \quad z = \vec{x} \cdot \vec{w} + b \quad y = h(z)$$

Not possible because require

$$\underbrace{b < 0}_{\text{for input } [0, 0]} \quad \underbrace{0 \geq w_1 + b}_{\text{for input } [1, 0]} \quad \underbrace{0 \geq w_2 + b}_{\text{for input } [0, 1]} \quad \underbrace{w_1 + w_2 + b < 0}_{\text{for input } [1, 1]}$$

\Rightarrow Need hidden layer

Expressive Capabilities of ANNs

Boolean functions

- Every boolean function* can be represented by network with single hidden layer ... but might require exponential (in number of inputs) hidden units.

Continuous functions

- Every bounded continuous function can be approximated with arbitrarily small error, by network with one hidden layer [Cybenko 1989; Hornik et al. 1989]
- Any function can be approximated to arbitrary accuracy by a network with two hidden layers [Cybenko 1988].

See Chapter 3 Neural Networks and Deep Learning for a nice non-technical argument why these claims are true.

*this is not just the elementary functions (AND,OR,NOT, etc.) but any logical expression

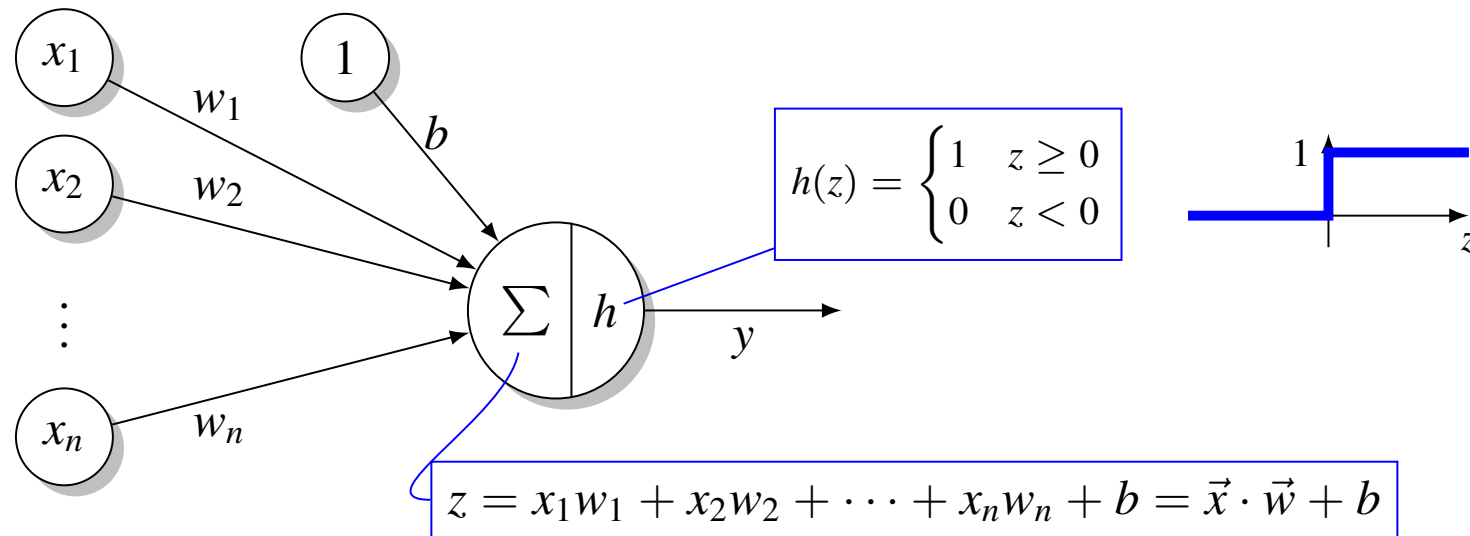
So What Now ?

- How do determine the design/structure of our network?
 - Number and size of hidden layers?
 - How do decisions flow? feed forward networks, recurrent networks
 - Level of interconnections? fully connected[†] / convolution[‡]
 - Which activation function should we use?
 - What encoding to use for output (single output, one-hot (with soft-max), ...)?
- How do we compute the output of a network? forward propagation
- How we we measure the accuracy of our neural network?
 - Have cost functions measuring the difference between computed output and expected output, similar to regression/classification models.
- How do we train the network? back propagation
 - Determine optimal weights and biases — proper treatment requires calculus — we won't go there today.
- Standard modelling concerns
 - Overfitting, bias — standard techniques such as regularisation but many, many network specific techniques (eg. dropout).

[†]Are all neurons in each layer connected to all neurons in the next layer

[‡]Localised fully connected with multiple hidden layers.

Concept: Perceptrons



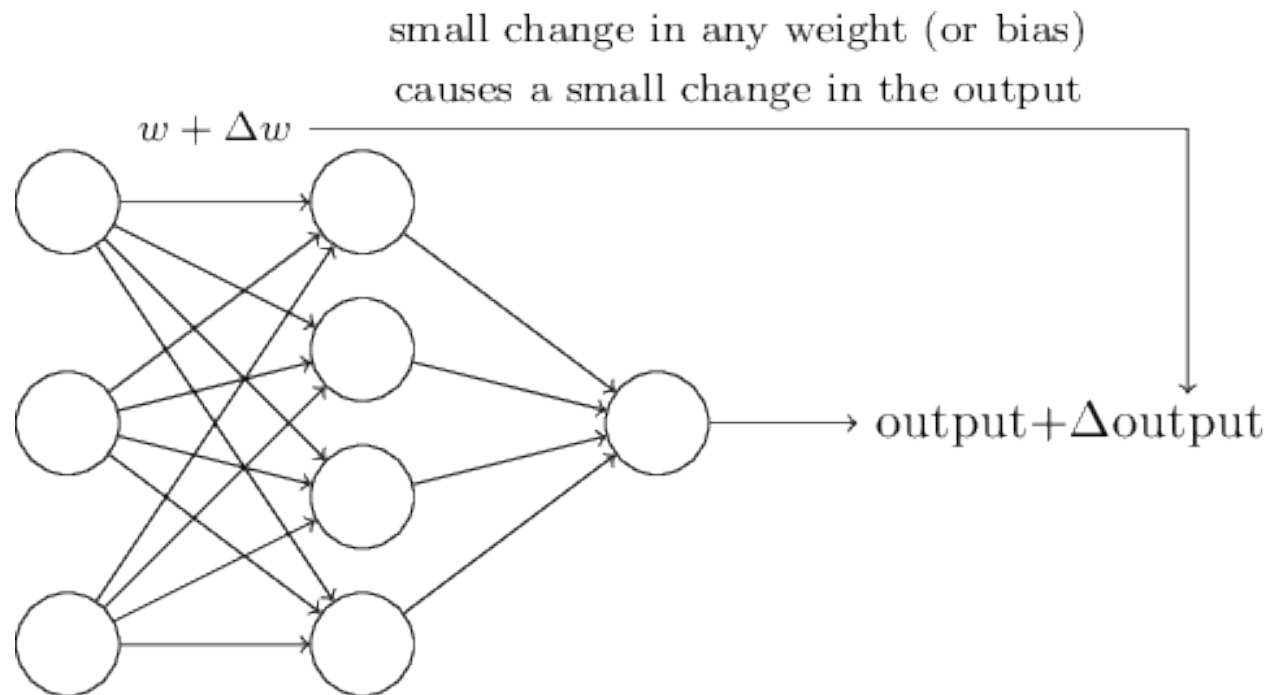
- Uses the step function as the activation function.
- ✓ A network of perceptrons can represent arbitrary boolean functions and arbitrary closely continuous functions — the difficulty is in the training.
- ✗ Was the original model for a neuron but rarely used now as zero sensitivity away from zero and chaotic[§] at zero.

[§]arbitrary small change when $z = 0$ results in a large change in output.

Working Towards Automated Training ...

To train a network we could start with, say random values for weights and biases, then pick random weights/bias to change and see effect on the output. Two problems

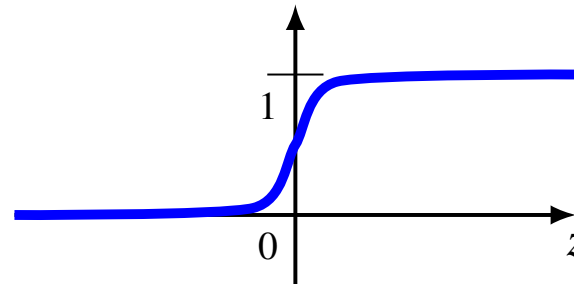
- Number of weights/bias can get very large, so need to be more focused than just random.
- Need structure where arbitrary small change in weights/bias results in a small change in the output — **not the case with perceptrons.**



Concept: Sigmoid Neuron

Uses the logistic/sigmoid function as the activation function ...

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

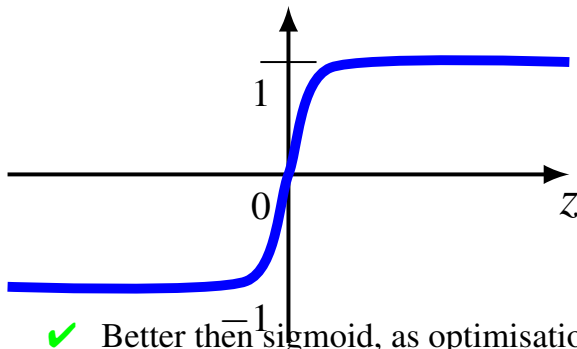


- ✓ For large positive or negative values of z , the result will be nearly the same as with the perceptron (i.e., output is near 0 or 1). For values close to the boundary of the separating hyperplane, values near 0.5 will be emitted.
- ✓ While sigmoid changes rapidly for z near zero, the change is smooth \implies can use calculus.
- A single neuron with the sigmoid activation function is equivalent to logistic regression.

Concept: Activation Functions

hyperbolic tan

$$\operatorname{atanh}(z) = 2\sigma(z) - 1$$



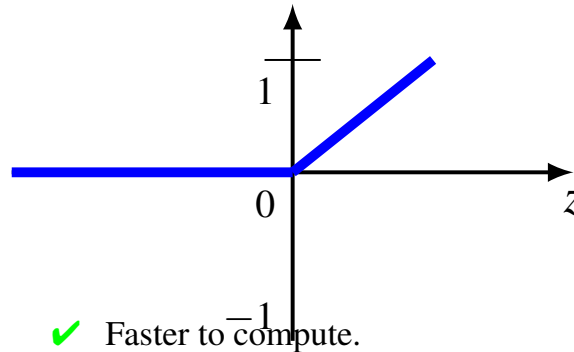
- ✓ Better than sigmoid, as optimisation is less likely to get trapped when inputs are negative.

- ✗ Vanishing derivative for large input

Current best practice: Use ReLU and lower learning rates if see many (20-40%) 'dead' neurons.

Rectified linear unit

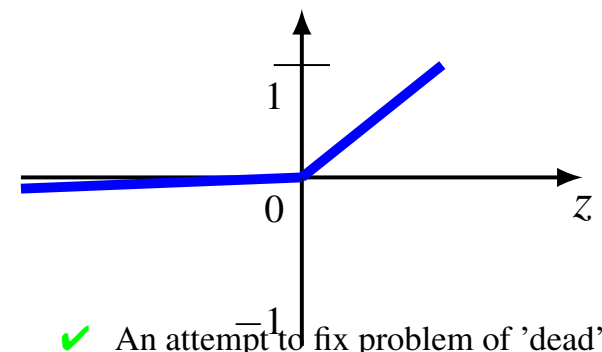
$$\operatorname{ReLU}(z) = \max(0, z)$$



- ✓ Faster to compute.
- ✓ Results in faster ($\times 6$) learning.
- ✓ No vanishing derivative for positive input.
- ✗ Can be fragile during training and can 'die', if input caught in negative region.

Leaky ReLU

$$\operatorname{LReLU}(z) = \begin{cases} z & z \geq 0 \\ 0.01z & z < 0 \end{cases}$$



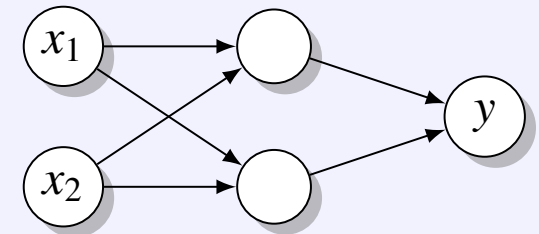
- ✓ An attempt to fix problem of 'dead' ReLU
- ✓ No vanishing derivative.
- Effect on improving training is inconsistent to date.
- Slope (0.01) for negative z can be parameterised.

Example: Sigmoid (logistic) vs ReLU to learn XOR function

```

1 import numpy as np
2 from sklearn.neural_network import MLPClassifier
3
4 xs = np.array([[0, 0],[0, 1],[1, 0],[1, 1]])
5 ys = np.array([0, 1, 1, 0])
6
7 for activation in ['logistic', 'relu']:
8     print ("\nUsing activation %s" % activation)
9
10     model = MLPClassifier(
11         activation=activation,
12         max_iter=10000,
13         hidden_layer_sizes=(2,),
14         random_state=20)
15
16     model.fit(xs, ys)
17
18     print('score:', model.score(xs, ys))
19     print('predictions:', model.predict(xs))
20     print('expected:', ys)

```



Using activation logistic
score: 0.5
predictions: [1 1 1 1]
expected: [0 1 1 0]

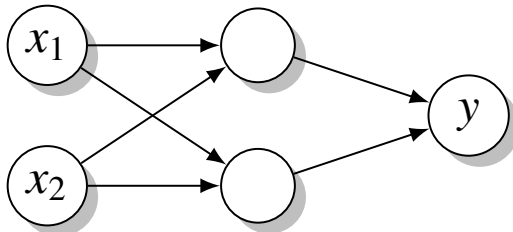
Using activation relu
score: 1.0
predictions: [0 1 1 0]
expected: [0 1 1 0]

Concept: One-Hot Encoding

Consider the following neural networks representations of the XOR function.

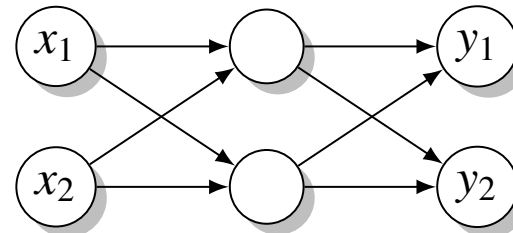
Minimal

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	0



One-Hot Encoding

x_1	x_2	y_1	y_2
0	0	0	1
0	1	1	0
1	0	1	0
1	1	0	1



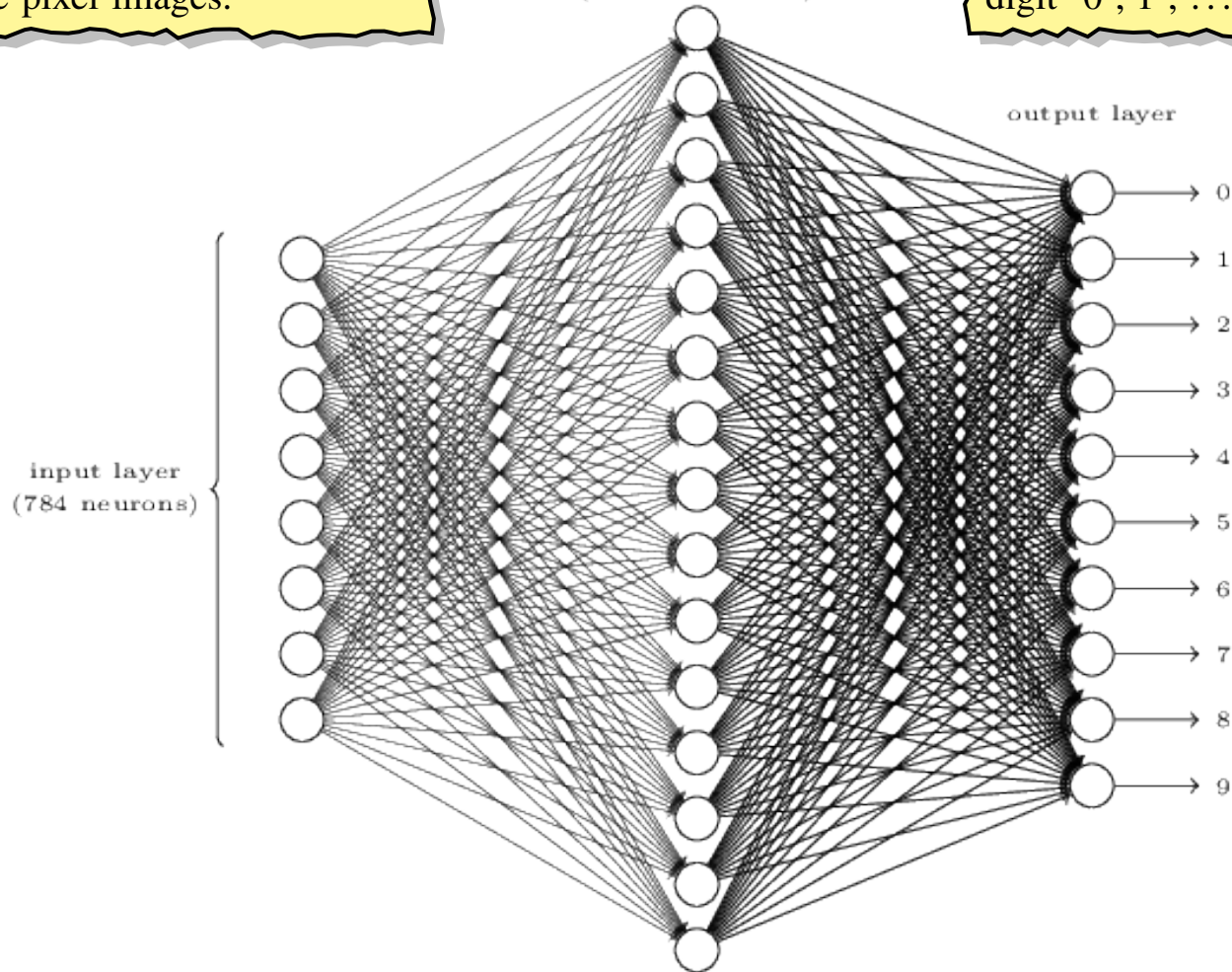
One-hot encoding with k output nodes is typically used in classification problems with k classes.

Example: One-Hot Encoding for MIST Digits Dataset

Input consists of $28 \times 28 = 784$ grayscale pixel images.

hidden layer
($n = 15$ neurons)

Desired output is classification as digit '0', '1', ..., '9'.

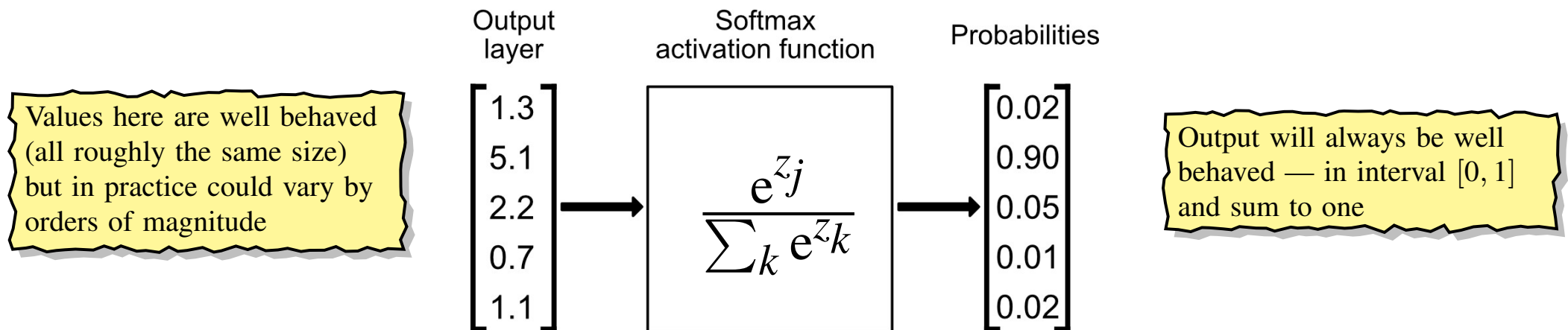


Concept: Soft-Max

The **soft-max** is an activation function[¶] that is usually applied to the output layer of a network when one-hot encoding is used. It is defined by

$$\text{softmax}(z_j) = \frac{e^{z_j}}{\sum_k e^{z_k}} \quad \text{for } j = 1, 2, \dots, n$$

- ✓ Output from soft-max are in interval $[0, 1]$ and sum (over nodes in layer) to one. Hence can be treated as probabilities.



[¶]i.e., is applied to $z = \vec{w} \cdot \vec{x} + b$, the result of a summation operation.

Concept: Cost Functions

The **cost function** (also known as a **error loss** function) measures how well the network predicts outputs. The goal is to then find a set of weights and biases that minimises the cost.

Squared error loss, L_2 error

$$C(w, b) = \frac{1}{2n} \sum_i^n \left\{ y_i - \hat{y}(x_i) \right\}^2$$

Cost relatively greater for larger errors

Absolute error loss, L_1 error

$$C(w, b) = \frac{1}{n} \sum_i^n \left| y_i - \hat{y}(x_i) \right|$$

Relative cost is constant with error

Average Cross Entropy (using logs^{||})

$$C(w, b) = -\frac{1}{n} \sum_i^n \left[y_i \log(\hat{y}(x_i)) + (1 - y_i) \log(1 - \hat{y}(x_i)) \right]$$

Cost based on certainty when wrong

^{||}The log function blows up as input approaches zero so it can be used to magnify differences between small positive numbers — in classification we want to distinguish between miss-classifications of zero with a probability of 0.01 versus miss-classifications of zero with a probability 0.000000001. (And similarly for a miss-classifications of one.)

Concept: Decomposable Cost Functions

- Notice in the previous slide, that to compute the cost function we had to compute its value for **all** of the n input-output pairs. What happens if n is large? ... everything sloooooows down \implies not great.
- If we define C_i as the cost for the i -th input-sample pair, then the total cost is just

$$C = \frac{1}{n} \sum_i C_i$$

This has two big advantages

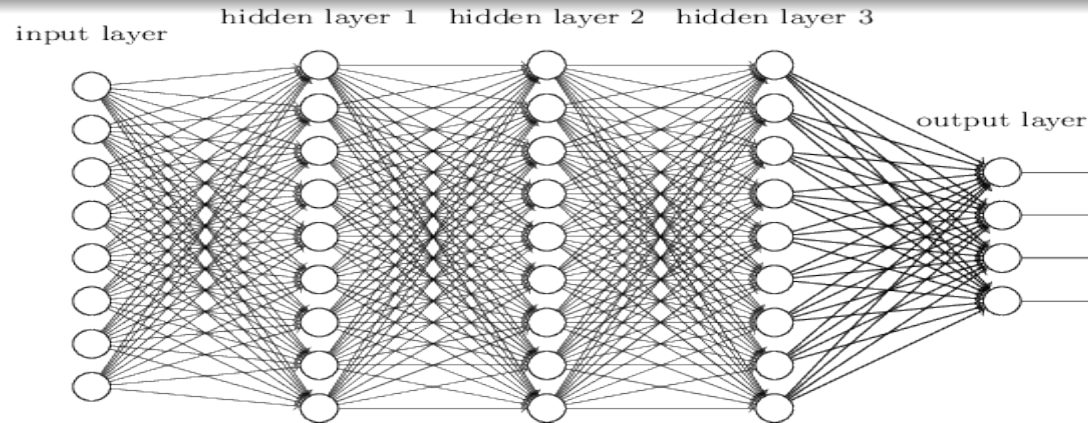
- Parallelisation — we can run over separate cores and compute C_i terms in parallel.
- Sampling — consider taking a subset $M \subseteq \{1, 2, \dots, n\}$ with size m of the training set. We can approximate the cost function using only this subsample of the data:

$$C = \frac{1}{n} \sum_{i=1}^n C_i \approx \frac{1}{m} \sum_{i \in M} C_i$$

So it seems that we can perhaps estimate the cost using only a small subset of the entire training set. And similarly for the gradient of the cost:

$$\nabla C = \frac{1}{n} \sum_{i=1}^n \nabla C_i \approx \frac{1}{m} \sum_{i \in M} \nabla C_i$$

Concept: Forward Propagation

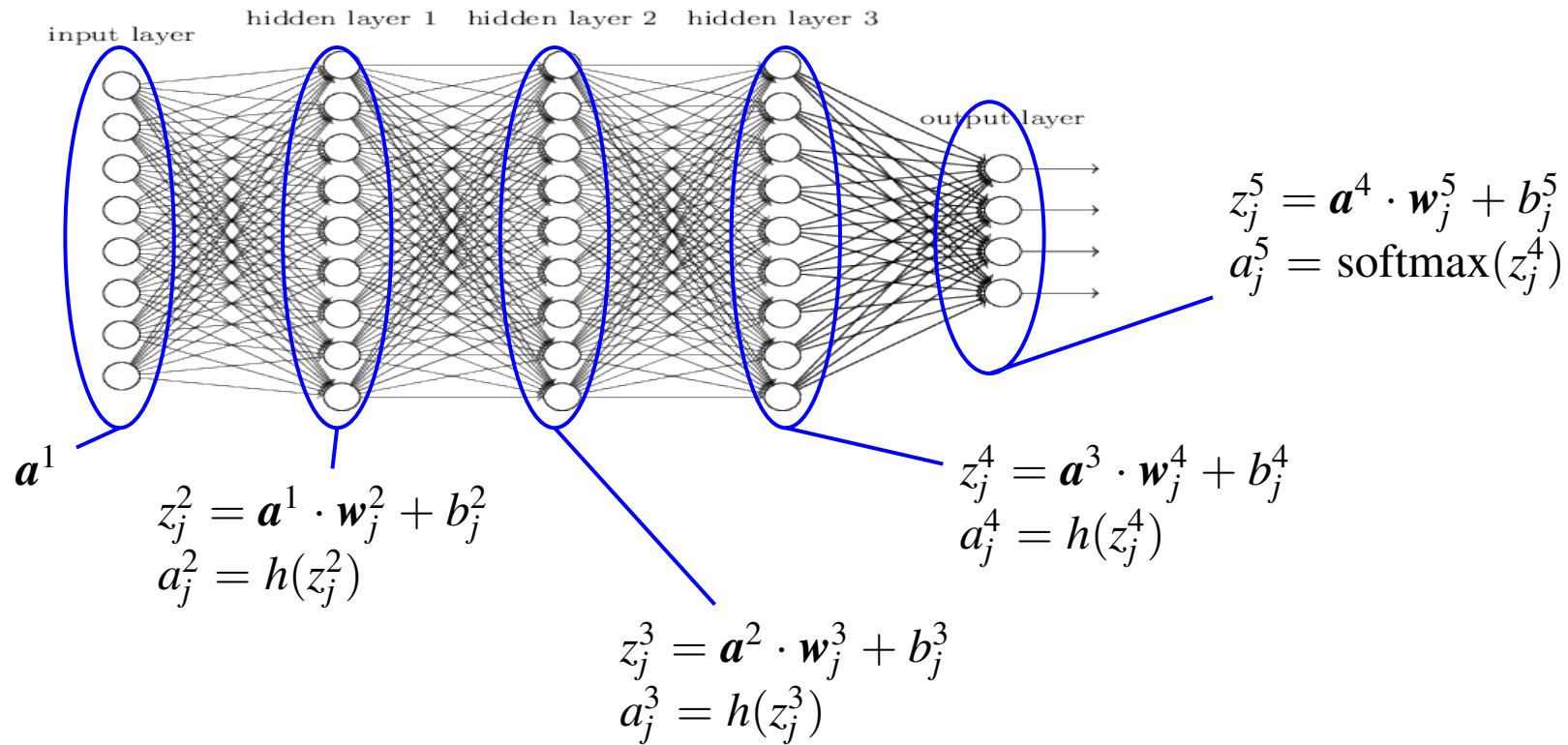


Define:

- L is number of layers (1 input + 1 output + $(L - 2)$ hidden layers).
 - a_j^l is output from applying the activation function on node j in layer l .
- $\Rightarrow a_j^1$ is value of input node j , and a_j^L is value of output node j .
- w_{jk}^l is the weight of node k in layer $l - 1$ as applied by node j in layer l .
 - b_j^l is the bias of node j of layer l .
 - z_j^l is the result of the summation operation on node j in layer l .

$$z_j^l = \sum_k a_k^{(l-1)} \times w_{jk}^l + b_j^l = \mathbf{a}^{(l-1)} \cdot \mathbf{w}_j^l + b_j^l \quad a_j^l = \sigma(z_j^l)$$

Concept: Forward Propagation



where:

- h is the activation function: σ , atanh , ReLU , etc

Concept: Optimisation – Gradient Decent

- Given a cost function that depends on the weights and the biases, training the network is effectively an optimisation problem.
- Standard technique is

Gradient Descent

Compute the gradient function, then move a small amount in the opposite direction of the gradient (because we are minimising), and then recalculate the gradient on the new spot, and repeat.

- Mathematically, we can describe these updates, on the k -th iteration, as:

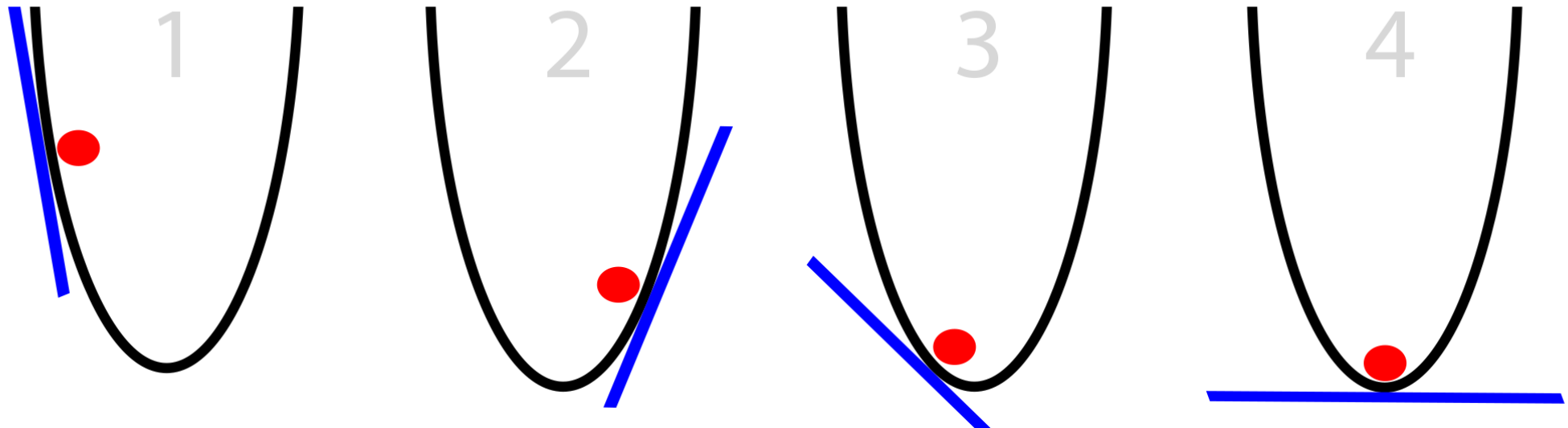
$$\vec{w}_{k+1} = \vec{w}_k - \eta \cdot \nabla_w C$$

$$\vec{b}_{k+1} = \vec{b}_k - \eta \cdot \nabla_b C$$

For some value** $\eta > 0$. This tuning parameter is called the **learning rate**. Too small, and learning takes a very long time. Too large, and it is likely to have trouble finding the true minimum (as it will keep ‘overshooting’ it).

**The symbol η is Greek "eta".

Gradient Descent in 1D



- Blue line represents the gradient.
 - If slope is negative, move right
 - If slope is positive, move left
 - (Repeat until slope == 0)

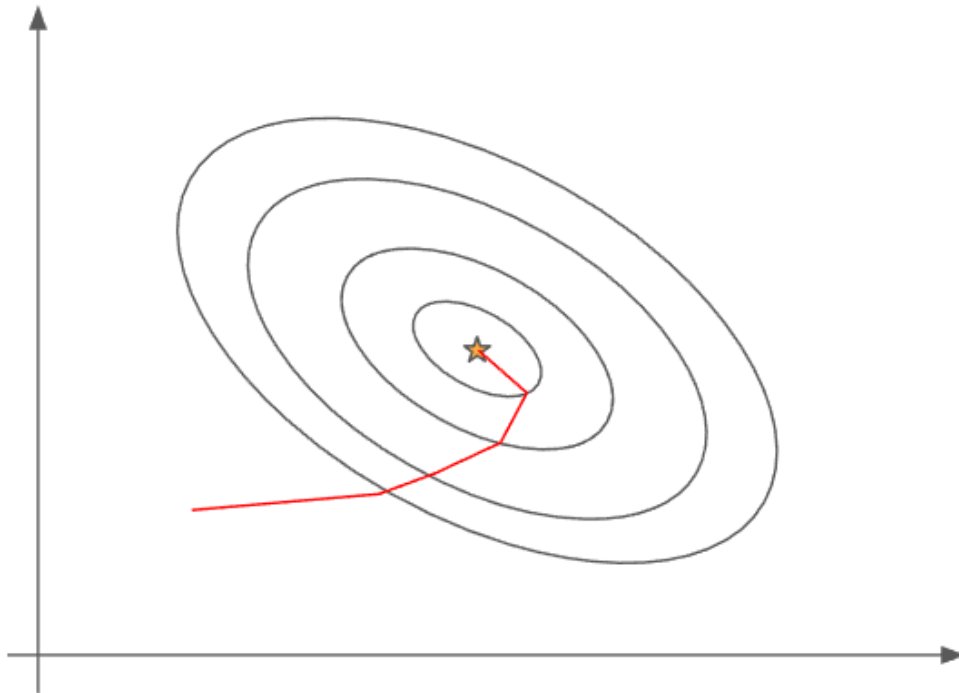
Concept: Optimisation – Stochastic gradient descent (SGD)

Stochastic gradient descent uses decomposable property of the cost function to speed up the process of doing gradient descent. Specifically, the input data are randomly partitioned into disjoint groups $M_1, M_2, \dots, M_{n/m}$. We then do the following updates to the weights (biases are done at the same time, but omitted for sake of space):

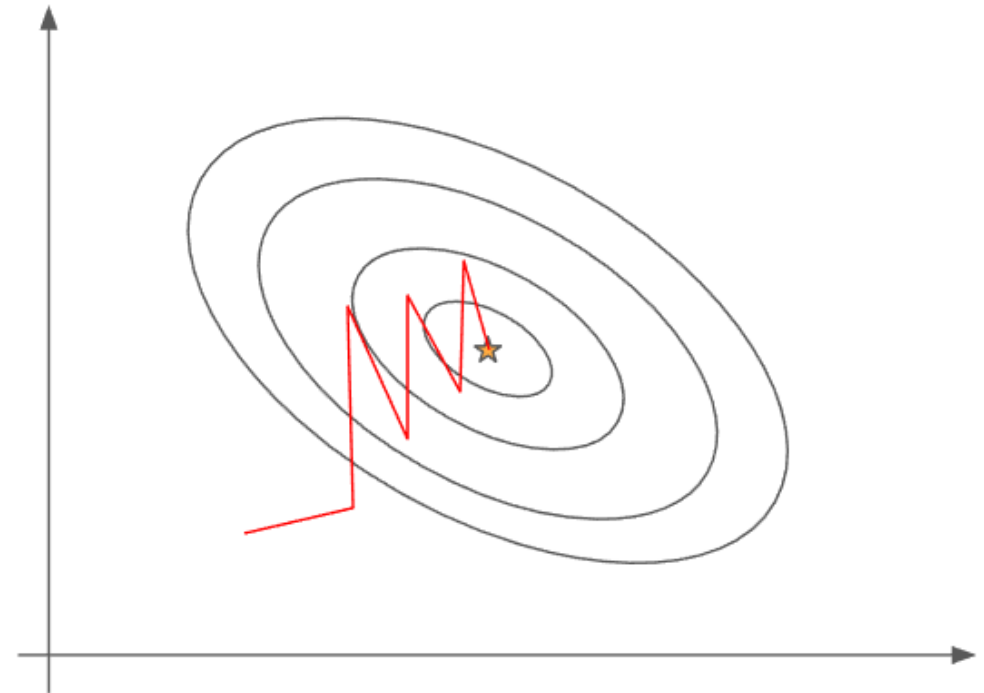
$$\begin{aligned}w_{k+1} &= w_k - \frac{\eta}{m} \sum_{i \in M_1} \nabla C_i \\w_{k+2} &= w_{k+1} - \frac{\eta}{m} \sum_{i \in M_2} \nabla C_i \\&\vdots \\w_{k+n/m+1} &= w_{k+n/m} - \frac{\eta}{m} \sum_{i \in M_{n/m}} \nabla C_i\end{aligned}$$

Each set M_j is called a **mini-batch** and going through the entire dataset as above is called an **epoch**.

Gradient Descent vs Stochastic Gradient Descent



Gradient Descent

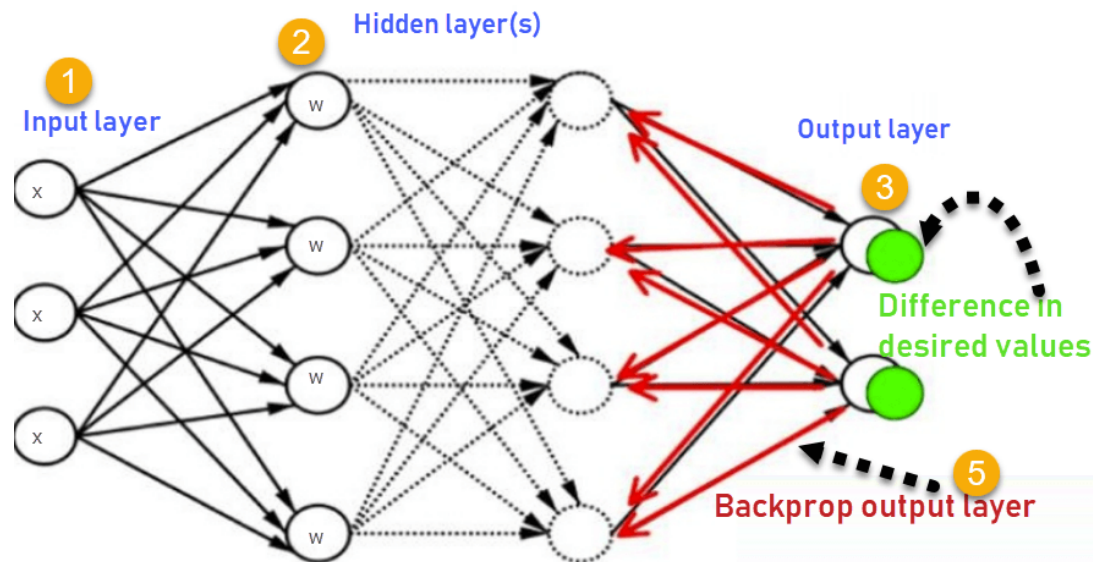


Stochastic Gradient Descent

- GD always head in the (locally) correct direction but each step takes a long time to compute.
- SGD will miss some local information so movement is more erratic. However computation of steps is much ($\times 100, \times 1000, \dots$) faster.

Concept: Back Propagation

- Back propagation deals with updating the weights of a neural network based on the error obtained in the previous epoch.
- We will not cover this today, as a proper treatment requires calculus — see resources at end of notes, if interested.
- To use neural networks you don't have to understand back propagation but it helps. See Medium article [Yes, you should understand backprop](https://www.guru99.com/backpropagation-neural-network.html).



[**https://www.guru99.com/backpropagation-neural-network.html](https://www.guru99.com/backpropagation-neural-network.html)

Concept: Addressing Overfitting by Regularisation

As the size of neural networks grow, the number of weights and biases can quickly become quite large. State of the art neural networks today often have billions of weight values. In order to avoid over-fitting, one common approach is to add a penalty term to the cost function. Common choices are the ℓ_2 -norm, given as:

$$C = C_0 + \lambda \sum_i w_i^2$$

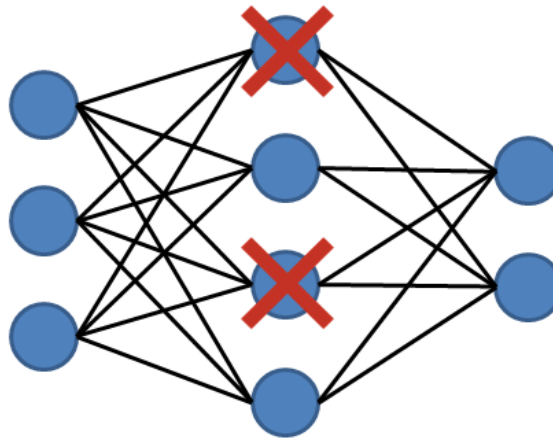
Where C_0 is the unregularized cost, and the ℓ_1 -norm:

$$C = C_0 + \lambda \sum_i |w_i|.$$

The distinction between these is similar to the differences between lasso and ridge regression.

Concept: Addressing Overfitting by Dropout

A very different approach to avoiding over-fitting is to use an approach called *dropout*. Here, the output of a randomly chosen subset of the neurons are temporarily set to zero during the training of a given mini-batch. This makes it so that the neurons cannot overly adapt to the output from prior layers as these are not always present. It has enjoyed wide-spread adoption and massive empirical evidence as to its usefulness.



From about 2018, dropout is been replaced by **Batch normalisation** between convolution and activation layers in convolutional networks. This helps to protect against vanishing gradient during training — resulting in lower training time and better performance.

Concept: Momentum

Problem

- Learning is slow if the learning rate is set too low.
- Gradient may be steep in some directions but shallow in others.

⇒ add a momentum term α .

Solution

Momentum, adds a fraction of the past weight update to the current weight update. This helps prevent the model from getting stuck in local minima, as even if the current gradient is 0, the past one most likely was not, so it will as easily get stuck. By using momentum, the movements along the error surface are also smoother in general and the network can move more quickly throughout it.

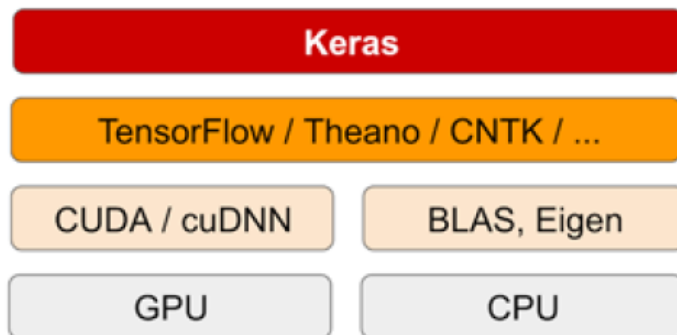
Typical value for α is 0.5.

If the direction of the gradient remains constant, the algorithm will take increasingly large steps.

Introduction to Keras and TensorFlow

K Keras

- Python package (Python 3.6+)
- Sits on top of TensorFlow or Theano
- High-level neural network API
- Runs seamlessly on CPU and GPU
- Open source <https://keras.io>
- Fewer code lines to build/run a model.



TensorFlow

- A python (3.5-3.7) package/C++ library
- Running on CPU or NVIDIA CUDA GPU
- End-to-end platform for machine/deep learning
- Multi platform (desktop, web by TF.js, mobile by TF Lite)
- Open source <https://www.tensorflow.org>
- More code lines to build/run a model

Keras and TensorFlow Installation

The screenshot shows the Anaconda Navigator application interface. On the left is a sidebar with navigation options: Home, Environments, Learning, and Community. The main area is divided into a search bar, a list of environments, and a table of search results. The search bar contains the text 'tensorflow'. The search results table lists various packages, with 'keras' and 'tensorflow' highlighted by red boxes, and 'keras-gpu' and 'tensorflow-gpu' highlighted by blue boxes.

Search Results Table:

Name	Description	Version
<input type="checkbox"/> keras CPU	Deep learning library for theano and tensorflow	2.3.1
<input checked="" type="checkbox"/> keras-gpu GPU	Deep learning library for theano and tensorflow	2.2.4
<input type="checkbox"/> r-tensorflow		1.8
<input checked="" type="checkbox"/> tensorflow CPU	Tensorflow is a machine learning library.	1.14.0
<input checked="" type="checkbox"/> tensorflow-base	Tensorflow is a machine learning library, base package contains only tensorflow.	1.14.0
<input type="checkbox"/> tensorflow-datasets		1.2.0
<input type="checkbox"/> tensorflow-eigen	Metapackage for selecting a tensorflow variant.	2.1.0
<input checked="" type="checkbox"/> tensorflow-estimator		1.14.0
<input checked="" type="checkbox"/> tensorflow-gpu GPU	Metapackage for selecting a tensorflow variant.	1.14.0
<input type="checkbox"/> tensorflow-gpu-base	Tensorflow is a machine learning library, base gpu package, tensorflow only.	1.8.0
<input type="checkbox"/> tensorflow-hub		0.7.0
<input type="checkbox"/> tensorflow-metadata		0.14.0

14 packages available matching "tensorflow"

Keras training XOR function

2

```
import numpy as np

from sklearn.metrics import accuracy_score

from keras.models import Sequential
from keras.layers.core import Dense, Dropout, Activation
from tensorflow.keras.optimizers import SGD

X = np.array( [[0,0],[0,1],[1,0],[1,1]] )
y = np.array( [[0],[1],[1],[0]] )

def initialize_weights(shape, dtype=None):
    return np.random.normal(loc=0.75, scale=1e-2, size=shape)

def summary(model, X, y):
    pred_prob = model.predict(X)
    pred = np.array(pred_prob>0.5, dtype=int)
    print(f"{'Pred prob':12s} {pred_prob.reshape(4)}")
    print(f"{'Pred':12s} {pred.reshape(4)}")
    print(f"{'True':12s} {y.reshape(4)}")
    print(f"{'Accuracy':12s} {accuracy_score(y, pred)}")
```

Model 1

```

3 • model = Sequential()

layer = Dense(2, activation='sigmoid',
              kernel_initializer=initialize_weights, input_dim=2)
model.add(layer)

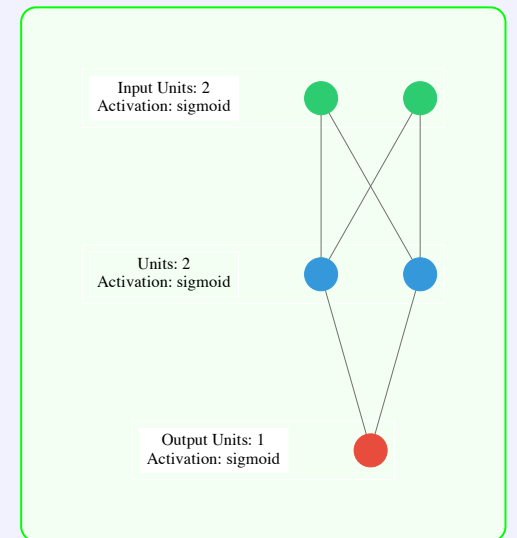
layer = Dense(1, activation='sigmoid')
model.add(layer)

model.compile(loss='mean_squared_error',
              optimizer='adam', metrics='accuracy')

model.fit(X, y, batch_size=4, epochs=1000, verbose=0)

pred_prob = model.predict(X)
summary(model, X, y)

```



```

Pred prob: [0.51681733 0.506059 0.50623363 0.49227926]
Pred:      [1 1 1 0]
True:      [0 1 1 0]
Accuracy:  0.75

```

Model 2

```

4 ● model = Sequential()

layer = Dense(2, activation='relu',
              kernel_initializer=initialize_weights, input_dim=2)
model.add(layer)

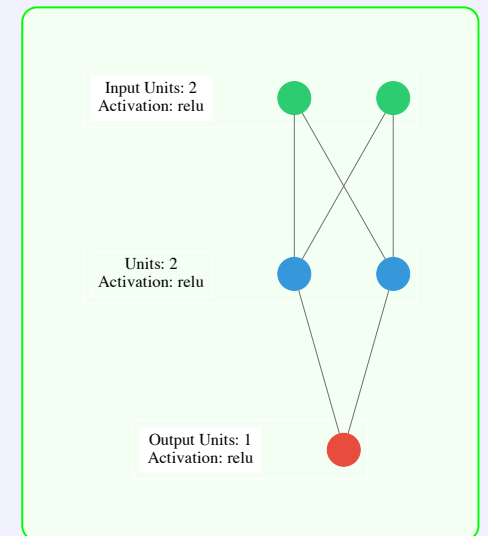
layer = Dense(1, activation='sigmoid')
model.add(layer)

model.compile(loss='mean_squared_error',
              optimizer='adam', metrics='accuracy')

model.fit(X, y, batch_size=4, epochs=1000, verbose=0)

pred_prob = model.predict(X)
summary(model, X, y)

```



```

Pred prob: [0.47793186 0.5813429 0.5805019 0.398048 ]
Pred:      [0 1 1 0]
True:      [0 1 1 0]
Accuracy:  1.0

```


Model 3

```

5 • model = Sequential()

layer = Dense(3, activation='relu',
              kernel_initializer=initialize_weights, input_dim=2)
model.add(layer)

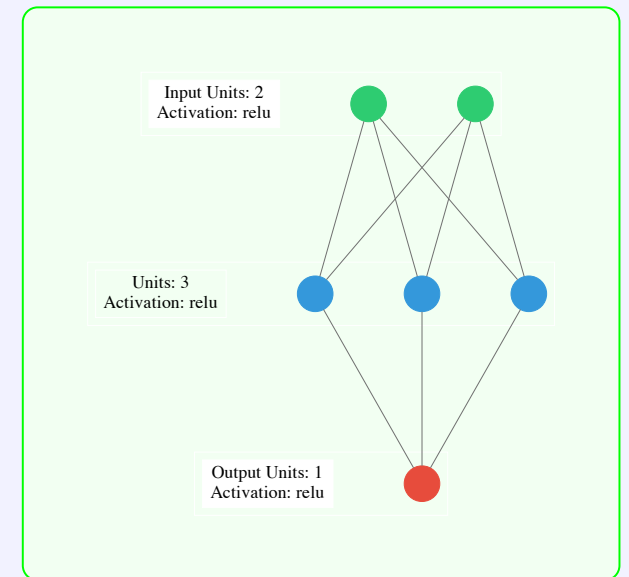
layer = Dense(1, activation='sigmoid')
model.add(layer)

model.compile(loss='mean_squared_error',
              optimizer='adam', metrics='accuracy')

model.fit(X, y, batch_size=4, epochs=1000, verbose=0)

pred_prob = model.predict(X)
summary(model, X, y)

```



```

Pred prob: [0.3195203 0.6992405 0.6991698 0.2968087]
Pred:      [0 1 1 0]
True:      [0 1 1 0]
Accuracy:   1.0

```

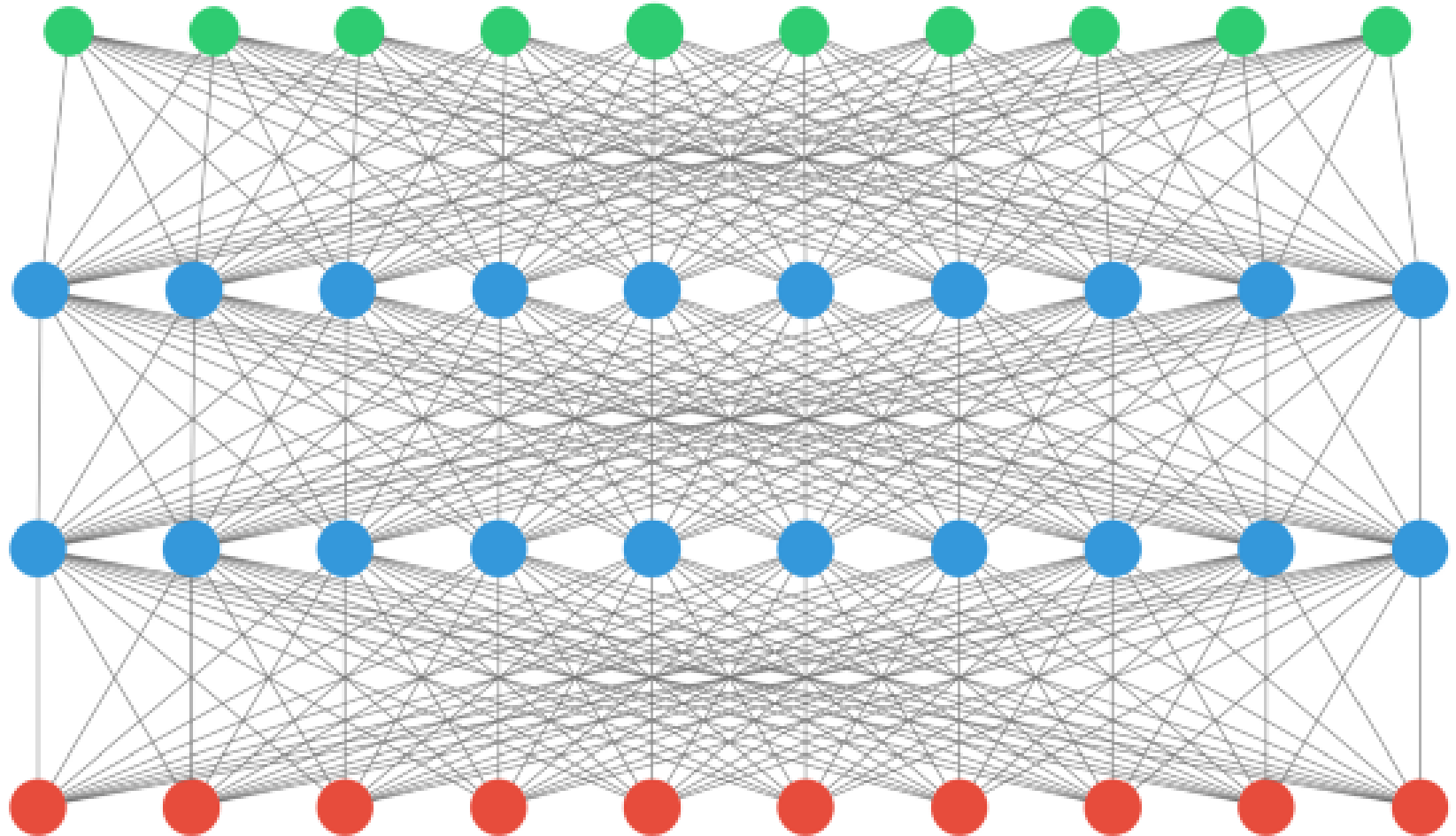
Keras Network for MNIST Dataset

Input Units: 784 (+774 more)
Activation: relu

Units: 32 (+22 more)
Activation: relu

Units: 10
Activation: sigmoid

Output Units: 10
Activation: relu



Resources



Neural Networks and Deep Learning is a free online book by Michael Nielsen. This is a lovely read and my notes very much follow his approach.



3Blue1Brown has 4 amazing videos on neural networks (and many others on Calculus and Linear Algebra). See:

- Chapter 1: But what *is* a Neural Network?
- Chapter 2: Gradient descent, how neural networks learn.
- Chapter 3: What is back propagation really doing?
- Appendix: Back propagation calculus



Learn TensorFlow and deep learning, without a PhD

- Basics of neural networks with Tensorflow
- Feed forward, convolution and recurrent networks,
- MIST data set - training issues <— brilliant



www.cs.stir.ac.uk/~kjt/techreps/pdf/TR148.pdf

A paper covering training XOR in detail. I'm including this for interest only.