# Data Mining 2

Topic 03: Review of Model Building

Lecture 02: Regression Models

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#### Outline

Regression Models

# Outline

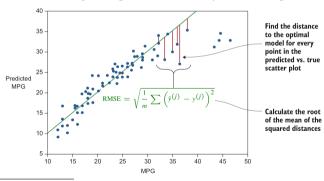
1. Regression Models (Evaluating Numeric Prediction)

### Regression Models (Evaluating Numeric Prediction)

We have covered using the MSE

$$MSE = \frac{1}{m} \sum \left( f\left(\mathbf{X}^{(j)}; \boldsymbol{\theta}\right) - y^{(j)} \right)^{2}$$

as the cost function in our curve fitting example. Geometrically this is computed as follows\*



<sup>\*</sup>Diagram (from Real World Machine Learning) shows the RMSE  $=\sqrt{\text{MSE}}$ 

# Common Cost Functions in Regression Models

Measure	Definition	Purpose/Advantage
Mean square error (MSE)	$\frac{(p_1-a_1)^2+\cdots+(p_m-a_m)^2}{m}$	Mathematically tractable but places greater emphasise on observations with large error
Root mean square error (RMSE)	$\sqrt{\frac{(p_1-a_1)^2+\cdots+(p_m-a_m)^2}{m}}$	Has same units as data
Mean absolute error (RMAE)	$\frac{ p_1-a_1 +\cdots+ p_m-a_m }{m}$	Does not overemphasise observa- tions with large error (as MSE does)
Relative square error (RSE)	$\frac{(p_1-a_1)^2+\cdots+(p_m-a_m)^2}{(p_1-\bar{a})^2+\cdots+(p_m-\bar{a})^2}$	Relative metric compares the
Root Relative square error (RRSE)	$\sqrt{\frac{(p_1-a_1)^2+\cdots+(p_m-a_m)^2}{(p_1-\bar{a})^2+\cdots+(p_m-\bar{a})^2}}$	error in the predictions with errors in the simplest model possible (a model just always pre-
Relative absolute error (RAE)	$\frac{ p_1-a_1 +\cdots+ p_m-a_m }{ p_1-\bar{a} +\cdots+ p_m-\bar{a} }$	dicting the average value of y)

where  $a_j$  is the actual value,  $p_j$  is the predicted value, m is the number of observations, and  $\bar{a}$  represents the mean of the  $a_j$ .

# Assumptions of (Linear) Regression Model

- Multivariate normality each of the independent variables must be normally distributed.
  - Graphical: histograms, Q-Q plots,
  - Numerical: goodness of fit tests, e.g., the Kolmogorov-Smirnov test, ...
  - Fix: non-linear transformations such as log, power, Box-Cox, etc
- No or little multicollinearity independent variables should not be too highly correlated with each other.
  - Numerical: correlation matrix using Pearson?s bivariate correlation coefficient.
  - Fix: Centre the data, filter out some of the independent variables,
- No **auto-correlation** the residuals should be independent, and normally distributed.
  - Graphical: residual plot.
  - Numerical: Durbin-Watson test.
- homoscedasticity constant variance in residuals.
  - Graphical: residual plot.
  - : Fix: transform data or use non-linear model.

And, in addition, for linear regression

• **Linearity** — relationship between the independent variables and the dependent variable is linear.